

An interpretation of the Fine Structure Constant formula founded by Hans de Vries

by Reinhard Kronberger

Abstract

The formula found by Hans de Vries for the fine structure constant is very elegant and accurate but there exists no explanation for it. In this paper, I try to give an interpretation. It is also shown why we have an electromagnetic field and why we have the value for the fine structure constant.

Email : simplemind1@gmx.at

Home : <https://www.standardmodell.at/>

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The Hans de Vries formula :

$$\alpha = \Gamma^2 \cdot e^{-\frac{\pi^2}{2}}$$

where $\Gamma = 1 + \frac{\alpha}{(2\pi)^0} (1 + \frac{\alpha}{(2\pi)^1} (1 + \frac{\alpha}{(2\pi)^2} (1 + \dots$

Someone can prove that the HdV formula is identical to

$$\alpha = \left[\sum_{n=0}^{\infty} \frac{\alpha^n}{(2\pi)^{\binom{n}{2}}} \right]^2 \cdot e^{-\frac{\pi^2}{2}}$$

then

$$\sqrt{\alpha} = \sum_{n=0}^{\infty} \frac{\alpha^n}{(2\pi)^{\binom{n}{2}}} \cdot e^{-\frac{\pi^2}{4}} = \underbrace{\left(1 + 1 \cdot \frac{\alpha}{(2\pi)^0} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} \cdot \frac{\alpha}{(2\pi)^2} + \dots \right)} \cdot e^{-\frac{\pi^2}{4}}$$

The challenge now is to interpret this formula.

The factor $e^{-\frac{\pi^2}{4}}$ looks like the expectation value of the wrapped normal distribution which is

$$\langle z \rangle = e^{i\mu - \frac{\sigma^2}{2}} = e^{-\frac{\pi^2}{4}} \quad \text{for } \mu = 0 \text{ and } \sigma = \frac{\pi}{\sqrt{2}}$$

see https://en.wikipedia.org/wiki/Wrapped_normal_distribution

And the factor

$$\left(1 + 1 \cdot \frac{\alpha}{(2\pi)^0} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} \cdot \frac{\alpha}{(2\pi)^2} + \dots \right)$$

looks like the series of conditional probabilities.

more concrete (details see https://en.wikipedia.org/wiki/Conditional_probability)

$$\sqrt{\alpha} = \sum_{n=1}^{\infty} P(A_1 \cap \dots \cap A_n) = \underbrace{\left(1 + 1 \cdot \frac{\alpha}{(2\pi)^0} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} \cdot \frac{\alpha}{(2\pi)^2} + \dots \right)} \cdot e^{-\frac{\pi^2}{4}}$$

with

$$P(A_1 \cap \dots \cap A_n) = P(A_1) \cdot P(A_2|A_1) \cdot P(A_3|A_1 \cap A_2) \dots P(A_n|A_1 \cap \dots \cap A_{n-1}) = \frac{\alpha^{n-1}}{(2\pi)^{\binom{n-1}{2}}} \cdot e^{-\frac{\pi^2}{4}}$$

$$e^{-\frac{\pi^2}{4}} \quad \frac{\alpha}{(2\pi)^0} \quad \frac{\alpha}{(2\pi)^1} \quad \frac{\alpha}{(2\pi)^{n-2}}$$

the denominator of $\frac{\alpha}{(2\pi)^i}$ looks like the i -dimensional 'volume' of a torus therefore

the factors $\frac{1}{(2\pi)^i}$ can be seen as normalization factors.

To understand the HdV formula we have to understand the two questions

- 1) what is A_1, A_2, A_3, \dots
- 2) why we have these values for the probabilities $P(A_1 \cap \dots \cap A_n)$

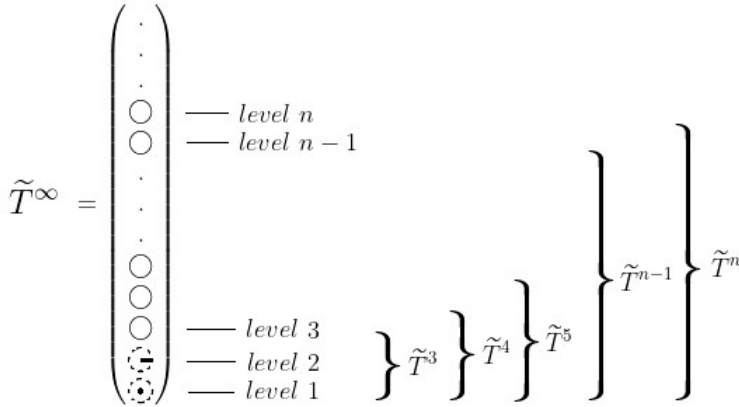
understanding question 1)

Normally a n -dimensional torus is defined as $T^n := S^1 \times \dots \times S^1 = (S^1)^n$
 But in our formular we have two denominators which have the dimension of a point and a line.

