

On the Ramanujan's mathematics (Rogers-Ramanujan continued fractions, taxicab numbers and Manuscript Book 1 formulae) applied to various sectors of String Theory and to the Black Hole Physics: Further new possible mathematical connections XII.

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Abstract

In this research thesis, we have analyzed and deepened further Ramanujan expressions (Rogers-Ramanujan continued fractions, taxicab numbers and Manuscript Book 1 formulae) applied to some sectors of String Theory and to the Black Hole Physics. We have therefore described other new possible mathematical connections.

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<https://www.britannica.com/biography/Srinivasa-Ramanujan>

Jf

(i) $\frac{1+53x+9x^2}{1-82x-82x^2+x^3} = a_0 + a_1x + a_2x^2 + a_3x^3 + \dots$
 or $\frac{\alpha_0}{x} + \frac{\alpha_1}{x^2} + \frac{\alpha_2}{x^3} + \dots$

(ii) $\frac{2-26x-12x^2}{1-82x-82x^2+x^3} = b_0 + b_1x + b_2x^2 + b_3x^3 + \dots$
 or $\frac{\beta_0}{x} + \frac{\beta_1}{x^2} + \frac{\beta_2}{x^3} + \dots$

(iii) $\frac{2+8x-10x^2}{1-82x-82x^2+x^3} = c_0 + c_1x + c_2x^2 + c_3x^3 + \dots$
 or $\frac{\gamma_0}{x} + \frac{\gamma_1}{x^2} + \frac{\gamma_2}{x^3} + \dots$

then

$$\left. \begin{aligned} a_n^3 + b_n^3 &= c_n^3 + (-1)^n \\ \text{and } d_n^3 + \beta_n^3 &= \gamma_n^3 + (-1)^n \end{aligned} \right\}$$

Examples

$$135^3 + 138^3 = 172^3 - 1$$

$$11161^3 + 11468^3 = 14258^3 + 1$$

$$791^3 + 812^3 = 1010^3 - 1$$

$$9^3 + 10^3 = 12^3 + 1$$

$$6^3 + 8^3 = 9^3 - 1$$

<https://plus.maths.org/content/ramanujan>

Ramanujan's manuscript

The representations of 1729 as the sum of two cubes appear in the bottom right corner. The equation expressing the near counter examples to Fermat's last theorem appears further up: $\alpha^3 + \beta^3 = \gamma^3 + (-1)^n$.

From Wikipedia

*The **taxicab number**, typically denoted $Ta(n)$ or $Taxicab(n)$, also called the n th **Hardy–Ramanujan number**, is defined as the smallest integer that can be expressed as a sum of two positive integer cubes in n distinct ways. The most famous taxicab number is $1729 = Ta(2) = 1^3 + 12^3 = 9^3 + 10^3$.*

Dark Spinors Hawking Radiation in String Theory Black Holes

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From:

(1). In Boyer-Lindquist coordinates it reads:

$$ds^2 = -\frac{\Delta - a^2 \sin^2 \theta}{\Sigma} dt^2 + \frac{\Sigma}{\Delta} dr^2 + \Sigma d\theta^2 + \frac{\sin^2 \theta}{\Sigma} \left[(r^2 - 2\beta r - a^2)^2 - \Delta a^2 \sin^2 \theta \right] d\varphi^2 + \frac{2a \sin^2 \theta}{\Sigma} \left[(r^2 - 2\beta r - a^2)^2 - \Delta \right] dt d\varphi \quad (2)$$

where

$$\Sigma = r^2 - 2\beta r + a^2 \cos^2 \theta, \quad \Delta = r^2 - 2\eta r + a^2 = (r - r_+)(r - r_-) \quad \beta = \eta \sin h^2 \frac{\alpha}{2} \quad (3)$$

and r_+ [r_-] are the coordinate outer [inner] singularities.

The metric (2) describes a black hole solution with charge Q , mass M , magnetic dipole moment μ , and angular momentum J , given by

$$Q = \frac{\eta}{\sqrt{2}} \sinh \alpha, \quad M = \frac{\eta}{2} (1 + \cosh \alpha), \quad \mu = \frac{1}{\sqrt{2}} \eta a \sinh \alpha, \quad J = \frac{\eta a}{2} (1 + \cosh \alpha). \quad (4)$$

The associated g -factor can be expressed as $g = \frac{2\mu M}{QJ} = 2$ [28]. The parameters can be expressed in terms of genuinely physical quantities as

$$\eta = M - \frac{Q^2}{2M}, \quad \alpha = \operatorname{arcsinh} \left(\frac{2\sqrt{2}QM}{2M^2 - Q^2} \right), \quad a = \frac{J}{M}$$

The coordinate singularities thus read $r_{\pm} = M - \frac{Q^2}{2M} \pm \sqrt{-\frac{J^2}{M^2} + \left(M - \frac{Q^2}{2M}\right)^2}$ which vanishes unless $|J| < M^2 - \frac{Q^2}{2}$. The area of the outer event horizon is given by

$$A = 8\pi M \left(M - \frac{Q^2}{2M} + \sqrt{-\frac{J^2}{M^2} + \left(M - \frac{Q^2}{2M}\right)^2} \right).$$

Thus in the extremal limit, since $|J| \rightarrow M - \frac{Q^2}{2M}$, it reads $A \rightarrow 8\pi|J|$. In this limit the horizon is hence finite and the surface gravity κ , or equivalently, the Hawking temperature $T_H = \kappa/2\pi$ is provided by [14]

$$\kappa = \frac{\sqrt{-4J^2 + (2M^2 - Q^2)^2}}{2M(2M^2 - Q^2 + \sqrt{-4J^2 + (2M^2 - Q^2)^2})}$$

$$A = 8\pi M \left(M - \frac{Q^2}{2M} + \sqrt{-\frac{J^2}{M^2} + \left(M - \frac{Q^2}{2M}\right)^2} \right).$$

$$M = 1.312806e+40, Q = \sqrt{5}$$

$$Q = \sqrt{3} \text{ or } Q > \sqrt{3}$$

Series expansion at $x = -1.50418 \times 10^{60}$:

$$\left\{ \begin{array}{ll} (4.33153 \times 10^{81} - 5.13045 \times 10^{53} i) + & 1.74554 \times 10^{-20} \operatorname{Im}(x) < 5.80228 \times 10^{-81} \\ (1.85193 \times 10^9 i) (x + 1.50418 \times 10^{60}) + & \operatorname{Im}((x + 1.50418 \times 10^{60})^2) \\ (3.34245 \times 10^{-36} i) & \\ (x + 1.50418 \times 10^{60})^2 + & \\ (1.20652 \times 10^{-80} i) & \\ (x + 1.50418 \times 10^{60})^3 + & \\ (5.44397 \times 10^{-125} i) & \\ (x + 1.50418 \times 10^{60})^4 + & \\ (2.75115 \times 10^{-169} i) & \\ (x + 1.50418 \times 10^{60})^5 + & \\ O((x + 1.50418 \times 10^{60})^6) & \end{array} \right.$$

$$\left\{ \begin{array}{ll} (4.33153 \times 10^{81} + 5.13045 \times 10^{53} i) - & \text{(otherwise)} \\ (1.85193 \times 10^9 i) (x + 1.50418 \times 10^{60}) - & \\ (3.34245 \times 10^{-36} i) & \\ (x + 1.50418 \times 10^{60})^2 - & \\ (1.20652 \times 10^{-80} i) & \\ (x + 1.50418 \times 10^{60})^3 - & \\ (5.44397 \times 10^{-125} i) & \\ (x + 1.50418 \times 10^{60})^4 - & \\ (2.75115 \times 10^{-169} i) & \\ (x + 1.50418 \times 10^{60})^5 + & \\ O((x + 1.50418 \times 10^{60})^6) & \end{array} \right.$$

Series expansion at $x = 0$:

$$4.33153 \times 10^{81} - 8.35428 \times 10^{-60} x^2 - 9.23097 \times 10^{-181} x^4 + O(x^5)$$

(Taylor series)

Series expansion at $x = 1.50418 \times 10^{60}$:

$$\begin{aligned} & \left(3.29944 \times 10^{41} \sqrt{2.62561 \times 10^{40} - 1.74554 \times 10^{-20} x} + 4.33153 \times 10^{81} \right) + \\ & 5.48377 \times 10^{-20} \sqrt{2.62561 \times 10^{40} - 1.74554 \times 10^{-20} x} (x - 1.50418 \times 10^{60}) - \\ & 4.5571 \times 10^{-81} \sqrt{2.62561 \times 10^{40} - 1.74554 \times 10^{-20} x} (x - 1.50418 \times 10^{60})^2 + \\ & 7.57405 \times 10^{-142} \sqrt{2.62561 \times 10^{40} - 1.74554 \times 10^{-20} x} (x - 1.50418 \times 10^{60})^3 - \\ & 1.57354 \times 10^{-202} \sqrt{2.62561 \times 10^{40} - 1.74554 \times 10^{-20} x} (x - 1.50418 \times 10^{60})^4 + \\ & O((x - 1.50418 \times 10^{60})^5) \end{aligned}$$

(generalized Puiseux series)

Series expansion at $x = \infty$:

$$\left(25.1327 \sqrt{-x^2} + 4.33153 \times 10^{81} \right) - \frac{2.84323 \times 10^{121} \sqrt{-x^2}}{x^2} + O\left(\left(\frac{1}{x}\right)^4\right)$$

(Puiseux series)

