

# On the Ramanujan's mathematics applications: connections with $\phi$ and various equations regarding Teleparallel Equivalent of General Relativity. IV

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## Abstract

*In this paper we have described some applications of Ramanujan's mathematics and obtained some connections with  $\phi$  and various expressions inherent Teleparallel Equivalent of General Relativity*

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**Reply to – The number 1729 is ‘dull’:**

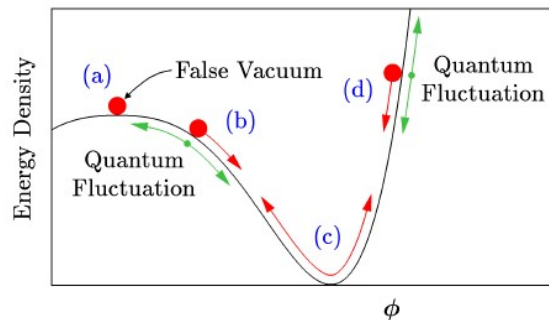
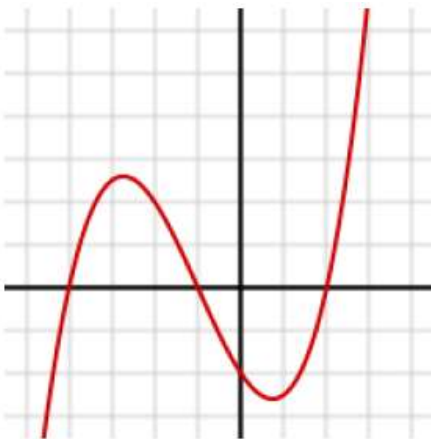
No, it is a very interesting number; it is the smallest number expressible as a *sum of two cubes* in two different ways, the two ways being  $1^3 + 12^3$  and  $9^3 + 10^3$ .

Srinivasa Ramanujan



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[https://todayinsci.com/R/Ramanujan\\_Srinivasa/RamanujanSrinivasa-Quotations.htm](https://todayinsci.com/R/Ramanujan_Srinivasa/RamanujanSrinivasa-Quotations.htm)



From:

**Rotating and non-rotating AdS black holes in  $f(T)$  gravity non-linear electrodynamics** - *Salvatore Capozziello, Gamal G.L. Nashed* (Dated: October 22, 2019) arXiv:1908.07381v2 [gr-qc] 19 Oct 2019

We have that:

## ANTI-DE-SITTER BLACK HOLE SOLUTIONS IN NON-LINEAR ELECTRODYNAMICS

### A. Asymptotically static AdS black holes

Considering the function (30) in (32), we get

$$\begin{aligned}
A(r) &= \Lambda_{eff} r^2 - \frac{4(d-3)^2 m q^2 P}{(d-2) a_1^2 c_1 r^{d-2} q_1^2 [e^{\frac{2q_1}{(d-3)mr^{d-3}}} + 1]^2} \left( 2\sqrt{3P|a_2|} e^{\frac{q_1}{(d-3)mr^{d-3}}} [q_1 \{e^{\frac{2q_1}{(d-3)mr^{d-3}}} - 1\} + [1 + e^{\frac{2q_1}{(d-3)mr^{d-3}}}] (d-2)mr^{d-3}] \right. \\
&\quad \left. + 3a_1 q_1 r^{d-2} [e^{\frac{2q_1}{(d-3)mr^{d-3}}} + 1] \right) + \frac{q^2}{(d-2) a_1^2 c_1} \int \frac{8(d-3)^2 P \sqrt{3P|a_2|} (q_1^2 - (d-2)m^2 r^{2(d-3)}) e^{\frac{q_1}{(d-3)mr^{d-3}}}}{q_1^2 r^{2(d-2)} [e^{\frac{2q_1}{(d-3)mr^{d-3}}} + 1]} dr + \frac{c_3}{r^{d-3}}, \\
&\approx \Lambda_{eff} r^2 - \frac{M}{r^{d-3}} + \frac{Q^2}{r^{2(d-3)}} + \frac{Q_1^4}{r^{3(d-8)}} + \frac{Q_2^4}{r^{4(d-3)}} + \dots, \\
g(r) &= \frac{a_1^2 c_1 r^{2(d-2)} [e^{\frac{2q_1}{(d-3)mr^{d-3}}} + 1]^2}{q^2 (d-3)^2 \{ a_1 r^{d-2} [e^{\frac{2q_1}{(d-3)mr^{d-3}}} + 1] - 4\sqrt{3P|a_2|} e^{\frac{q_1}{(d-3)mr^{d-3}}} \}^2} \\
&\approx \frac{c_1}{(d-3)^2 q^2} \left[ 1 + \frac{4(d-3)^2 \sqrt{3P|a_2|}}{a_1 r^{d-2}} - \frac{2q_1^2 \sqrt{3P|a_2|}}{a_1 (d-3)^2 m^2 r^{3d-8}} - \frac{36Pa_2}{a_1^2 r^{2(d-2)}} + \dots \right], \tag{33}
\end{aligned}$$

For:

$$\begin{aligned}
q &= 0.3; & Q^2 &= 0.135; & Q_1^4 &= 0.0519615; & Q_2^4 &= -0.020; & \Lambda_{eff} &= 0.375 \\
\phi &= -1/6; & P &= -0.5; & a_2 &= -0.5; & d &= 4; & r &= 5; & q_1 &= 0.2; & m &= 1; & c_{1,2,3} &= 1
\end{aligned}$$

From:

$$M = c_3 - \frac{6(d-3)^2 P q^2}{q_1 a_1 c_1 (d-2)},$$

$$1 - (((6 * (-0.5) * 0.3^2))) / (((0.2 * 2)))$$

$$1 - \frac{6 \times (-0.5) \times 0.3^2}{0.2 \times 2}$$

1.675

$$M = 1.675$$

$$\approx \Lambda_{eff} r^2 - \frac{M}{r^{d-3}} + \frac{Q^2}{r^{2(d-3)}} + \frac{Q_1^4}{r^{(3d-8)}} + \frac{Q_2^4}{r^{4(d-3)}} + \dots,$$

$$0.375 \times 25 - 1.675/5 + 0.135/25 + 0.0519615/5^4 - 0.020/5^4$$

**Input interpretation:**

$$0.375 \times 25 - \frac{1.675}{5} + \frac{0.135}{25} + \frac{0.0519615}{5^4} - \frac{0.02}{5^4}$$

**Result:**

9.0454511384

**9.0454511384**

From which:

$$(((0.375 \times 25 - 1.675/5 + 0.135/25 + 0.0519615/5^4 - 0.020/5^4)))^{1/4} - 2/10^3$$

**Input interpretation:**

$$\sqrt[4]{0.375 \times 25 - \frac{1.675}{5} + \frac{0.135}{25} + \frac{0.0519615}{5^4} - \frac{0.02}{5^4}} - \frac{2}{10^3}$$

**Result:**

1.732233...

1.732233...  $\approx \sqrt{3}$  that is the ratio between the gravitating mass  $M_0$  and the Wheelerian mass  $q$

$$M_0 = \sqrt{3q^2 - \Sigma^2},$$

$$q = \frac{(3\sqrt{3}) M_s}{2}.$$

(see: Can massless wormholes mimic a Schwarzschild black hole in the strong field lensing? - arXiv:1909.13052v1 [gr-qc] 28 Sep 2019)

and:

$$\left(\left(\left(0.375 \times 25 - 1.675/5 + 0.135/25 + 0.0519615/5^4 - 0.020/5^4\right)\right)^{1/2} / (\pi + \sqrt{2}) - \pi/10^3\right)$$

**Input interpretation:**

$$\pi + \sqrt{2} \sqrt{0.375 \times 25 - \frac{1.675}{5} + \frac{0.135}{25} + \frac{0.0519615}{5^4} - \frac{0.02}{5^4}} - \frac{\pi}{10^3}$$

**Result:**

1.61843...

1.61843.... result that is a very good approximation to the value of the golden ratio 1.618033988749...

**Series representations:**

$$\pi + \sqrt{2} \sqrt{0.375 \times 25 - \frac{1.675}{5} + \frac{0.135}{25} + \frac{0.0519615}{5^4} - \frac{0.02}{5^4}} - \frac{\pi}{10^3} = \pi + \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \binom{-1}{k} (2-z_0)^k z_0^{-k}}{k!} \sqrt{9.04545} - \frac{\pi}{1000} \text{ for (not } (z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\pi + \sqrt{2} \sqrt{0.375 \times 25 - \frac{1.675}{5} + \frac{0.135}{25} + \frac{0.0519615}{5^4} - \frac{0.02}{5^4}} - \frac{\pi}{10^3} = \pi + \exp\left(i \pi \left\lfloor \frac{\arg(2-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2-x)^k x^{-k} \binom{-1}{k}}{k!} \sqrt{9.04545} - \frac{\pi}{1000} \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\pi + \sqrt{2} \sqrt{0.375 \times 25 - \frac{1.675}{5} + \frac{0.135}{25} + \frac{0.0519615}{5^4} - \frac{0.02}{5^4}} - \frac{\pi}{10^3} = \pi + \left(\frac{1}{z_0}\right)^{1/2} \left\lfloor \frac{\arg(2-z_0)}{2\pi} \right\rfloor \frac{1}{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \binom{-1}{k} (2-z_0)^k z_0^{-k}}{k!} \sqrt{9.04545} - \frac{\pi}{1000}$$

Now, we have that:

$$\approx \frac{c_1}{(d-3)^2 q^2} \left[ 1 + \frac{4(d-3)^2 \sqrt{3P|a_2|}}{a_1 r^{d-2}} - \frac{2q_1^2 \sqrt{3P|a_2|}}{a_1 (d-3)^2 m^2 r^{3d-8}} - \frac{36Pa_2}{a_1^2 r^{2(d-2)}} + \dots \right],$$

For:

$$P = -0.5; \quad a_2 = -0.5; \quad d = 4; \quad r = 5; \quad q_1 = 0.2; \quad m = 1; \quad c_{1,2,3} = 1$$

We obtain:

$$1/(0.2)^2 * [1 + (4 * \sqrt{3 * 0.5^2})/25 - (2 * 0.2^2 * \sqrt{3 * 0.5^2})/(5^4) - (36 * 0.5^2)/(5^4)]$$

**Input:**

$$\frac{1}{0.2^2} \left( 1 + \frac{1}{25} \left( 4 \sqrt{3 \times 0.5^2} \right) - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{5^4} - \frac{36 \times 0.5^2}{5^4} \right)$$

**Result:**

28.1013...

28.1013...

From which:

$$5 * 1/(0.2)^2 * [1 + (4 * \sqrt{3 * 0.5^2})/25 - (2 * 0.2^2 * \sqrt{3 * 0.5^2})/(5^4) - (36 * 0.5^2)/(5^4)] - 1$$

**Input:**

$$5 \times \frac{1}{0.2^2} \left( 1 + \frac{1}{25} \left( 4 \sqrt{3 \times 0.5^2} \right) - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{5^4} - \frac{36 \times 0.5^2}{5^4} \right) - 1$$

**Result:**

139.507...

139.507... result practically equal to the rest mass of Pion meson 139.57 MeV

$$5 \times \frac{1}{(0.2)^2} \left[ 1 + \frac{4 \sqrt{3 \times 0.5^2}}{25} - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{(5^4)} - \frac{36 \times 0.5^2}{(5^4)} \right] - 13 - 2$$

**Input:**

$$5 \times \frac{1}{0.2^2} \left( 1 + \frac{1}{25} \left( 4 \sqrt{3 \times 0.5^2} \right) - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{5^4} - \frac{36 \times 0.5^2}{5^4} \right) - 13 - 2$$

**Result:**

125.507...

125.507... result very near to the Higgs boson mass 125.18 GeV

$$27 \times \frac{1}{2} \left( \left( 5 \times \frac{1}{(0.2)^2} \left[ 1 + \frac{4 \sqrt{3 \times 0.5^2}}{25} - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{(5^4)} - \frac{36 \times 0.5^2}{(5^4)} \right] - 13 + \frac{1}{2} \right) \right) + 1$$

**Input:**

$$27 \times \frac{1}{2} \left( 5 \times \frac{1}{0.2^2} \left( 1 + \frac{1}{25} \left( 4 \sqrt{3 \times 0.5^2} \right) - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{5^4} - \frac{36 \times 0.5^2}{5^4} \right) - 13 + \frac{1}{2} \right) + 1$$

**Result:**

1729.09...

1729.09...

This result is very near to the mass of candidate glueball **f<sub>0</sub>(1710) scalar meson**. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

With regard 27 (From Wikipedia):

*“The fundamental group of the complex form, compact real form, or any algebraic version of E<sub>6</sub> is the cyclic group  $\mathbf{Z}/3\mathbf{Z}$ , and its outer automorphism group is the cyclic group  $\mathbf{Z}/2\mathbf{Z}$ . Its fundamental representation is 27-dimensional (complex), and a basis is given by the 27 lines on a cubic surface. The dual representation, which is inequivalent, is also 27-dimensional. In particle physics, E<sub>6</sub> plays a role in some grand unified theories”.*

$$[27 \times \frac{1}{2} \left( \left( \frac{5 \times \frac{1}{0.2^2} \left[ 1 + \frac{4 \sqrt{3 \times 0.5^2}}{25} - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{5^4} - \frac{36 \times 0.5^2}{5^4} \right] - 13 + \frac{1}{2} \right) - \frac{36 \times 0.5^2}{5^4} \right) - 13 + \frac{1}{2} \right) + 1 \right]^{1/15} - \frac{21+5}{10^3}$$

**Input:**

$$\left( 27 \times \frac{1}{2} \left( 5 \times \frac{1}{0.2^2} \left( 1 + \frac{4 \sqrt{3 \times 0.5^2}}{25} - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{5^4} - \frac{36 \times 0.5^2}{5^4} \right) - 13 + \frac{1}{2} \right) - \frac{36 \times 0.5^2}{5^4} \right) + 1 \right)^{1/15} - \frac{21+5}{10^3}$$

**Result:**

1.617820920168714750240429307163106132695316232238940975787...

1.61782092016.... result that is a very good approximation to the value of the golden ratio 1.618033988749...

$$\sqrt[15]{\frac{27}{2} \left( \frac{5 \left( 1 + \frac{4 \sqrt{3 \times 0.5^2}}{25} - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{5^4} - \frac{36 \times 0.5^2}{5^4} \right)}{0.2^2} - 13 + \frac{1}{2} \right) + 1 - \frac{21+5}{10^3}} = 1.61782$$

is 1.58168% smaller than

$$\sqrt[15]{\frac{27}{2} \left( \frac{5 \left( 1 + \frac{4 \sqrt{3 \times 0.5^2}}{25} - \frac{2 \times 0.2^2 \sqrt{3 \times 0.5^2}}{5^4} - \frac{36 \times 0.5^2}{5^4} \right)}{0.2^2} - 13 + \frac{1}{2} \right) + 1} = 1.64382.$$

Now, we have that:

where  $\kappa$  is the surface gravity. The Hawking temperature associated with the black hole solution (33) is

$$T_{b_{Eq(33)}} = \frac{1}{4\pi} \left\{ (d-1)r_b \Lambda_{eff} - \frac{(d-3)Q^2}{r_b^{2d-5}} - \frac{(2d-5)Q_1^4}{r_b^{(3d-7)}} + \frac{3(d-3)Q_2^4}{r_b^{(4d-11)}} + \dots \right\}$$



From

$$T_{b \text{ Eq.(33)}} = \frac{1}{4\pi} \left\{ (d-1)r_b \Lambda_{eff} - \frac{(d-3)Q^2}{r_b^{2d-5}} - \frac{(2d-5)Q_1^4}{r_b^{(3d-7)}} + \frac{3(d-3)Q_2^4}{r_b^{(4d-11)}} + \dots \right\},$$

For:  $q = 0.3$ ;  $Q^2 = 0.135$ ;  $Q_1^4 = 0.0519615$ ;  $Q_2^4 = -0.020$ ;

$\Lambda_{eff} = 0.375$ ;  $r_b = 0.8$ ;  $d = 4$ ;

We obtain:

$$1/(4\pi) [3*0.8*0.375 - 0.135/(0.8^3) - (3*0.0519615)/(0.8^5) + (3*-0.020)/(0.8^5)]$$

**Input interpretation:**

$$\frac{1}{4\pi} \left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right)$$

**Result:**

-0.00179042...

-0.00179042...

**Alternative representations:**

$$\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}{4\pi} = \frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{720^\circ}$$

$$\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}{4\pi} = -\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{4i \log(-1)}$$

$$\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}{4\pi} = \frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{4 \cos^{-1}(-1)}$$

**Series representations:**

$$\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}{4\pi} = -\frac{0.00140619}{\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}$$

$$\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}{4\pi} = -\frac{0.00281239}{-1 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}}$$

$$\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}{4\pi} = -\frac{0.00562477}{\sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}}$$

**Integral representations:**

$$\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}{4\pi} = -\frac{0.00281239}{\int_0^{\infty} \frac{1}{1+t^2} dt}$$

$$\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}{4\pi} = -\frac{0.00140619}{\int_0^1 \sqrt{1-t^2} dt}$$

$$\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}{4\pi} = -\frac{0.00281239}{\int_0^{\infty} \frac{\sin(t)}{t} dt}$$

From which:

$$-1/((((1/(4\pi)) [3*0.8*0.375-0.135/(0.8^3)-(3*0.0519615)/(0.8^5)+(3*-0.020)/(0.8^5)]))))$$

**Input interpretation:**

$$-\frac{1}{4\pi \left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right)}$$

**Result:**

558.528...

