

# The Scholar Dictionary Portuguese and The Graphical Law

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## Abstract

We study the words of Scholar Dictionary Portuguese. We draw the natural logarithm of the number of headwords, normalised, starting with a letter vs the natural logarithm of the rank of the letter, normalised. We conclude that the dictionary can be characterised by the magnetisation curve,  $BP(4, \beta H = 0)$ , in the Bethe-Peierls approximation of the Ising model, in the presence of four nearest neighbours and in the absence of external magnetic field,  $\beta H = 0$ .  $\beta$  is  $\frac{1}{k_B T}$  where,  $T$  is temperature and  $k_B$  is the tiny Boltzmann constant.

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A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
3030	1041	2886	2243	2223	1081	807	344	1572	224	26	811	1651	520	538	2751	206	1481	1608	1283	193	685	16	52	5	74

TABLE I. Headwords of Scholar Dictionary Portuguese

## I. INTRODUCTION

In one summer evening, the author asked one Garo tribesman, "What is the word for mosquito in the Garo language?". He replied "gangu". The author was wondering since then, from where the word "gangu" might have come. As he was going through the Scholar Dictionary Portuguese, [1], he found that the word "gangu" means gang in Portuguese. Similarly, we came to know from the dictionary,[1], that bata means robe, disco means disk, fama means fame, fuzil means rifle, gusa means pig iron, janela means window, jarda means yard, manta means blanket, maré means tide, muda means seedling, nadar means to swim, negrume means darkness, nexo means sense, nova means piece of news, nuvem means cloud, óptica means optics, pai means father, pais means parents, pala means eyeshade, pasta means paste, pata means claw, patim means ice skate, pátria means homeland, pejo means modesty, perecível means perishable, permutar means to permute, petiz means small child, pioc means peak, pino means pin, pinto means young chicken, polo means pole, Polônia means Poland, posta means slice, posto means post, prova means proof, sacal means boring, sadia means healthy, sala means room, Sampa means São Paulo, soja means soyabean, solário means sunroom, som means sound, subida means upward slope, subir means to climb, varanda means balcony, so on and so forth.

In this dictionary, [1], we count all the headwords one by one, beginning with each letter. The result is the table, tableI. To visualise we plot the number of headwords against the respective letters in the dictionary sequence, [1] , in the adjoining figure, fig.1.

Looking for the Graphical Law in this dictionary, we proceed narrating the precedence. We have started considering magnetic field pattern in [2], in the languages we converse with. We have studied there, a set of natural languages, [2] and have found existence of a magnetisation curve under each language. We have termed this phenomenon as the Graphical Law.

Then, we moved on to investigate into, [3], dictionaries of five disciplines of knowledge and found existence of a curve magnetisation under each discipline. This was followed by finding of the graphical law behind the bengali language,[4] and the basque language[5].

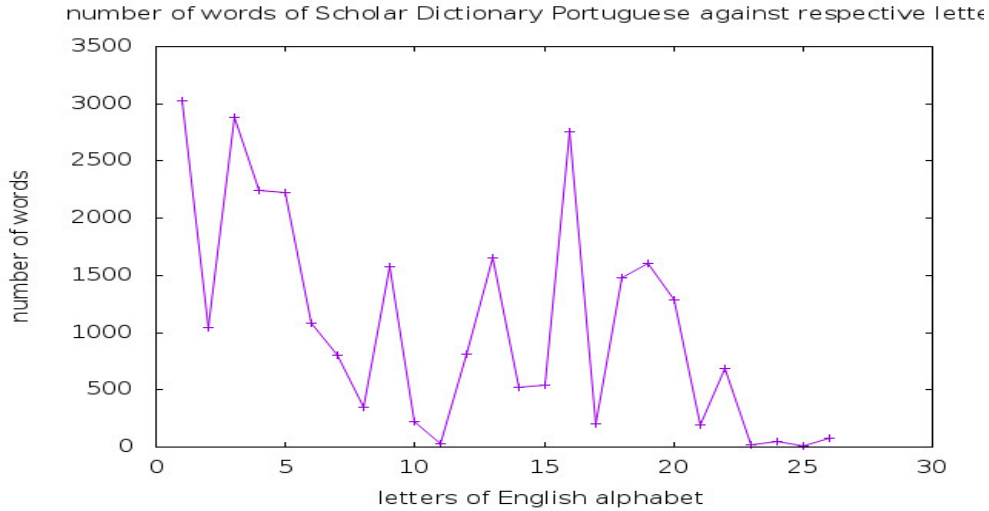


FIG. 1. The vertical axis is number of headwords in the Scholar Dictionary Portuguese,[1]. The horizontal axis is the letters of the English alphabet. Letters are represented by the sequence number in the alphabet.

This was pursued by finding of the graphical law behind the Romanian language, [6], five more disciplines of knowledge, [7], Onsager core of Abor-Miri, Mising languages,[8], Onsager Core of Romanised Bengali language,[9], the graphical law behind the Little Oxford English Dictionary, [10], the Oxford Dictionary of Social Work and Social Care, [11], the Visayan-English Dictionary, [12], Garo to English School Dictionary, [13], Mursi-English-Amharic Dictionary, [14] and Names of Minor Planets, [15], A Dictionary of Tibetan and English, [16], Khasi English Dictionary, [17], Turkmen-English Dictionary, [18], Websters Universal Spanish-English Dictionary, [19], A Dictionary of Modern Italian, [20], Langenscheidt's German-English Dictionary, [21], Essential Dutch dictionary by G. Quist and D. Strik, [22], Swahili-English dictionary by C. W. Rechenbach, [23], Larousse Dictionnaire De Poche for the French, [24], the Onsager's solution behind the Arabic, [25], the graphical law behind Langenscheidt Taschenwörterbuch Deutsch-Englisch / Englisch-Deutsch, Völlige Neubearbeitung, [26], the graphical law behind the NTC's Hebrew and English Dictionary by Arie Comey and Naomi Tsur, [27], the graphical law behind the Oxford Dictionary Of Media and Communication, [28], the graphical law behind the Oxford Dictionary Of Mathematics, Penguin Dictionary Of Mathematics, [29], the Onsager's solution behind the Arabic Second part, [30], the graphical law behind the Penguin Dictionary Of Sociology, [31], behind the Concise