Derivative:

$$\begin{aligned} & \frac{d}{dx} \left(329\,944\,134\,815\,088\,149\,437\,614\,228\,845\,320\,585\,871\,360 \right. \\ & \left. \left(\sqrt{(13\,128\,059\,999\,999\,999\,398\,713\,729\,449\,103\,615\,590\,400 - 5.80228 \times 10^{-81} x^2) + 13\,128\,059\,999\,999\,999\,398\,713\,729\,449\,103\,615\,590\,400} \right) \right) = \\ & \frac{1.91443 \times 10^{-39} x}{\sqrt{13\,128\,059\,999\,999\,999\,398\,713\,729\,449\,103\,615\,590\,400 - 5.80228 \times 10^{-81} x^2}} \end{aligned}$$

Indefinite integral:

$$\begin{aligned} & \int 8 \pi 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \cdot 1.312806 \times 10^{40}} + \right. \\ & \left. \sqrt{-\frac{x^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \cdot 1.312806 \times 10^{40}} \right)^2 \right)} \right) dx = \\ & x \left(1.64972 \times 10^{41} \sqrt{1.31281 \times 10^{40} - 5.80228 \times 10^{-81} x^2} + 4.33153 \times 10^{81} \right) + \\ & 2.84323 \times 10^{121} \sin^{-1}(6.64812 \times 10^{-61} x) + \text{constant} \end{aligned}$$

$\sin^{-1}(x)$ is the inverse sine function

Global maximum:

$$\max\left\{329\,944\,134\,815\,088\,149\,437\,614\,228\,845\,320\,585\,871\,360\right. \\ \left. \left(\sqrt{(13\,128\,059\,999\,999\,999\,398\,713\,729\,449\,103\,615\,590\,400 - 5.80228 \times 10^{-81} x^2) + 13\,128\,059\,999\,999\,999\,398\,713\,729\,449\,103\,615\,590\,400}\right)\right\} = \\ 3\,627\,774\,127\,456\,815\,639\,530\,787\,597\,196\,574\,102\,919\,810\,209\,388\,953\,600 \\ \left(1\,193\,990\,101\,455\,710\,773\,617\,623\,040 + \sqrt{108\,592\,767\,124\,329}\right) \text{ at } x = 0$$

Global minimal:

$$\min\left\{329\,944\,134\,815\,088\,149\,437\,614\,228\,845\,320\,585\,871\,360\right. \\ \left. \left(\sqrt{(13\,128\,059\,999\,999\,999\,398\,713\,729\,449\,103\,615\,590\,400 - 5.80228 \times 10^{-81} x^2) + 13\,128\,059\,999\,999\,999\,398\,713\,729\,449\,103\,615\,590\,400}\right)\right\} = \\ 4\,331\,526\,398\,500\,565\,932\,715\,087\,540\,028\,575\,347\,223\,021\,213\,577\,359\,699\,712 \cdot \\ 851\,560\,462\,974\,864\,850\,944\,000 \text{ at } \\ x = -15\,820\,279\,490\,848\,302\,930\,678\,856\,003\,092\,480 \\ \sqrt{9\,040\,102\,512\,832\,509\,502\,646\,974\,031\,232\,662\,040\,622\,266\,291\,576\,609}$$

$$\min\left\{329\,944\,134\,815\,088\,149\,437\,614\,228\,845\,320\,585\,871\,360\right. \\ \left. \left(\sqrt{(13\,128\,059\,999\,999\,999\,398\,713\,729\,449\,103\,615\,590\,400 - 5.80228 \times 10^{-81} x^2) + 13\,128\,059\,999\,999\,999\,398\,713\,729\,449\,103\,615\,590\,400}\right)\right\} = \\ 4\,331\,526\,398\,500\,565\,932\,715\,087\,540\,028\,575\,347\,223\,021\,213\,577\,359\,699\,712 \cdot \\ 851\,560\,462\,974\,864\,850\,944\,000 \text{ at } \\ x = 15\,820\,279\,490\,848\,302\,930\,678\,856\,003\,092\,480 \\ \sqrt{9\,040\,102\,512\,832\,509\,502\,646\,974\,031\,232\,662\,040\,622\,266\,291\,576\,609}$$

Limit:

$$\lim_{x \rightarrow \pm\infty} \frac{3.29944 \times 10^{41} \left(1.31281 \times 10^{40} + \sqrt{1.31281 \times 10^{40} - 5.80228 \times 10^{-81} x^2}\right)}{4.33153 \times 10^{81}} =$$

thence, we have, for $J = -1.50418e+60$:

$$8\text{Pi} \cdot (1.312806e+40) \cdot \left[(1.312806e+40 - (5/(2 \cdot 1.312806e+40))) + \sqrt{(((-1.50418e+60)^2 / (1.312806e+40)^2 + (1.312806e+40 - (5/(2 \cdot 1.312806e+40)))^2))} \right]$$

Input interpretation:

$$8\pi \times 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{-\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}}\right)^2\right)} \right)$$

Result:

$$4.33153... \times 10^{81}$$

$$4.33153... \times 10^{81} = A$$

$$\ln(\left(\left(\left(\left(8\pi \times (1.312806 \times 10^{40}) \times \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}}\right) + \sqrt{\left(-\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}}\right)^2\right)}\right)\right)\right)\right))$$

Input interpretation:

$$\log \left(8\pi \times 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{-\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}}\right)^2\right)} \right) \right)$$

log(x) is the natural logarithm

Result:

$$187.97531...$$

$$187.97531...$$

$$1 + \frac{1}{3 \times 187.97531252938}$$

Input interpretation:

$$1 + \frac{1}{3 \times 187.97531252938}$$

Result:

1.001773282506346328288704817065864358161065637225958727487...

1.0017732825.... result very near to the following Rogers-Ramanujan continued fraction:

$$\frac{e^{\frac{2\pi}{5}}}{\sqrt{\phi\sqrt{5} - \phi}} = 1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \frac{e^{-8\pi}}{1 + \dots}}}} \approx 1.0018674362$$

3Pi*(187.97531252938)-55+13-1/golden ratio

Input interpretation:

$$3\pi \times 187.97531252938 - 55 + 13 - \frac{1}{\phi}$$

φ is the golden ratio

Result:

1729.0075487069...

1729.0075487069....

This result is very near to the mass of candidate glueball f₀(1710) meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Alternative representations:

$$3\pi \times 187.975312529380000 - 55 + 13 - \frac{1}{\phi} = -42 + 101506.668765865200^\circ - \frac{1}{2 \cos(216^\circ)}$$

$$3 \pi 187.975312529380000 - 55 + 13 - \frac{1}{\phi} = -42 + 563.925937588140000 \pi - \frac{1}{2 \cos(216^\circ)}$$

$$3 \pi 187.975312529380000 - 55 + 13 - \frac{1}{\phi} = -42 + 101506.668765865200^\circ - \frac{1}{2 \cos\left(\frac{\pi}{5}\right)}$$

Series representations:

$$3 \pi 187.975312529380000 - 55 + 13 - \frac{1}{\phi} = -42 - \frac{1}{\phi} + 2255.70375035256000 \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$3 \pi 187.975312529380000 - 55 + 13 - \frac{1}{\phi} = -1169.851875176280 - \frac{1.0000000000000000}{\phi} + 1127.851875176280 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$3 \pi 187.975312529380000 - 55 + 13 - \frac{1}{\phi} = -42 - \frac{1}{\phi} + 563.925937588140000 \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}}$$

Integral representations:

$$3 \pi 187.975312529380000 - 55 + 13 - \frac{1}{\phi} = -42 - \frac{1}{\phi} + 1127.85187517628000 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$3 \pi 187.975312529380000 - 55 + 13 - \frac{1}{\phi} = -42 - \frac{1}{\phi} + 2255.70375035256000 \int_0^1 \sqrt{1-t^2} dt$$

$$3 \pi 187.975312529380000 - 55 + 13 - \frac{1}{\phi} = -42 - \frac{1}{\phi} + 1127.85187517628000 \int_0^{\infty} \frac{\sin(t)}{t} dt$$

$$-47 + \ln[8\pi \cdot (1.312806 \times 10^{40}) \cdot [(1.312806 \times 10^{40} - (5/(2 \cdot 1.312806 \times 10^{40})) + \sqrt{((-1.50418 \times 10^{60})^2 / (1.312806 \times 10^{40})^2 + (1.312806 \times 10^{40} - (5/(2 \cdot 1.312806 \times 10^{40}))^2)})]]]$$

Input interpretation:

$$-47 + \log \left(8 \pi \times 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{-\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}}\right)^2\right)} \right) \right)$$

log(x) is the natural logarithm

Result:

140.97531...

140.97531...

From:

(140.975312529387315154 - golden ratio)

Input interpretation:

140.975312529387315154 - ϕ

ϕ is the golden ratio

Result:

139.357278540637420306...

139.3572785.... result practically equal to the rest mass of Pion meson 139.57 MeV

(140.975312529387315154 - 13-golden ratio²)

Input interpretation:

140.975312529387315154 - 13 - ϕ^2

ϕ is the golden ratio

Result:

125.357278540637420306...

