

1 Optimum Solution to Global Warming due to a Greenhouse Gas-Albedo Hotspot Theorem

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5 **Key Words:** Albedo Solution, Global Warming Solution, Global Warming Re-radiation Model,, Hotspot Mitigation, UHI Global
6 Warming Estimates
7

8 Abstract

9 In this paper we suggest that a fundamental GHG-albedo hotspot surface theorem, when applied to the
10 reality of today's climate challenges, appears to indicate that the albedo solution would be the optimum
11 and safest way to mitigate climate change. The theorem also indicates that CO2 solutions has an
12 associated risk in stopping climate change. We also detail the albedo-GHG factor is detailed.

13 1. Introduction

14 Since GHGs need long wavelength radiation to work, then changing a hotspot surfaces albedo is
15 associated with the greenhouse gas mechanism. Therefore, we can devise *a greenhouse gas (GHG)*
16 *albedo hotspot surface theorem* stating:

- 17 • *Increasing the reflectivity of a hotspot surface has the same effect as reducing greenhouse gases*
- 18 • *Decreasing the reflectivity of a hotspot surface has the same effect as increasing greenhouse*
19 *gases*
- 20 • *The global warming change associated with the reflectivity hotspot change is given by the*
21 *albedo-GHG radiation factor having an approximate value of 1.6.*

22 This fundamental theorem is important because it leads one to the reality that conservatively, the albedo
23 solution is our fastest and safest method to stop climate change. There have been a number of
24 geoengineering resolutions proposed [1-3] that are either atmospheric or surface-based.

25 The reflectivity solution is safest because of

- 26 • the slow progress reported in GHG reduction
- 27 • the yearly increases in reports on large desertification and deforestation occurring [4]
- 28 • UHI hotspot contested issues
- 29 • Lack of hotspot and hydro-hotspot control [5]
- 30 • CO2 solutions are not guaranteed to be optimum
- 31 • this theorem indicates the albedo solution has minimal risk [6]

32 To clarify the last items, many authors have contested that a significant portion of global warming is due
33 to UHIs. This is now confirmed both with measurements [7-18] and more recently assessed in modeling
34 [5,19]. Furthermore, humankind has a lack of hotspot controls in the construction of UHIs and impermeable
35 surfaces which are increasing with population [5, 19] growth. We have two key forcing issues, hotspots
36 and greenhouse gas issues. Hydro-hotspots [5, 20] also increase local atmospheric water vapor GHG in
37 the presence of precipitation. This is not well understood in its contribution to global warming. However,
38 we do know that cities in humid environments are hotter [21]. Therefore, CO₂ solutions themselves are
39 not guarantee to mitigating global warming and puts our planet at risk. ***Yet, the albedo solution must***
40 ***according to this theorem, guarantee success with little if any risk.*** The albedo solution would also

41 promote hotspot controls reducing the inherent global warming. Guaranteeing success is not only
 42 important for real-world implementing solutions but also for optimum financial success.

43 One aspect of that is of interest is to demonstrate the albedo-GHG radiation 1.6 factor [5] and its change
 44 since the pre-industrial revolution. Such values relates to the effective emissivity constant of the planetary
 45 system β^4 . Because of its importance as it relates to the albedo-GHG mechanism, it is a primary focus in
 46 the rest of this paper.

47 2. Albedo-GHG Radiation Global Warming Pre-Industrial Factor

48
 49 When initial solar absorption occurs, part of the long wavelength radiation given off is re-radiated back to
 50 Earth. In the absence of forcing we denote this fraction as f_1 . This presents a simplistic but effective
 51 model

$$52$$

$$53 \quad P_{Pre-Industrial} = P_\alpha + P_{GHG} = P_\alpha + f_1 P_\alpha = P_\alpha (1 + f_1) = 1.618034 P_\alpha = \sigma T_s^4 \quad (1)$$

54 where

$$55 \quad P_\alpha = \frac{S_0}{4} (1 - \alpha) \quad (2)$$

56
 57 and T_s is the surface temperature. As one might suspect, f_1 turns out to be exactly β^4 in the absence of
 58 forcing, so that f_1 is a redefined variable taken from the effective emissivity constant of the planetary
 59 system. We identify this as 0.618034 [5] in the next section.