558.528...

### Alternative representations:

$$-\frac{1}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi} = -\frac{1}{\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{720^\circ}}$$

$$-\frac{1}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi} = -\frac{1}{\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{4i \log(-1)}}$$

$$-\frac{1}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi} = -\frac{1}{\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{4 \cos^{-1}(-1)}}$$

### Series representations:

$$-\frac{1}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi} = 711.14 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}$$

$$-\frac{1}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi} = -355.57 + 355.57 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$-\frac{1}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi} = 177.785 \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}}$$

### Integral representations:

$$-\frac{1}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi} = 355.57 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$-\frac{1}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi} = 711.14 \int_0^1 \sqrt{1-t^2} dt$$

$$-\frac{1}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi} = 355.57 \int_0^{\infty} \frac{\sin(t)}{t} dt$$

From the formula of coefficients of the '5th order' mock theta function  $\psi_1(q)$ :  
(A053261 OEIS Sequence)

$\sqrt{\phi} \times \exp(\pi \sqrt{n/15}) / (2 \cdot 5^{1/4} \sqrt{n})$  for  $n = 142$ , and  
subtracting 5, we obtain:

$$\sqrt{\phi} \times \exp(\pi \sqrt{142/15}) / (2 \cdot 5^{1/4} \sqrt{142}) - 5$$

**Input:**

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{142}{15}}\right)}{2 \sqrt[4]{5} \sqrt{142}} - 5$$

$\phi$  is the golden ratio

**Exact result:**

$$\frac{e^{\sqrt{142/15} \pi} \sqrt{\frac{\phi}{142}}}{2 \sqrt[4]{5}} - 5$$

**Decimal approximation:**

557.9674901451270624093141698696704992272545861579538471347...

557.96749014...

**Property:**

$$-5 + \frac{e^{\sqrt{142/15} \pi} \sqrt{\frac{\phi}{142}}}{2 \sqrt[4]{5}} \text{ is a transcendental number}$$

**Alternate forms:**

$$\frac{1}{4} \sqrt{\frac{1}{355} (5 + \sqrt{5})} e^{\sqrt{142/15} \pi} - 5$$

$$\frac{\sqrt{\frac{1}{71} (1 + \sqrt{5})} e^{\sqrt{142/15} \pi}}{4 \sqrt[4]{5}} - 5$$

$$\frac{5^{3/4} \sqrt{71 (1 + \sqrt{5})} e^{\sqrt{142/15} \pi} - 7100}{1420}$$

## Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{142}{15}}\right)}{2^{\frac{4}{3}} \sqrt{5} \sqrt{142}} - 5 = \left( -50 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (142 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right. \\ \left. \exp\left[ \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{142}{15} - z_0\right)^k z_0^{-k}}{k!} \right] \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left( 10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (142 - z_0)^k z_0^{-k}}{k!} \right) \text{ for (not } (z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{142}{15}}\right)}{2^{\frac{4}{3}} \sqrt{5} \sqrt{142}} - 5 = \left( -50 \exp\left(i\pi \left\lfloor \frac{\arg(142 - x)}{2\pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (142 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\ \left. 5^{3/4} \exp\left(i\pi \left\lfloor \frac{\arg(\phi - x)}{2\pi} \right\rfloor\right) \exp\left[ \pi \exp\left(i\pi \left\lfloor \frac{\arg\left(\frac{142}{15} - x\right)}{2\pi} \right\rfloor\right) \sqrt{x} \right. \right. \\ \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{142}{15} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right] \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\ \left( 10 \exp\left(i\pi \left\lfloor \frac{\arg(142 - x)}{2\pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (142 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)$$

for ( $x \in \mathbb{R}$  and  $x < 0$ )

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{142}{15}}\right)}{2^{\frac{4}{3}} \sqrt{5} \sqrt{142}} - 5 = \left( \left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(142 - z_0)/(2\pi) \rfloor} z_0^{-1/2 \lfloor \arg(142 - z_0)/(2\pi) \rfloor} \right. \\ \left( -50 \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(142 - z_0)/(2\pi) \rfloor} z_0^{1/2 \lfloor \arg(142 - z_0)/(2\pi) \rfloor} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (142 - z_0)^k z_0^{-k}}{k!} + \right. \\ \left. 5^{3/4} \exp\left[ \pi \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg\left(\frac{142}{15} - z_0\right)/(2\pi) \rfloor} z_0^{1/2 (1 + \lfloor \arg\left(\frac{142}{15} - z_0\right)/(2\pi) \rfloor)} \right. \right. \\ \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{142}{15} - z_0\right)^k z_0^{-k}}{k!} \right] \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(\phi - z_0)/(2\pi) \rfloor} \right. \\ \left. \left. z_0^{1/2 \lfloor \arg(\phi - z_0)/(2\pi) \rfloor} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right] \right) / \\ \left( 10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (142 - z_0)^k z_0^{-k}}{k!} \right)$$

From which:

$$-1/4 / [1/(4\pi) [3*0.8*0.375 - 0.135/(0.8^3) - (3*0.0519615)/(0.8^5) + (3*-0.020)/(0.8^5)]]$$

**Input interpretation:**

$$\frac{1}{4 \left( \frac{1}{4\pi} \left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right) \right)}$$

**Result:**

139.632...

139.632... result practically equal to the rest mass of Pion meson 139.57 MeV

**Alternative representations:**

$$\frac{1}{\frac{\left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right) 4}{4\pi}} = \frac{1}{4 \left( 0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5} \right) 720^\circ}$$

$$\frac{1}{\frac{\left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right) 4}{4\pi}} = \frac{1}{4 \left( 0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5} \right) 4 i \log(-1)}$$

$$\frac{1}{\frac{\left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right) 4}{4\pi}} = \frac{1}{4 \left( 0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5} \right) 4 \cos^{-1}(-1)}$$

**Series representations:**

$$\frac{1}{\frac{\left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right) 4}{4\pi}} = 177.785 \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$\frac{1}{\frac{\left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right) 4}{4\pi}} = -88.8925 + 88.8925 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{1}{\frac{\left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right) 4}{4\pi}} = 44.4463 \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}}$$

**Integral representations:**

$$-\frac{1}{\frac{(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5})}{4}} = 88.8925 \int_0^\infty \frac{1}{1+t^2} dt$$

$$-\frac{1}{\frac{(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5})}{4}} = 177.785 \int_0^1 \sqrt{1-t^2} dt$$

$$-\frac{1}{\frac{(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5})}{4}} = 88.8925 \int_0^\infty \frac{\sin(t)}{t} dt$$

$-1/4 / [1/(4\pi) [3*0.8*0.375-0.135/(0.8^3)-(3*0.0519615)/(0.8^5)+(3*-0.020)/(0.8^5)]]-11-\pi$

**Input interpretation:**

$$-\frac{1}{4 \left( \frac{1}{4\pi} \left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right) \right)} - 11 - \pi$$

**Result:**

125.490...

125.49... result very near to the Higgs boson mass 125.18 GeV

**Alternative representations:**

$$-\frac{1}{\frac{(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5})}{4}} - 11 - \pi =$$

$$-11 - 180^\circ - \frac{1}{4 \left( 0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5} \right)}$$

$$-11 - \pi =$$

$$-11 + i \log(-1) - \frac{1}{4 \left( 0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5} \right)}$$

$$- \frac{1}{4 i \log(-1)}$$

$$-\frac{1}{\left(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}\right)^4} - 11 - \pi =$$

$$-11 - \cos^{-1}(-1) - \frac{1}{4 \cos^{-1}(-1)}$$

### Series representations:

$$-\frac{1}{\left(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}\right)^4} - 11 - \pi = -11 + 173.785 \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$-\frac{1}{\left(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}\right)^4} - 11 - \pi = -97.8925 + 86.8925 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$-\frac{1}{\left(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}\right)^4} - 11 - \pi = -11 + 43.4463 \sum_{k=0}^{\infty} \frac{2^{-k}(-6 + 50k)}{\binom{3k}{k}}$$

### Integral representations:

$$-\frac{1}{\left(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}\right)^4} - 11 - \pi = -11 + 86.8925 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$-\frac{1}{\left(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}\right)^4} - 11 - \pi = -11 + 173.785 \int_0^1 \sqrt{1-t^2} dt$$

$$-\frac{1}{\left(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}\right)^4} - 11 - \pi = -11 + 86.8925 \int_0^{\infty} \frac{\sin(t)}{t} dt$$



$$\left(\left(\left(-\pi/\left(\left(\left(1/(4\pi)\left[3 \times 0.8 \times 0.375 - 0.135/(0.8^3) - (3 \times 0.0519615)/(0.8^5) + (3 \times -0.020)/(0.8^5)\right]\right)\right)\right)\right)\right)\right) - 21 - 5 + 1/2$$

**Input interpretation:**

$$-\frac{\pi}{4\pi \left(3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5}\right)} - 21 - 5 + \frac{1}{2}$$

**Result:**

1729.17...

1729.17...

This result is very near to the mass of candidate glueball **f<sub>0</sub>(1710) scalar meson**. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

**Alternative representations:**

$$-\frac{\pi}{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} = -\frac{51}{2} - \frac{180^\circ}{\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{720^\circ}}$$

$$-\frac{\pi}{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} = -\frac{51}{2} + \frac{i \log(-1)}{-\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{4 i \log(-1)}}$$

$$-\frac{\pi}{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} = -\frac{51}{2} - \frac{\cos^{-1}(-1)}{\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{4 \cos^{-1}(-1)}}$$

**Series representations:**

$$-\frac{\pi}{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} = -25.5 + 2844.56 \left( \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k} \right)^2$$

$$-\frac{\pi}{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} =$$

$$-25.5 + 177.785 \left( \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}} \right)^2$$

$$-\frac{\pi}{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} =$$

$$-25.5 + 711.14 \sqrt{3}^2 \left( \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{3}\right)^k}{1 + 2k} \right)^2$$

### Integral representations:

$$-\frac{\pi}{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} = -25.5 + 711.14 \left( \int_0^{\infty} \frac{1}{1+t^2} dt \right)^2$$

$$-\frac{\pi}{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} =$$

$$-25.5 + 2844.56 \left( \int_0^1 \sqrt{1-t^2} dt \right)^2$$

$$-\frac{\pi}{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} = -25.5 + 711.14 \left( \int_0^{\infty} \frac{\sin(t)}{t} dt \right)^2$$

$$[\frac{-\pi}{(4\pi) [3*0.8*0.375-0.135/(0.8^3)-(3*0.0519615)/(0.8^5)+(3*-0.020)/(0.8^5)]}] - 21 - 5 + 1/2]^{1/15} - (21+5)1/10^3$$

### Input interpretation:

$$\sqrt[15]{-\frac{1}{4\pi} \left( 3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3 \times (-0.02)}{0.8^5} \right) - 21 - 5 + \frac{1}{2} - (21 + 5) \times \frac{1}{10^3}}$$

**Result:**

1.617825859704035485452539936147753103508858970162566796414...

1.6178258597.... result that is a very good approximation to the value of the golden ratio 1.618033988749...

**Alternative representations:**

$$\sqrt[15]{-\frac{\pi}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi}} - 21 - 5 + \frac{1}{2} - \frac{21+5}{10^3} = \\
-\frac{26}{10^3} + \sqrt[15]{-\frac{51}{2} - \frac{180^\circ}{\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{720^\circ}}}$$

$$\sqrt[15]{-\frac{\pi}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi}} - 21 - 5 + \frac{1}{2} - \frac{21+5}{10^3} = \\
-\frac{26}{10^3} + \sqrt[15]{-\frac{51}{2} + \frac{i \log(-1)}{\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{4i \log(-1)}}}$$

$$\sqrt[15]{-\frac{\pi}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi}} - 21 - 5 + \frac{1}{2} - \frac{21+5}{10^3} = \\
-\frac{26}{10^3} + \sqrt[15]{-\frac{51}{2} - \frac{\cos^{-1}(-1)}{\frac{0.9 - \frac{0.135}{0.8^3} - \frac{0.215885}{0.8^5}}{4 \cos^{-1}(-1)}}}$$

**Series representations:**

$$\sqrt[15]{-\frac{\pi}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}}}{4\pi}} - 21 - 5 + \frac{1}{2} - \frac{21+5}{10^3} = \\
-0.026 + 1.69929 \sqrt[15]{-0.00896448 + \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}\right)^2}$$

$$\sqrt[15]{-\frac{\pi}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} - \frac{21+5}{10^3}} =$$

$$-\frac{13}{500} + \sqrt[15]{-\frac{51}{2} + 711.14 \left( -1 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}} \right)^2}$$

$$\sqrt[15]{-\frac{\pi}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} - \frac{21+5}{10^3}} =$$

$$-0.026 + 1.41251 \sqrt[15]{-0.143432 + \left( \sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}} \right)^2}$$

### Integral representations:

$$\sqrt[15]{-\frac{\pi}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} - \frac{21+5}{10^3}} =$$

$$-\frac{13}{500} + \sqrt[15]{-25.5 + 711.14 \left( \int_0^{\infty} \frac{1}{1+t^2} dt \right)^2}$$

$$\sqrt[15]{-\frac{\pi}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} - \frac{21+5}{10^3}} =$$

$$-\frac{13}{500} + \sqrt[15]{-25.5 + 2844.56 \left( \int_0^1 \sqrt{1-t^2} dt \right)^2}$$

$$\sqrt[15]{-\frac{\pi}{\frac{3 \times 0.8 \times 0.375 - \frac{0.135}{0.8^3} - \frac{3 \times 0.0519615}{0.8^5} + \frac{3(-0.02)}{0.8^5}} - 21 - 5 + \frac{1}{2} - \frac{21+5}{10^3}} =$$

$$-\frac{13}{500} + \sqrt[15]{-25.5 + 711.14 \left( \int_0^{\infty} \frac{\sin(t)}{t} dt \right)^2}$$

Now, we have that:

Let us now calculate the heat capacity  $C_b h$  horizon and substitute Eqs. (45) and (48) into Eq. (44). We have

$$C_{b_{Eq(33)}} \approx -4\pi r_b^2 - \frac{288\pi(d-2)\alpha P}{r_b^{d-2}} + \frac{576\pi(d-2)\alpha P \sqrt{3P|\alpha|}}{r_b^{2(d-2)}} + \frac{288\pi(2d-5)\alpha q_1^2 P}{(d-3)^2 m^2 r_b^{(3d-8)}}.$$

From:

$$C_{b_{Eq(33)}} \approx -4\pi r_b^2 - \frac{288\pi(d-2)\alpha P}{r_b^{d-2}} + \frac{576\pi(d-2)\alpha P \sqrt{3P|\alpha|}}{r_b^{2(d-2)}} + \frac{288\pi(2d-5)\alpha q_1^2 P}{(d-3)^2 m^2 r_b^{(3d-8)}}.$$

For:  $P = 0.5$ ;  $a_2 = -0.5$ ;  $d = 4$ ;  $r = 5$ ;  $q_1 = 0.2$ ;  $m = 1$ ;  $c_{1,2,3} = 1$ ,

we obtain:

$$-4 * \pi * 0.8^2 -$$

$$(288 * \pi * 2 * (0.5)) / (0.8^2) + (576 * \pi * 2 * (0.5) * \sqrt{3 * 0.5}) / (0.8^4) + (288 * \pi * 3 * 0.2^2 * 0.5) / (0.8^4)$$

**Input:**

$$-4\pi \times 0.8^2 - \frac{288\pi \times 2 \times 0.5}{0.8^2} + \frac{576\pi \times 2 \times 0.5 \sqrt{3 \times 0.5}}{0.8^4} + \frac{288\pi \times 3 \times 0.2^2 \times 0.5}{0.8^4}$$

**Result:**

4121.53...

4121.53...

**Series representations:**

$$-4\pi 0.8^2 - \frac{288\pi \times 2 \times 0.5}{0.8^2} + \frac{576(\pi \times 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi \times 3 \times 0.2^2 \times 0.5)}{0.8^4} =$$

$$-410.372\pi + 1406.25\pi \sum_{k=0}^{\infty} \frac{(-0.5)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4} =$$

$$-410.372\pi - \frac{703.125\pi \sum_{j=0}^{\infty} \text{Res}_{s=-j} e^{0.693147s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)}{\sqrt{\pi}}$$

$$-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4} =$$

$$-410.372\pi + 1406.25\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1.5 - z_0)^k z_0^{-k}}{k!}$$

for (not ( $z_0 \in \mathbb{R}$  and  $-\infty < z_0 \leq 0$ ))

$$2\left(\left(-4\pi \cdot 0.8^2 - \frac{288\pi \cdot 2 \cdot (0.5)}{0.8^2} + \frac{576\pi \cdot 2 \cdot (0.5) \cdot \sqrt{3 \cdot 0.5}}{0.8^4} + \frac{288\pi \cdot 3 \cdot 0.2^2 \cdot 0.5}{0.8^4}\right)\right)^{1/2} - \pi$$

**Input:**

$$2\sqrt{-4\pi \times 0.8^2 - \frac{288\pi \times 2 \times 0.5}{0.8^2} + \frac{576\pi \times 2 \times 0.5 \sqrt{3 \times 0.5}}{0.8^4} + \frac{288\pi \times 3 \times 0.2^2 \times 0.5}{0.8^4}} - \pi$$

**Result:**

125.257...