125.3572785.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

Alternative representations:

$$140.9753125293873151540000 - 13 - \phi^2 = \\ 127.9753125293873151540000 - (2 \sin(54^\circ))^2$$

$$140.9753125293873151540000 - 13 - \phi^2 = \\ 127.9753125293873151540000 - (-2 \cos(216^\circ))^2$$

$$140.9753125293873151540000 - 13 - \phi^2 = \\ 127.9753125293873151540000 - (-2 \sin(666^\circ))^2$$

We have also:

$$-21 + \left[\left[8\pi \times (1.312806 \times 10^{40}) \times \left[1.312806 \times 10^{40} - \frac{5}{(2 \times 1.312806 \times 10^{40})} \right] + \sqrt{\left(-\frac{1.50418 \times 10^{60}}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \frac{5}{(2 \times 1.312806 \times 10^{40})} \right)^2} \right) \right] \right]^{1/37}$$

Input interpretation:

$$-21 + \left(8\pi \times 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}} \right)^2} \right)^2} \right) \right)^{1/37}$$

Result:

139.8406...

139.8406.... result practically equal to the rest mass of Pion meson 139.57 MeV

$$-34 - \phi + \left[\left[8\pi \times (1.312806 \times 10^{40}) \times \left[1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}} \right)^2} \right)} \right] \right] \right]^{1/37}$$

Input interpretation:

$$-34 - \phi + \left(8\pi \times 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}} \right)^2} \right)} \right) \right)^{1/37}$$

φ is the golden ratio

Result:

125.2225723979358381924159675830050004216576576900037213713...

125.22257239.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

$$-34 - x + \left[\left[8\pi \times (1.312806 \times 10^{40}) \times \left[1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}} \right)^2} \right)} \right] \right] \right]^{1/37} = 125.2225723979358$$

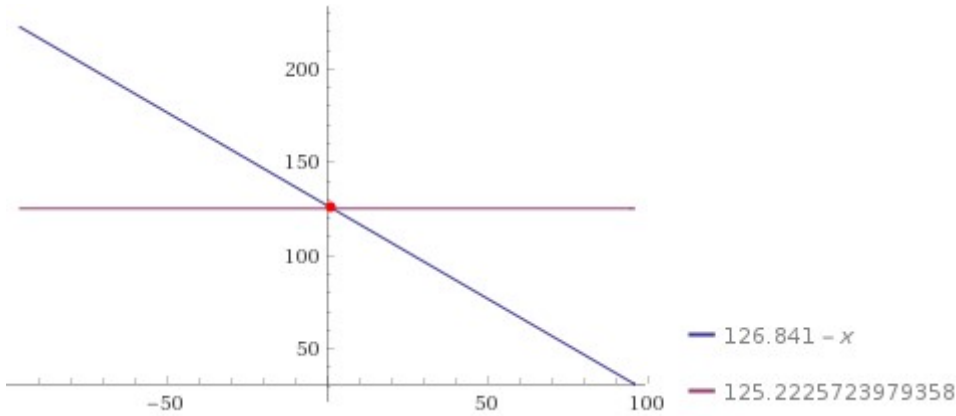
Input interpretation:

$$-34 - x + \left(8\pi \times 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}} \right)^2} \right)} \right) \right)^{1/37} = 125.2225723979358$$

Result:

126.841 - x = 125.2225723979358

Plot:



Alternate forms:

$$1.61803 - x = 0$$

$$126.841 - x = 125.2225723979358$$

Solution:

$$x \approx 1.61803$$

1.61803 result equal to the value of the golden ratio

$$-21 - \text{golden ratio} - \pi + \left[\left[8\pi * (1.312806e+40) * \left[1.312806e+40 - \frac{5}{2 * 1.312806e+40} + \sqrt{\frac{(-1.50418e+60)^2}{(1.312806e+40)^2} + \left(1.312806e+40 - \frac{5}{2 * 1.312806e+40} \right)^2} \right] \right] \right]^{1/37}$$

Input interpretation:

$$-21 - \phi - \pi + \left(8\pi \times 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}} \right)^2 \right)} \right) \right)^{1/37}$$

ϕ is the golden ratio

Result:

135.0810...

135.081... ≈ 135 (Ramanujan taxicab number) and result practically equal to the rest mass of Pion meson 134.9766 MeV

$$-21 - \phi - x + \left[\left[8\pi \times (1.312806 \times 10^{40}) \times \left[1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}} \right)^2} \right)^2} \right] \right] \right]^{1/37} = 135.080979744346$$

Input interpretation:

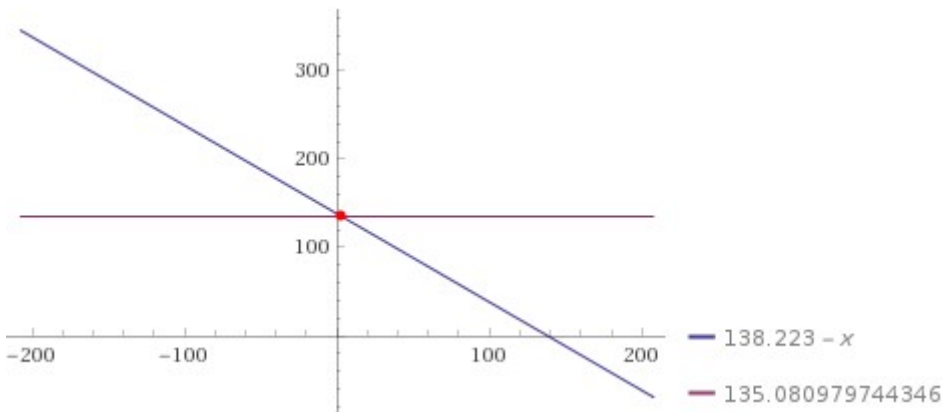
$$-21 - \phi - x + \left(8\pi \times 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}} \right)^2} \right)^2} \right) \right)^{1/37} = 135.080979744346$$

φ is the golden ratio

Result:

$$138.223 - x = 135.080979744346$$

Plot:



Alternate forms:

$$3.14159 - x = 0$$

$$138.223 - x = 135.080979744346$$

Solution:

$$x \approx 3.14159$$

$$3.14159 = \pi$$

$$-21-x-\pi+[[[8\pi*(1.312806e+40)*[1.312806e+40-(5/(2*1.312806e+40)))+\text{sqrt}((-(-1.50418e+60)^2/(1.312806e+40)^2+(1.312806e+40-(5/(2*1.312806e+40))^2)))]]]^{1/37} = 135.080979744346$$

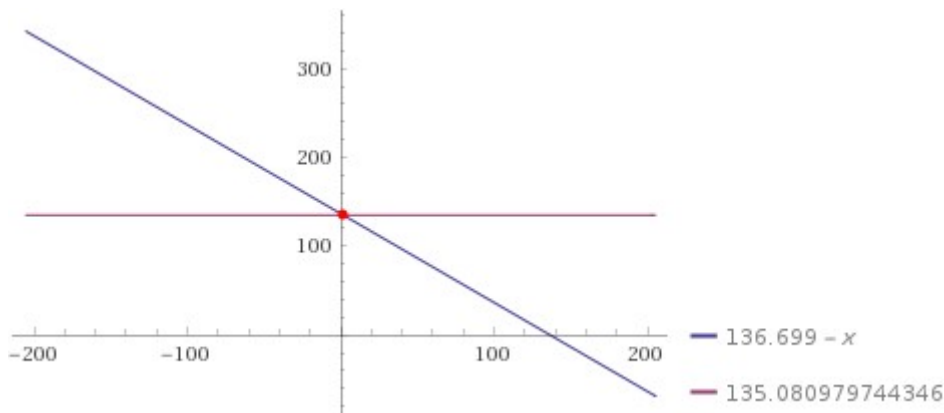
Input interpretation:

$$-21 - x - \pi + \left(8\pi \times 1.312806 \times 10^{40} \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{-\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \left(\frac{5}{2 \times 1.312806 \times 10^{40}} \right)^2 \right)^2} \right) \right)^{1/37} = 135.080979744346$$

Result:

$$136.699 - x = 135.080979744346$$

Plot:



Alternate forms:

$$1.61803 - x = 0$$

$$136.699 - x = 135.080979744346$$

Solution:

$$x \approx 1.61803$$

$$1.61803 = \text{golden ratio}$$

Now, we have that:

$$\kappa = \frac{\sqrt{-4J^2 + (2M^2 - Q^2)^2}}{2M(2M^2 - Q^2 + \sqrt{-4J^2 + (2M^2 - Q^2)^2})}$$

$$M = 1.312806e+40, Q = \sqrt{5} \quad J = -1.50418e+60$$

$$\text{sqrt}(((-4 * (-1.50418e+60)^2 + (2 * 1.312806e+40^2 - 5)^2))) / (((2 * 1.312806e+40(2 * 1.312806e+40^2 - 5 + \text{sqrt}(((-4 * (-1.50418e+60)^2 + (2 * 1.312806e+40^2 - 5)^2))))))$$

Input interpretation:

$$\left(\sqrt{-4(-1.50418 \times 10^{60})^2 + (2(1.312806 \times 10^{40})^2 - 5)^2} \right) / \left(2 \times 1.312806 \times 10^{40} \left(2(1.312806 \times 10^{40})^2 - 5 + \sqrt{-4(-1.50418 \times 10^{60})^2 + (2(1.312806 \times 10^{40})^2 - 5)^2} \right) \right)$$

Result:

$$1.90432... \times 10^{-41}$$

$$1.90432... * 10^{-41} = \kappa$$

We have also:

$$(((((((\text{sqrt}(((-4 * (-1.50418e+60)^2 + (2 * 1.312806e+40^2 - 5)^2)))) / (((2 * 1.312806e+40(2 * 1.312806e+40^2 - 5 + \text{sqrt}(((-4 * (-1.50418e+60)^2 + (2 * 1.312806e+40^2 - 5)^2))))))))))))))))^{1/2048}$$

Input interpretation:

$$\left(\left(\sqrt{-4(-1.50418 \times 10^{60})^2 + (2(1.312806 \times 10^{40})^2 - 5)^2} \right) / \right. \\ \left. \left(2 \times 1.312806 \times 10^{40} \left(2(1.312806 \times 10^{40})^2 - 5 + \right. \right. \right. \\ \left. \left. \left. \sqrt{-4(-1.50418 \times 10^{60})^2 + (2(1.312806 \times 10^{40})^2 - 5)^2} \right) \right) \right)^{(1/2048)}$$

Result:

0.955250031...