60 2.1 Basic Re-radiation Model and Estimating f_1

61
 62 In geoengineering, we are working with absorption and re-radiation, we define

$$63 \quad P_{Total} = \sigma T_s^4 = \sigma \left(\frac{T_e}{\beta} \right)^4 \quad \text{and} \quad P_\alpha = \sigma T_\alpha^4 = \sigma (\beta T_s)^4 \quad (3)$$

64 The definitions of $T_\alpha = T_e$, T_s and β are the emission temperature, surface temperature and typically $\beta \approx 0.887$,
 65 respectively. Consider a time when there is **no forcing issues** causing warming trends. Then by conservation of
 66 energy, the equivalent power re-radiated from GHGs in this model is dependent on P_α with

$$67$$

$$68 \quad P_{GHG} = P_{Total} - P_\alpha = \sigma T_s^4 - \sigma T_\alpha^4 \quad (4)$$

69
 70 To be consistent with $T_\alpha = T_e$, since typically $T_\alpha \approx 255^\circ\text{K}$ and $T_s \approx 288^\circ\text{K}$, then in keeping with a common definition of
 71 the global beta (the proportionality between surface temperature and emission temperature) for the moment
 72 $\beta = T_\alpha / T_s = T_e / T_s$.

73
 74 This allows us to write the dependence

$$75$$

$$76 \quad P_{GHG} = \sigma T_s^4 - \sigma T_\alpha^4 = \frac{\sigma T_\alpha^4}{\beta^4} - \sigma T_\alpha^4 = \sigma T_\alpha^4 \left(\frac{1}{\beta^4} - 1 \right) = \sigma T_\alpha^4 \left(\frac{1}{f} - 1 \right) \quad (5)$$

77
 78 Note that when $\beta^4 = 1$, there are no GHG contributions. We note that f , the re-radiation parameter equals β^4 in the
 79 absence of forcing.

80
 81 We can also define the blackbody re-radiated by GHGs given by some fraction f_1 such that

$$82$$

$$83 \quad P_{GHG} = f_1 P_\alpha = f_1 \sigma T_\alpha^4 \quad (6)$$

84
 85 Consider $f = f_1$, in this case according to Equations 5 and 6, it requires
 86

87
$$P_{GHG} = \sigma T_{\alpha}^4 \left(\frac{1}{f_1} - 1 \right) = f_1 \sigma T_{\alpha}^4 \quad (7)$$

88
89 This dependence leads us to the solution of the quadratic expression
90

91
$$f_1^2 + f_1 - 1 = 0 \text{ yielding } f_1 = 0.618034 = \beta^4, \beta = (0.618034)^{1/4} = 0.886652 \quad (8)$$

92
93 This is very close to the common value estimated for β and this has been obtained through energy balance in the
94 planetary system providing a self-determining assessment. In geoengineering we can view the re-radiation as part of
95 the albedo effect. Consistency with the Planck parameter is shown in Section 6. We note that the assumption $f=f_1$
96 only works if planetary energy is in balance without forcing. In the next section, we double check this model in
97 another way by balancing energy in and out of our global system.
98

99 3. Balancing P_{out} and P_{in} in 1950

100
101 In equilibrium the radiation that leaves must balance P_{α} , the energy absorbed, so that
102

103
$$\begin{aligned} Energy_{Out} &= (1-f_1)P_{\alpha} + (1-f_1)P_{Total} = (1-f_1)P_{\alpha} + (1-f_1)\{P_{\alpha} + f_1P_{\alpha}\} \\ &= 2P_{\alpha} - f_1P_{\alpha} - f_1^2P_{\alpha} = Energy_{In} = P_{\alpha} \end{aligned} \quad (9)$$