Oxford Dictionary Of Politics, [32], a Dictionary Of Critical Theory by Ian Buchanan, [33], the Penguin Dictionary Of Economics, [34], the Concise Gojri-English Dictionary by Dr. Rafeeq Anjum, [35], A Dictionary of the Kachin Language by Rev.O.Hanson, [36], A Dictionary Of World History by Edmund Wright, [37], Ekagi-Dutch-English-Indonesian Dictionary by J. Steltenpool, [38], A Dictionary of Plant Sciences by Michael Allaby, [39], respectively. The graphical law was pursued more in Along the side of the Onsager’s solution, the Ekagi language ,[40], Along the side of the Onsager’s solution, the Ekagi language-Part Three, [41], Oxford Dictionary of Biology by Robert S. Hine and the Graphical law, [42], A Dictionary of the Mikir Language by G. D. Walker and the Graphical law, [43], A Dictionary of Zoology by Michael Allaby and the Graphical Law, [44], Dictionary of all Scriptures and Myths by G. A. Gaskell and the Graphical Law, [45], Dictionary of Culinary Terms by Philippe Pilibossian and the Graphical law, [46], A Greek and English Lexicon by H.G.Liddle et al simplified by Didier Fontaine and the Graphical law, [47], Learner’s Mongol-English Dictionary and the Graphical law, [48], Complete Bulgarian-English Dictionary and the Graphical law, [49], A Dictionary of Sindhi Literature by Dr. Motilal Jotwani and the Graphical Law, [50], Penguin Dictionary of Physics, the Fourth Edition, by John Cullerne, and the Graphical law, [51], Oxford Dictionary of Chemistry, the seventh edition and the Graphical Law, [52], A Burmese-English Dictionary, Part I-Part V, by J. A. Stewart and C. W. Dunn et al, head words and the Graphical Law, [53], The Graphical Law behind the head words of Dictionary Kannada and English written by W. Reeve, revised, corrected and enlarged by Daniel Sanderson, [54], Sanchayita and the Graphical Law, [55], Samsad Bangla Abhidan and The Graphical Law, [56], Bangiya Sabdakosh and The Graphical Law, [57], Samsad Bengali-English Dictionary and The Graphical Law, [58], Rudyard Kipling’s Verse and the Graphical Law, [59], W. B. Yeats, The Poems and the Graphical Law, [60], The Penguin Encyclopedia of Places by W. G. Moore and the Graphical law, [61], The Poems of Tennyson and the Graphical Law, [62], Khasi-Jaintia Jaid(Surnames) and the Graphical law, [63], Age, Amplitude of accommodation and the Graphical law, [64], Dictionary of Ayurveda by Dr. Ravindra Sharma and the Graphical law, [65], The Practical Sanskrit-English Dictionary by Vaman Shivram Apte and The Graphical Law, [66], The Langenscheidt’s Pocket Russian Dictionary and The Graphical Law, [67], respectively.

The planning of the paper is as follows. In the next section, we describe the Graphical Law analysis of headwords of the Scholar Dictionary Portuguese, [1]. The section III, we give

an introduction to the standard curves of magnetisation of Ising model. The section IV is Acknowledgment. The last section is Bibliography.

## II. THE GRAPHICAL LAW ANALYSIS

For the purpose of exploring graphical law, we assort the letters according to the number of words, in the descending order, denoted by  $f$  and the respective rank, [68], denoted by  $k$ .  $k$  is a positive integer starting from one. Moreover, the minimum non-zero number of headwords is five. Hence, we attach a limiting word number one. The limiting rank is maximum rank plus one, here it is twenty seven. As a result both  $\frac{\ln f}{\ln f_{max}}$  and  $\frac{\ln k}{\ln k_{lim}}$  varies from zero to one. Then we tabulate in the adjoining table,II, and plot  $\frac{\ln f}{\ln f_{max}}$  against  $\frac{\ln k}{\ln k_{lim}}$  in the figure fig.3. We then ignore the letter with the highest number of headwords, tabulate in the adjoining table,II,and redo the plot, normalising the  $\ln f$ s with  $\ln f_{n-max}$ , and starting from  $k = 2$  in the figure fig.4. Normalising the  $\ln f$ s with  $\ln f_{2n-max}$ , we tabulate in the adjoining table,II, and starting from  $k = 3$  we draw in the figure fig.5. Normalising the  $\ln f$ s with  $\ln f_{3n-max}$  we record in the adjoining table,II, and plot starting from  $k = 4$  in the figure fig.6. In this way we obtain up to the figure fig.7.

k	lnk	lnk/ $lnk_{lim}$	f	lnf	lnf/ $lnf_{max}$	lnf/ $lnf_{nmax}$	lnf/ $lnf_{2nmax}$	lnf/ $lnf_{3nmax}$	lnf/ $lnf_{4nmax}$	lnf/ $lnf_{5nmax}$
1	0	0	3030	8.016	1	Blank	Blank	Blank	Blank	Blank
2	0.69	0.209	2886	7.968	0.994	1	Blank	Blank	Blank	Blank
3	1.10	0.333	2751	7.920	0.988	0.994	1	Blank	Blank	Blank
4	1.39	0.421	2243	7.716	0.963	0.968	0.974	1	Blank	Blank
5	1.61	0.488	2223	7.707	0.961	0.967	0.973	0.999	1	Blank
6	1.79	0.542	1651	7.409	0.924	0.930	0.935	0.960	0.961	1
7	1.95	0.591	1608	7.383	0.921	0.927	0.932	0.957	0.958	0.996
8	2.08	0.630	1572	7.360	0.918	0.924	0.929	0.954	0.955	0.993
9	2.20	0.667	1481	7.300	0.911	0.916	0.922	0.946	0.947	0.985
10	2.30	0.697	1283	7.157	0.893	0.898	0.904	0.928	0.929	0.966
11	2.40	0.727	1081	6.986	0.872	0.877	0.882	0.905	0.906	0.943
12	2.48	0.752	1041	6.948	0.867	0.872	0.877	0.900	0.902	0.938
13	2.56	0.776	811	6.698	0.836	0.841	0.846	0.868	0.869	0.904
14	2.64	0.800	807	6.693	0.835	0.840	0.845	0.867	0.868	0.903
15	2.71	0.821	685	6.529	0.814	0.819	0.824	0.846	0.847	0.881
16	2.77	0.839	538	6.288	0.784	0.789	0.794	0.815	0.816	0.849
17	2.83	0.858	520	6.254	0.780	0.785	0.790	0.811	0.811	0.844
18	2.89	0.876	344	5.841	0.729	0.733	0.738	0.757	0.758	0.788
19	2.94	0.891	224	5.412	0.675	0.679	0.683	0.701	0.702	0.730
20	3.00	0.909	206	5.328	0.665	0.669	0.673	0.691	0.691	0.719
21	3.04	0.921	193	5.263	0.657	0.661	0.665	0.682	0.683	0.710
22	3.09	0.936	74	4.304	0.537	0.540	0.543	0.558	0.558	0.581
23	3.14	0.952	52	3.951	0.493	0.496	0.499	0.512	0.513	0.533
24	3.18	0.964	26	3.258	0.406	0.409	0.411	0.422	0.423	0.440
25	3.22	0.976	16	2.773	0.346	0.348	0.350	0.359	0.360	0.374
26	3.26	0.988	5	1.609	0.201	0.202	0.203	0.209	0.209	0.217
27	3.30	1	1	0	0	0	0	0	0	0

TABLE II. The Scholar Dictionary Portuguese headwords: ranking, natural logarithms, normalizations