0.955250031.... result very near to the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1)\sqrt{5}-\varphi+1}} = 1 - \frac{e^{-\pi}}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-3\pi}}{1 + \frac{e^{-4\pi}}{1 + \dots}}}}} \approx 0.9568666373$$

$$A = 4.33153... * 10^{81}$$

$$1 + 1 / (((((4.33153e+81) * (1.90432 \times 10^{-41})^2))) - 18 / 10^3)$$

Input interpretation:

$$1 + \frac{1}{4.33153 \times 10^{81} (1.90432 \times 10^{-41})^2} - \frac{18}{10^3}$$

Result:

1.618617856783841036057906862489493826207174523035915763218...

1.6186178567.... result that is a very good approximation to the value of the golden ratio 1,618033988749...

Now, we have:

$$Q = \frac{\eta}{\sqrt{2}} \sinh \alpha, \quad M = \frac{\eta}{2}(1 + \cosh \alpha), \quad \mu = \frac{1}{\sqrt{2}} \eta a \sinh \alpha, \quad J = \frac{\eta a}{2}(1 + \cosh \alpha). \quad (4)$$

The associated g -factor can be expressed as $g = \frac{2\mu M}{QJ} = 2$ [28]. The parameters can be expressed in terms of genuinely physical quantities as

$$\eta = M - \frac{Q^2}{2M}, \quad \alpha = \operatorname{arcsinh} \left(\frac{2\sqrt{2}QM}{2M^2 - Q^2} \right), \quad a = \frac{J}{M}$$

The coordinate singularities thus read $r_{\pm} = M - \frac{Q^2}{2M} \pm \sqrt{-\frac{J^2}{M^2} + \left(M - \frac{Q^2}{2M}\right)^2}$ which vanishes unless

Finally the Hawking temperature of the Kerr-Sen dilaton-axion black hole is acquired:

$$T_H = \frac{1}{2\pi} \frac{(r_+ + m)}{r_+^2 - 2\beta r_+ + a^2} \quad (34)$$

which is an universal formula also obtained by other methods for the Hawking temperature from fermions tunnelling [30]. Obviously when the parameter a tends to zero, Eq.(34) provides the well-known Hawking radiation associated to the static black hole.

For:

$$r_{\pm} = M - \frac{Q^2}{2M} \pm \sqrt{-\frac{J^2}{M^2} + \left(M - \frac{Q^2}{2M}\right)^2}$$

$$\beta = \eta \sinh^2 \frac{\alpha}{2}$$

$$T_H = \frac{1}{2\pi} \frac{(r_+ + m)}{r_+^2 - 2\beta r_+ + a^2}$$

$M = 1.312806\text{e}+40$, $Q = \sqrt{5}$; $J = -1.50418\text{e}+60$

$$\eta = M - \frac{Q^2}{2M}, \quad \alpha = \operatorname{arcsinh} \left(\frac{2\sqrt{2}QM}{2M^2 - Q^2} \right), \quad a = \frac{J}{M}$$

From

$$r_{\pm} = M - \frac{Q^2}{2M} \pm \sqrt{-\frac{J^2}{M^2} + \left(M - \frac{Q^2}{2M}\right)^2}$$

We obtain:

$$(1.312806e+40) - 5 / (2 * 1.312806e+40) + \text{sqrt}[(((- (-1.50418e+60)^2 / (1.312806e+40)^2 + (((1.312806e+40) - 5 / (2 * 1.312806e+40))^2)))]$$

Input interpretation:

$$1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}} + \sqrt{-\frac{(-1.50418 \times 10^{60})^2}{(1.312806 \times 10^{40})^2} + \left(1.312806 \times 10^{40} - \frac{5}{2 \times 1.312806 \times 10^{40}}\right)^2}$$

Result:

$$2.62561... \times 10^{40}$$

$$2.62561 * 10^{40} = r_{\pm}$$

Now:

$$\beta = \eta \sinh^2 \frac{\alpha}{2}$$

$$1.3128059999e+40 \sinh^2(1/2 * 2.40879e-40)$$

Input interpretation:

$$1.3128059999 \times 10^{40} \sinh^2\left(\frac{1}{2} \times 2.40879 \times 10^{-40}\right)$$

$\sinh(x)$ is the hyperbolic sine function

Result:

$$1.90431... \times 10^{-40}$$

$$1.90431 * 10^{-40} = \beta$$

From

$$T_H = \frac{1}{2\pi} \frac{(r_+ + m)}{r_+^2 - 2\beta r_+ + a^2}$$

we obtain, in conclusion:

$$\frac{1}{2\pi} \cdot (2.62561e+40+x) / (((((2.62561e+40)^2 - (2 \cdot 1.90431e-40 \cdot 2.62561e+40) + (-1.145774775557e+20)^2)))$$

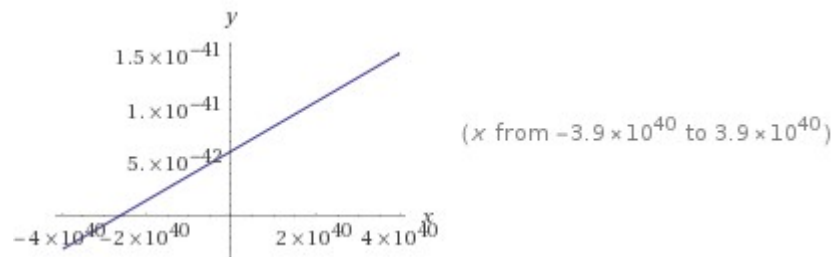
Input interpretation:

$$\frac{1}{2\pi} \times (2.62561 \times 10^{40} + x) / ((2.62561 \times 10^{40})^2 - 2 \times 1.90431 \times 10^{-40} \times 2.62561 \times 10^{40} + (-1.145774775557 \times 10^{20})^2)$$

Result:

$$2.30866 \times 10^{-82} (x + 2.62561 \times 10^{40})$$

Plot:



Geometric figure:

line

Alternate form:

$$2.30866 \times 10^{-82} x + 6.06164 \times 10^{-42}$$

Root:

$$x = -26\,256\,099\,999\,999\,997\,661\,706\,325\,792\,465\,457\,512\,448$$

Integer root:

$$x = -26\,256\,099\,999\,999\,997\,661\,706\,325\,792\,465\,457\,512\,448$$

Properties as a real function:

Domain

\mathbb{R} (all real numbers)

Range

\mathbb{R} (all real numbers)

Surjectivity

surjective onto \mathbb{R}

\mathbb{R} is the set of real numbers

Derivative:

$$\frac{d}{dx}(2.30866 \times 10^{-82} (x + 26\,256\,099\,999\,999\,997\,661\,706\,325\,792\,465\,457\,512\,448)) = 2.30866 \times 10^{-82}$$

Indefinite integral:

$$\int \left(\frac{(2.62561 \times 10^{40} + x) / ((2\pi) \left((2.62561 \times 10^{40})^2 - 2 \cdot 1.90431 \times 10^{-40} \cdot 2.62561 \times 10^{40} + (-1.145774775557 \times 10^{20})^2 \right))}{1.15433 \times 10^{-82} x^2 + 6.06164 \times 10^{-42} x + \text{constant}} \right) dx =$$

Definite integral after subtraction of diverging parts:

$$\int_0^\infty (2.30866 \times 10^{-82} (2.62561 \times 10^{40} + x) - (6.06164 \times 10^{-42} + 2.30866 \times 10^{-82} x)) dx =$$

Result:

$$-2.62560999999999997661706325792465457512448 \times 10^{40} - 2.62560999 \dots \cdot 10^{40} = m$$

Thence:

$$T_H = \frac{1}{2\pi} \frac{(r_+ + m)}{r_+^2 - 2\beta r_+ + a^2}$$

$$1/(2\pi) * ((2.62561e+40) + (-2.6256099999999999e+40)) / (((((2.62561e+40)^2 - (2 * 1.90431e-40 * 2.62561e+40) + (-1.145774775557e+20)^2)))$$

Input interpretation:

$$\frac{1}{2\pi} \times \frac{(2.62561 \times 10^{40} - 2.6256099999999999 \times 10^{40})}{(2.62561 \times 10^{40})^2 - 2 \times 1.90431 \times 10^{-40} \times 2.62561 \times 10^{40} + (-1.145774775557 \times 10^{20})^2}$$

Result:2.30866... × 10⁻⁵⁴2.30866*10⁻⁵⁴

$$\left(\frac{1}{2\pi} \times ((2.62561e+40) + (-2.625609999999e+40)) / \left((2.62561e+40)^2 - 2 \times 1.90431e-40 \times 2.62561e+40 + (-1.145774775557e+20)^2 \right) \right)^{1/2048}$$
Input interpretation:

$$\left(\frac{1}{2\pi} \times (2.62561 \times 10^{40} - 2.625609999999 \times 10^{40}) / \left((2.62561 \times 10^{40})^2 - 2 \times 1.90431 \times 10^{-40} \times 2.62561 \times 10^{40} + (-1.145774775557 \times 10^{20})^2 \right) \right)^{(1/2048)}$$

Result:

0.941478126032570097150860406962716674916829330183207457169...