125.257... result very near to the Higgs boson mass 125.18 GeV

**Series representations:**

$$2\sqrt{-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}} - \pi =$$

$$-\pi + 2\sqrt{\pi \left(-410.372 + 1406.25 \sum_{k=0}^{\infty} \frac{(-0.5)^k \left(-\frac{1}{2}\right)_k}{k!}\right)}$$

$$2\sqrt{-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}} - \pi =$$

$$-\pi + 2\sqrt{\pi \left(-410.372 - \frac{703.125 \sum_{j=0}^{\infty} \text{Res}_{s=-j} e^{0.693147s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)}{\sqrt{\pi}}\right)}$$

$$2\sqrt{-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}} - \pi =$$

$$- \pi + 2\sqrt{\pi \left( -410.372 + 1406.25 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1.5 - z_0)^k z_0^{-k}}{k!} \right)}$$

for (not ( $z_0 \in \mathbb{R}$  and  $-\infty < z_0 \leq 0$ ))

$$2\left(\left(-4\pi \cdot 0.8^2 - \frac{288\pi \cdot 2 \cdot 0.5}{0.8^2} + \frac{576\pi \cdot 2 \cdot 0.5 \cdot \sqrt{3 \cdot 0.5}}{0.8^4} + \frac{288\pi \cdot 3 \cdot 0.2^2 \cdot 0.5}{0.8^4}\right)\right)^{1/2} + 11$$

**Input:**

$$2\sqrt{-4\pi \times 0.8^2 - \frac{288\pi \times 2 \times 0.5}{0.8^2} + \frac{576\pi \times 2 \times 0.5 \sqrt{3 \times 0.5}}{0.8^4} + \frac{288\pi \times 3 \times 0.2^2 \times 0.5}{0.8^4}} + 11$$

**Result:**

139.398...

139.398... result practically equal to the rest mass of Pion meson 139.57 MeV

**Series representations:**

$$2\sqrt{-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}} + 11 =$$

$$11 + 2\sqrt{\pi \left( -410.372 + 1406.25 \sum_{k=0}^{\infty} \frac{(-0.5)^k \left(-\frac{1}{2}\right)_k}{k!} \right)}$$

$$2\sqrt{-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}} + 11 =$$

$$11 + 2\sqrt{\pi \left( -410.372 - \frac{703.125 \sum_{j=0}^{\infty} \text{Res}_{s=-j} e^{0.693147s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)}{\sqrt{\pi}} \right)}$$

$$2\sqrt{-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}} + 11 =$$

$$11 + 2\sqrt{\pi \left( -410.372 + 1406.25 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1.5 - z_0)^k z_0^{-k}}{k!} \right)}$$

for (not ( $z_0 \in \mathbb{R}$  and  $-\infty < z_0 \leq 0$ ))

$$-4 - \frac{1}{3} + 27 \sqrt{\left( -4\pi \cdot 0.8^2 - \frac{288\pi \cdot 2 \cdot 0.5}{0.8^2} + \frac{576\pi \cdot 2 \cdot 0.5 \cdot \sqrt{3 \cdot 0.5}}{0.8^4} + \frac{288\pi \cdot 3 \cdot 0.2^2 \cdot 0.5}{0.8^4} \right) + \pi \left( -410.372 + 1406.25 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1.5 - z_0)^k z_0^{-k}}{k!} \right)}$$

**Input:**

$$-4 - \frac{1}{3} + 27\sqrt{-4\pi \times 0.8^2 - \frac{288\pi \times 2 \times 0.5}{0.8^2} + \frac{576\pi \times 2 \times 0.5 \sqrt{3 \times 0.5}}{0.8^4} + \frac{288\pi \times 3 \times 0.2^2 \times 0.5}{0.8^4}}$$

**Result:**

1729.04...

1729.04...

This result is very near to the mass of candidate glueball **f<sub>0</sub>(1710) scalar meson**. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

**Series representations:**

$$-4 - \frac{1}{3} + 27\sqrt{-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}} =$$

$$-\frac{13}{3} + 27\sqrt{\pi \left( -410.372 + 1406.25 \sum_{k=0}^{\infty} \frac{(-0.5)^k \left(-\frac{1}{2}\right)_k}{k!} \right)}$$



$$-4 - \frac{1}{3} + 27 \sqrt{-4\pi \cdot 0.8^2 - \frac{288\pi \cdot 2 \times 0.5}{0.8^2} + \frac{576(\pi \cdot 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi \cdot 3 \times 0.2^2 \times 0.5)}{0.8^4}} = -\frac{13}{3} + 27 \sqrt{\pi \left( -410.372 - \frac{703.125 \sum_{j=0}^{\infty} \text{Res}_{s=-j} e^{0.693147s} \Gamma(-\frac{1}{2}-s) \Gamma(s)}{\sqrt{\pi}} \right)}$$

$$-4 - \frac{1}{3} + 27 \sqrt{-4\pi \cdot 0.8^2 - \frac{288\pi \cdot 2 \times 0.5}{0.8^2} + \frac{576(\pi \cdot 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi \cdot 3 \times 0.2^2 \times 0.5)}{0.8^4}} = -\frac{13}{3} + 27 \sqrt{\pi \left( -410.372 + 1406.25 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1.5 - z_0)^k z_0^{-k}}{k!} \right)}$$

for (not ( $z_0 \in \mathbb{R}$  and  $-\infty < z_0 \leq 0$ ))

((( (-4 - 1/3 + 27 \* ((( -4 \* Pi \* 0.8^2 - (288 \* Pi \* 2 \* (0.5)) / (0.8^2) + (576 \* Pi \* 2 \* (0.5) \* sqrt(3 \* 0.5)) / (0.8^4) + (288 \* Pi \* 3 \* 0.2^2 \* 0.5) / (0.8^4) ) ) ) ) ^ (1/2) ) ) ) ^ (1/15) - (21 + 5) / 10^3

**Input:**

$$\left( -4 - \frac{1}{3} + 27 \sqrt{\left( -4\pi \times 0.8^2 - \frac{288\pi \times 2 \times 0.5}{0.8^2} + \frac{576\pi \times 2 \times 0.5 \sqrt{3 \times 0.5}}{0.8^4} + \frac{288\pi \times 3 \times 0.2^2 \times 0.5}{0.8^4} \right)} \right)^{(1/15) - (21+5) \times \frac{1}{10^3}}$$

**Result:**

1.617818039608387419045008778173615872002417065323599984195...

1.617818039.... result that is a very good approximation to the value of the golden ratio 1.618033988749...

**Series representations:**

$$\left(-4 - \frac{1}{3} + 27 \sqrt{\left(-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}\right)}\right)^{(1/15) - \frac{21+5}{10^3}} =$$

$$-\frac{13}{500} + \sqrt[15]{-\frac{13}{3} + 27 \sqrt{\pi \left(-410.372 + 1406.25 \sum_{k=0}^{\infty} \frac{(-0.5)^k \left(-\frac{1}{2}\right)_k}{k!}\right)}}$$

$$\left(-4 - \frac{1}{3} + 27 \sqrt{\left(-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}\right)}\right)^{(1/15) - \frac{21+5}{10^3}} =$$

$$-\frac{13}{500} + \sqrt[15]{-\frac{13}{3} + 27 \sqrt{\pi \left(-410.372 - \frac{703.125 \sum_{j=0}^{\infty} \text{Res}_{s=-j} e^{0.693147s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)}{\sqrt{\pi}}\right)}}$$

$$\left(-4 - \frac{1}{3} + 27 \sqrt{\left(-4\pi 0.8^2 - \frac{288\pi 2 \times 0.5}{0.8^2} + \frac{576(\pi 2 \times 0.5 \sqrt{3 \times 0.5})}{0.8^4} + \frac{288(\pi 3 \times 0.2^2 \times 0.5)}{0.8^4}\right)}\right)^{(1/15) - \frac{21+5}{10^3}} = -\frac{13}{500} +$$

$$\sqrt[15]{-\frac{13}{3} + 27 \sqrt{\pi \left(-410.372 + 1406.25 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1.5 - z_0)^k z_0^{-k}}{k!}\right)}}$$

for (not  $(z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0)$ )

From:

**Charged Anti-de Sitter BTZ black holes in Maxwell-f(T) gravity**

*G. G. L. Nashed and S. Capozziello - arXiv:1710.06620v2 [gr-qc] 14 Apr 2018*

We have that:

$c_4$ ,  $c_5$  and  $c_6$  are integration constants.

The first two sets of the charged solution (24) are the same as the two sets of the non-charged solution. The metric of the third set of Eq. (24) takes the form

$$ds_3^2 = \frac{r^3[c_5^6 - 2c_6^2] - 4c_5^3 - 12r\epsilon c_4 c_5^2 - 2rc_5^4 - 6rc_5^4 \ln r}{2r} dt^2 - \frac{12c_5^2 \epsilon (rc_5 - 1)^2}{r(r^3 c_5^4 - 4c_5 - 12r\epsilon c_4 - 2rc_5^2 - 6rc_5^2 \ln r)} dr^2 - r^2 d\phi^2 - 2r^2 c_6 dt d\phi. \quad (31)$$

From:

$$ds_3^2 = \frac{r^3[c_5^6 - 2c_6^2] - 4c_5^3 - 12r\epsilon c_4 c_5^2 - 2rc_5^4 - 6rc_5^4 \ln r}{2r} dt^2 - \frac{12c_5^2 \epsilon (rc_5 - 1)^2}{r(r^3 c_5^4 - 4c_5 - 12r\epsilon c_4 - 2rc_5^2 - 6rc_5^2 \ln r)} dr^2 - r^2 d\phi^2 - 2r^2 c_6 dt d\phi.$$

For  $r = 5$ ;  $c_4 = 1$ ;  $c_5 = 2$ ;  $c_6 = 3$  and  $\epsilon = 1/12$ , we obtain:

$$(((5^3(2^6 - 2 \cdot 3^2) - 4 \cdot 2^3 - 12 \cdot 5 \cdot 1/12 \cdot 2^2 - 2 \cdot 5 \cdot 2^4 - 6 \cdot 5 \cdot 2^4 \ln(5))))/10$$

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right)$$

$$\frac{1}{10} (5538 - 480 \log(5))$$

476.5469802031631820191635520051429933027711349951111493481...

$$(((12 \cdot 2^2 \cdot 1/12 (5 \cdot 2 - 1)^2))) / (((5^3 \cdot 2^4 - 4 \cdot 2 - 12 \cdot 5 \cdot 1/12 - 2 \cdot 5 \cdot 2^2 - 6 \cdot 5 \cdot 2^2 \ln(5))))$$

**Input:**

$$\frac{12 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^2}{5 \left( 5^3 \times 2^4 - 4 \times 2 - 12 \times 5 \times \frac{1}{12} - 2 \times 5 \times 2^2 - (6 \times 5 \times 2^2) \log(5) \right)}$$

$\log(x)$  is the natural logarithm

**Exact result:**

$$\frac{324}{5 (1947 - 120 \log(5))}$$

**Decimal approximation:**

0.036946919780759010909767187294784679543447276664345434557...

0.03694691978.....

**Property:**

$\frac{324}{5(1947 - 120 \log(5))}$  is a transcendental number

Thence, we obtain:

$$\frac{((5^3(2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - 6 \times 5 \times 2^4 \ln(5)))}{10} - 0.036946919780759$$

**Input interpretation:**

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.036946919780759$$

$\log(x)$  is the natural logarithm

**Result:**

476.510033283382423...

476.51003....

**Alternative representations:**

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 = -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log_e(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right)$$

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 = -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log(a) \log_a(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right)$$

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 = -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 + 30 \operatorname{Li}_1(-4) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right)$$

### Series representations:

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) -$$

$$0.0369469197807590000 = 553.76305308021924 -$$

$$48.000000000000000000 \log(4) + 48.000000000000000000 \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{4}\right)^k}{k}$$

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) -$$

$$0.0369469197807590000 = 553.76305308021924 -$$

$$96.000000000000000000 i \pi \left[ \frac{\arg(5-x)}{2\pi} \right] - 48.000000000000000000 \log(x) +$$

$$48.000000000000000000 \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k} \text{ for } x < 0$$

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) -$$

$$0.0369469197807590000 =$$

$$553.7630530802192410000 - 48 \left[ \frac{\arg(5-z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) -$$

$$48 \log(z_0) - 48 \left[ \frac{\arg(5-z_0)}{2\pi} \right] \log(z_0) + 48 \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k}$$

### Integral representations:

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) -$$

$$0.0369469197807590000 =$$

$$553.76305308021924 - 48.000000000000000000 \int_1^5 \frac{1}{t} dt$$

$$\frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) -$$

$$0.0369469197807590000 = 553.7630530802192 -$$

$$\frac{24.000000000000000000}{i \pi} \int_{-i \infty + \gamma}^{i \infty + \gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$$\pi * (((((((5^3(2^6 - 2 \cdot 3^2) - 4 \cdot 2^3 - 12 \cdot 5 \cdot \frac{1}{12} \cdot 2^2 - 2 \cdot 5 \cdot 2^4 - 6 \cdot 5 \cdot 2^4 \ln(5)))))))/10 - 0.036946919780759)) + 144 + 89 - 1$$

**Input interpretation:**

$$\pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.036946919780759 \right) + 144 + 89 - 1$$

$\log(x)$  is the natural logarithm

**Result:**

1729.00041992490208...

1729.0004....

This result is very near to the mass of candidate glueball  **$f_0(1710)$  scalar meson**. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

**Alternative representations:**

$$\pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) +$$

$$144 + 89 - 1 = 232 + \pi \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log_e(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right)$$

$$\pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) +$$

$$144 + 89 - 1 = 232 + \pi \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log(a) \log_a(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right)$$

$$\pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 = 232 + \pi \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 + 30 \operatorname{Li}_1(-4) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right)$$

### Series representations:

$$\pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 = 232.0000000000000000 + 553.76305308021924 \pi - 48.0000000000000000 \pi \log(4) + 48.0000000000000000 \pi \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{4}\right)^k}{k}$$

$$\pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 = 232.0000000000000000 + 553.76305308021924 \pi - 96.0000000000000000 i \pi^2 \left[ \frac{\arg(5-x)}{2 \pi} \right] - 48.0000000000000000 \pi \log(x) + 48.0000000000000000 \pi \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k} \text{ for } x < 0$$

$$\pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 = 232 + 553.7630530802192410000 \pi - 48 \pi \left[ \frac{\arg(5-z_0)}{2 \pi} \right] \log\left(\frac{1}{z_0}\right) - 48 \pi \log(z_0) - 48 \pi \left[ \frac{\arg(5-z_0)}{2 \pi} \right] \log(z_0) + 48 \pi \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k}$$

**Integral representations:**

$$\pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 =$$

$$232.0000000000000000 + 553.76305308021924 \pi - 48.00000000000000000 \pi \int_1^5 \frac{1}{t} dt$$

$$\pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 =$$

$$\frac{232.0000000000000000 + 553.7630530802192 \pi - 24.00000000000000000}{i} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$$\left( \left( \left( \left( \left( \left( \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - 6 \times 5 \times 2^4 \ln(5) \right) \right) \right) \right) \right) \right) / 10 - 0.036946919780759 \right) + 21$$

**Input interpretation:**

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.036946919780759 \right) + 21$$

log(x) is the natural logarithm

**Result:**

497.510033283382423...

497.51003.... result practically equal to the rest mass of Kaon meson 497.614

**Alternative representations:**

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 21 = 20.9630530802192410000 +$$

$$\frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log_e(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right)$$



$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 21 = 20.9630530802192410000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log(a) \log_a(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right)$$

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 21 = 20.9630530802192410000 + \frac{1}{10} \left( -32 - 10 \times 2^4 + 30 \operatorname{Li}_1(-4) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right)$$

### Series representations:

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 21 = 574.76305308021924100 - 48.00000000000000000000 \log(4) + 48.00000000000000000000 \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{4}\right)^k}{k}$$

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 21 = 574.76305308021924100 - 96.00000000000000000000 i \pi \left[ \frac{\arg(5-x)}{2\pi} \right] - 48.00000000000000000000 \log(x) + 48.00000000000000000000 \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k} \text{ for } x < 0$$

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 21 = 574.7630530802192410000 - 48 \left[ \frac{\arg(5-z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) - 48 \log(z_0) - 48 \left[ \frac{\arg(5-z_0)}{2\pi} \right] \log(z_0) + 48 \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k}$$

**Integral representations:**

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 21 = 574.76305308021924100 - 48.00000000000000000000 \int_1^5 \frac{1}{t} dt$$

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 21 = 574.7630530802192410 - \frac{24.00000000000000000000}{i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$$1/\text{Pi}(((((((5^3(2^6-2*3^2)-4*2^3-12*5*1/12*2^2-2*5*2^4-6*5*2^4 \ln(5))))/10 - 0.036946919780759))))-7-3-2$$

**Input interpretation:**

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.036946919780759 \right) - 7 - 3 - 2$$

log(x) is the natural logarithm

**Result:**

139.677854459867764...