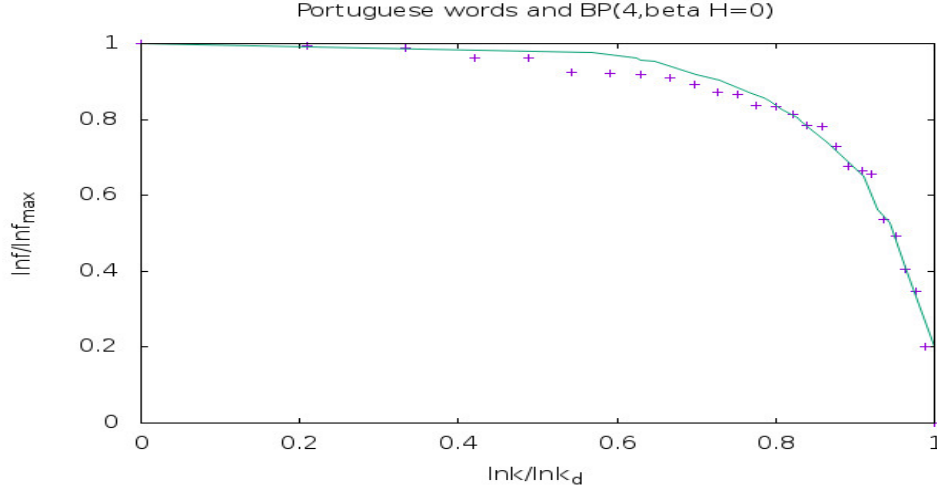


FIG. 2. The vertical axis is  $\frac{\ln f}{\ln f_{max}}$  and the horizontal axis is  $\frac{\ln k}{\ln k_{lim}}$ . The + points represent the headwords of the Scholar Dictionary Portuguese, with the fit curve  $BP(4, \beta H = 0)$ , being the Bethe-Peierls curve in the presence of four nearest neighbours and in the absence of external magnetic field,  $\beta H = 0$ .

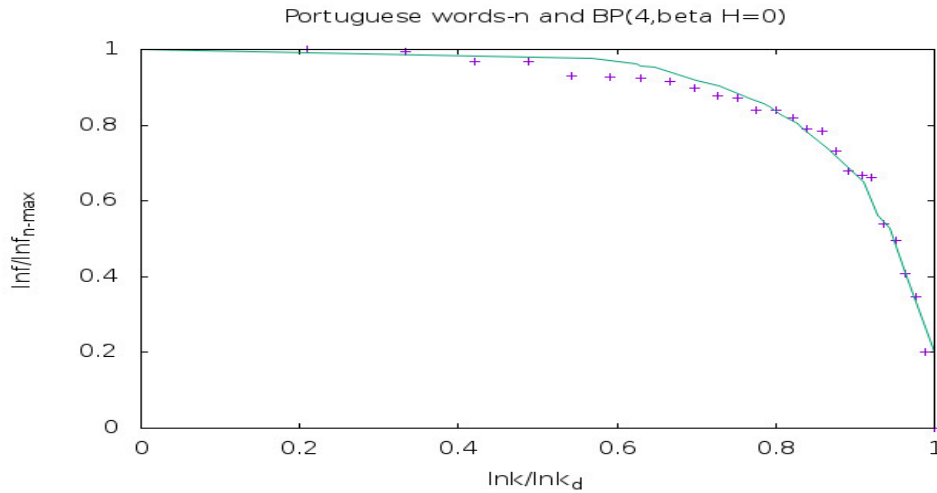


FIG. 3. The vertical axis is  $\frac{\ln f}{\ln f_{n-max}}$  and the horizontal axis is  $\frac{\ln k}{\ln k_{lim}}$ . The + points represent the headwords of the Scholar Dictionary Portuguese, with the fit curve  $BP(4, \beta H = 0)$ , being the Bethe-Peierls curve in the presence of four nearest neighbours and in the absence of external magnetic field,  $\beta H = 0$ .

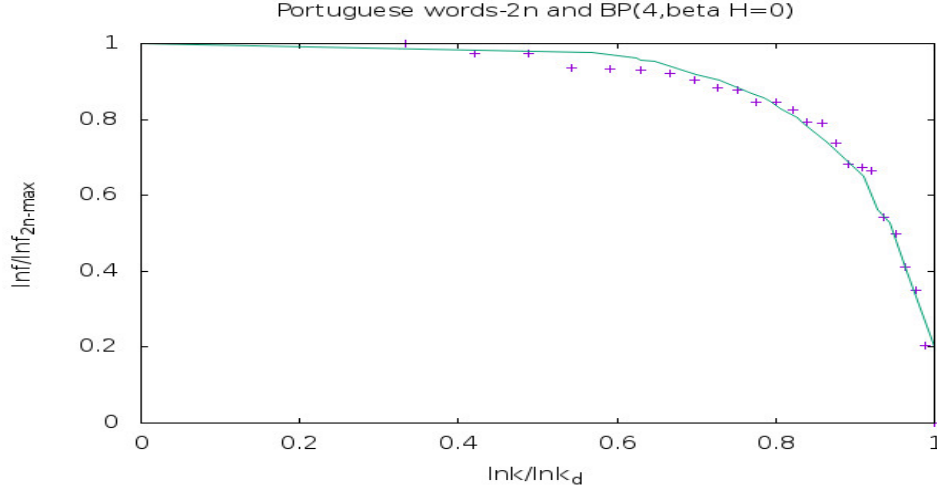


FIG. 4. The vertical axis is  $\frac{\ln f}{\ln f_{2n-max}}$  and the horizontal axis is  $\frac{\ln k}{\ln k_{lim}}$ . The + points represent the headwords of the Scholar Dictionary Portuguese, with the fit curve BP(4,  $\beta H = 0$ ), being the Bethe-Peierls curve in the presence of four nearest neighbours and in the absence of external magnetic field,  $\beta H = 0$ .

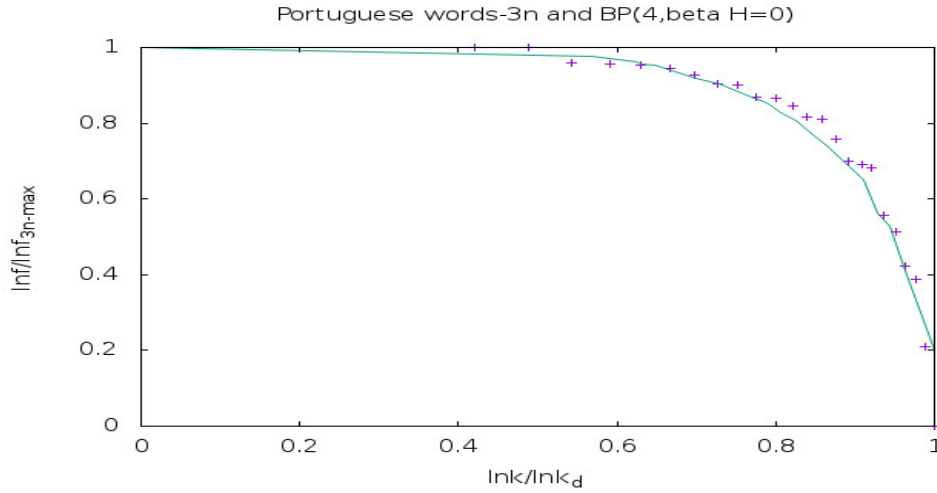


FIG. 5. The vertical axis is  $\frac{\ln f}{\ln f_{3n-max}}$  and the horizontal axis is  $\frac{\ln k}{\ln k_{lim}}$ . The + points represent the headwords of the Scholar Dictionary Portuguese, with the fit curve BP(4,  $\beta H = 0$ ), being the Bethe-Peierls curve in the presence of four nearest neighbours and in the absence of external magnetic field,  $\beta H = 0$ .