0.941478126...result very near to the spectral index n_s , to the mesonic Regge slope, to the inflaton value at the end of the inflation 0.9402 (see Appendix) and to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1)\sqrt{5}} - \varphi + 1} = 1 - \frac{e^{-\pi}}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-3\pi}}{1 + \frac{e^{-4\pi}}{1 + \dots}}}} \approx 0.9568666373$$

From:

Astronomy & Astrophysics manuscript no. ms c ESO 2019 - September 24, 2019
Planck 2018 results. VI. Cosmological parameters

The primordial fluctuations are consistent with Gaussian purely adiabatic scalar perturbations characterized by a power spectrum with a spectral index $n_s = 0.965 \pm 0.004$, consistent with the predictions of slow-roll, single-field, inflation.

We know that α' is the Regge slope (string tension). With regard the Omega mesons, the values are:

$$\omega \quad | \quad 6 \quad | \quad m_{u/d} = 0 - 60 \quad | \quad 0.910 - 0.918$$

$$\omega/\omega_3 \quad | \quad 5 + 3 \quad | \quad m_{u/d} = 255 - 390 \quad | \quad 0.988 - 1.18$$

$$\omega/\omega_3 \quad | \quad 5 + 3 \quad | \quad m_{u/d} = 240 - 345 \quad | \quad 0.937 - 1.000$$

1/16*log base 0.941478126((((1/(2Pi))*((2.62561e+40)+(-2.625609999999999e+40)))/((((2.62561e+40)^2-(2*1.90431e-40*2.62561e+40)+(-1.145774775557e+20)^2)))))))-Pi+1/golden ratio

Input interpretation:

$$\frac{1}{16} \log_{0.941478126} \left(\frac{1}{2\pi} \times (2.62561 \times 10^{40} - 2.625609999999999 \times 10^{40}) / \left((2.62561 \times 10^{40})^2 - 2 \times 1.90431 \times 10^{-40} \times 2.62561 \times 10^{40} + (-1.145774775557 \times 10^{20})^2 \right) \right) - \pi + \frac{1}{\phi}$$

log_b(x) is the base- b logarithm

φ is the golden ratio

Result:

125.4764412617304468835898852604086515598353238092466896923...

125.4764412617... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

Note that:

$$125.4764412617 \text{ GeV} = K$$

Input interpretation:

convert

125.4764412617 GeV/k_B (gigaelectronvolts per Boltzmann constant) to kelvins

Result:

1.45609363645 × 10¹⁵ K (kelvins)

$$1.45609363645 \times 10^{15} \text{ K}$$

Thence from a result as $2.30866 \cdot 10^{-54}$, that tend to 0, we obtain the corresponding values: $125.4764412617 \text{ GeV} = 1.45609363645 \cdot 10^{15} \text{ K}$, i.e. a large number

Additional conversions:

$1.45609363645 \times 10^{15} \text{ }^\circ\text{C}$ (degrees Celsius)

$2.62096854561 \times 10^{15} \text{ }^\circ\text{F}$ (degrees Fahrenheit)

$2.62096854561 \times 10^{15} \text{ }^\circ\text{R}$ (degrees Rankine)

$1.16487490916 \times 10^{15} \text{ }^\circ\text{Ré}$ (degrees Réaumur)

$7.64449159136 \times 10^{14} \text{ }^\circ\text{Rø}$ (degrees Rømer)

Interpretations:

temperature

Basic unit dimensions:

[temperature]

Corresponding quantities:

Thermodynamic energy E from $E = kT$:

125 GeV (gigaelectronvolts)

Approximate luminous exitance from a planar blackbody radiator perpendicular to its surface:

$2.973 \times 10^{22} \text{ lx}$ (lux)

Acceleration a needed to achieve given temperature as an Unruh temperature from $T = \hbar a / (2\pi c k)$:

$3.591 \times 10^{35} \text{ m/s}^2$ (meters per second squared)

Gravitational acceleration g needed to achieve given temperature as a Hawking temperature from $T = \hbar g / (2\pi c k)$:

$3.591 \times 10^{35} \text{ m/s}^2$ (meters per second squared)

$1/16 * \log_{\text{base } 0.941478126}(\frac{1}{2\pi} * ((2.62561e+40) + (-2.625609999999e+40)) / (((((2.62561e+40)^2 - (2 * 1.90431e-40 * 2.62561e+40) + (-1.145774775557e+20)^2)))))) + 11 + 1/\text{golden ratio}$

Input interpretation:

$$\frac{1}{16} \log_{0.941478126} \left(\frac{1}{2\pi} \times (2.62561 \times 10^{40} - 2.625609999999 \times 10^{40}) / \left((2.62561 \times 10^{40})^2 - 2 \times 1.90431 \times 10^{-40} \times 2.62561 \times 10^{40} + (-1.145774775557 \times 10^{20})^2 \right) \right) + 11 + \frac{1}{\phi}$$

$\log_b(x)$ is the base- b logarithm

ϕ is the golden ratio

Result:

139.6180339153202401220525286436881544440324932086217955133...

139.618033915.... result practically equal to the rest mass of Pion meson 139.57 MeV

$27 * 1/32 * \log_{\text{base } 0.941478126}(\frac{1}{2\pi} * ((2.62561e+40) + (-2.625609999999e+40)) / (((((2.62561e+40)^2 - (2 * 1.90431e-40 * 2.62561e+40) + (-1.145774775557e+20)^2)))))) + 1$

Input interpretation:

$$27 \times \frac{1}{32} \log_{0.941478126} \left(\frac{1}{2\pi} \times (2.62561 \times 10^{40} - 2.625609999999 \times 10^{40}) / \left((2.62561 \times 10^{40})^2 - 2 \times 1.90431 \times 10^{-40} \times 2.62561 \times 10^{40} + (-1.145774775557 \times 10^{20})^2 \right) \right) + 1$$

$\log_b(x)$ is the base- b logarithm

Result:

1728.999999008699661196947214425853970405214484389016440791...

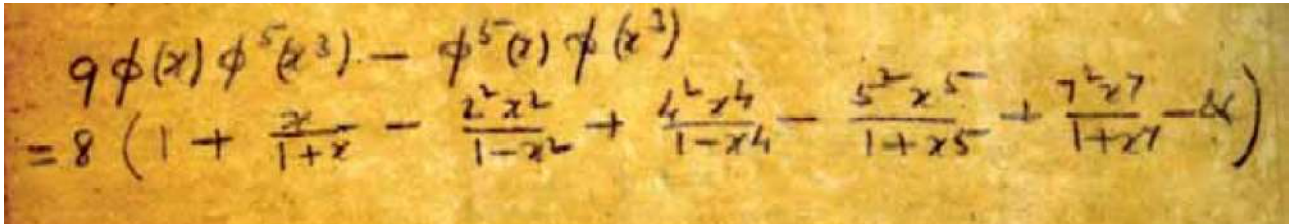
1728.99999... \approx 1729

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

From

Manuscript Book I of Srinivasa Ramanujan

Now, we have that (page 211)



A photograph of a handwritten mathematical formula on aged, yellowed paper. The formula is written in dark ink and consists of two lines. The first line is $9\phi(x)\phi^5(x^3) - \phi^5(x)\phi(x^3)$. The second line is $= 8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} - 11 \right)$.

$$8(1+2/(1+2)-(2^2*2^2)/(1-2^2)+(4^2*2^4)/(1-2^4)-(5^2*2^5)/(1+2^5)+(7^2*2^7)/(1+2^7))$$

Input:

$$8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right)$$

Exact result:

$$\frac{812296}{7095}$$

Decimal approximation:

114.4885130373502466525722339675828047921071176885130373502...

114.4885130735.....

$$8(1+2/(1+2)-(2^2*2^2)/(1-2^2)+(4^2*2^4)/(1-2^4)-(5^2*2^5)/(1+2^5)+(7^2*2^7)/(1+2^7))+11$$

Input:

$$8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 11$$

Exact result:

$$\frac{890341}{7095}$$

Decimal approximation:

125.4885130373502466525722339675828047921071176885130373502...

125.488513037... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

$$8(1+2/(1+2)-(2^2*2^2)/(1-2^2)+(4^2*2^4)/(1-2^4)-(5^2*2^5)/(1+2^5)+(7^2*2^7)/(1+2^7))+18+7$$

Input:

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 18 + 7$$

Exact result:

$$\frac{989671}{7095}$$

Decimal approximation:

139.4885130373502466525722339675828047921071176885130373502...

139.488513.... result practically equal to the rest mass of Pion meson 139.57 MeV

$$400/(3\pi^2)*((8(1+2/(1+2)-(2^2*2^2)/(1-2^2)+(4^2*2^4)/(1-2^4)-(5^2*2^5)/(1+2^5)+(7^2*2^7)/(1+2^7))+11+\text{golden ratio}^2))-\text{golden ratio}$$

Input:

$$\frac{400}{3\pi^2} \left(8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 11 + \phi^2 \right) - \phi$$

ϕ is the golden ratio

Result:

$$\frac{400 \left(\phi^2 + \frac{890341}{7095} \right)}{3\pi^2} - \phi$$

Decimal approximation:

1729.036229613553056810703672448709590226904853036141637678...