139.677854.... result practically equal to the rest mass of Pion meson 139.57 MeV

**Alternative representations:**

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 7 - 3 - 2 = -12 + \frac{1}{\pi} \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log_e(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right)$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 7 - 3 - 2 =$$

$$-12 + \frac{1}{\pi} \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log(a) \log_a(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right)$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 7 - 3 - 2 =$$

$$-12 + \frac{1}{\pi} \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 + 30 \operatorname{Li}_1(-4) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right)$$

### Series representations:

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 7 - 3 - 2 =$$

$$-12.000000000000000000 + \frac{553.76305308021924}{\pi} -$$

$$\frac{48.000000000000000000 \log(4)}{\pi} + \frac{48.000000000000000000 \sum_{k=1}^{\infty} \frac{(-\frac{1}{4})^k}{k}}{\pi}$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 7 - 3 - 2 =$$

$$-12.000000000000000000 + \frac{553.76305308021924}{\pi} -$$

$$96.000000000000000000 i \left[ \frac{\arg(5-x)}{2\pi} \right] - \frac{48.000000000000000000 \log(x)}{\pi} +$$

$$\frac{48.000000000000000000 \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k}}{\pi} \quad \text{for } x < 0$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 7 - 3 - 2 =$$

$$-12.000000000000000000 + \frac{553.76305308021924}{\pi} -$$

$$96.000000000000000000 i \left[ -\frac{-\pi + \arg\left(\frac{5}{z_0}\right) + \arg(z_0)}{2\pi} \right] -$$

$$\frac{48.000000000000000000 \log(z_0)}{\pi} + \frac{48.000000000000000000 \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k}}{\pi}$$

**Integral representations:**

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 7 - 3 - 2 = -12.000000000000000000 +$$

$$\frac{553.76305308021924}{\pi} - \frac{48.000000000000000000}{\pi} \int_1^5 \frac{1}{t} dt$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 7 - 3 - 2 =$$

$$-12.000000000000000000 + \frac{553.76305308021924}{\pi} -$$

$$\frac{24.000000000000000000}{i\pi^2} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$$1/\text{Pi}(((((((5^3(2^6-2*3^2)-4*2^3-12*5*1/12*2^2-2*5*2^4-6*5*2^4 \ln(5)))))/10 - 0.036946919780759))))-21-5$$

**Input interpretation:**

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.036946919780759 \right) - 21 - 5$$

log(x) is the natural logarithm

**Result:**

125.677854459867764...

125.677854.... result very near to the Higgs boson mass 125.18 GeV

**Alternative representations:**

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 21 - 5 = -26 + \frac{1}{\pi} \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log_e(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right)$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 21 - 5 = -26 + \frac{1}{\pi} \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log(a) \log_a(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right)$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 21 - 5 = -26 + \frac{1}{\pi} \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 + 30 \operatorname{Li}_1(-4) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right)$$

**Series representations:**

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 21 - 5 = -26.000000000000000000 + \frac{553.76305308021924}{\pi} - \frac{48.000000000000000000 \log(4)}{\pi} + \frac{48.000000000000000000 \sum_{k=1}^{\infty} \frac{(-1)^k}{k}}{\pi}$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 21 - 5 = -26.000000000000000000 + \frac{553.76305308021924}{\pi} - \frac{96.000000000000000000 i \left[ \frac{\arg(5-x)}{2\pi} \right]}{\pi} - \frac{48.000000000000000000 \log(x)}{\pi} + \frac{48.000000000000000000 \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k}}{\pi} \text{ for } x < 0$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 21 - 5 =$$

$$-26.000000000000000000 + \frac{553.76305308021924}{\pi} -$$

$$96.000000000000000000 i \left[ -\frac{-\pi + \arg\left(\frac{5}{z_0}\right) + \arg(z_0)}{2\pi} \right] -$$

$$\frac{48.000000000000000000 \log(z_0)}{\pi} + \frac{48.000000000000000000 \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k}}{\pi}$$

**Integral representations:**

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 21 - 5 = -26.000000000000000000 +$$

$$\frac{553.76305308021924}{\pi} - \frac{48.000000000000000000}{\pi} \int_1^5 \frac{1}{t} dt$$

$$\frac{1}{\pi} \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12}{12} (5 \times 2^2) - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.0369469197807590000 \right) - 21 - 5 =$$

$$-26.000000000000000000 + \frac{553.76305308021924}{\pi} -$$

$$\frac{24.000000000000000000}{i\pi^2} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$[Pi*(((5^3(2^6-2*3^2)-4*2^3-12*5*1/12*2^2-2*5*2^4-6*5*2^4 \ln(5))))/10 - 0.036946919780759)))+144+89-1]^{1/15}-(21+5)1/10^3$

**Input interpretation:**

$$\left( \pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.036946919780759 \right) + 144 + 89 - 1 \right)^{1/15} - (21 + 5) \times \frac{1}{10^3}$$

$\log(x)$  is the natural logarithm

**Result:**

1.617815255364454783...

1.6178152553644.... result that is a very good approximation to the value of the golden ratio 1.618033988749...

**Alternative representations:**

$$\left( \pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 \right)^{(1/15)} - \frac{21+5}{10^3} = -\frac{26}{10^3} + \left( 232 + \pi \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log_e(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right) \right)^{(1/15)}$$

$$\left( \pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 \right)^{(1/15)} - \frac{21+5}{10^3} = -\frac{26}{10^3} + \left( 232 + \pi \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 - 30 \log(a) \log_a(5) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right) \right)^{(1/15)}$$

$$\left( \pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 \right)^{(1/15)} - \frac{21+5}{10^3} = -\frac{26}{10^3} + \left( 232 + \pi \left( -0.0369469197807590000 + \frac{1}{10} \left( -32 - 10 \times 2^4 + 30 \operatorname{Li}_1(-4) 2^4 + (-18 + 2^6) 5^3 - \frac{240}{12} \right) \right) \right)^{(1/15)}$$





$$\left( \pi \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - \log(5) 6 (5 \times 2^4) \right) - 0.0369469197807590000 \right) + 144 + 89 - 1 \right)^{(1/15)} - \frac{21+5}{10^3} =$$

$$-\frac{13}{500} + 15 \sqrt[15]{232 + 553.7630530802192410000 \pi - \frac{24}{i} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds}$$

for  $-1 < \gamma < 0$

$\Gamma(x)$  is the gamma function

We have also:

$$dr^2 - r^2 d\phi^2 - 2r^2 c_6 dt d\phi.$$

For  $r = 5$ ,  $c_6 = 3$ , we obtain:

**Input interpretation:**

$$\frac{\partial 25}{\partial x} - 25 \times \frac{\partial (x^2 - 2 \times 25 \times 3)}{\partial x} x'(x)$$

**Result:**

$$-50x$$

For  $x = 1$ ;  $-50$

Thence:

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - \frac{12 \times 5 \times 2^2}{12} - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) - 0.036946919780759 \right) \times \frac{\partial (-25)}{\partial x} x^2 - (2 \times 25 \times 3) x'(x)$$

**Input interpretation:**

$$\left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) + \frac{\partial 25}{\partial x} \times (-0.036946919780759) \right) \times \frac{\partial (-25)}{\partial x} x^2 - (2 \times 25 \times 3) x'(x)$$

$\log(x)$  is the natural logarithm

**Exact result:**

-150

-150

From which:

-((((((((5^3(2^6-2\*3^2)-4\*2^3-12\*5\*1/12\*2^2-2\*5\*2^4-6\*5\*2^4 ln(5)))))/10 - 0.036946919780759\*(partial derivative 25))))- 25 partial derivative x^2 - 2\*25\*3 partial derivative x]+11-1/golden ratio))

**Input interpretation:**

$$-\left(\left(\left(\frac{1}{10} \left(5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5)\right) + \frac{\partial 25}{\partial x} \times (-0.036946919780759)\right) \times \frac{\partial(-25)}{\partial x} x^2 - (2 \times 25 \times 3) x'(x)\right) + 11 - \frac{1}{\phi}\right)$$

log(x) is the natural logarithm

φ is the golden ratio

**Result:**

$$\frac{1}{\phi} + 139$$

**Decimal approximation:**

139.6180339887498948482045868343656381177203091798057628621...

139.61803398.... result practically equal to the rest mass of Pion meson 139.57 MeV

**Alternate forms:**

$$\frac{139 \phi + 1}{\phi}$$

$$\frac{1}{2} (277 + \sqrt{5})$$

$$\frac{\sqrt{5}}{2} + \frac{277}{2}$$

-((((((((5^3(2^6-2\*3^2)-4\*2^3-12\*5\*1/12\*2^2-2\*5\*2^4-6\*5\*2^4 ln(5)))))/10 - 0.036946919780759\*(partial derivative 25))))- 25 partial derivative x^2 - 2\*25\*3 partial derivative x]+18+7-1/golden ratio))

**Input interpretation:**

$$-\left(\left(\left(\frac{1}{10} \left(5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5)\right) + \frac{\partial 25}{\partial x} \times (-0.036946919780759)\right) \times \frac{\partial(-25)}{\partial x} x^2 - (2 \times 25 \times 3) x'(x)\right) + 18 + 7 - \frac{1}{\phi}\right)$$

log(x) is the natural logarithm

φ is the golden ratio

**Result:**

$$\frac{1}{\phi} + 125$$

**Decimal approximation:**

125.6180339887498948482045868343656381177203091798057628621...

125.61803398... result very near to the Higgs boson mass 125.18 GeV

**Alternate forms:**

$$\frac{125 \phi + 1}{\phi}$$

$$\frac{1}{2} (249 + \sqrt{5})$$

$$\frac{\sqrt{5}}{2} + \frac{249}{2}$$

27\*1/2\*-(((5^3(2^6-2\*3^2)-4\*2^3-12\*5\*1/12\*2^2-2\*5\*2^4-6\*5\*2^4 ln(5))))/10 - 0.036946919780759\*(partial derivative 25))- 25 partial derivative x^2 - 2\*25\*3 partial derivative x]+18+4))+1

**Input interpretation:**

$$27 \times \frac{1}{2} \times (-1) \left( \left( \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) + \frac{\partial 25}{\partial x} \times (-0.036946919780759) \right) \times \frac{\partial(-25)}{\partial x} x^2 - (2 \times 25 \times 3) x'(x) \right) + 18 + 4 \right) + 1$$

log(x) is the natural logarithm

**Exact result:**

1729  
1729

This result is very near to the mass of candidate glueball **f<sub>0</sub>(1710) scalar meson**. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

$$[27 \times \frac{1}{2} \times (-1) \times ((((((5^3(2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - 6 \times 5 \times 2^4 \ln(5)))))/10 - 0.036946919780759 \times (\partial_{25})) - 25 \partial_{x^2} - 2 \times 25 \times 3 \partial_{x'} + 18 + 4) + 1]^{1/15} - \frac{21 + 5}{10^3}$$

**Input interpretation:**

$$\left( 27 \times \frac{1}{2} \times (-1) \times \left( \left( \frac{1}{10} \left( 5^3 (2^6 - 2 \times 3^2) - 4 \times 2^3 - 12 \times 5 \times \frac{1}{12} \times 2^2 - 2 \times 5 \times 2^4 - (6 \times 5 \times 2^4) \log(5) \right) + \frac{\partial 25}{\partial x} \times (-0.036946919780759) \right) \times \frac{\partial(-25)}{\partial x} x^2 - (2 \times 25 \times 3) x'(x) + 18 + 4 \right) + 1 \right)^{1/15} - \frac{21 + 5}{10^3}$$

log(x) is the natural logarithm

**Result:**

$$\sqrt[15]{1729} - \frac{13}{500}$$

**Decimal approximation:**

1.617815228748728130580088031324769514329283143699940172645...

1.617815228748..... result that is a very good approximation to the value of the golden ratio 1.618033988749...

**Alternate forms:**

$$\frac{1}{500} \left( 500 \sqrt[15]{1729} - 13 \right)$$

$$\frac{1}{500} \left( 500 \left( \begin{array}{l} \text{root of} \\ 31250000000000x^5 + 68656250000000x^4 + 603351125000000x^3 + \\ 2651124843250000x^2 + 58245212806202500x - \\ 527648925781249999999999999948814106985909243 \\ \text{near } x = 1.11045 \times 10^6 \end{array} \right) + 2197 \right)^{(1/3) - 13}$$

We have that:

$$\nabla_{\alpha} T^{\alpha} = \frac{13c_5^2 + 12|\epsilon|c_4 + 6c_5^2 \ln r - 6rc_5^3 - 6r^2c_5^4 + 4r^3c_5^5}{6c_5^2 |\epsilon| (rc_5 - 1)^3} \sim \left( \frac{1}{r} \right),$$

For:  $r = 5$ ;  $c_4 = 1$ ;  $c_5 = 2$ ;  $c_6 = 3$  and  $\epsilon = 1/12$ , we obtain:

$$\left( \frac{13 \cdot 2^2 + 12 \cdot \frac{1}{12} + 6 \cdot 2^2 \ln(5) - 6 \cdot 5 \cdot 2^3 - 6 \cdot 25 \cdot 2^4 + 4 \cdot 5^3 \cdot 2^5}{6 \cdot 2^2 \cdot \frac{1}{12} \cdot (5 \cdot 2 - 1)^3} \right)$$

**Input:**

$$\frac{13 \times 2^2 + 12 \times \frac{1}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{6 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^3}$$

$\log(x)$  is the natural logarithm

**Exact result:**

$$\frac{13413 + 24 \log(5)}{1458}$$

**Decimal approximation:**

9.226081282509203298347337602193023664848158046983843913117...

9.2260812825...

**Property:**

$$\frac{13413 + 24 \log(5)}{1458} \text{ is a transcendental number}$$

**Alternate forms:**

$$\frac{4471}{486} + \frac{4 \log(5)}{243}$$

$$\frac{1}{486} (4471 + 8 \log(5))$$

**Alternative representations:**

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} =$$

$$\frac{-188 + 24 \log_e(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}}$$

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} =$$

$$\frac{-188 + 24 \log(a) \log_a(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}}$$

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} =$$

$$\frac{-188 - 24 \operatorname{Li}_1(-4) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}}$$

**Series representations:**

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} =$$

$$\frac{4471}{486} + \frac{4 \log(4)}{243} - \frac{4}{243} \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{4}\right)^k}{k}$$

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} =$$

$$\frac{4471}{486} + \frac{8}{243} i \pi \left[ \frac{\arg(5-x)}{2\pi} \right] + \frac{4 \log(x)}{243} - \frac{4}{243} \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k} \quad \text{for } x < 0$$

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} =$$

$$\frac{4471}{486} + \frac{4}{243} \left[ \frac{\arg(5 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \frac{4 \log(z_0)}{243} +$$

$$\frac{4}{243} \left[ \frac{\arg(5 - z_0)}{2\pi} \right] \log(z_0) - \frac{4}{243} \sum_{k=1}^{\infty} \frac{(-1)^k (5 - z_0)^k z_0^{-k}}{k}$$

**Integral representations:**

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} =$$

$$\frac{4471}{486} + \frac{4}{243} \int_1^5 \frac{1}{t} dt$$

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} =$$

$$\frac{4471}{486} - \frac{2i}{243\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$$1/(3+\sqrt{7}) (((13*2^2+12*1/12+6*2^2 \ln(5) - 6*5*2^3-6*25*2^4+4*5^3*2^5))/((6*2^2*1/12*(5*2-1)^3)))-((13+3)/10^3)$$

**Input:**

$$\frac{1}{3 + \sqrt{7}} \times \frac{13 \times 2^2 + 12 \times \frac{1}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{6 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^3} -$$

$$(13 + 3) \times \frac{1}{10^3}$$

log(x) is the natural logarithm

**Exact result:**

$$\frac{13413 + 24 \log(5)}{1458 (3 + \sqrt{7})} - \frac{2}{125}$$

**Decimal approximation:**

1.618163599170202930410423187542076603669365975631431240523...

1.61816359917.... result that is a very good approximation to the value of the golden ratio 1.618033988749...

**Property:**

$-\frac{2}{125} + \frac{13413 + 24 \log(5)}{1458(3 + \sqrt{7})}$  is a transcendental number

**Alternate forms:**

$$\frac{(3 - \sqrt{7})(13413 + 24 \log(5))}{2916} - \frac{2}{125}$$

$$-\frac{-555959 + 972\sqrt{7} - 1000 \log(5)}{60750(3 + \sqrt{7})}$$

$$\frac{555959 - 972\sqrt{7} + 1000 \log(5)}{60750(3 + \sqrt{7})}$$

**Alternative representations:**

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{1}{12} (6 \times 2^2 (5 \times 2 - 1)^3) (3 + \sqrt{7})} - \frac{13 + 3}{10^3} =$$

$$-\frac{16}{10^3} + \frac{-188 + 24 \log_e(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{1}{12} (24 \times 9^3) (3 + \sqrt{7})}$$

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{1}{12} (6 \times 2^2 (5 \times 2 - 1)^3) (3 + \sqrt{7})} - \frac{13 + 3}{10^3} =$$

$$-\frac{16}{10^3} + \frac{-188 + 24 \log(a) \log_a(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{1}{12} (24 \times 9^3) (3 + \sqrt{7})}$$

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{1}{12} (6 \times 2^2 (5 \times 2 - 1)^3) (3 + \sqrt{7})} - \frac{13 + 3}{10^3} =$$

$$-\frac{16}{10^3} + \frac{-188 - 24 \operatorname{Li}_1(-4) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{1}{12} (24 \times 9^3) (3 + \sqrt{7})}$$

**Series representations:**

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{1}{12} (6 \times 2^2 (5 \times 2 - 1)^3) (3 + \sqrt{7})} - \frac{13 + 3}{10^3} =$$

$$-\frac{2}{125} + \frac{4471}{486(3 + \sqrt{7})} + \frac{4 \log(4)}{243(3 + \sqrt{7})} - \frac{4 \sum_{k=1}^{\infty} \frac{(-\frac{1}{4})^k}{k}}{243(3 + \sqrt{7})}$$



$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{1}{12} (6 \times 2^2 (5 \times 2 - 1)^3) (3 + \sqrt{7})} - \frac{13 + 3}{10^3} =$$

$$-\frac{2}{125} + \frac{4471 + 8 \log(z_0) + 8 \left[ \frac{\arg(5-z_0)}{2\pi} \right] \left( \log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - 8 \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k}}{486 (3 + \sqrt{7})}$$

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{1}{12} (6 \times 2^2 (5 \times 2 - 1)^3) (3 + \sqrt{7})} - \frac{13 + 3}{10^3} =$$

$$-\frac{2}{125} + \frac{13413 + 24 \left( \log(z_0) + \left[ \frac{\arg(5-z_0)}{2\pi} \right] \left( \log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k} \right)}{1458 (3 + \sqrt{7})}$$

### Integral representations:

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{1}{12} (6 \times 2^2 (5 \times 2 - 1)^3) (3 + \sqrt{7})} - \frac{13 + 3}{10^3} =$$

$$-\frac{2}{125} + \frac{4471}{486 (3 + \sqrt{7})} + \frac{4}{243 (3 + \sqrt{7})} \int_1^5 \frac{1}{t} dt$$

$$\frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{1}{12} (6 \times 2^2 (5 \times 2 - 1)^3) (3 + \sqrt{7})} - \frac{13 + 3}{10^3} = -\frac{2}{125} +$$

$$\frac{4471}{486 (3 + \sqrt{7})} - \frac{2i}{243 (3 + \sqrt{7}) \pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$$10^3 + \left( \frac{13 \times 2^2 + 12 \times \frac{1}{12} + 6 \times 2^2 \ln(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{6 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^3} \right)^3$$

### Input:

$$10^3 + \left( \frac{13 \times 2^2 + 12 \times \frac{1}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{6 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^3} \right)^3$$

$\log(x)$  is the natural logarithm

### Exact result:

$$1000 + \frac{(13413 + 24 \log(5))^3}{3099363912}$$

### Decimal approximation:

1785.329351435099867732870606269497943875892837859548217412...