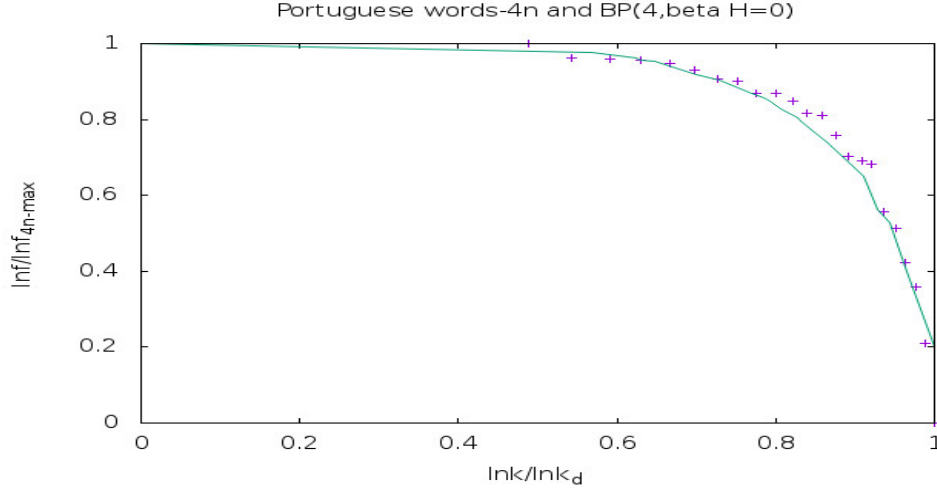


FIG. 6. The vertical axis is  $\frac{\ln f}{\ln f_{4n-max}}$  and the horizontal axis is  $\frac{\ln k}{\ln k_{lim}}$ . The + points represent the headwords of the Scholar Dictionary Portuguese, with the fit curve BP(4,  $\beta H = 0$ ), being the Bethe-Peierls curve in the presence of four nearest neighbours and in the absence of external magnetic field,  $\beta H = 0$ .

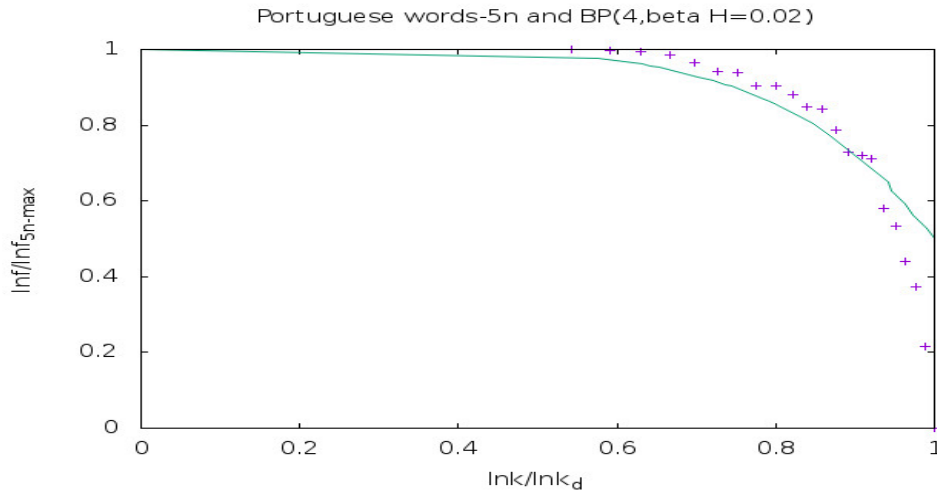


FIG. 7. The vertical axis is  $\frac{\ln f}{\ln f_{5n-max}}$  and the horizontal axis is  $\frac{\ln k}{\ln k_{lim}}$ . The + points represent the headwords of the Scholar Dictionary Portuguese, with the fit curve, BP(4,  $\beta H = 0.02$ ), being the Bethe-Peierls curve in the presence of four nearest neighbours and external magnetic field,  $m = 0.01$  or,  $\beta H = 0.02$ .

## A. conclusion

From the figures (fig.2-fig.7), we observe that there is a curve of magnetisation, behind the headwords of the Scholar Dictionary Portuguese,[1]. This is the magnetisation curve in the Bethe-Peierls approximation of the Ising model,  $BP(4, \beta H = 0)$ , in the presence of four nearest neighbours and in the absence of external magnetic field,  $\beta H = 0$ .

Moreover, the associated correspondence is,

$$\frac{\ln f}{\ln f_{2n-max}} \longleftrightarrow \frac{M}{M_{max}},$$
$$\ln k \longleftrightarrow T.$$

$k$  corresponds to temperature in an exponential scale, [75].

### III. APENDIX: MAGNETISATION

#### A. Bragg-Williams approximation

Let us consider a coin. Let us toss it many times. Probability of getting head or, tale is half i.e. we will get head and tale equal number of times. If we attach value one to head, minus one to tale, the average value we obtain, after many tossing is zero. Instead let us consider a one-sided loaded coin, say on the head side. The probability of getting head is more than one half, getting tale is less than one-half. Average value, in this case, after many tossing we obtain is non-zero, the precise number depends on the loading. The loaded coin is like ferromagnet, the unloaded coin is like para magnet, at zero external magnetic field. Average value we obtain is like magnetisation, loading is like coupling among the spins of the ferromagnetic units. Outcome of single coin toss is random, but average value we get after long sequence of tossing is fixed. This is long-range order. But if we take a small sequence of tossing, say, three consecutive tossing, the average value we obtain is not fixed, can be anything. There is no short-range order.

Let us consider a row of spins, one can imagine them as spears which can be vertically up or, down. Assume there is a long-range order with probability to get a spin up is two third. That would mean when we consider a long sequence of spins, two third of those are with spin up. Moreover, assign with each up spin a value one and a down spin a value minus one. Then total spin we obtain is one third. This value is referred to as the value of long-range order parameter. Now consider a short-range order existing which is identical with the long-range order. That would mean if we pick up any three consecutive spins, two will be up, one down. Bragg-Williams approximation means short-range order is identical with long-range order, applied to a lattice of spins, in general. Row of spins is a lattice of one dimension.