1729.0362296...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic

curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number [1729](#)

Property:

$$-\phi + \frac{400 \left(\frac{890341}{7095} + \phi^2 \right)}{3 \pi^2} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{-144\,157\,360 - 567\,600\sqrt{5} + 4257\pi^2 + 4257\sqrt{5}\pi^2}{8514\pi^2}$$

$$\frac{567\,600\phi^2 - 4257\pi^2\phi + 71\,227\,280}{4257\pi^2}$$

$$-\phi + \frac{400\phi^2}{3\pi^2} + \frac{71\,227\,280}{4257\pi^2}$$

Alternative representations:

$$\frac{\left(8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 11 + \phi^2 \right) 400}{3 \pi^2} - \phi =$$

$$2 \cos(216^\circ) + \frac{400 \left(11 + (-2 \cos(216^\circ))^2 + 8 \left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7} \right) \right)}{3 \pi^2}$$

$$\frac{\left(8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 11 + \phi^2 \right) 400}{3 \pi^2} - \phi =$$

$$-2 \cos\left(\frac{\pi}{5}\right) + \frac{400 \left(11 + \left(2 \cos\left(\frac{\pi}{5}\right) \right)^2 + 8 \left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7} \right) \right)}{3 \pi^2}$$

$$\frac{\left(8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 11 + \phi^2 \right) 400}{3 \pi^2} - \phi =$$

$$2 \cos(216^\circ) + \frac{400 \left(11 + (-2 \cos(216^\circ))^2 + 8 \left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7} \right) \right)}{3 (180^\circ)^2}$$

Series representations:

$$\frac{\left(8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 11 + \phi^2\right) 400}{3\pi^2} - \phi =$$

$$-\phi + \frac{400\left(\frac{890341}{7095} + \phi^2\right)}{3\left(\sum_{k=0}^{\infty} \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k}\right)^2}$$

$$\frac{\left(8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 11 + \phi^2\right) 400}{3\pi^2} - \phi =$$

$$-\phi + \frac{400\left(\frac{890341}{7095} + \phi^2\right)}{3\left(\sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{2}{1+4k} + \frac{2}{2+4k} + \frac{1}{3+4k}\right)\right)^2}$$

$$\frac{\left(8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 11 + \phi^2\right) 400}{3\pi^2} - \phi =$$

$$-\phi + \frac{400\left(\frac{890341}{7095} + \phi^2\right)}{3\left(\sum_{k=0}^{\infty} 16^{-k} \left(\frac{4}{1+8k} - \frac{2}{4+8k} - \frac{1}{5+8k} - \frac{1}{6+8k}\right)\right)^2}$$

Integral representations:

$$\frac{\left(8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 11 + \phi^2\right) 400}{3\pi^2} - \phi =$$

$$-\phi + \frac{6400\left(\frac{890341}{7095} + \phi^2\right)}{27\left(\sqrt{3} + 32 \int_0^{\frac{1}{4}} \sqrt{-(-1+t)t} dt\right)^2}$$

$$\frac{\left(8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 11 + \phi^2\right) 400}{3\pi^2} - \phi =$$

$$\frac{36\,039\,340 + 141\,900\sqrt{5} - 4257\left(\int_0^{\infty} \frac{1}{1+t^2} dt\right)^2 - 4257\sqrt{5}\left(\int_0^{\infty} \frac{1}{1+t^2} dt\right)^2}{8514\left(\int_0^{\infty} \frac{1}{1+t^2} dt\right)^2}$$

$$\frac{\left(8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 11 + \phi^2\right) 400}{3\pi^2} - \phi =$$

$$\frac{36\,039\,340 + 141\,900\sqrt{5} - 4257\left(\int_0^{\infty} \frac{\sin(t)}{t} dt\right)^2 - 4257\sqrt{5}\left(\int_0^{\infty} \frac{\sin(t)}{t} dt\right)^2}{8514\left(\int_0^{\infty} \frac{\sin(t)}{t} dt\right)^2}$$

$2\pi \cdot (8(1+2/(1+2)-(2^2 \cdot 2^2)/(1-2^2)+(4^2 \cdot 2^4)/(1-2^4)-(5^2 \cdot 2^5)/(1+2^5)+(7^2 \cdot 2^7)/(1+2^7)))+7+\text{golden ratio}$

Input:

$$2\pi \left(8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) \right) + 7 + \phi$$

ϕ is the golden ratio

Result:

$$\phi + 7 + \frac{1624592 \pi}{7095}$$

Decimal approximation:

727.9705769458674955332648742661928614642527727273183655272...

[727.97057... ≈ 728 \(Ramanujan taxicab number\)](#)

Property:

$7 + \phi + \frac{1624592 \pi}{7095}$ is a transcendental number

Alternate forms:

$$\frac{106425 + 7095\sqrt{5} + 3249184\pi}{14190}$$

$$\frac{7095\phi + 49665 + 1624592\pi}{7095}$$

$$\frac{15}{2} + \frac{\sqrt{5}}{2} + \frac{1624592\pi}{7095}$$

Alternative representations:

$$(2\pi)8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 7 + \phi =$$

$$7 - 2 \cos(216^\circ) + 16\pi \left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7} \right)$$

$$(2\pi)8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 7 + \phi =$$

$$7 - 2 \cos(216^\circ) + 2880^\circ \left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7} \right)$$

$$(2\pi)8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 7 + \phi =$$

$$7 + 2 \cos\left(\frac{\pi}{5}\right) + 16\pi \left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7} \right)$$

Series representations:

$$(2\pi)8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 7 + \phi =$$

$$7 + \phi + \frac{6498368 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}{7095}$$

$$(2\pi)8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 7 + \phi =$$

$$7 + \phi + \sum_{k=0}^{\infty} - \frac{6498368 (-1)^k 5^{-2(1+k)} \times 239^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1419(1+2k)}$$

$$(2\pi)8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 7 + \phi =$$

$$7 + \phi + \frac{1624592 \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right)}{7095}$$

Integral representations:

$$(2\pi)8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 7 + \phi =$$

$$7 + \phi + \frac{6498368}{7095} \int_0^1 \sqrt{1-t^2} dt$$

$$(2\pi)8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 7 + \phi =$$

$$7 + \phi + \frac{3249184}{7095} \int_0^1 \frac{1}{\sqrt{1-t^2}} dt$$

$$(2\pi)8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 7 + \phi =$$

$$7 + \phi + \frac{3249184}{7095} \int_0^\infty \frac{1}{1+t^2} dt$$

$$(8(1+2/(1+2)-(2^2*2^2)/(1-2^2)+(4^2*2^4)/(1-2^4)-(5^2*2^5)/(1+2^5)+(7^2*2^7)/(1+2^7)))+18+\text{golden ratio}^2$$

Input:

$$8 \left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7} \right) + 18 + \phi^2$$

ϕ is the golden ratio

Result:

$$\phi^2 + \frac{940006}{7095}$$

Decimal approximation:

135.1065470261001415007768208019484429098274268683188002123...

135.10654702... \approx 135 (Ramanujan taxicab number) and result practically equal to the rest mass of Pion meson 134.9766 MeV

Alternate forms:

$$\frac{1901297 + 7095\sqrt{5}}{14190}$$

$$\frac{7095\phi^2 + 940006}{7095}$$

$$\frac{1901297}{14190} + \frac{\sqrt{5}}{2}$$

Alternative representations:

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 18 + \phi^2 =$$

$$18 + 8\left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7}\right) + (2 \sin(54^\circ))^2$$

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 18 + \phi^2 =$$

$$18 + (-2 \cos(216^\circ))^2 + 8\left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7}\right)$$

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 18 + \phi^2 =$$

$$18 + 8\left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7}\right) + (-2 \sin(666^\circ))^2$$

$$(8(1+2/(1+2)-(2^2*2^2)/(1-2^2)+(4^2*2^4)/(1-2^4)-$$

$$(5^2*2^5)/(1+2^5)+(7^2*2^7)/(1+2^7)))+21+\text{golden ratio}^2$$

Input:

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 21 + \phi^2$$

ϕ is the golden ratio

Result:

$$\phi^2 + \frac{961291}{7095}$$

Decimal approximation:

138.1065470261001415007768208019484429098274268683188002123...

138.10654702... \approx 138 (Ramanujan taxicab number)

Alternate forms:

$$\frac{1943867 + 7095\sqrt{5}}{14190}$$

$$\frac{7095\phi^2 + 961291}{7095}$$

$$\frac{1943867}{14190} + \frac{\sqrt{5}}{2}$$

Alternative representations:

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 21 + \phi^2 =$$

$$21 + 8\left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7}\right) + (2 \sin(54^\circ))^2$$

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 21 + \phi^2 =$$

$$21 + (-2 \cos(216^\circ))^2 + 8\left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7}\right)$$

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 21 + \phi^2 =$$

$$21 + 8\left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7}\right) + (-2 \sin(666^\circ))^2$$

$$(8(1+2/(1+2)-(2^2*2^2)/(1-2^2)+(4^2*2^4)/(1-2^4)-(5^2*2^5)/(1+2^5)+(7^2*2^7)/(1+2^7)))+55+\text{golden ratio}^2$$

Input:

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 55 + \phi^2$$

Result:

$$\phi^2 + \frac{1202521}{7095}$$

Decimal approximation:

172.1065470261001415007768208019484429098274268683188002123...