1785.329351435... result in the range of the hypothetical mass of Gluino (gluino = 1785.16 GeV).

### Property:

$1000 + \frac{(13413 + 24 \log(5))^3}{3099363912}$  is a transcendental number

### Alternate forms:

$$1000 + \frac{(4471 + 8 \log(5))^3}{114791256}$$

$$\frac{(9331 + 8 \log(5))(21880381 + 64 \log^2(5) + 32656 \log(5))}{114791256}$$

$$\frac{204165835111 + 512 \log^3(5) + 858432 \log^2(5) + 479756184 \log(5)}{114791256}$$

### Alternative representations:

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 =$$
$$10^3 + \left( \frac{-188 + 24 \log_e(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times \varphi^3}{12}} \right)^3$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 =$$
$$10^3 + \left( \frac{-188 + 24 \log(a) \log_a(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times \varphi^3}{12}} \right)^3$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 =$$
$$10^3 + \left( \frac{-188 - 24 \text{Li}_1(-4) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times \varphi^3}{12}} \right)^3$$

### Series representations:

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 =$$

$$1000 + \frac{\left( 4471 + 8 \log(4) - 8 \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{4}\right)^k}{k} \right)^3}{114791256}$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 =$$

$$1000 + \frac{\left( 13413 + 24 \left( 2i\pi \left\lfloor \frac{\arg(5-x)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k} \right) \right)^3}{3099363912} \quad \text{for } x < 0$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 =$$

$$1000 + \frac{\left( 13413 + 24 \left( \log(z_0) + \left\lfloor \frac{\arg(5-z_0)}{2\pi} \right\rfloor \right) \left( \log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k} \right)^3}{3099363912}$$

### Integral representations:

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 =$$

$$1000 + \frac{\left( 4471 + 8 \int_1^5 \frac{1}{t} dt \right)^3}{114791256}$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 =$$

$$1000 + \frac{\left( 4471\pi - 4i \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \right)^3}{114791256 \pi^3} \quad \text{for } -1 < \gamma < 0$$

$$10^3 + \left( \frac{13 \times 2^2 + 12 \times \frac{1}{12} + 6 \times 2^2 \ln(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{6 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2}$$

**Input:**

$$10^3 + \left( \frac{13 \times 2^2 + 12 \times \frac{1}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{6 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2}$$

$\log(x)$  is the natural logarithm

**Exact result:**

$$945 - \sqrt{2} + \frac{(13413 + 24 \log(5))^3}{3099363912}$$

**Decimal approximation:**

1728.915137872726772684068917545288245797323165984171269339...

$$1728.915137872... \approx 1729$$

This result is very near to the mass of candidate glueball  **$f_0(1710)$  scalar meson**. Furthermore, 1728 occurs in the algebraic formula for the  $j$ -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

**Property:**

$$945 - \sqrt{2} + \frac{(13413 + 24 \log(5))^3}{3099363912} \text{ is a transcendental number}$$

**Alternate forms:**

$$945 - \sqrt{2} + \frac{(4471 + 8 \log(5))^3}{114791256}$$

$$\frac{1}{114791256} \left( 197852316031 - 114791256 \sqrt{2} + 512 \log^3(5) + 858432 \log^2(5) + 479756184 \log(5) \right)$$

$$\frac{197852316031}{114791256} - \sqrt{2} + \frac{64 \log^3(5)}{14348907} + \frac{35768 \log^2(5)}{4782969} + \frac{19989841 \log(5)}{4782969}$$

### Alternative representations:

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2} =$$

$$-55 + 10^3 + \left( \frac{-188 + 24 \log_e(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}} \right)^3 - \sqrt{2}$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2} =$$

$$-55 + 10^3 + \left( \frac{-188 + 24 \log(a) \log_a(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}} \right)^3 - \sqrt{2}$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2} =$$

$$-55 + 10^3 + \left( \frac{-188 - 24 \operatorname{Li}_1(-4) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}} \right)^3 - \sqrt{2}$$

### Series representations:

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2} =$$

$$945 - \sqrt{2} + \frac{\left( 4471 + 8 \log(4) - 8 \sum_{k=1}^{\infty} \frac{(-\frac{1}{4})^k}{k} \right)^3}{114791256}$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2} =$$

$$945 - \sqrt{2} + \frac{\left( 13413 + 24 \left( 2i\pi \left[ \frac{\operatorname{arg}(5-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k} \right) \right)^3}{3099363912} \quad \text{for } x < 0$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2} =$$

$$945 - \sqrt{2} + \frac{\left( 4471 + 8 \log(z_0) + 8 \left[ \frac{\operatorname{arg}(5-z_0)}{2\pi} \right] \left( \log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - 8 \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k} \right)^3}{114791256}$$

**Integral representations:**

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2} =$$

$$945 - \sqrt{2} + \frac{(4471 + 8 \int_1^5 \frac{1}{t} dt)^3}{114791256}$$

$$10^3 + \left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^3 - 55 - \sqrt{2} =$$

$$945 - \sqrt{2} + \frac{(4471 \pi - 4 i \int_{-i \infty + \gamma}^{i \infty + \gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds)^3}{114791256 \pi^3} \text{ for } -1 < \gamma < 0$$

(((13\*2^2+12\*1/12+6\*2^2 ln(5) - 6\*5\*2^3- 6\*25\*2^4+4\*5^3\*2^5))/((6\*2^2\*1/12\*(5\*2-1)^3)))^2+55-1/golden ratio

**Input:**

$$\left( \frac{13 \times 2^2 + 12 \times \frac{1}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{6 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^3} \right)^2 + 55 - \frac{1}{\phi}$$

log(x) is the natural logarithm

φ is the golden ratio

**Exact result:**

$$-\frac{1}{\phi} + 55 + \frac{(13413 + 24 \log(5))^2}{2125764}$$

**Decimal approximation:**

139.5025418427167707152847671369378051619897982544675315556...

139.5025418427... result practically equal to the rest mass of Pion meson 139.57 MeV

**Property:**

$55 - \frac{1}{\phi} + \frac{(13413 + 24 \log(5))^2}{2125764}$  is a transcendental number

**Alternate forms:**

$$-\frac{1}{\phi} + 55 + \frac{(4471 + 8 \log(5))^2}{236196}$$

$$-\frac{1}{\phi} + \frac{32980621}{236196} + \frac{16 \log^2(5)}{59049} + \frac{17884 \log(5)}{59049}$$

$$\frac{32980621 + 64 \log^2(5) + 71536 \log(5)}{236196} - \frac{1}{\phi}$$

**Alternative representations:**

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 55 - \frac{1}{\phi} =$$

$$55 - \frac{1}{\phi} + \left( \frac{-188 + 24 \log_e(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}} \right)^2$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 55 - \frac{1}{\phi} =$$

$$55 - \frac{1}{\phi} + \left( \frac{-188 + 24 \log(a) \log_a(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}} \right)^2$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 55 - \frac{1}{\phi} =$$

$$55 - \frac{1}{\phi} + \left( \frac{-188 - 24 \text{Li}_1(-4) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}} \right)^2$$

**Series representations:**

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 55 - \frac{1}{\phi} =$$

$$55 - \frac{1}{\phi} + \frac{\left( 4471 + 8 \log(4) - 8 \sum_{k=1}^{\infty} \frac{\left(\frac{-1}{4}\right)^k}{k} \right)^2}{236196}$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 55 - \frac{1}{\phi} =$$

$$55 - \frac{1}{\phi} + \frac{\left( 13413 + 24 \left( 2i\pi \left[ \frac{\text{arg}(5-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k} \right) \right)^2}{2125764} \text{ for } x < 0$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 55 - \frac{1}{\phi} =$$

$$55 - \frac{1}{\phi} + \frac{\left( 13413 + 24 \left( \log(z_0) + \left[ \frac{\text{arg}(5-z_0)}{2\pi} \right] \right) \left( \log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k} \right)^2}{2125764}$$

### Integral representations:

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 55 - \frac{1}{\phi} =$$

$$\frac{1}{236196(1+\sqrt{5})} \left( 32508229 + 32980621\sqrt{5} + 71536 \int_1^5 \frac{1}{t} dt + \right.$$

$$\left. 71536\sqrt{5} \int_1^5 \frac{1}{t} dt + 64 \left( \int_1^5 \frac{1}{t} dt \right)^2 + 64\sqrt{5} \left( \int_1^5 \frac{1}{t} dt \right)^2 \right)$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 55 - \frac{1}{\phi} =$$

$$55 - \frac{1}{\phi} + \frac{\left( 4471\pi - 4i \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \right)^2}{236196\pi^2} \text{ for } -1 < \gamma < 0$$

$$\left( \frac{13 \times 2^2 + 12 \times \frac{1}{12} + 6 \times 2^2 \ln(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{6 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^3} \right)^2 + 47 - 7$$

### Input:

$$\left( \frac{13 \times 2^2 + 12 \times \frac{1}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{6 \times 2^2 \times \frac{1}{12} (5 \times 2 - 1)^3} \right)^2 + 47 - 7$$

$\log(x)$  is the natural logarithm

### Exact result:

$$40 + \frac{(13413 + 24 \log(5))^2}{2125764}$$



**Decimal approximation:**

125.1205758314666655634893539713034432797101074342732944177...

125.1205758314... result very near to the Higgs boson mass 125.18 GeV

**Property:**

$40 + \frac{(13413 + 24 \log(5))^2}{2125764}$  is a transcendental number

**Alternate forms:**

$$40 + \frac{(4471 + 8 \log(5))^2}{236196}$$

$$\frac{29437681 + 64 \log^2(5) + 71536 \log(5)}{236196}$$

$$\frac{29437681}{236196} + \frac{16 \log^2(5)}{59049} + \frac{17884 \log(5)}{59049}$$

**Alternative representations:**

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 47 - 7 =$$

$$40 + \left( \frac{-188 + 24 \log_e(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}} \right)^2$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 47 - 7 =$$

$$40 + \left( \frac{-188 + 24 \log(a) \log_a(5) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}} \right)^2$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 47 - 7 =$$

$$40 + \left( \frac{-188 - 24 \text{Li}_1(-4) - 150 \times 2^4 + 4 \times 2^5 \times 5^3 + \frac{12}{12}}{\frac{24 \times 9^3}{12}} \right)^2$$

**Series representations:**

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 47 - 7 =$$

$$40 + \frac{\left( 4471 + 8 \log(4) - 8 \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{4}\right)^k}{k} \right)^2}{236196}$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 47 - 7 =$$

$$40 + \frac{\left( 13413 + 24 \left( 2i\pi \left\lfloor \frac{\text{arg}(5-x)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (5-x)^k x^{-k}}{k} \right) \right)^2}{2125764} \quad \text{for } x < 0$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 47 - 7 =$$

$$40 + \frac{\left( 13413 + 24 \left( \log(z_0) + \left\lfloor \frac{\text{arg}(5-z_0)}{2\pi} \right\rfloor \right) \left( \log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k (5-z_0)^k z_0^{-k}}{k} \right)^2}{2125764}$$

**Integral representations:**

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 47 - 7 =$$

$$\frac{29437681 + 71536 \int_1^5 \frac{1}{t} dt + 64 \left( \int_1^5 \frac{1}{t} dt \right)^2}{236196}$$

$$\left( \frac{13 \times 2^2 + \frac{12}{12} + 6 \times 2^2 \log(5) - 6 \times 5 \times 2^3 - 6 \times 25 \times 2^4 + 4 \times 5^3 \times 2^5}{\frac{6}{12} \times 2^2 (5 \times 2 - 1)^3} \right)^2 + 47 - 7 =$$

$$40 + \frac{\left( 4471\pi - 4i \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \right)^2}{236196 \pi^2} \quad \text{for } -1 < \gamma < 0$$

We have that:

$$T = \frac{r_h^3 - 3r_h \sqrt[3]{36\epsilon^2} + 2\sqrt[3]{6\epsilon}}{24\pi |\epsilon| r_h^2}, \quad r = r_h.$$

$$\left( (5^3 - 3 \cdot 5 \cdot (36 \cdot (1/12)^2)^{1/3} + 2 \cdot (6 \cdot 1/12)^{1/3} \right) / (24\pi \cdot 1/12 \cdot 5^2)$$

**Input:**

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{6 \times \frac{1}{12}}}{24 \pi \times \frac{1}{12} \times 5^2}$$

**Result:**

$$\frac{125 - \frac{15}{2^{2/3}} + 2^{2/3}}{50 \pi}$$

**Decimal approximation:**

0.745723625524187353223969522127963195037365848771555089405...

0.745723625524...

**Property:**

$$\frac{125 - \frac{15}{2^{2/3}} + 2^{2/3}}{50 \pi} \text{ is a transcendental number}$$

**Alternate forms:**

$$\frac{250 - 15 \sqrt[3]{2} + 2 \times 2^{2/3}}{2 (50 \pi)}$$

$$\frac{250 - 15 \sqrt[3]{2} + 2 \times 2^{2/3}}{100 \pi}$$

$$\frac{\frac{5}{2} - \frac{3}{10 \times 2^{2/3}} + \frac{1}{25 \sqrt[3]{2}}}{\pi}$$

**Alternative representations:**

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}} = \frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36 \left(\frac{1}{12}\right)^2}}{\frac{4320 \cdot 5^2}{12}}$$

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}} = - \frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36 \left(\frac{1}{12}\right)^2}}{\frac{24}{12} i \log(-1) 5^2}$$

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}} = \frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36 \left(\frac{1}{12}\right)^2}}{\frac{24}{12} \cos^{-1}(-1) 5^2}$$

### Series representations:

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}} = \frac{125 - \frac{15}{2^{2/3}} + 2^{2/3}}{200 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}$$

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}} = \frac{125 - \frac{15}{2^{2/3}} + 2^{2/3}}{50 \sum_{k=0}^{\infty} \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k}}$$

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}} = \frac{125 - \frac{15}{2^{2/3}} + 2^{2/3}}{50 \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right)}$$

### Integral representations:

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}} = \frac{125 - \frac{15}{2^{2/3}} + 2^{2/3}}{200 \int_0^1 \sqrt{1-t^2} dt}$$

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}} = \frac{125 - \frac{15}{2^{2/3}} + 2^{2/3}}{100 \int_0^{\infty} \frac{1}{1+t^2} dt}$$

$$\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}} = \frac{125 - \frac{15}{2^{2/3}} + 2^{2/3}}{100 \int_0^1 \frac{1}{\sqrt{1-t^2}} dt}$$

$$\left[ \frac{2}{\left( \left( \left( \left( \left( 5^3 - 3 \times 5 \sqrt[3]{36 \left( \frac{1}{12} \right)^2} + 2 \sqrt[3]{6 \times \frac{1}{12}} \right) \right)^{\frac{1}{3}} + 2 \left( 6 \times \frac{1}{12} \right)^{\frac{1}{3}} \right) \right) / (24 \pi \times \frac{1}{12} \times 5^2)} \right)^{\frac{1}{2}} - (18+2) \frac{1}{10^3} \right]$$

**Input:**

$$\sqrt{\frac{2}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left( \frac{1}{12} \right)^2} + 2 \sqrt[3]{6 \times \frac{1}{12}}}{24 \pi \times \frac{1}{12} \times 5^2}}} - (18+2) \times \frac{1}{10^3}$$

**Exact result:**

$$10 \sqrt{\frac{\pi}{125 - \frac{15}{2^{2/3}} + 2^{2/3}}} - \frac{1}{50}$$

**Decimal approximation:**

1.617668692554153584248850028139741407032414227080169541134...

1.61766869255.... result that is a very good approximation to the value of the golden ratio 1.618033988749...