Now let us imagine an arbitrary lattice, with each up spin assigned a value one and a down spin a value minus one, with an unspecified long-range order parameter defined as above by  $L = \frac{1}{N}\sum_i\sigma_i$ , where  $\sigma_i$  is i-th spin, N being total number of spins. L can vary from minus one to one.  $N = N_+ + N_-$ , where  $N_+$  is the number of up spins,  $N_-$  is the number of down spins.  $L = \frac{1}{N}(N_+ - N_-)$ . As a result,  $N_+ = \frac{N}{2}(1 + L)$  and  $N_- = \frac{N}{2}(1 - L)$ . Magnetisation or, net magnetic moment ,  $M$  is  $\mu\sum_i\sigma_i$  or,  $\mu(N_+ - N_-)$  or,  $\mu NL$ ,  $M_{max} = \mu N$ .  $\frac{M}{M_{max}} = L$ .  $\frac{M}{M_{max}}$  is

referred to as reduced magnetisation. Moreover, the Ising Hamiltonian,[69], for the lattice of spins, setting  $\mu$  to one, is  $-\epsilon \sum_{n.n} \sigma_i \sigma_j - H \sum_i \sigma_i$ , where n.n refers to nearest neighbour pairs. The difference  $\Delta E$  of energy if we flip an up spin to down spin is, [70],  $2\epsilon\gamma\bar{\sigma} + 2H$ , where  $\gamma$  is the number of nearest neighbours of a spin. According to Boltzmann principle,  $\frac{N_-}{N_+}$  equals  $exp(-\frac{\Delta E}{k_B T})$ , [71]. In the Bragg-Williams approximation,[72],  $\bar{\sigma} = L$ , considered in the thermal average sense. Consequently,

$$\ln \frac{1+L}{1-L} = 2 \frac{\gamma\epsilon L + H}{k_B T} = 2 \frac{L + \frac{H}{\gamma\epsilon}}{\frac{T}{\gamma\epsilon/k_B}} = 2 \frac{L + c}{\frac{T}{T_c}} \quad (1)$$

where,  $c = \frac{H}{\gamma\epsilon}$ ,  $T_c = \gamma\epsilon/k_B$ , [73].  $\frac{T}{T_c}$  is referred to as reduced temperature.

Plot of  $L$  vs  $\frac{T}{T_c}$  or, reduced magnetisation vs. reduced temperature is used as reference curve. In the presence of magnetic field,  $c \neq 0$ , the curve bulges outward. Bragg-Williams is a Mean Field approximation. This approximation holds when number of neighbours interacting with a site is very large, reducing the importance of local fluctuation or, local order, making the long-range order or, average degree of freedom as the only degree of freedom of the lattice. To have a feeling how this approximation leads to matching between experimental and Ising model prediction one can refer to FIG.12.12 of [70]. W. L. Bragg was a professor of Hans Bethe. Rudolf Peierls was a friend of Hans Bethe. At the suggestion of W. L. Bragg, Rudolf Peierls following Hans Bethe improved the approximation scheme, applying quasi-chemical method.

## B. Bethe-peierls approximation in presence of four nearest neighbours, in absence of external magnetic field

In the approximation scheme which is improvement over the Bragg-Williams, [69],[70],[71],[72],[73], due to Bethe-Peierls, [74], reduced magnetisation varies with reduced temperature, for  $\gamma$  neighbours, in absence of external magnetic field, as

$$\frac{\ln \frac{\gamma}{\gamma-2}}{\ln \frac{factor-1}{factor^{\frac{\gamma-1}{\gamma}} - factor^{\frac{1}{\gamma}}}} = \frac{T}{T_c}; factor = \frac{\frac{M}{M_{max}} + 1}{1 - \frac{M}{M_{max}}} \quad (2)$$

$\ln \frac{\gamma}{\gamma-2}$  for four nearest neighbours i.e. for  $\gamma = 4$  is 0.693. For a snapshot of different kind of magnetisation curves for magnetic materials the reader is urged to give a google search "reduced magnetisation vs reduced temperature curve". In the following, we describe

BW	BW( $c=0.01$ )	BP(4, $\beta H = 0$ )	reduced magnetisation
0	0	0	1
0.435	0.439	0.563	0.978
0.439	0.443	0.568	0.977
0.491	0.495	0.624	0.961
0.501	0.507	0.630	0.957
0.514	0.519	0.648	0.952
0.559	0.566	0.654	0.931
0.566	0.573	0.7	0.927
0.584	0.590	0.7	0.917
0.601	0.607	0.722	0.907
0.607	0.613	0.729	0.903
0.653	0.661	0.770	0.869
0.659	0.668	0.773	0.865
0.669	0.676	0.784	0.856
0.679	0.688	0.792	0.847
0.701	0.710	0.807	0.828
0.723	0.731	0.828	0.805
0.732	0.743	0.832	0.796
0.756	0.766	0.845	0.772
0.779	0.788	0.864	0.740
0.838	0.853	0.911	0.651
0.850	0.861	0.911	0.628
0.870	0.885	0.923	0.592
0.883	0.895	0.928	0.564
0.899	0.918		0.527
0.904	0.926	0.941	0.513
0.946	0.968	0.965	0.400
0.967	0.998	0.965	0.300
0.987		1	0.200
0.997		1	0.100
1	1	1	0

TABLE III. Reduced magnetisation vs reduced temperature data s for Bragg-Williams approximation, in absence of and in presence of magnetic field,  $c = \frac{H}{\gamma\epsilon} = 0.01$ , and Bethe-Peierls approximation in absence of magnetic field, for four nearest neighbours.

data s generated from the equation(1) and the equation(2) in the table, III, and curves of magnetisation plotted on the basis of those data s. BW stands for reduced temperature in Bragg-Williams approximation, calculated from the equation(1). BP(4) represents reduced temperature in the Bethe-Peierls approximation, for four nearest neighbours, computed from the equation(2). The data set is used to plot fig.8. Empty spaces in the table, III, mean corresponding point pairs were not used for plotting a line.