172.10654702... \approx 172 (Ramanujan taxicab number)

Alternate forms:

$$\frac{2426327 + 7095\sqrt{5}}{14190}$$

$$\frac{7095\phi^2 + 1202521}{7095}$$

$$\frac{2426327}{14190} + \frac{\sqrt{5}}{2}$$

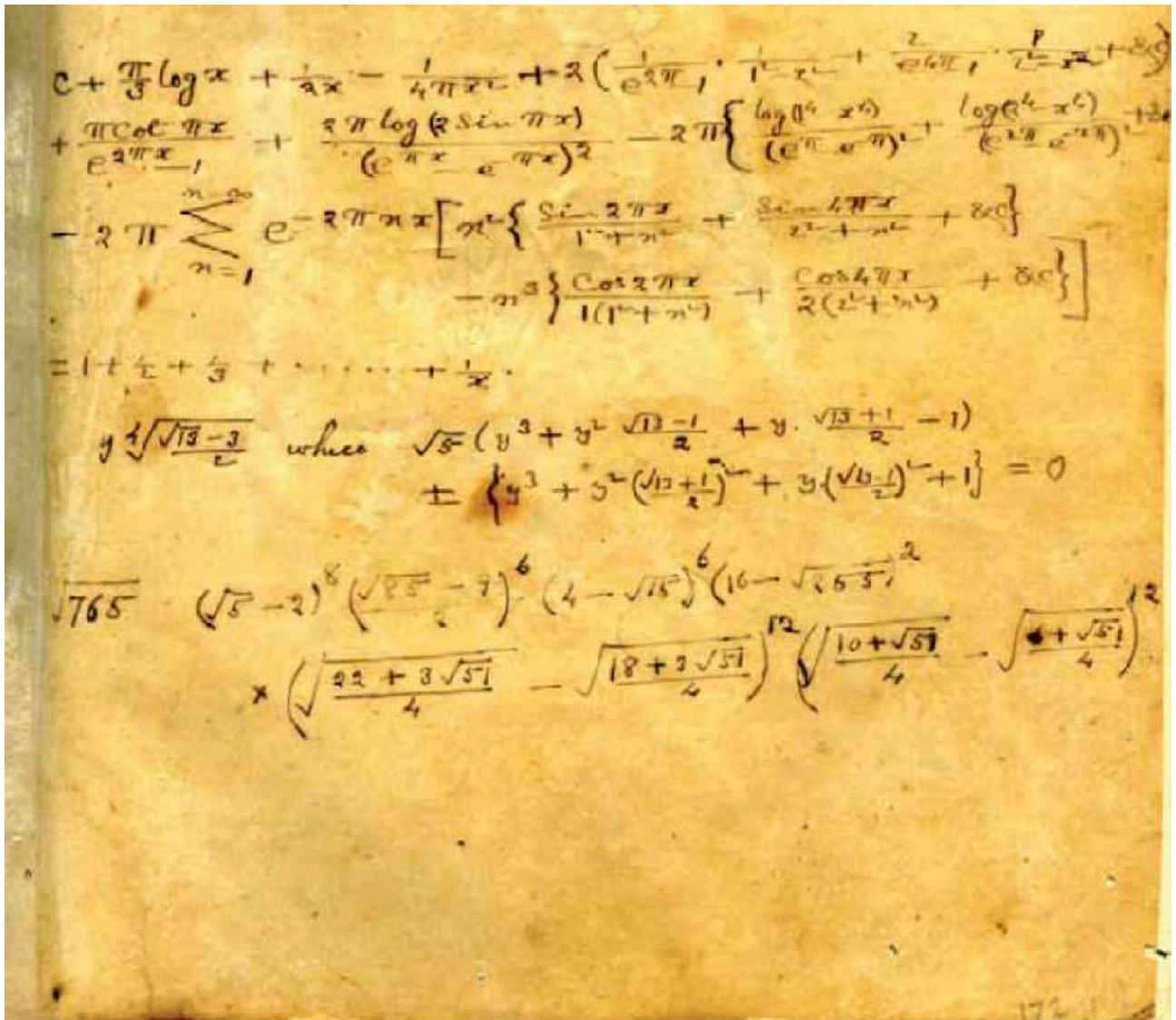
Alternative representations:

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 55 + \phi^2 =$$
$$55 + 8\left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7}\right) + (2 \sin(54^\circ))^2$$

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 55 + \phi^2 =$$
$$55 + (-2 \cos(216^\circ))^2 + 8\left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7}\right)$$

$$8\left(1 + \frac{2}{1+2} - \frac{2^2 \times 2^2}{1-2^2} + \frac{4^2 \times 2^4}{1-2^4} - \frac{5^2 \times 2^5}{1+2^5} + \frac{7^2 \times 2^7}{1+2^7}\right) + 55 + \phi^2 =$$
$$55 + 8\left(\frac{5}{3} - \frac{16}{3} + \frac{2^4 \times 4^2}{1-2^4} - \frac{2^5 \times 5^2}{1+2^5} + \frac{2^7 \times 7^2}{1+2^7}\right) + (-2 \sin(666^\circ))^2$$

Now, we have that, page 330:



$$\sqrt{765} (\sqrt{5}-2)^8 \left(\frac{\sqrt{85}-9}{2} \right)^6 (4-\sqrt{15})^6 (16-\sqrt{255})^2 \\ \left(\sqrt{\frac{22+3\sqrt{51}}{4}} - \sqrt{\frac{18+2\sqrt{51}}{4}} \right)^{12} \left(\sqrt{\frac{10+\sqrt{51}}{4}} - \sqrt{\frac{6+\sqrt{51}}{4}} \right)^{12}$$

Input:

$$\sqrt{765} (\sqrt{5}-2)^8 \left(\frac{1}{2} (\sqrt{85}-9) \right)^6 (4-\sqrt{15})^6 (16-\sqrt{255})^2 \\ \left(\sqrt{\frac{1}{4} (22+3\sqrt{51})} - \sqrt{\frac{1}{4} (18+2\sqrt{51})} \right)^{12} \left(\sqrt{\frac{1}{4} (10+\sqrt{51})} - \sqrt{\frac{1}{4} (6+\sqrt{51})} \right)^{12}$$

Exact result:

$$\frac{3}{64} \sqrt{85} (\sqrt{5} - 2)^8 (4 - \sqrt{15})^6 (\sqrt{85} - 9)^6 (16 - \sqrt{255})^2$$

$$\left(\frac{\sqrt{10 + \sqrt{51}}}{2} - \frac{1}{2} \sqrt{6 + \sqrt{51}} \right)^{12} \left(\frac{1}{2} \sqrt{22 + 3\sqrt{51}} - \frac{1}{2} \sqrt{18 + 2\sqrt{51}} \right)^{12}$$

Decimal approximation:

1.2513812697516692337121210310662441747073457071340161... × 10⁻²⁹

1.25138126... * 10⁻²⁹ this value tend to 0

$$1/((((\sqrt{765} (\sqrt{5}-2)^8 ((\sqrt{85}-9)/2)^6 (4-\sqrt{15})^6 (16-\sqrt{255})^2$$

$$((\sqrt{((22+3\sqrt{51})/4)}-\sqrt{((18+2\sqrt{51})/4)}))^12 (((\sqrt{((10+\sqrt{51})/4)}-\sqrt{((6+\sqrt{51})/4)}))^12))))$$

Input:

$$1/\left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9)\right)^6 (4 - \sqrt{15})^6$$

$$(16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})}\right)^{12}$$

$$\left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})}\right)^{12}\right)$$

Exact result:

$$64 / \left(3 \sqrt{85} (\sqrt{5} - 2)^8 (4 - \sqrt{15})^6 (\sqrt{85} - 9)^6 (16 - \sqrt{255})^2$$

$$\left(\frac{\sqrt{10 + \sqrt{51}}}{2} - \frac{1}{2} \sqrt{6 + \sqrt{51}} \right)^{12} \left(\frac{1}{2} \sqrt{22 + 3\sqrt{51}} - \frac{1}{2} \sqrt{18 + 2\sqrt{51}} \right)^{12} \right)$$

Decimal approximation:

7.9911696312862771855884885130292454321992734529379903... × 10²⁸

7.99116963... * 10²⁸ this value is a large number (tend to ∞)

$$2\ln(((1/((((\sqrt{765} (\sqrt{5}-2)^8 ((\sqrt{85}-9)/2)^6 (4-\sqrt{15})^6 (16-\sqrt{255})^2$$

$$((\sqrt{((22+3\sqrt{51})/4)}-\sqrt{((18+2\sqrt{51})/4)}))^12 (((\sqrt{((10+\sqrt{51})/4)}-\sqrt{((6+\sqrt{51})/4)}))^12))))))) - 5 - 2.618034$$

Input interpretation:

$$2 \log \left(1 / \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \right. \\ \left. \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right) \right)^{12} \right. \\ \left. \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \right) - 5 - 2.618034$$

$\log(x)$ is the natural logarithm

Result:

125.483405...