**Property:**

$$-\frac{1}{50} + 10 \sqrt{\frac{\pi}{125 - \frac{15}{2^{2/3}} + 2^{2/3}}} \text{ is a transcendental number}$$

**Alternate forms:**

$$10 \sqrt{\frac{(62560 + 3758 \sqrt[3]{2} - 275 \times 2^{2/3}) \pi}{7831641}} - \frac{1}{50}$$

$$\frac{1}{50} \left( 500 \sqrt{\frac{2 \pi}{250 - 15 \sqrt[3]{2} + 2 \times 2^{2/3}}} - 1 \right)$$

$$10 \sqrt[3]{2} \sqrt{\frac{\pi}{-15 + 2 \sqrt[3]{2} + 125 \times 2^{2/3}}} - \frac{1}{50}$$

$[1/((((5^3-3*5(36*(1/12)^2)^{1/3})+2(6*1/12)^{1/3})) 1/(24\pi*1/12*5^2)))]^{16}+29+1/2+1/\text{golden ratio}$

**Input:**

$$\left( \frac{1}{\left( 5^3 - 3 \times 5 \sqrt[3]{36 \left( \frac{1}{12} \right)^2} + 2 \sqrt[3]{6 \times \frac{1}{12}} \right) \times \frac{1}{24 \pi \times \frac{1}{12} \times 5^2}} \right)^{16} + 29 + \frac{1}{2} + \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Exact result:**

$$\frac{1}{\phi} + \frac{59}{2} + \frac{1\,525\,878\,906\,250\,000\,000\,000\,000\,000\,\pi^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$

**Decimal approximation:**

139.4516124173459537324237893425205482033248962274164259272...

139.4516124173... result practically equal to the rest mass of Pion meson 139.57 MeV

**Property:**

$$\frac{59}{2} + \frac{1}{\phi} + \frac{1\,525\,878\,906\,250\,000\,000\,000\,000\,000\,\pi^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$
 is a transcendental number

**Alternate forms:**

$$\frac{1}{\phi} + \frac{59}{2} + \frac{1\,562\,500\,000\,000\,000\,000\,000\,000\,000\,000 \times 2^{2/3} \pi^{16}}{\left(-15 + 2 \sqrt[3]{2} + 125 \times 2^{2/3}\right)^{16}}$$

$$\frac{59}{2} + \frac{2}{1 + \sqrt{5}} + \frac{1\,525\,878\,906\,250\,000\,000\,000\,000\,000\,\pi^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$



$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36\left(\frac{1}{12}\right)^2 + 2\sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 29 + \frac{1}{2} + \frac{1}{\phi} =$$

$$\frac{59}{2} + \frac{1}{2 \cos\left(\frac{\pi}{5}\right)} + \left( \frac{1}{\frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36\left(\frac{1}{12}\right)^2}}{\frac{24\pi 5^2}{12}}} \right)^{16}$$

**Series representations:**

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36\left(\frac{1}{12}\right)^2 + 2\sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 29 + \frac{1}{2} + \frac{1}{\phi} =$$

$$\frac{59}{2} + \frac{2}{1 + \sqrt{5}} + \frac{655360000000000000000000000000000 \left( \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^{16}}{\left( 125 - \frac{15}{2^{2/3}} + 2^{2/3} \right)^{16}}$$

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36\left(\frac{1}{12}\right)^2 + 2\sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 29 + \frac{1}{2} + \frac{1}{\phi} = \frac{59}{2} + \frac{1}{\phi} +$$

$$\frac{15258789062500000000000000 \left( \sum_{k=0}^{\infty} - \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \cdot 239^{1+2k})}{1+2k} \right)^{16}}{\left( 125 - \frac{15}{2^{2/3}} + 2^{2/3} \right)^{16}}$$



$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2 + 2 \sqrt[3]{\frac{6}{12}}}}{\frac{24 \pi 5^2}{12}}} \right)^{16} + 29 + \frac{1}{2} + \frac{1}{\phi} = \frac{59}{2} + \frac{2}{1 + \sqrt{5}} +$$

$$\frac{1525\,878\,906\,250\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000 \left( \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left( \frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k} \right) \right)^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$

**Integral representations:**

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2 + 2 \sqrt[3]{\frac{6}{12}}}}{\frac{24 \pi 5^2}{12}}} \right)^{16} + 29 + \frac{1}{2} + \frac{1}{\phi} = \frac{59}{2} + \frac{2}{1 + \sqrt{5}} +$$

$$\frac{6553\,600\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000 \left( \int_0^1 \sqrt{1-t^2} dt \right)^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2 + 2 \sqrt[3]{\frac{6}{12}}}}{\frac{24 \pi 5^2}{12}}} \right)^{16} + 29 + \frac{1}{2} + \frac{1}{\phi} =$$

$$\frac{59}{2} + \frac{2}{1 + \sqrt{5}} + \frac{100\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000 \left( \int_0^{\infty} \frac{1}{1+t^2} dt \right)^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2 + 2 \sqrt[3]{\frac{6}{12}}}}{\frac{24 \pi 5^2}{12}}} \right)^{16} + 29 + \frac{1}{2} + \frac{1}{\phi} =$$

$$\frac{59}{2} + \frac{2}{1 + \sqrt{5}} + \frac{100\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000 \left( \int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$



$$\frac{1}{2} \left( 37 + \sqrt{5} \right) - \pi + \left( 1562500000000000000000000000000 \right. \\
\left. \left( 1015453839476400012162962303745111457126030887038381 \right. \right. \\
016369934977747040 + \\
873911939530203391184492011043439887712012158869637 \\
706784533386115392 \sqrt[3]{2} + \\
327339718588787625808656974337466387139559085836125 \\
\left. \left. \left. 315874637356048025 \times 2^{2/3} \right) \pi^{16} \right) / \right. \\
3391812169316749774548836922718062303562367845317732123443 \\
815354452188694057476533214301606529461776893209$$

**Alternative representations:**

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left( \frac{1}{12} \right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 - \pi + \phi = \\
18 - \pi - 2 \cos(216^\circ) + \left( \frac{1}{\frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36 \left( \frac{1}{12} \right)^2}}{\frac{24\pi 5^2}{12}}} \right)^{16}$$

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left( \frac{1}{12} \right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 - \pi + \phi = \\
18 - 180^\circ - 2 \cos(216^\circ) + \left( \frac{1}{\frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36 \left( \frac{1}{12} \right)^2}}{\frac{4320^\circ 5^2}{12}}} \right)^{16}$$

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 - \pi + \phi =$$

$$18 - \pi + 2 \cos\left(\frac{\pi}{5}\right) + \left( \frac{1}{\frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36 \left(\frac{1}{12}\right)^2}}{\frac{24\pi 5^2}{12}}} \right)^{16}$$

### Series representations:

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 - \pi + \phi =$$

$$\left( 16 \left( 147835494843627011415064707375716760000 - \right. \right.$$

$$216791138181594424936718014808418001755 \sqrt[3]{2} +$$

$$138917131707756891332632978078125684624 \times 2^{2/3} +$$

$$3995553914692621930136883983127480000 \sqrt{5} -$$

$$5859219950853903376668054454281567615 \sqrt[3]{2} \sqrt{5} +$$

$$3754517073182618684665756164273667152 \times 2^{2/3} \sqrt{5} -$$

$$31964431317540975441095071865019840000 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} +$$

$$46873759606831227013344435634252540920 \sqrt[3]{2} \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} -$$

$$3003613658546094977326049314189337216 \times 2^{2/3} \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} +$$

$$26843545600$$

$$\left. \left. \left( \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^{16} \right) \right) / \left( 250 - 15 \sqrt[3]{2} + 2 \times 2^{2/3} \right)^{16}$$

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36\left(\frac{1}{12}\right)^2 + 2\sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 - \pi + \phi =$$

$$\left( 16 \left( 147835494843627011415064707375716760000 - \right. \right.$$

$$216791138181594424936718014808418001755\sqrt[3]{2} +$$

$$138917131707756891332632978078125684624 \times 2^{2/3} +$$

$$3995553914692621930136883983127480000\sqrt{5} -$$

$$5859219950853903376668054454281567615\sqrt[3]{2}\sqrt{5} +$$

$$3754517073182618684665756164273667152 \times 2^{2/3}\sqrt{5} -$$

$$7991107829385243860273767966254960000$$

$$\left. \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right) + \right.$$

$$11718439901707806753336108908563135230$$

$$\left. \sqrt[3]{2} \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right) - \right.$$

$$7509034146365237369331512328547334304 \times$$

$$\left. 2^{2/3} \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right) + \right.$$

$$625000000000000000000000000000000$$

$$\left. \left. \left. \left. \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right)\right)^{16} \right) \right) \right) / \left( 250 - 15\sqrt[3]{2} + 2 \times 2^{2/3} \right)^{16}$$

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36\left(\frac{1}{12}\right)^2 + 2\sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 - \pi + \phi =$$

$$\left( 16 \left( 147\,835\,494\,843\,627\,011\,415\,064\,707\,375\,716\,760\,000 - \right. \right.$$

$$216\,791\,138\,181\,594\,424\,936\,718\,014\,808\,418\,001\,755 \sqrt[3]{2} +$$

$$138\,917\,131\,707\,756\,891\,332\,632\,978\,078\,125\,684\,624 \times 2^{2/3} +$$

$$3\,995\,553\,914\,692\,621\,930\,136\,883\,983\,127\,480\,000 \sqrt{5} -$$

$$5\,859\,219\,950\,853\,903\,376\,668\,054\,454\,281\,567\,615 \sqrt[3]{2} \sqrt{5} +$$

$$3\,754\,517\,073\,182\,618\,684\,665\,756\,164\,273\,667\,152 \times 2^{2/3} \sqrt{5} +$$

$$6\,250\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000$$

$$\left. \left( \sum_{k=0}^{\infty} \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k} \right)^{16} + \right.$$

$$7\,991\,107\,829\,385\,243\,860\,273\,767\,966\,254\,960\,000$$

$$\left. \sum_{k=0}^{\infty} \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k} - \right.$$

$$11\,718\,439\,901\,707\,806\,753\,336\,108\,908\,563\,135\,230$$

$$\left. \sqrt[3]{2} \sum_{k=0}^{\infty} \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k} + \right.$$

$$7\,509\,034\,146\,365\,237\,369\,331\,512\,328\,547\,334\,304 \times$$

$$\left. \left. 2^{2/3} \sum_{k=0}^{\infty} \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k} \right) \right) /$$

$$\left( 250 - 15 \sqrt[3]{2} + 2 \times 2^{2/3} \right)^{16}$$

**Integral representations:**

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36\left(\frac{1}{12}\right)^2 + 2\sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 - \pi + \phi = 18 - \frac{3\sqrt{3}}{4} + \phi - 24 \int_0^{\frac{1}{4}} \sqrt{t-t^2} dt +$$

$$\frac{1525\,878\,906\,250\,000\,000\,000\,000\,000\,000 \left( \frac{3\sqrt{3}}{4} + 24 \int_0^{\frac{1}{4}} \sqrt{t-t^2} dt \right)^{16}}{\left( 125 - \frac{15}{2^{2/3}} + 2^{2/3} \right)^{16}}$$

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36\left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 - \pi + \phi =$$

$$\begin{aligned} & \left( 16 \left( 147835494843627011415064707375716760000 - \right. \right. \\ & \quad 216791138181594424936718014808418001755 \sqrt[3]{2} + \\ & \quad 138917131707756891332632978078125684624 \times 2^{2/3} + \\ & \quad 3995553914692621930136883983127480000 \sqrt{5} - \\ & \quad 5859219950853903376668054454281567615 \sqrt[3]{2} \sqrt{5} + \\ & \quad 3754517073182618684665756164273667152 \times 2^{2/3} \sqrt{5} - \\ & \quad 15982215658770487720547535932509920000 \int_0^\infty \frac{1}{1+t^2} dt + \\ & \quad 23436879803415613506672217817126270460 \sqrt[3]{2} \int_0^\infty \frac{1}{1+t^2} dt - \\ & \quad 15018068292730474738663024657094668608 \times 2^{2/3} \int_0^\infty \frac{1}{1+t^2} dt + \\ & \quad \left. \left. 409600000000000000000000000000000000000 \left( \int_0^\infty \frac{1}{1+t^2} dt \right)^{16} \right) \right) / \\ & \left( 250 - 15 \sqrt[3]{2} + 2 \times 2^{2/3} \right)^{16} \end{aligned}$$

$$\left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36\left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 - \pi + \phi =$$

$$\begin{aligned} & \left( 16 \left( 147835494843627011415064707375716760000 - \right. \right. \\ & \quad 216791138181594424936718014808418001755 \sqrt[3]{2} + \\ & \quad 138917131707756891332632978078125684624 \times 2^{2/3} + \\ & \quad 3995553914692621930136883983127480000 \sqrt{5} - \\ & \quad 5859219950853903376668054454281567615 \sqrt[3]{2} \sqrt{5} + \\ & \quad 3754517073182618684665756164273667152 \times 2^{2/3} \sqrt{5} - \\ & \quad 15982215658770487720547535932509920000 \int_0^\infty \frac{\sin(t)}{t} dt + \\ & \quad 23436879803415613506672217817126270460 \sqrt[3]{2} \int_0^\infty \frac{\sin(t)}{t} dt - \\ & \quad 15018068292730474738663024657094668608 \times 2^{2/3} \int_0^\infty \frac{\sin(t)}{t} dt + \\ & \quad \left. \left. 409600000000000000000000000000000000000 \left( \int_0^\infty \frac{\sin(t)}{t} dt \right)^{16} \right) \right) / \\ & \left( 250 - 15 \sqrt[3]{2} + 2 \times 2^{2/3} \right)^{16} \end{aligned}$$

$27 \times \frac{1}{2} \left( \left( \left[ \frac{1}{\left( \left( \left( \left( 5^3 - 3 \times 5 \sqrt[3]{36 \left( \frac{1}{12} \right)^2} \right)^{1/3} + 2 \left( 6 \times \frac{1}{12} \right)^{1/3} \right) \right) \right] \right)^{16} + 18 + \frac{1}{\text{golden ratio}} \right) \right) + \text{golden ratio}$

**Input:**

$$27 \times \frac{1}{2} \left( \left( \frac{1}{\left( 5^3 - 3 \times 5 \sqrt[3]{36 \left( \frac{1}{12} \right)^2} + 2 \sqrt[3]{6 \times \frac{1}{12}} \right) \times \frac{1}{24 \pi \times \frac{1}{12} \times 5^2}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi$$

$\phi$  is the golden ratio

**Exact result:**

$$\phi + \frac{27}{2} \left( \frac{1}{\phi} + 18 + \frac{1\,525\,878\,906\,250\,000\,000\,000\,000\,000\,000\,\pi^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}} \right)$$

**Decimal approximation:**

1728.964801622920270235925742958393038862606408249927512880...

1728.964801622...  $\approx$  1729

This result is very near to the mass of candidate glueball **f<sub>0</sub>(1710) scalar meson**. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

**Property:**

$$\phi + \frac{27}{2} \left( 18 + \frac{1}{\phi} + \frac{1\,525\,878\,906\,250\,000\,000\,000\,000\,000\,000\,\pi^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}} \right)$$

is a transcendental number

**Alternate forms:**

$$\frac{27}{2\phi} + \phi + 243 + \frac{21\,093\,750\,000\,000\,000\,000\,000\,000\,000\,000\,000 \times 2^{2/3} \pi^{16}}{\left(-15 + 2\sqrt[3]{2} + 125 \times 2^{2/3}\right)^{16}}$$

$$\frac{487}{2} + \frac{\sqrt{5}}{2} + \frac{27}{1 + \sqrt{5}} + \frac{20\,599\,365\,234\,375\,000\,000\,000\,000\,000\,000 \pi^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$



$$\frac{1}{2} (1 + \sqrt{5}) + \frac{27}{2} \left( 18 + \frac{2}{1 + \sqrt{5}} + \frac{1525878906250000000000000000 \pi^{16}}{(125 - \frac{15}{2^{2/3}} + 2^{2/3})^{16}} \right)$$

**Alternative representations:**

$$\frac{27}{2} \left( \left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi =$$

$$-2 \cos(216^\circ) + \frac{27}{2} \left( 18 + -\frac{1}{2 \cos(216^\circ)} + \left( \frac{1}{\frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36 \left(\frac{1}{12}\right)^2}}{\frac{24 \pi 5^2}{12}}} \right)^{16} \right)$$

$$\frac{27}{2} \left( \left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi =$$

$$-2 \cos(216^\circ) + \frac{27}{2} \left( 18 + -\frac{1}{2 \cos(216^\circ)} + \left( \frac{1}{\frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36 \left(\frac{1}{12}\right)^2}}{\frac{4320 \pi 5^2}{12}}} \right)^{16} \right)$$

$$\frac{27}{2} \left( \left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi =$$

$$2 \cos\left(\frac{\pi}{5}\right) + \frac{27}{2} \left( 18 + \frac{1}{2 \cos\left(\frac{\pi}{5}\right)} + \left( \frac{1}{\frac{5^3 + 2 \sqrt[3]{\frac{6}{12}} - 15 \sqrt[3]{36 \left(\frac{1}{12}\right)^2}}{\frac{24 \pi 5^2}{12}}} \right)^{16} \right)$$

**Series representations:**

$$\frac{27}{2} \left( \left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi = \frac{487}{2} + \frac{\sqrt{5}}{2} + \frac{27}{1 + \sqrt{5}} +$$

$$\frac{88\,473\,600\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000 \left( \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$

$$\frac{27}{2} \left( \left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2} + 2 \sqrt[3]{\frac{6}{12}}}{\frac{24 \pi 5^2}{12}}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi =$$

$$\phi + \frac{27}{2} \left( 18 + \frac{1}{\phi} + \left( 1525\,878\,906\,250\,000\,000\,000\,000\,000 \right. \right.$$

$$\left. \left. \left( \sum_{k=0}^{\infty} -\frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k} \right)^{16} \right) \right) /$$

$$\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}$$

$$\frac{27}{2} \left( \left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2 + 2 \sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi = \frac{487}{2} + \frac{\sqrt{5}}{2} + \frac{27}{1 + \sqrt{5}} +$$

$$\frac{205993652343750000000000000000 \left( \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right) \right)^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$

**Integral representations:**

$$\frac{27}{2} \left( \left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2 + 2 \sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi = \frac{487}{2} + \frac{\sqrt{5}}{2} + \frac{27}{1 + \sqrt{5}} +$$

$$\frac{884736000000000000000000000000 \left( \int_0^1 \sqrt{1-t^2} dt \right)^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$

$$\frac{27}{2} \left( \left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2 + 2 \sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi = \frac{487}{2} + \frac{\sqrt{5}}{2} +$$

$$\frac{27}{1 + \sqrt{5}} + \frac{135000000000000000000000000000 \left( \int_0^{\infty} \frac{1}{1+t^2} dt \right)^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$

$$\frac{27}{2} \left( \left( \frac{1}{\frac{5^3 - 3 \times 5 \sqrt[3]{36 \left(\frac{1}{12}\right)^2 + 2 \sqrt[3]{\frac{6}{12}}}}{\frac{24\pi 5^2}{12}}} \right)^{16} + 18 + \frac{1}{\phi} \right) + \phi = \frac{487}{2} + \frac{\sqrt{5}}{2} + \frac{27}{1 + \sqrt{5}} +$$

$$\frac{135000000000000000000000000000 \left( \int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^{16}}{\left(125 - \frac{15}{2^{2/3}} + 2^{2/3}\right)^{16}}$$

We have that:

$$S = \pi r_h^2 \left[ 1 + \frac{r_h \sqrt[6]{6|\epsilon|} + 2}{3r_h \sqrt[6]{6|\epsilon|}} \right]$$

For:  $r_h = 5$  and  $\epsilon = 1/12$ , we obtain:

$$\text{Pi} * 25 \left[ 1 + \frac{5 * (6 * 1/12)^{1/6} + 2}{3 * 5 * (6 * 1/12)^{1/6}} \right]$$

**Input:**

$$\pi \times 25 \left( 1 + \frac{5 \sqrt[6]{6 \times \frac{1}{12}} + 2}{3 \times 5 \sqrt[6]{6 \times \frac{1}{12}}} \right)$$

**Result:**

$$25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \pi$$

**Decimal approximation:**

116.4741502026667004688617460853396989434312242918942010852...