Therefore we define the torus as

$$\tilde{T}^n := \{0\} \times [0, 1] \times S^1 \times \dots \times S^1 = \{0\} \times [0, 1] \times (S^1)^{n-2}$$

The infinit torus \tilde{T}^∞ then can be seen as infinit ladder.



With this geometrical picture we can explain our probability sum.

$P(\text{absorbing or emitting a photon}) = P(\pm\gamma) = \sqrt{\alpha}$ is given by the different levels of the \tilde{T}^∞ .

A photon is emitted when we climb down from one level to the prior level.

or is absorbed when we climb up on the torusladder one step from one level to the next

Our events A_1, A_2, \dots are then

$A_1 \dots$ absorbing a photon by climbing up to level 1 from vacuum or emitting a photon by climbing down from level 1 to vacuum

$A_2 \dots$ absorbing a photon by climbing up to level 2 from level 1 or emitting a photon by climbing down from level 2 to level 1.

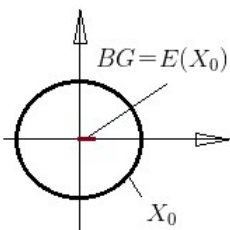
and so on.

\Rightarrow understood question 1)

understanding question 2)

We call the factor $e^{-\frac{\pi^2}{4}}$ the Basic-Generator of the electromagnetic field (short BG).

Explanation and visualisation of the Basic Generator BG.



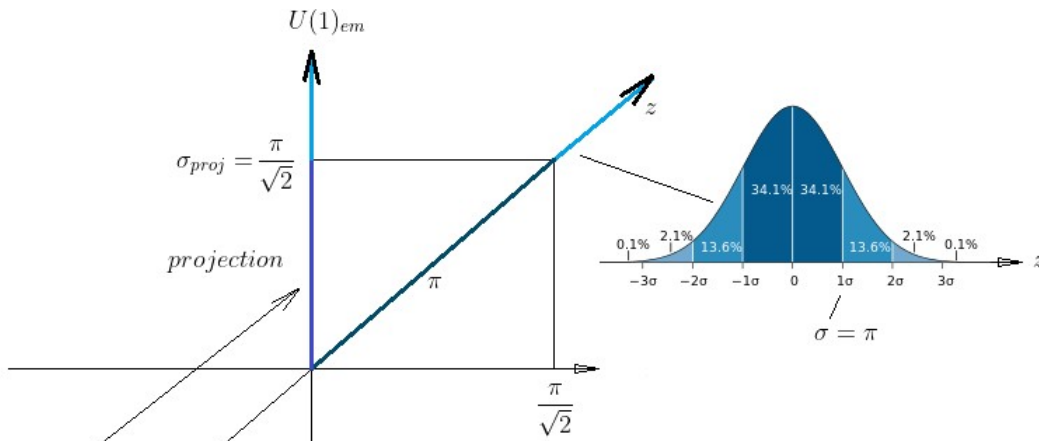
$BG = E(X_0) =$ expectation value of the wrapped normal distribution which is

$$\langle z \rangle = e^{i\mu - \frac{\sigma^2}{2}} = e^{-\frac{\pi^2}{4}} \quad \text{for } \mu = 0 \text{ and } \sigma = \frac{\pi}{\sqrt{2}}$$

see https://en.wikipedia.org/wiki/Wrapped_normal_distribution

We write $E(X_0) = e^{-\frac{\pi^2}{4}}$ $X_0 = \{x \mid x = e^{i\theta}, 0 \leq \theta < 2\pi\}$

The factor $\frac{\pi}{\sqrt{2}}$ comes from a projection of a distribution with standard deviation $\sigma = \pi$.



the projective normaldistribution with $\sigma = \frac{\pi}{\sqrt{2}}$
then will be wrapped.

Schematic representation of the formular and its probabilities

the probability to absorb a photon is :

$$\sqrt{\alpha} = e^{-\frac{\pi^2}{4}} + e^{-\frac{\pi^2}{4}} \cdot \frac{\alpha}{(2\pi)^0} + e^{-\frac{\pi^2}{4}} \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} + e^{-\frac{\pi^2}{4}} \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} \cdot \frac{\alpha}{(2\pi)^2} + e^{-\frac{\pi^2}{4}} \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} \cdot \frac{\alpha}{(2\pi)^2} \cdot \frac{\alpha}{(2\pi)^3} + \dots$$

$P(A_5 | A_1 \cap A_2 \cap A_3 \cap A_4)$

$P(A_1)$ $P(A_1 \cap A_2)$ $P(A_1 \cap A_2 \cap A_3)$ $P(A_1 \cap A_2 \cap A_3 \cap A_4)$ $P(A_1 \cap A_2 \cap A_3 \cap A_4 \cap A_5)$

level 1 level 2 level 3 level 4 level 5

possible excitations ■

How to understand the single components, the multipliers of $P(A_1 \cap \dots \cap A_n)$?

We want to restrict our examinations on the case of absorbing a photon.
For that we have to understand that a photon can only be absorbed if another source is emitting a photon.

We have two different types of possible sources.