104
105 This is consistent, so that in 1950, Eq. 9 requires the same quadratic solution as Eq. 8. It is also apparent that
106

107
$$P_{\alpha} = f_1 P_{Total_1950} = \beta_1^4 P_{Total_1950} \quad (10)$$

108 since
109

110
$$P_{\alpha} = f_1(P_{\alpha} + f_1P_{\alpha}) \text{ or } 1 = f_1(1 + f_1) \quad (11)$$

112
113 The RHS of Eq. 11 is Eq. 8. This illustrates f_1 from another perspective as the fractional amount of total radiation in
114 equilibrium. As a final check, the application in the next Section in Table 1, illustrate that f_1 provides reasonable
115 results.
116

117 4. Re-radiation Model Applied to 2019

118
119 In 2019 due to global warming trends, to apply the model we assume that feedback can be applied as a separate term
120 and we make use of some IPCC estimates for GHG forcing as a way to calibrate our model. In the traditional sense
121 of forcing, we assume some small change to the albedo and most of the forcing due to IPCC estimates for GHGs
122 where
123

124
$$P_{Total2019} = P_{\alpha'} + P_{GHG'} = P_{\alpha'}(1 + f_2) \quad (12)$$

125
126 Then we introduce feedback through an amplification factor A_F as follows
127

128
$$P_{Total2019\&Feedback} = P_{1950} + (\Delta P) A_F = P_{1950} + (P_{2019} - P_{1950}) A_F = \sigma T_S^4 \quad (13)$$

129
130 Here, we assume a small change in the albedo denoted as P_{α}' and f_2 is adjusted to the IPCC GHG forcing value
131 estimated between 1950 and 2019 of $2.38W/m^2$ [39]. Then the feedback amplification factor, is calibrated so that
132 $T_S=T_{2019}$ (see Table 1) yielding $A_F=2.022$ [also see ref. 22]. The main difference in our model is that the forcing is
133 about 6% higher than the IPCC for this period. Here, we take into account a small albedo decline of 0.15% that the
134 author has estimated in another study due to likely issues from UHIs [20] and their coverage. We note that unlike f_1 ,
135 f_2 is not a strict measure of the emissivity due the increase in GHGs.
136

137 5. Results Applied to 1950 and 2019 with an Estimate for f_2

138
139 In 1950 we will simplify estimates by assuming the re-radiation parameter is fixed at the pre-industrial level of
140 $f_1=0.618034$. Then, to obtain the average surface temperature $T_{1950}=13.89^{\circ}C$ ($287.04^{\circ}K$), the only adjustable

141 parameter left in our basic model is the global albedo. This requires an albedo value of 0.3008 (see Table 1) to
 142 obtain $T_{1950}=287.04^{\circ}\text{K}$. This albedo number is reasonable and similar to values cited in the literature [31].

143
 144 In 2019, the average temperature of the Earth is $T_{2019}=14.84^{\circ}\text{C}$ (287.99°K) given in Eq. 15. We have assumed a
 145 small change in the Earth's albedo due to UHIs [20]. The f_2 parameter is adjusted to 0.6276 to obtain the GHG
 146 forcing shown in Column 7 of $2.38\text{W}/\text{m}^2$ [23]. Therefore the next to last row in Table 1 is a summary without
 147 feedback, and the last row incorporated the $A_F=2.022$ feedback amplification factor.