116.4741502...

**Property:**

$25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \pi$  is a transcendental number

**Alternate forms:**

$$\frac{10}{3} \pi \left( 10 + \sqrt[6]{2} \right)$$

$$\frac{100 \pi}{3} + \frac{10 \sqrt[6]{2} \pi}{3}$$

$$\left( 25 + \sqrt[6]{2} \left( \frac{10}{3} + \frac{25}{3 \sqrt[6]{2}} \right) \right) \pi$$

**Alternative representations:**

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) = 4500^\circ \left( 1 + \frac{2 + 5 \sqrt[6]{\frac{6}{12}}}{15 \sqrt[6]{\frac{6}{12}}} \right)$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) = -25 i \log(-1) \left( 1 + \frac{2 + 5 \sqrt[6]{\frac{6}{12}}}{15 \sqrt[6]{\frac{6}{12}}} \right)$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) = 25 \cos^{-1}(-1) \left( 1 + \frac{2 + 5 \sqrt[6]{\frac{6}{12}}}{15 \sqrt[6]{\frac{6}{12}}} \right)$$

**Series representations:**

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) = \frac{40}{3} (10 + \sqrt[6]{2}) \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) = \frac{40}{3} (10 + \sqrt[6]{2}) \sum_{k=0}^{\infty} \frac{(-1)^{1+k} 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k}$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) = \frac{10}{3} (10 + \sqrt[6]{2}) \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left( \frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k} \right)$$

**Integral representations:**

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) = \frac{40}{3} (10 + \sqrt[6]{2}) \int_0^1 \sqrt{1-t^2} dt$$

$$\pi \times 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) = \frac{20}{3} (10 + \sqrt[6]{2}) \int_0^1 \frac{1}{\sqrt{1-t^2}} dt$$

$$\pi \times 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) = \frac{20}{3} (10 + \sqrt[6]{2}) \int_0^\infty \frac{1}{1+t^2} dt$$

$$\pi \times 25 \left[ 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right] + 21 + 2$$

**Input:**

$$\pi \times 25 \left( 1 + \frac{5 \sqrt[6]{6 \times \frac{1}{12} + 2}}{3 \times 5 \sqrt[6]{6 \times \frac{1}{12}}} \right) + 21 + 2$$

**Result:**

$$23 + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \pi$$

**Decimal approximation:**

139.4741502026667004688617460853396989434312242918942010852...

139.4741502... result practically equal to the rest mass of Pion meson 139.57 MeV

**Property:**

$$23 + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \pi \text{ is a transcendental number}$$

**Alternate forms:**

$$\frac{1}{3} (69 + 100\pi + 10 \sqrt[6]{2} \pi)$$

$$23 + \frac{10}{3} (10 + \sqrt[6]{2}) \pi$$

$$23 + \frac{100\pi}{3} + \frac{10 \sqrt[6]{2} \pi}{3}$$

**Alternative representations:**

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 21 + 2 = 23 + 4500^\circ \left( 1 + \frac{2 + 5 \sqrt[6]{\frac{6}{12}}}{15 \sqrt[6]{\frac{6}{12}}} \right)$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 21 + 2 = 23 - 25 i \log(-1) \left( 1 + \frac{2 + 5 \sqrt[6]{\frac{6}{12}}}{15 \sqrt[6]{\frac{6}{12}}} \right)$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 21 + 2 = 23 + 25 \cos^{-1}(-1) \left( 1 + \frac{2 + 5 \sqrt[6]{\frac{6}{12}}}{15 \sqrt[6]{\frac{6}{12}}} \right)$$

**Series representations:**

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 21 + 2 = 23 + \frac{40}{3} \left( 10 + \sqrt[6]{2} \right) \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 21 + 2 = 23 + \frac{10}{3} \left( 10 + \sqrt[6]{2} \right) \sum_{k=0}^{\infty} \left( -\frac{1}{4} \right)^k \left( \frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k} \right)$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 21 + 2 = 23 + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \sum_{k=0}^{\infty} -\frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1 + 2k}$$

**Integral representations:**

$$\pi \times 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 21 + 2 = 23 + \frac{40}{3} (10 + \sqrt[6]{2}) \int_0^1 \sqrt{1-t^2} dt$$

$$\pi \times 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 21 + 2 = 23 + \frac{20}{3} (10 + \sqrt[6]{2}) \int_0^1 \frac{1}{\sqrt{1-t^2}} dt$$

$$\pi \times 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 21 + 2 = 23 + \int_0^\infty \frac{20(10 + \sqrt[6]{2})}{3(1+t^2)} dt$$

$\pi \times 25 [1 + (((5 * (6 * 1/12)^(1/6)) + 2)) / (((3 * 5 * (6 * 1/12)^(1/6))))] + 8 + 1/\text{golden ratio}$

**Input:**

$$\pi \times 25 \left( 1 + \frac{5 \sqrt[6]{6 \times \frac{1}{12} + 2}}{3 \times 5 \sqrt[6]{6 \times \frac{1}{12}}} \right) + 8 + \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Result:**

$$\frac{1}{\phi} + 8 + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \pi$$

**Decimal approximation:**

125.0921841914165953170663329197053370611515334716999639474...

125.0921841914... result very near to the Higgs boson mass 125.18 GeV

**Property:**

$$8 + \frac{1}{\phi} + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \pi \text{ is a transcendental number}$$



**Alternate forms:**

$$\frac{1}{6} (45 + 3\sqrt{5} + 200\pi + 20\sqrt[6]{2}\pi)$$

$$\frac{1}{\phi} + 8 + 25\pi + \frac{5}{3} (5 + 2\sqrt[6]{2})\pi$$

$$\frac{1}{2} (15 + \sqrt{5}) + \frac{10}{3} (10 + \sqrt[6]{2})\pi$$

**Alternative representations:**

$$\pi 25 \left( 1 + \frac{5\sqrt[6]{\frac{6}{12}} + 2}{3 \times 5\sqrt[6]{\frac{6}{12}}} \right) + 8 + \frac{1}{\phi} = 8 + \frac{1}{2 \cos(216^\circ)} + 25\pi \left( 1 + \frac{2 + 5\sqrt[6]{\frac{6}{12}}}{15\sqrt[6]{\frac{6}{12}}} \right)$$

$$\pi 25 \left( 1 + \frac{5\sqrt[6]{\frac{6}{12}} + 2}{3 \times 5\sqrt[6]{\frac{6}{12}}} \right) + 8 + \frac{1}{\phi} = 8 + \frac{1}{2 \cos(216^\circ)} + 4500^\circ \left( 1 + \frac{2 + 5\sqrt[6]{\frac{6}{12}}}{15\sqrt[6]{\frac{6}{12}}} \right)$$

$$\pi 25 \left( 1 + \frac{5\sqrt[6]{\frac{6}{12}} + 2}{3 \times 5\sqrt[6]{\frac{6}{12}}} \right) + 8 + \frac{1}{\phi} = 8 + \frac{1}{2 \cos\left(\frac{\pi}{5}\right)} + 25\pi \left( 1 + \frac{2 + 5\sqrt[6]{\frac{6}{12}}}{15\sqrt[6]{\frac{6}{12}}} \right)$$

**Series representations:**

$$\pi 25 \left( 1 + \frac{5\sqrt[6]{\frac{6}{12}} + 2}{3 \times 5\sqrt[6]{\frac{6}{12}}} \right) + 8 + \frac{1}{\phi} = 8 + \frac{2}{1 + \sqrt{5}} + \sum_{k=0}^{\infty} \frac{40(-1)^k (10 + \sqrt[6]{2})}{3 + 6k}$$

$$\pi 25 \left( 1 + \frac{5\sqrt[6]{\frac{6}{12}} + 2}{3 \times 5\sqrt[6]{\frac{6}{12}}} \right) + 8 + \frac{1}{\phi} = 8 + \frac{1}{\phi} + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \sum_{k=0}^{\infty} - \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1 + 2k}$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 8 + \frac{1}{\phi} =$$

$$8 + \frac{1}{\phi} + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \sum_{k=0}^{\infty} \left( -\frac{1}{4} \right)^k \left( \frac{2}{1+4k} + \frac{2}{2+4k} + \frac{1}{3+4k} \right)$$

**Integral representations:**

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 8 + \frac{1}{\phi} = 8 + \frac{1}{\phi} + \frac{40}{3} \left( 10 + \sqrt[6]{2} \right) \int_0^1 \sqrt{1-t^2} dt$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 8 + \frac{1}{\phi} = 8 + \frac{1}{\phi} + \frac{20}{3} \left( 10 + \sqrt[6]{2} \right) \int_0^1 \frac{1}{\sqrt{1-t^2}} dt$$

$$\pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 8 + \frac{1}{\phi} = 8 + \frac{1}{\phi} + \frac{20}{3} \left( 10 + \sqrt[6]{2} \right) \int_0^{\infty} \frac{\sin(t)}{t} dt$$

27\*1/2(((Pi\*25[1+(((5\*(6\*1/12)^(1/6))+2))/((3\*5\*(6\*1/12)^(1/6)))]+11+1/golden ratio))))

**Input:**

$$27 \times \frac{1}{2} \left( \pi \times 25 \left( 1 + \frac{5 \sqrt[6]{6 \times \frac{1}{12} + 2}}{3 \times 5 \sqrt[6]{6 \times \frac{1}{12}}} \right) + 11 + \frac{1}{\phi} \right)$$

φ is the golden ratio

**Result:**

$$\frac{27}{2} \left( \frac{1}{\phi} + 11 + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \right) \pi$$

**Decimal approximation:**

1729.244486584124036780395494416022050325545701867949513290...

1729.2444865841...

This result is very near to the mass of candidate glueball **f<sub>0</sub>(1710) scalar meson**. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

**Property:**

$\frac{27}{2} \left( 11 + \frac{1}{\phi} + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \pi \right)$  is a transcendental number

**Alternate forms:**

$$\frac{9}{4} \left( 63 + 3\sqrt{5} + 200\pi + 20\sqrt[6]{2}\pi \right)$$

$$\frac{27}{4} \left( 21 + \sqrt{5} \right) + 45 \left( 10 + \sqrt[6]{2} \right) \pi$$

$$\frac{9 \left( (33 + 10(10 + \sqrt[6]{2})\pi)\phi + 3 \right)}{2\phi}$$

**Alternative representations:**

$$\frac{27}{2} \left( \pi 25 \left( 1 + \frac{5\sqrt[6]{\frac{6}{12}} + 2}{3 \times 5\sqrt[6]{\frac{6}{12}}} \right) + 11 + \frac{1}{\phi} \right) = \frac{27}{2} \left( 11 + -\frac{1}{2 \cos(216^\circ)} + 25\pi \left( 1 + \frac{2 + 5\sqrt[6]{\frac{6}{12}}}{15\sqrt[6]{\frac{6}{12}}} \right) \right)$$

$$\frac{27}{2} \left( \pi 25 \left( 1 + \frac{5\sqrt[6]{\frac{6}{12}} + 2}{3 \times 5\sqrt[6]{\frac{6}{12}}} \right) + 11 + \frac{1}{\phi} \right) = \frac{27}{2} \left( 11 + -\frac{1}{2 \cos(216^\circ)} + 4500^\circ \left( 1 + \frac{2 + 5\sqrt[6]{\frac{6}{12}}}{15\sqrt[6]{\frac{6}{12}}} \right) \right)$$

$$\frac{27}{2} \left( \pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12}} + 2}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 11 + \frac{1}{\phi} \right) = \frac{27}{2} \left( 11 + \frac{1}{2 \cos\left(\frac{\pi}{5}\right)} + 25 \pi \left( 1 + \frac{2 + 5 \sqrt[6]{\frac{6}{12}}}{15 \sqrt[6]{\frac{6}{12}}} \right) \right)$$

### Series representations:

$$\frac{27}{2} \left( \pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12}} + 2}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 11 + \frac{1}{\phi} \right) = \frac{27}{2} \left( 11 + \frac{1}{\phi} + \frac{40}{3} (10 + \sqrt[6]{2}) \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)$$

$$\frac{27}{2} \left( \pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12}} + 2}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 11 + \frac{1}{\phi} \right) = \frac{27}{2} \left( 11 + \frac{1}{\phi} + 25 \left( 1 + \frac{1}{15} \sqrt[6]{2} \left( 2 + \frac{5}{\sqrt[6]{2}} \right) \right) \sum_{k=0}^{\infty} - \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k} \right)$$

$$\frac{27}{2} \left( \pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12}} + 2}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 11 + \frac{1}{\phi} \right) = \frac{297}{2} + \frac{27}{1 + \sqrt{5}} + \sum_{k=0}^{\infty} \frac{45 (-1)^k 2^{1-2k} (10 + \sqrt[6]{2}) (5 + 21k + 20k^2)}{(1+2k)(1+4k)(3+4k)}$$

### Integral representations:

$$\frac{27}{2} \left( \pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12}} + 2}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 11 + \frac{1}{\phi} \right) = \frac{27}{2} \left( 11 + \frac{1}{\phi} + \frac{40}{3} (10 + \sqrt[6]{2}) \int_0^1 \sqrt{1-t^2} dt \right)$$

$$\frac{27}{2} \left( \pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12}} + 2}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 11 + \frac{1}{\phi} \right) = \frac{27}{2} \left( 11 + \frac{1}{\phi} + \frac{20}{3} (10 + \sqrt[6]{2}) \int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)$$

$$\frac{27}{2} \left( \pi 25 \left( 1 + \frac{5 \sqrt[6]{\frac{6}{12} + 2}}{3 \times 5 \sqrt[6]{\frac{6}{12}}} \right) + 11 + \frac{1}{\phi} \right) = \frac{27}{2} \left( 11 + \frac{1}{\phi} + 10 (10 + \sqrt[6]{2}) \int_0^\infty \frac{\sin^4(t)}{t^4} dt \right)$$

From the entropy 116.47415 , we obtain:

Mass = 6.62621E-8

Radius = 9.84102E-35

Temperature = 1.85167E30

from the Ramanujan-Nardelli mock formula, we obtain:

sqrt[[[1/((((((4\*1.962364415e+19)/(5\*0.0864055^2)))\*1/(6.62621e-8)\* sqrt[[-(((1.85167e+30 \* 4\*Pi\*(9.84102e-35)^3-(9.84102e-35)^2)))/ ((6.67\*10^-11))]]]]]]]

**Input interpretation:**

$$\sqrt{\left( 1 / \left( \frac{4 \times 1.962364415 \times 10^{19}}{5 \times 0.0864055^2} \times \frac{1}{6.62621 \times 10^{-8}} \right) \sqrt{-\frac{1.85167 \times 10^{30} \times 4 \pi (9.84102 \times 10^{-35})^3 - (9.84102 \times 10^{-35})^2}{6.67 \times 10^{-11}}} \right)}$$

**Result:**

1.618078060772200542454453924514248164763287943959318428397...

1.6180780607722.... result that is a very good approximation to the value of the golden ratio 1.618033988749...

