

Riemann hypothesis

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Abstract

This short paper is about the nontrivial zeros of Riemann's zeta function.

Assume $\xi(z)$ is the real part of a nontrivial zero between $0 < \text{Re}(z) < 1$

define:

$$\xi(z) = 1/2 z (1 - z) \pi^{-z/2} \Gamma(z/2) \zeta(z)$$

which satisfies the reflection formula

$$\xi(z) = \xi(1 - z)$$

if we put in any real part between $0 < \text{Re}(z) < 1$ in the reflection formula

$$\xi(0) = \xi(1) = 1/2$$

the only invariant real part in $\xi(z)$ is $\text{Re}(z) = 1/2$

$$\xi(1/2) = \xi(1/2)$$

because $\text{Re}(z) = 1/2$ is the real part of a nontrivial zero and $\text{Re}(z) = 1/2$ is invariant in $\xi(z)$, the real part of every nontrivial zero of the Riemann zeta function is invariant at $1/2$.

References:

https://en.wikipedia.org/wiki/Riemann_Xi_function