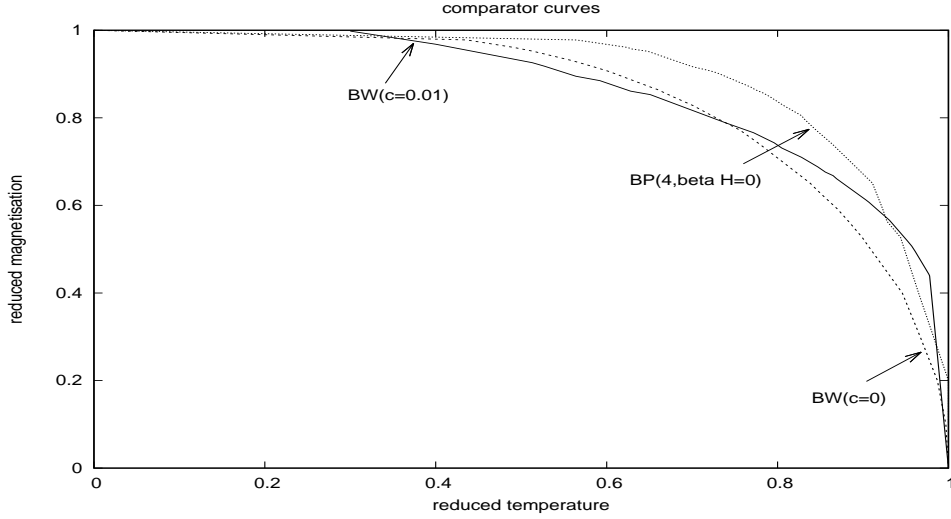


FIG. 8. Reduced magnetisation vs reduced temperature curves for Bragg-Williams approximation, in absence(dark) of and presence(inner in the top) of magnetic field,  $c = \frac{H}{\gamma\epsilon} = 0.01$ , and Bethe-Peierls approximation in absence of magnetic field, for four nearest neighbours (outer in the top).

### C. Bethe-peierls approximation in presence of four nearest neighbours, in the presence of external magnetic field

In the Bethe-Peierls approximation scheme , [74], reduced magnetisation varies with reduced temperature, for  $\gamma$  neighbours, in presence of external magnetic field, as

$$\frac{\ln \frac{\gamma}{\gamma-2}}{\ln \frac{e^{-\frac{2\beta H}{\gamma}} \text{factor}^{\frac{\gamma-1}{\gamma}} - e^{-\frac{2\beta H}{\gamma}} \text{factor}^{\frac{1}{\gamma}}}{\text{factor} - 1}} = \frac{T}{T_c}; \text{factor} = \frac{\frac{M}{M_{max}} + 1}{1 - \frac{M}{M_{max}}}. \quad (3)$$

Derivation of this formula ala [74] is given in the appendix of [7].

$\ln \frac{\gamma}{\gamma-2}$  for four nearest neighbours i.e. for  $\gamma = 4$  is 0.693. For four neighbours,

$$\frac{0.693}{\ln \frac{e^{-\frac{2\beta H}{\gamma}} \text{factor}^{\frac{\gamma-1}{\gamma}} - e^{-\frac{2\beta H}{\gamma}} \text{factor}^{\frac{1}{\gamma}}}{\text{factor} - 1}} = \frac{T}{T_c}; \text{factor} = \frac{\frac{M}{M_{max}} + 1}{1 - \frac{M}{M_{max}}}. \quad (4)$$

In the following, we describe datas in the table, IV, generated from the equation(4) and curves of magnetisation plotted on the basis of those datas. BP(m=0.03) stands for reduced temperature in Bethe-Peierls approximation, for four nearest neighbours, in presence of a variable external magnetic field, H, such that  $\beta H = 0.06$ . calculated from the equation(4). BP(m=0.025) stands for reduced temperature in Bethe-Peierls approximation, for four nearest neighbours, in presence of a variable external magnetic field, H, such that

$\beta H = 0.05$ . calculated from the equation(4). BP(m=0.02) stands for reduced temperature in Bethe-Peierls approximation, for four nearest neighbours, in presence of a variable external magnetic field, H, such that  $\beta H = 0.04$ . calculated from the equation(4). BP(m=0.01) stands for reduced temperature in Bethe-Peierls approximation, for four nearest neighbours, in presence of a variable external magnetic field, H, such that  $\beta H = 0.02$ . calculated from the equation(4). BP(m=0.005) stands for reduced temperature in Bethe-Peierls approximation, for four nearest neighbours, in presence of a variable external magnetic field, H, such that  $\beta H = 0.01$ . calculated from the equation(4). The data set is used to plot fig.9. Empty spaces in the table, IV, mean corresponding point pairs were not used for plotting a line.

BP(m=0.03)	BP(m=0.025)	BP(m=0.02)	BP(m=0.01)	BP(m=0.005)	reduced magnetisation
0	0	0	0	0	1
0.583	0.580	0.577	0.572	0.569	0.978
0.587	0.584	0.581	0.575	0.572	0.977
0.647	0.643	0.639	0.632	0.628	0.961
0.657	0.653	0.649	0.641	0.637	0.957
0.671	0.667		0.654	0.650	0.952
	0.716			0.696	0.931
0.723	0.718	0.713	0.702	0.697	0.927
0.743	0.737	0.731	0.720	0.714	0.917
0.762	0.756	0.749	0.737	0.731	0.907
0.770	0.764	0.757	0.745	0.738	0.903
0.816	0.808	0.800	0.785	0.778	0.869
0.821	0.813	0.805	0.789	0.782	0.865
0.832	0.823	0.815	0.799	0.791	0.856
0.841	0.833	0.824	0.807	0.799	0.847
0.863	0.853	0.844	0.826	0.817	0.828
0.887	0.876	0.866	0.846	0.836	0.805
0.895	0.884	0.873	0.852	0.842	0.796
0.916	0.904	0.892	0.869	0.858	0.772
0.940	0.926	0.914	0.888	0.876	0.740
	0.929			0.877	0.735
	0.936			0.883	0.730
	0.944			0.889	0.720
	0.945				0.710
	0.955			0.897	0.700
	0.963			0.903	0.690
	0.973			0.910	0.680
				0.909	0.670
	0.993			0.925	0.650
		0.976	0.942		0.651
	1.00				0.640
		0.983	0.946	0.928	0.628
		1.00	0.963	0.943	0.592
			0.972	0.951	0.564
			0.990	0.967	0.527
			1.00	0.964	0.513
				1.00	0.500
					0.400
					0.300
					0.200
					0.100
					0

TABLE IV. Bethe-Peierls approx. in presence of little external magnetic fields

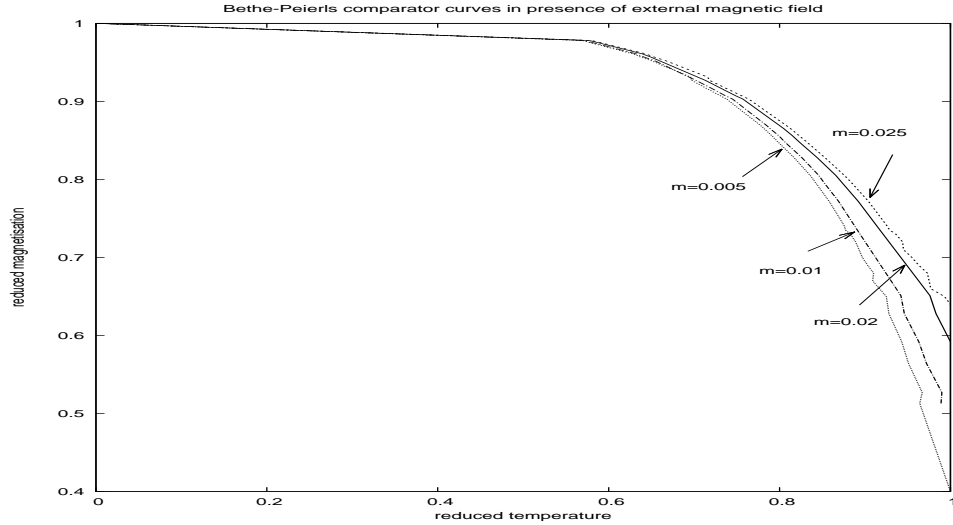


FIG. 9. Reduced magnetisation vs reduced temperature curves for Bethe-Peierls approximation in presence of little external magnetic fields, for four nearest neighbours, with  $\beta H = 2m$ .