**Possible closed forms:**

$$\phi \approx 1.618033988$$

$$\frac{25 e}{42} \approx 1.618024897$$

$$-e! + 5 - \frac{5}{e} + e \approx 1.618064146$$

$$\Phi + 1 \approx 1.618033988$$

$$\sqrt{\frac{3\mathcal{K}_1}{2}} \approx 1.618057011$$

$$\frac{1}{\Phi} \approx 1.618033988$$

**With regard the golden ratio, we have the following Ramanujan calculation:**

$$1/(((1/32(-1+\sqrt{5}))^5+5*(e^{(-\sqrt{5}*\pi))^5}))$$

**Input:**

$$\frac{1}{\frac{1}{32} (-1 + \sqrt{5})^5 + 5 e^{(-\sqrt{5} \pi)^5}}$$

**Exact result:**

$$\frac{1}{\frac{1}{32} (\sqrt{5} - 1)^5 + 5 e^{-25 \sqrt{5} \pi^5}}$$

**Decimal approximation:**

11.09016994374947424102293417182819058860154589902881431067...

$$(11*5*(e^{(-\sqrt{5}*\pi))^5})) / (((2*(((1/32(-1+\sqrt{5}))^5+5*(e^{(-\sqrt{5}*\pi))^5))))$$

**Input:**

$$\frac{11 \times 5 e^{(-\sqrt{5} \pi)^5}}{2 \left( \frac{1}{32} (-1 + \sqrt{5})^5 + 5 e^{(-\sqrt{5} \pi)^5} \right)}$$

**Exact result:**

$$\frac{55 e^{-25 \sqrt{5} \pi^5}}{2 \left( \frac{1}{32} (\sqrt{5} - 1)^5 + 5 e^{-25 \sqrt{5} \pi^5} \right)}$$

**Decimal approximation:**

$$9.99290225070718723070536304129457122742436976265255... \times 10^{-7428}$$

$$(5\sqrt{5}) * 5 * (e^{(-\sqrt{5} * \pi)^5}) / (((2 * (((1/32 * (-1 + \sqrt{5}))^5 + 5 * (e^{(-\sqrt{5} * \pi)^5}))))))$$

**Input:**

$$\frac{5 \sqrt{5} \times 5 e^{(-\sqrt{5} \pi)^5}}{2 \left( \frac{1}{32} (-1 + \sqrt{5})^5 + 5 e^{(-\sqrt{5} \pi)^5} \right)}$$

**Exact result:**

$$\frac{25 \sqrt{5} e^{-25 \sqrt{5} \pi^5}}{2 \left( \frac{1}{32} (\sqrt{5} - 1)^5 + 5 e^{-25 \sqrt{5} \pi^5} \right)}$$

**Decimal approximation:**

$$1.01567312386781438874777576295646917898823529098784... \times 10^{-7427}$$

**Input interpretation:**

$$\left( \frac{1}{\left( \frac{1}{32} (-1 + \sqrt{5})^5 + 5 e^{(-\sqrt{5} \pi)^5} \right)} \right) \frac{9.99290225070718723070536304129457122742436976265255}{10^{7428}} \frac{1.01567312386781438874777576295646917898823529098784}{10^{7427}} \Big)^{(1/5)}$$

$$\left( \left( \left( \frac{1}{\left( \left( \frac{1}{32}(-1 + \sqrt{5})^5 + 5 * (e^{(-\sqrt{5} * \pi)})^5 \right) \right) - (9.99290225070718723070536304129457122742436976265255 \times 10^{-7428}) - (1.01567312386781438874777576295646917898823529098784 \times 10^{-7427}) \right) \right) \right)^{1/5}$$

**Result:**

1.618033988749894848204586834365638117720309179805762862135...  
[1.61803398874989...](#)

Or:

$$\left( \left( \left( \frac{1}{\left( \left( \frac{1}{32}(-1 + \sqrt{5})^5 + 5 * (e^{(-\sqrt{5} * \pi)})^5 \right) \right) - (-1.6382898797095665677239458827012056245798314722584 \times 10^{-7429}) \right) \right) \right)^{1/5}$$

**Input interpretation:**

$$\sqrt[5]{\frac{1}{\left( \frac{1}{32} (-1 + \sqrt{5})^5 + 5 e^{(-\sqrt{5} \pi)^5} \right) - \frac{1.6382898797095665677239458827012056245798314722584}{10^{7429}}}}$$

**Result:**

1.618033988749894848204586834365638117720309179805762862135...

The result, thence, is:

[1.6180339887498948482045868343656381177203091798057628](#)

This is a wonderful golden ratio, fundamental constant of various fields of mathematics and physics

**Possible closed forms:**

$\phi \approx 1.618033988749894848204586834365638117720309179805762862135$   
 $\Phi + 1 \approx 1.618033988749894848204586834365638117720309179805762862135$   
 $\frac{1}{\Phi} \approx 1.618033988749894848204586834365638117720309179805762862135$



We have the following Ramanujan taxicab number

$$9^3 + 10^3 = 12^3 + 1$$

$$729 + 1000 = 1728 + 1$$

1729

## Observations

Figs.

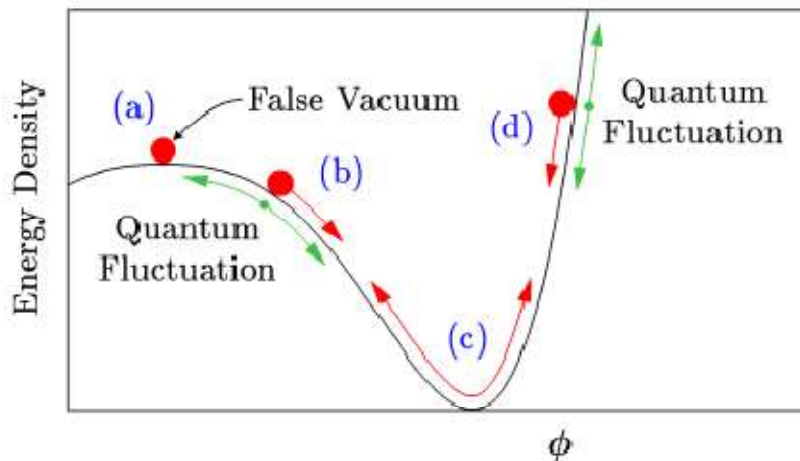
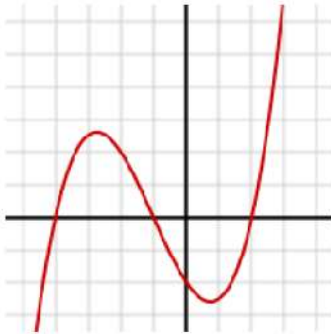


FIG. 1: In simple inflationary models, the universe at early times is dominated by the potential energy density of a scalar field,  $\phi$ . Red arrows show the classical motion of  $\phi$ . When  $\phi$  is near region (a), the energy density will remain nearly constant,  $\rho \cong \rho_f$ , even as the universe expands. Moreover, cosmic expansion acts like a frictional drag, slowing the motion of  $\phi$ : Even near regions (b) and (d),  $\phi$  behaves more like a marble moving in a bowl of molasses, slowly creeping down the side of its potential, rather than like a marble sliding down the inside of a polished bowl. During this period of “slow roll,”  $\rho$  remains nearly constant. Only after  $\phi$  has slid most of the way down its potential will it begin to oscillate around its minimum, as in region (c), ending inflation.



Graph of a cubic function with 3 real roots (where the curve crosses the horizontal axis at  $y = 0$ ). The case shown has two critical points. Here the function is:  
 $f(x) = (x^3 + 3x^2 - 6x - 8)/4$ .

The ratio between  $M_0$  and  $q$

$$M_0 = \sqrt{3q^2 - \Sigma^2},$$

$$q = \frac{(3\sqrt{3}) M_s}{2}.$$

i.e. the gravitating mass  $M_0$  and the Wheelerian mass  $q$  of the wormhole, is equal to:

$$\frac{\sqrt{3(2.17049 \times 10^{37})^2 - 0.001^2}}{\frac{1}{2}((3\sqrt{3})(4.2 \times 10^6 \times 1.9891 \times 10^{30}))}$$

1.732050787905194420703947625671018160083566548802082460520...

1.7320507879

$1.7320507879 \approx \sqrt{3}$  that is the ratio between the gravitating mass  $M_0$  and the Wheelerian mass  $q$  of the wormhole

We note that:

$$\left(-\frac{1}{2} + \frac{i}{2} \sqrt{3}\right) - \left(-\frac{1}{2} - \frac{i}{2} \sqrt{3}\right)$$

$$i\sqrt{3}$$

$i$  is the imaginary unit

$$1.732050807568877293527446341505872366942805253810380628055... i$$

$$r \approx 1.73205 \text{ (radius), } \theta = 90^\circ \text{ (angle)}$$

$$1.73205$$

This result is very near to the ratio between  $M_0$  and  $q$ , that is equal to  $1.7320507879 \approx \sqrt{3}$

With regard  $\sqrt{3}$ , we note that is a fundamental value of the formula structure that we need to calculate a Cubic Equation

We have that the previous result

$$\left(-\frac{1}{2} + \frac{i}{2} \sqrt{3}\right) - \left(-\frac{1}{2} - \frac{i}{2} \sqrt{3}\right) = i\sqrt{3} =$$

$$= 1.732050807568877293527446341505872366942805253810380628055... i$$

$$r \approx 1.73205 \text{ (radius), } \theta = 90^\circ \text{ (angle)}$$

can be related with:

$$u^2(-u)\left(\frac{1}{2} \pm \frac{i\sqrt{3}}{2}\right) + v^2(-v)\left(\frac{1}{2} \pm \frac{i\sqrt{3}}{2}\right) = q$$

Considering:

$$(-1)\left(\frac{1}{2}-\frac{i\sqrt{3}}{2}\right)-(-1)\left(\frac{1}{2}+\frac{i\sqrt{3}}{2}\right)=q$$

$$= i\sqrt{3} = 1.732050807568877293527446341505872366942805253810380628055... i$$

$r \approx 1.73205$  (radius),  $\theta = 90^\circ$  (angle)

Thence:

$$\left(-\frac{1}{2}+\frac{i}{2}\sqrt{3}\right)-\left(-\frac{1}{2}-\frac{i}{2}\sqrt{3}\right) \Rightarrow$$

$$\Rightarrow (-1)\left(\frac{1}{2}-\frac{i\sqrt{3}}{2}\right)-(-1)\left(\frac{1}{2}+\frac{i\sqrt{3}}{2}\right)=q=1.73205 \approx \sqrt{3}$$

**We observe how the graph above, concerning the cubic function, is very similar to the graph that represent the scalar field (in red). It is possible to hypothesize that cubic functions and cubic equations, with their roots, are connected to the scalar field.**

*From:*

[https://www.scientificamerican.com/article/mathematics-ramanujan/?fbclid=IwAR2caRXrn\\_RpOSvJIQxWsVLBcJ6KVgd\\_Af\\_hrmDYBNyU8mpSjRs1BDeremA](https://www.scientificamerican.com/article/mathematics-ramanujan/?fbclid=IwAR2caRXrn_RpOSvJIQxWsVLBcJ6KVgd_Af_hrmDYBNyU8mpSjRs1BDeremA)

*Ramanujan's statement concerned the deceptively simple concept of partitions—the different ways in which a whole number can be subdivided into smaller numbers. Ramanujan's original statement, in fact, stemmed from the observation of patterns, such as the fact that  $p(9) = 30$ ,  $p(9 + 5) = 135$ ,  $p(9 + 10) = 490$ ,  $p(9 + 15) = 1,575$  and so on are all divisible by 5. Note that here the  $n$ 's come at intervals of five units.*

*Ramanujan posited that this pattern should go on forever, and that similar patterns exist when 5 is replaced by 7 or 11—there are infinite sequences of  $p(n)$  that are all divisible by 7 or 11, or, as mathematicians say, in which the "moduli" are 7 or 11.*

*Then, in nearly oracular tone Ramanujan went on: "There appear to be corresponding properties," he wrote in his 1919 paper, "in which the moduli are*

*powers of 5, 7 or 11...and no simple properties for any moduli involving primes other than these three." (Primes are whole numbers that are only divisible by themselves or by 1.) Thus, for instance, there should be formulas for an infinity of n's separated by  $5^3 = 125$  units, saying that the corresponding p(n)'s should all be divisible by 125. In the past methods developed to understand partitions have later been applied to physics problems such as the theory of the strong nuclear force or the entropy of black holes.*

*From Wikipedia*

*In particle physics, Yukawa's interaction or Yukawa coupling, named after Hideki Yukawa, is an interaction between a scalar field  $\phi$  and a Dirac field  $\psi$ . The Yukawa interaction can be used to describe the nuclear force between nucleons (which are fermions), mediated by pions (which are pseudoscalar mesons). The Yukawa interaction is also used in the Standard Model to describe the coupling between the Higgs field and massless quark and lepton fields (i.e., the fundamental fermion particles). Through spontaneous symmetry breaking, these fermions acquire a mass proportional to the vacuum expectation value of the Higgs field.*

*Can be this the motivation that from the development of the Ramanujan's equations we obtain results very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV and practically equal to the rest mass of Pion meson 139.57 MeV*

*Note that:*

$$g_{22} = \sqrt{(1 + \sqrt{2})}.$$

Hence

$$\begin{aligned} 64g_{22}^{24} &= e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} - \dots, \\ 64g_{22}^{-24} &= 4096e^{-\pi\sqrt{22}} + \dots, \end{aligned}$$

so that

$$64(g_{22}^{24} + g_{22}^{-24}) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots = 64\{(1 + \sqrt{2})^{12} + (1 - \sqrt{2})^{12}\}.$$

Hence

$$e^{\pi\sqrt{22}} = 2508951.9982 \dots$$

Thence:

$$64g_{22}^{-24} = 4096e^{-\pi\sqrt{22}} + \dots$$

And

$$64(g_{22}^{24} + g_{22}^{-24}) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots = 64\{(1 + \sqrt{2})^{12} + (1 - \sqrt{2})^{12}\}$$

That are connected with 64, 128, 256, 512, 1024 and  $4096 = 64^2$

(Modular equations and approximations to  $\pi$  - S. Ramanujan - Quarterly Journal of Mathematics, XLV, 1914, 350 – 372)

All the results of the most important connections are signed in blue throughout the drafting of the paper. We highlight as in the development of the various equations we use always the constants  $\pi$ ,  $\phi$ ,  $1/\phi$ , the Fibonacci and Lucas numbers, linked to the golden ratio, that play a fundamental role in the development, and therefore, in the final results of the analyzed expressions.

In mathematics, the Fibonacci numbers, commonly denoted  $F_n$ , form a sequence, called the Fibonacci sequence, such that each number is the sum of the two preceding ones, starting from 0 and 1. Fibonacci numbers are strongly related to the golden ratio: Binet's formula expresses the  $n$ th Fibonacci number in terms of  $n$  and the golden ratio, and implies that the ratio of two consecutive Fibonacci numbers tends to the golden ratio as  $n$  increases.

Fibonacci numbers are also closely related to Lucas numbers, in that the Fibonacci and Lucas numbers form a complementary pair of Lucas sequences

The beginning of the sequence is thus:

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, 233, 377, 610, 987, 1597, 2584, 4181, 6765, 10946, 17711, 28657, 46368, 75025, 121393, 196418, 317811, 514229, 832040, 1346269, 2178309, 3524578, 5702887, 9227465, 14930352, 24157817, 39088169, 63245986, 102334155...

The Lucas numbers or Lucas series are an integer sequence named after the mathematician François Édouard Anatole Lucas (1842–91), who studied both that sequence and the closely related Fibonacci numbers. Lucas numbers and Fibonacci numbers form complementary instances of Lucas sequences.

The Lucas sequence has the same recursive relationship as the Fibonacci sequence, where each term is the sum of the two previous terms, but with different starting values. This produces a sequence where the ratios of successive terms approach the golden ratio, and in fact the terms

themselves are roundings of integer powers of the golden ratio.<sup>[1]</sup> The sequence also has a variety of relationships with the Fibonacci numbers, like the fact that adding any two Fibonacci numbers two terms apart in the Fibonacci sequence results in the Lucas number in between.

The sequence of Lucas numbers is:

2, 1, 3, 4, 7, 11, 18, 29, 47, 76, 123, 199, 322, 521, 843, 1364, 2207, 3571, 5778, 9349, 15127, 24476, 39603, 64079, 103682, 167761, 271443, 439204, 710647, 1149851, 1860498, 3010349, 4870847, 7881196, 12752043, 20633239, 33385282, 54018521, 87403803.....

All Fibonacci-like integer sequences appear in shifted form as a row of the Wythoff array; the Fibonacci sequence itself is the first row and the Lucas sequence is the second row. Also like all Fibonacci-like integer sequences, the ratio between two consecutive Lucas numbers converges to the golden ratio.

A Lucas prime is a Lucas number that is prime. The first few Lucas primes are:

2, 3, 7, 11, 29, 47, 199, 521, 2207, 3571, 9349, 3010349, 54018521, 370248451, 6643838879, ...  
(sequence A005479 in the OEIS).

In geometry, a golden spiral is a logarithmic spiral whose growth factor is  $\phi$ , the golden ratio.<sup>[1]</sup> That is, a golden spiral gets wider (or further from its origin) by a factor of  $\phi$  for every quarter turn it makes. Approximate logarithmic spirals can occur in nature, for example the arms of spiral galaxies<sup>[3]</sup> - golden spirals are one special case of these logarithmic spirals

**We note how the following three values: 137.508 (golden angle), 139.57 (mass of the Pion - meson Pi) and 125.18 (mass of the Higgs boson), are connected to each other. In fact, just add 2 to 137.508 to obtain a result very close to the mass of the Pion and subtract 12 to 137.508 to obtain a result that is also very close to the mass of the Higgs boson. We can therefore hypothesize that it is the golden angle (and the related golden ratio inherent in it) to be a fundamental ingredient both in the structures of the microcosm and in those of the macrocosm.**

## References

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