- 1) the vacuum
- 2) a second particle with EM charge

For example the multipliers of $P(A_1 \cap A_2 \cap A_3)$

As we have seen above

$$P(A_1 \cap A_2 \cap A_3) = P(A_1) \cdot P(A_2 | A_1) \cdot P(A_3 | A_1 \cap A_2) = e^{-\frac{\pi^2}{4}} \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1}$$

We have multipliers without α and with α

$$e^{-\frac{\pi^2}{4}} \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1}$$

The first without α has the vacuum as source for emitting a photon and the one with α has another EM charged particle as source for emitting a photon.

So we have the picture of source and sink in the HdV formular.

We observe the sink and say that we have the vacuum and another EM charged particle as possible sources.

What does the multipliers with α express?

To understand this we split the multipliers in two components $\frac{\alpha}{(2\pi)^i} = \frac{\sqrt{\alpha}}{(2\pi)^i} \cdot \sqrt{\alpha}$

The first component is the probability that the sink absorbs a photon

(if the level = $i + 1$ is already reached) and

the second component is the probability that the source emit a photon

It does not matter on which level the source emit the photon so the probability is $\sqrt{\alpha}$.

How can we understand the probability $\frac{\sqrt{\alpha}}{(2\pi)^i}$ (the sink absorbs a photon on level $i+1$)?

Actually i only can give a hint for that.

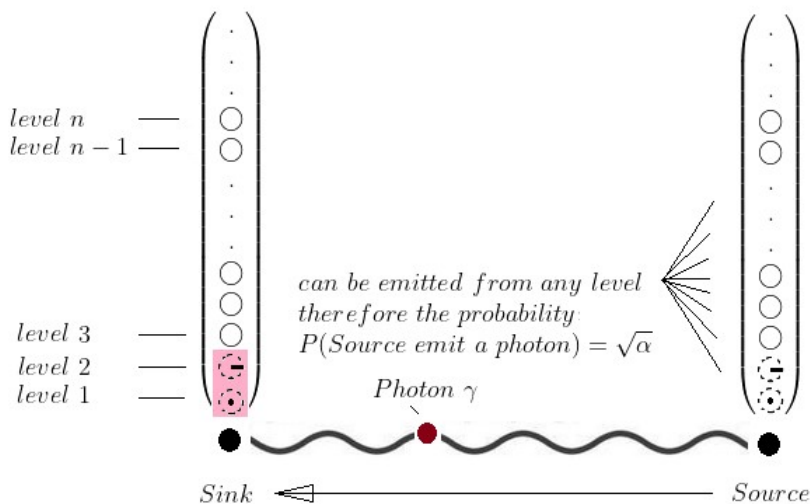
For the probability that the source emit a photon we can write

$$\sqrt{\alpha} = \frac{\sqrt{\alpha}}{1} = \frac{\sqrt{\alpha}}{\text{volumne}(\tilde{T}^{i+2})} \cdot (2\pi)^i$$

Now the sink absorbs the photon on a volumne $(2\pi)^i$ of the torus \tilde{T}^{i+2} which is $(2\pi)^i$ times bigger as volumne = 1 so the probability is getting smaller to $\frac{\sqrt{\alpha}}{(2\pi)^i}$

$$\sqrt{\alpha} = \frac{\sqrt{\alpha}}{1}$$

Schematic representation



the sink is in the state of level 2 before absorbing the photon.

after absorbing the photon the state is level 3.

the probability to reach level 2 is $P(A_1 \cap A_2) = e^{-\frac{\pi^2}{4}} \cdot \frac{\alpha}{(2\pi)^0}$

to climb from level 2 to level 3 the source must

- 1) emit a photon by probability $\sqrt{\alpha}$ and
- 2) the sink must absorb the photon by probability $\frac{\sqrt{\alpha}}{(2\pi)^1}$

therefore the probability to change the excitation from level 2 to level 3

$$\text{is } \frac{\sqrt{\alpha}}{(2\pi)^1} \sqrt{\alpha}$$

this explains the factor

$$P(A_1 \cap A_2 \cap A_3) = e^{-\frac{\pi^2}{4}} \cdot \frac{\alpha}{(2\pi)^0} \boxed{\frac{\alpha}{(2\pi)^1}} = e^{-\frac{\pi^2}{4}} \cdot \frac{\alpha}{(2\pi)^0} \boxed{\frac{\sqrt{\alpha}}{(2\pi)^1} \sqrt{\alpha}}$$

\Rightarrow understood question 2)

Last but not least the value for the Finestructure Constant by the Hans de Vries formular.

I have cutted the sum on $n = 100$ and calculated the result by iteration.

$$\alpha = \left[\sum_{n=0}^{\infty} \frac{\alpha^n}{(2\pi)^{\binom{n}{2}}} \right]^2 \cdot e^{-\frac{\pi^2}{2}}$$

$$\alpha \approx 0,0072973525686 \approx \frac{1}{137,035\,999\,096}$$

Value for α by Wikipedia

$$\alpha = 0,0072973525693(11)$$

The calculated value by the HdV formular fits very good to the empirical measurements.