#### IV. ACKNOWLEDGMENT

We have used gnuplot for plotting the figures in this paper.

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- [1] Scholar Dictionary Portuguese, English-Portuguese Portuguese-English, Martins Fontes, First Indian Edition: 2016, Goyal Publishers and Distributors Pvt. Ltd., 86, U.B. Jawahar Nagar, Kamla Nagar, Delhi-110007(India); ISBN: 978-81-8307-790-3.
  - [2] Anindya Kumar Biswas, "Graphical Law beneath each written natural language", arXiv:1307.6235v3[physics.gen-ph]. A preliminary study of words of dictionaries of twenty six languages, more accurate study of words of dictionary of Chinese usage and all parts of speech of dictionary of Lakher(Mara) language and of verbs, adverbs and adjectives of dictionaries of six languages are included.
  - [3] Anindya Kumar Biswas, "A discipline of knowledge and the graphical law", IJARPS Volume 1(4), p 21, 2014; viXra: 1908:0090[Linguistics].
  - [4] Anindya Kumar Biswas, "Bengali language and Graphical law", viXra: 1908:0090[Linguistics].
  - [5] Anindya Kumar Biswas, "Basque language and the Graphical Law", viXra: 1908:0414[Linguistics].
  - [6] Anindya Kumar Biswas, "Romanian language, the Graphical Law and More", viXra: 1909:0071[Linguistics].
  - [7] Anindya Kumar Biswas, "Discipline of knowledge and the graphical law, part II", viXra:1912.0243 [Condensed Matter],International Journal of Arts Humanities and Social Sciences Studies Volume 5 Issue 2 February 2020.
  - [8] Anindya Kumar Biswas, "Onsager Core of Abor-Miri and Mising Languages", viXra: 2003.0343[Condensed Matter].
  - [9] Anindya Kumar Biswas, "Bengali language, Romanisation and Onsager Core", viXra: 2003.0563[Linguistics].
  - [10] Anindya Kumar Biswas, "Little Oxford English Dictionary and the Graphical Law", viXra: 2008.0041[Linguistics].
  - [11] Anindya Kumar Biswas, "Oxford Dictionary Of Social Work and Social Care and the Graphical law", viXra: 2008.0077[Condensed Matter].

- [12] Anindya Kumar Biswas, "Visayan-English Dictionary and the Graphical law", viXra: 2009.0014[Linguistics].
- [13] Anindya Kumar Biswas, "Garo to English School Dictionary and the Graphical law", viXra: 2009.0056[Condensed Matter].
- [14] Anindya Kumar Biswas, "Mursi-English-Amharic Dictionary and the Graphical law", viXra: 2009.0100[Linguistics].
- [15] Anindya Kumar Biswas, "Names of Minor Planets and the Graphical law", viXra: 2009.0158[History and Philosophy of Physics].
- [16] Anindya Kumar Biswas, "A Dictionary of Tibetan and English and the Graphical law", viXra: 2010.0237[Condensed Matter].
- [17] Anindya Kumar Biswas, "Khasi English Dictionary and the Graphical law", viXra: 2011.0011[Linguistics].
- [18] Anindya Kumar Biswas, "Turkmen-English Dictionary and the Graphical law", viXra: 2011.0069[Linguistics].
- [19] Anindya Kumar Biswas, " Webster's Universal Spanish-English Dictionary, the Graphical law and A Dictionary of Geography of Oxford University Press", viXra: 2103.0175[Condensed Matter].
- [20] Anindya Kumar Biswas, "A Dictionary of Modern Italian, the Graphical law and Dictionary of Law and Administration, 2000, National Law Development Foundation", viXra: 2107.0171[Condensed Matter].
- [21] Anindya Kumar Biswas, "Langenscheidt's German-English English-German Dictionary and the Graphical law", viXra: 2107.0179[Linguistics].
- [22] Anindya Kumar Biswas, "Essential Dutch dictionary by G. Quist and D. Strik, the Graphical law Classification", viXra: 2108.0040[Linguistics].
- [23] Anindya Kumar Biswas, "Swahili, a lingua franca, Swahili-English Dictionary by C. W. Rechenbach and the Graphical law", viXra: 2108.0101[Linguistics].
- [24] Anindya Kumar Biswas, "The French, Larousse Dictionnaire De Poche and the Graphical law", viXra: 2109.0080[Linguistics].
- [25] Anindya Kumar Biswas, "An Arabic dictionary: "al-Mujam al-wáfi" or, "adhunik arabi-bangla abhidhan" and the Onsager's solution", viXra: 2109.0119[Condensed Matter].

- [26] Anindya Kumar Biswas, "Langenscheidt Taschenwörterbuch Deutsch-Englisch / Englisch-Deutsch, Völlige Neubearbeitung and the Graphical law", viXra: 2109.0141[Linguistics].
- [27] Anindya Kumar Biswas, Bawansuk Lyngkhai, "The Graphical law behind the NTC's Hebrew and English Dictionary by Arie Comey and Naomi Tsur", viXra: 2109.0164[Linguistics].
- [28] Anindya Kumar Biswas, "Oxford Dictionary Of Media and Communication and the Graphical law", viXra: 2109.0202[Social Science].
- [29] Anindya Kumar Biswas, "Oxford Concise Dictionary Of Mathematics, Penguin Dictionary Of Mathematics and the Graphical law", viXra: 2112.0054[Social Science].
- [30] Anindya Kumar Biswas, "An Arabic dictionary: "al-Mujam al-wáfi" or, "adhunik arabi-bangla abhidhan" and the Onsager's solution Second part", viXra: 2201.0021[Condensed Matter].
- [31] Anindya Kumar Biswas, "The Penguin Dictionary Of Sociology and the Graphical law", viXra: 2201.0046[Social Science].
- [32] Anindya Kumar Biswas, "The Concise Oxford Dictionary Of Politics and the Graphical law", viXra: 2201.0069[Social Science].
- [33] Anindya Kumar Biswas, "A Dictionary Of Critical Theory by Ian Buchanan and the Graphical law", viXra: 2201.0136[Social Science].
- [34] Anindya Kumar Biswas, "The Penguin Dictionary Of Economics and the Graphical law", viXra: 2201.0169[Economics and Finance].
- [35] Anindya Kumar Biswas, "The Concise Gojri-English Dictionary by Dr. Rafeeq Anjum and the Graphical law", viXra: 2201.0205[Linguistics].
- [36] Anindya Kumar Biswas, "A Dictionary of the Kachin Language by Rev.O.Hanson and the Graphical law" ("A Dictionary of the Kachin Language by Rev.o.Hanson and the Graphical law", viXra: 2202.0030[Linguistics]).
- [37] Anindya Kumar Biswas, "A Dictionary Of World History by Edmund Wright and the Graphical law", viXra: 2202.0130[History and Philosophy of Physics].
- [38] Anindya Kumar Biswas, "Ekagi-Dutch-English-Indonesian Dictionary by J. Steltenpool and the Onsager's solution", viXra: 2202.0157[Condensed Matter].
- [39] Anindya Kumar Biswas, "A Dictionary of Plant Sciences by Michael Allaby and the Graphical law", viXra: 2203.0011[Mind Science].
- [40] Anindya Kumar Biswas, "Along the side of the Onsager's solution, the Ekagi language", viXra: 2205.0065[Condensed Matter].