148
 149 **Table 1 Model results**

Year	$T_S(^{\circ}\text{K})$	$T_{\alpha}(^{\circ}\text{K})$	f_1, f_2	α, α'	Power Absorbed $\frac{\text{W}}{\text{m}^2}$	$P_{\text{GHG}}, P_{\text{GHG}}$	P_{Total}^2 W/m^2
2019	287.5107	254.55	0.6276	30.03488	238.056	149.4041	387.4605
1950	287.04	254.51	0.6180	30.08	237.9028	147.024	384.9267
$\Delta 2019-1950$	0.471	0.041	0.0096	(0.15%)	0.15352	2.38	2.53
$\Delta P_{\text{Feedback}} A_F=2.022$	0.95	0.083	-	-	0.3104	4.81	5.12

150
 151 From Table 1 we now have identified the reverse forcing at the surface needed since

152
 153
$$P_{\text{Total}_{2019_Feedback_Amp}} = P_{1950} + (P_{2019} - P_{1950}) A_F = 384.927\text{W} / \text{m}^2 + (2.5337\text{W} / \text{m}^2) 2.022 = 390.05\text{W} / \text{m}^2 \quad (14)$$

154
 155 and

156
$$\Delta T_S = T_{2019} - T_{1950} = (390.05 / \sigma)^{1/4} - 287.04^{\circ}\text{K} = 287.9899^{\circ}\text{K} - 287.04^{\circ}\text{K} = 0.95^{\circ}\text{K} \quad (15)$$

157
 158 as modeled. We also note an estimate has now been obtained in Table 1 for $f_2=0.6276$, $A_F=2.022$, and
 159 $\Delta P_{\text{Total_Feedback_amp}}=5.12\text{W}/\text{m}^2$.

160
 161 **6. Model Consistency with the Planck Parameter**

162
 163 As a measure of model consistency, the forcing change with feedback, and resulting temperatures T_{1950} and T_{2019} ,
 164 should be in agreement with expected results using the Planck feedback parameter. From the definition of the Planck
 165 parameter λ_o and results in Table 1, we estimate [24]

166
 167
$$\lambda_o = -4 \frac{\Delta R_{OLW}}{T_S} = -4 \left(\frac{237.9028\text{W} / \text{m}^2}{287.041^{\circ}\text{K}} \right)_{1950} = -3.31524\text{W} / \text{m}^2 / ^{\circ}\text{K} \quad (16)$$

168 and

169
$$\lambda_o = -4 \frac{\Delta R_{OLW}}{T_S} = -4 \left(\frac{238.056\text{W} / \text{m}^2}{287.99^{\circ}\text{K}} \right)_{2019} = -3.306\text{W} / \text{m}^2 / ^{\circ}\text{K} \quad (17)$$

170
 171 Here ΔR_{OLW} is the outgoing long wave radiation change. We note these are very close in value showing minor error
 172 and consistency with Planck parameter value, often taken as $3.3\text{W}/\text{m}^2/^{\circ}\text{K}$.

173
 174 Also note the Betas are very consistent with Eq. 8 for the two different time periods since from Table 1

175
 176
$$\beta_{1950} = \frac{T_{\alpha}}{T_S} = \frac{T_e}{T_S} = \frac{254.51}{287.041} = 0.88667 \text{ and } \beta_{1950}^4 = 0.6180785 \quad (18)$$

177
 178 and

179
 180
$$\beta_{2019} = \frac{T_{\alpha}}{T_S} = \frac{T_e}{T_S} = \frac{254.55}{287.5107} = 0.88526 \text{ and } \beta_{2019}^4 = 0.6144 \quad (19)$$

181
 182 **7. Summary**

183 In this paper we have devised a greenhouse gas albedo surface theorem. The theorem includes a re-
184 radiation factor which has been fully described and applied to two time periods. Results show that the re-
185 radiation factor for 1950 is taken as a pre-industrial value of 1.6181 while in present day the factor has
186 increase to 1.6276 due to the increase in GHGs.

187 We suggest the theorem, when applied to the reality of today's challenges, appears to indicate that the
188 albedo solution would be the safest and fastest way to mitigate climate change. Furthermore, focusing
189 solely on the CO2 solution is unrealistic and puts our planet at risk.

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