- [41] Anindya Kumar Biswas, "Along the side of the Onsager's solution, the Ekagi language-Part Three", viXra: 2205.0137[Condensed Matter].
- [42] Anindya Kumar Biswas, "Oxford Dictionary of Biology by Robert S. Hine and the Graphical law", viXra: 2207.0089[Physics of Biology].
- [43] Anindya Kumar Biswas, "A Dictionary of the Mikir Language by G. D. Walker and the Graphical law", viXra: 2207.0165[Linguistics].
- [44] Anindya Kumar Biswas, "A Dictionary of Zoology by Michael Allaby and the Graphical law", viXra: 2208.0075[Physics of Biology].
- [45] Anindya Kumar Biswas, "Dictionary of all Scriptures and Myths by G. A. Gaskell and the Graphical law", viXra: 2208.0093[Religion and Spiritualism].
- [46] Anindya Kumar Biswas, "Dictionary of Culinary Terms by Philippe Pilibossian and the Graphical law", viXra: 2211.0061[Social Sciences].
- [47] Anindya Kumar Biswas, "A Greek and English Lexicon by H.G.Liddle et al simplified by Didier Fontaine and the Graphical law", viXra: 2211.0087[Linguistics].
- [48] Anindya Kumar Biswas, "Learner's Mongol-English Dictionary and the Graphical law", viXra: 2211.0101[Linguistics].
- [49] Anindya Kumar Biswas, "Complete Bulgarian-English Dictionary and the Graphical law", viXra: 2212.0009[Linguistics].
- [50] Anindya Kumar Biswas, "A Dictionary of Sindhi Literature by Dr. Motilal Jotwani and the Graphical Law", viXra: 2212.0015[Social Sciences].
- [51] Anindya Kumar Biswas, "Penguin Dictionary of Physics, the Fourth Edition, by John Cullerne, and the Graphical law", viXra: 2212.0072[History and Philosophy of Physics].
- [52] Anindya Kumar Biswas, "Oxford Dictionary of Chemistry, the seventh edition and the Graphical Law", viXra: 2212.0113[Chemistry].
- [53] Anindya Kumar Biswas, "A Burmese-English Dictionary, Part I-Part V, by J. A. Stewart and C. W. Dunn et al, head words and the Graphical Law", viXra: 2212.0127[Linguistics].
- [54] Anindya Kumar Biswas, "The Graphical Law behind the head words of Dictionary Kannada and English written by W. Reeve, revised, corrected and enlarged by Daniel Sanderson", viXra: 2212.0185[Linguistics].
- [55] Anindya Kumar Biswas, "Sanchayita and the Graphical Law", viXra: 2301.0075[Social Science].

- [56] Anindya Kumar Biswas, "Samsad Bangla Abhidan and The Graphical Law", viXra: 2302.0026[Linguistics].
- [57] Anindya Kumar Biswas, "Bangiya Sabdakosh and The Graphical Law", viXra: 2302.0060[Linguistics].
- [58] Anindya Kumar Biswas, "Samsad Bengali-English Dictionary and The Graphical Law ", viXra: 2304.0047[Linguistics].
- [59] Anindya Kumar Biswas, "Rudyard Kipling's Verse and the Graphical Law", viXra: 2304.0207[Social Science].
- [60] Anindya Kumar Biswas, "W. B. Yeats, The Poems and the Graphical Law", viXra: 2305.0008[Social Science].
- [61] Anindya Kumar Biswas, "The Penguin Encyclopedia of Places by W. G. Moore and the Graphical Law", viXra: 2305.0147[Archaeology].
- [62] Anindya Kumar Biswas, "The Poems of Tennyson and the Graphical Law", viXra: 2305.0157[Social Science].
- [63] Anindya Kumar Biswas, "Khasi-Jaintia Jaidis(Surnames) and the Graphical law", viXra:2307.0135[Social Science].
- [64] Anindya Kumar Biswas, "Age, Amplitude of accommodation and the Graphical law", viXra:2311.0110[Physics of Biology].
- [65] Anindya Kumar Biswas, "Dictionary of Ayurveda by Dr. Ravindra Sharma and the Graphical law", viXra:2401.0030[General Science and Philosophy].
- [66] Anindya Kumar Biswas, "The Practical Sanskrit-English Dictionary by Vaman Shivram Apte and The Graphical Law", viXra:2402.0041[Linguistics].
- [67] Anindya Kumar Biswas, "The Langenscheidt's Pocket Russian Dictionary and The Graphical Law", to appear
- [68] A. M. Gun, M. K. Gupta and B. Dasgupta, Fundamentals of Statistics Vol 1, Chapter 12, eighth edition, 2012, The World Press Private Limited, Kolkata.
- [69] E. Ising, Z.Physik 31,253(1925).
- [70] R. K. Pathria, Statistical Mechanics, p400-403, 1993 reprint, Pergamon Press,© 1972 R. K. Pathria.
- [71] C. Kittel, Introduction to Solid State Physics, p. 438, Fifth edition, thirteenth Wiley Eastern Reprint, May 1994, Wiley Eastern Limited, New Delhi, India.

- [72] W. L. Bragg and E. J. Williams, Proc. Roy. Soc. A, vol.145, p. 699(1934);
- [73] P. M. Chaikin and T. C. Lubensky, Principles of Condensed Matter Physics, p. 148, first edition, Cambridge University Press India Pvt. Ltd, New Delhi.
- [74] Kerson Huang, Statistical Mechanics, second edition, John Wiley and Sons(Asia) Pte Ltd.
- [75] Sonntag, Borgnakke and Van Wylen, Fundamentals of Thermodynamics, p206-207, fifth edition, John Wiley and Sons Inc.