125.483405... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

Alternative representations:

$$2 \log \left(1 / \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \right. \\ \left. \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right) \right)^{12} \right. \\ \left. \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \right) - 5 - 2.61803 = \\ -7.61803 + 2 \log_e \left(1 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 \left(\frac{1}{2} (-9 + \sqrt{85}) \right)^6 \right. \right. \\ \left. \left. (16 - \sqrt{255})^2 \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right) \right)^{12} \right. \\ \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \sqrt{765} \right) \right)$$

$$\begin{aligned}
& 2 \log \left(1 / \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \right) - 5 - 2.61803 = \\
& -7.61803 + 2 \log(a) \log_a \left(1 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 \left(\frac{1}{2} (-9 + \sqrt{85}) \right)^6 \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \sqrt{765} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& 2 \log \left(1 / \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \right) - 5 - 2.61803 = \\
& -7.61803 - 2 \operatorname{Li}_1 \left(1 - 1 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 \left(\frac{1}{2} (-9 + \sqrt{85}) \right)^6 \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \sqrt{765} \right) \right)
\end{aligned}$$

Series representations:

$$\begin{aligned}
& 2 \log \left(1 / \left(\sqrt{765} (\sqrt{5} - 2) \right)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \\
& \quad \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \\
& \quad \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \Bigg) - 5 - 2.61803 = \\
& -7.61803 + 2 \log \left(-1 + 64 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right) \right) \Bigg) - \\
& 2 \sum_{k=1}^{\infty} \frac{1}{k} (-1)^k \left(-1 + 64 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 (16 - \sqrt{255})^2 \right. \right. \\
& \quad \left. \left. \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right) \right) \Bigg)^{-k}
\end{aligned}$$

$$\begin{aligned}
& 2 \log \left(1 / \left(\sqrt{765} (\sqrt{5} - 2) \right)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \\
& \quad \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \\
& \quad \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \Bigg) - 5 - 2.61803 = \\
& -7.61803 + 4i\pi \left[\frac{1}{2\pi} \arg \left(-x + 64 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 \right. \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right) \right) \Bigg] + 2 \log(x) - \\
& 2 \sum_{k=1}^{\infty} \frac{1}{k} (-1)^k x^{-k} \left(-x + 64 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 (16 - \sqrt{255})^2 \right. \right. \\
& \quad \left. \left. \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right) \right) \Bigg)^k \quad \text{for } x < 0
\end{aligned}$$

$$\begin{aligned}
& 2 \log \left(1 / \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \right) - 5 - 2.61803 = \\
& -7.61803 + 4i\pi \left[\frac{1}{2\pi} \left(\pi - \arg \left(64 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 \right. \right. \right. \right. \\
& \quad \left. \left. \left. (16 - \sqrt{255})^2 \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} z_0 \right) - \arg(z_0) \right) \right] + \\
& 2 \log(z_0) - 2 \sum_{k=1}^{\infty} \frac{1}{k} (-1)^k \left(64 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 (16 - \sqrt{255})^2 \right. \right. \\
& \quad \left. \left. \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right) - z_0 \right)^k z_0^{-k}
\end{aligned}$$

Integral representations:

$$\begin{aligned}
& 2 \log \left(1 / \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \right) - 5 - 2.61803 = -7.61803 + 2 \\
& \quad \frac{64}{\int_1^{\infty} \frac{1}{t} dt} \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 (16 - \sqrt{255})^2 \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \\
& \quad \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right)^{12}
\end{aligned}$$

$$\begin{aligned}
& 2 \log \left(1 / \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \right) - \\
& 5 - 2.61803 = -7.61803 + \frac{1}{i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{1}{\Gamma(1-s)} \Gamma(-s)^2 \Gamma(1+s) \\
& \quad \left(-1 + 64 / \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 (16 - \sqrt{255})^2 \right. \right. \\
& \quad \quad \left. \left. \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \\
& \quad \quad \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \right. \right. \right. \\
& \quad \quad \left. \left. \left. \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right) \right)^{-s} ds \text{ for } -1 < \gamma < 0
\end{aligned}$$

and:

$$\begin{aligned}
& (((1/((((\sqrt{765} (\sqrt{5}-2)^8 ((\sqrt{85}-9)/2)^6 (4-\sqrt{15})^6 (16-\sqrt{255})^2 \\
& ((\sqrt{((22+3\sqrt{51})/4)}-\sqrt{((18+2\sqrt{51})/4)}))^{12} (((\sqrt{((10+\sqrt{51})/4)})- \\
& \sqrt{((6+\sqrt{51})/4)}))^{12}))))))))^{1/16}
\end{aligned}$$

Input:

$$\begin{aligned}
& \left(1 / \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \right. \\
& \quad \left. \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \right. \\
& \quad \left. \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \right) \right)^{(1/16)}
\end{aligned}$$

Exact result:

$$\begin{aligned}
& 2^{3/8} / \left(\sqrt[16]{3} \sqrt[32]{85} \sqrt{\sqrt{5} - 2} \left((4 - \sqrt{15}) (\sqrt{85} - 9) \right)^{3/8} \sqrt[8]{16 - \sqrt{255}} \right. \\
& \quad \left. \left(\left(\frac{\sqrt{10 + \sqrt{51}}}{2} - \frac{1}{2} \sqrt{6 + \sqrt{51}} \right) \left(\frac{1}{2} \sqrt{22 + 3\sqrt{51}} - \frac{1}{2} \sqrt{18 + 2\sqrt{51}} \right) \right)^{3/4} \right)
\end{aligned}$$

Decimal approximation:

64.03437085018596448899062285621186164034559757349438166452...

64.03437085... \approx 64

Alternate forms:

$$(2 \times 2^{7/8}) / \left(\sqrt[16]{3} \sqrt[32]{85} \sqrt{\sqrt{5} - 2} (-36 + 9\sqrt{15} - 5\sqrt{51} + 4\sqrt{85})^{3/8} \sqrt[8]{16 - \sqrt{255}} \right. \\ \left. \left(\left(\sqrt{6 + \sqrt{51}} - \sqrt{10 + \sqrt{51}} \right) \left(\sqrt{2(9 + \sqrt{51})} - \sqrt{22 + 3\sqrt{51}} \right) \right)^{3/4} \right)$$

$$(4 \sqrt[4]{2}) / \left(\sqrt[16]{3} \sqrt[32]{85} \sqrt{\sqrt{5} - 2} \right. \\ \left. \left((4 - \sqrt{15})(\sqrt{85} - 9) \right)^{3/8} \sqrt[8]{16 - \sqrt{255}} \left(\left(\sqrt{6 + \sqrt{51}} - \sqrt{10 + \sqrt{51}} \right) \right. \right. \\ \left. \left. \left(\sqrt{18 - 2\sqrt{30}} + \sqrt{2} \left(-3\sqrt{\frac{3}{2}} - \sqrt{\frac{17}{2}} + \sqrt{9 + \sqrt{30}} \right) \right) \right)^{3/4} \right)$$

$$2 \left(\frac{1}{\left(\left(\left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{(\sqrt{85} - 9)}{2} \right)^6 (4 - \sqrt{15})^6 (16 - \sqrt{255})^2 \right. \right. \right. \right. \right. \right. \\ \left. \left. \left(\left(\sqrt{\frac{22 + 3\sqrt{51}}{4}} - \sqrt{\frac{18 + 2\sqrt{51}}{4}} \right) \right)^{12} \left(\left(\sqrt{\frac{10 + \sqrt{51}}{4}} - \sqrt{\frac{6 + \sqrt{51}}{4}} \right) \right)^{12} \right) \right) \right)^{1/16 - \pi + 0.618}$$

Input:

$$2 \left(\frac{1}{\left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \right. \right. \\ \left. \left. \left(16 - \sqrt{255} \right)^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \right. \\ \left. \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) \right) \right)^{(1/16) - \pi + 0.618}$$

Result:

125.54515...

125.54515... result very near to the dilaton mass calculated as a type of Higgs boson:
125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

$$\left(\left(\left(\sqrt{765} (\sqrt{5}-2)^8 \left(\frac{(\sqrt{85}-9)}{2} \right)^6 (4-\sqrt{15})^6 (16-\sqrt{255})^2 \right. \right. \right. \\ \left. \left. \left(\sqrt{\frac{(22+3\sqrt{51})}{4}} - \sqrt{\frac{(18+2\sqrt{51})}{4}} \right) \right)^{12} \left(\sqrt{\frac{(10+\sqrt{51})}{4}} - \sqrt{\frac{(6+\sqrt{51})}{4}} \right) \right)^{12} \right)^{1/4096}$$

Input:

$$\left(\sqrt{765} (\sqrt{5}-2)^8 \left(\frac{(\sqrt{85}-9)}{2} \right)^6 (4-\sqrt{15})^6 \right. \\ \left. (16-\sqrt{255})^2 \left(\sqrt{\frac{(22+3\sqrt{51})}{4}} - \sqrt{\frac{(18+2\sqrt{51})}{4}} \right) \right)^{12} \\ \left(\sqrt{\frac{(10+\sqrt{51})}{4}} - \sqrt{\frac{(6+\sqrt{51})}{4}} \right)^{12} \right)^{1/4096}$$

Exact result:

$$\frac{1}{2^{3/2048}} 4096 \sqrt{3}^{8192} \sqrt{85}^{512} \sqrt{\sqrt{5}-2} \left((4-\sqrt{15})(\sqrt{85}-9) \right)^{3/2048} 2048 \sqrt{16-\sqrt{255}} \\ \left(\left(\frac{\sqrt{10+\sqrt{51}}}{2} - \frac{1}{2} \sqrt{6+\sqrt{51}} \right) \left(\frac{1}{2} \sqrt{22+3\sqrt{51}} - \frac{1}{2} \sqrt{18+2\sqrt{51}} \right) \right)^{3/1024}$$

Decimal approximation:

0.983883548147829266478393436639226701986992577874056680881...

0.983883548... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

[log base 0.983883548((((sqrt765 (sqrt5-2)^8 ((sqrt85-9)/2)^6 (4-sqrt15)^6 (16-sqrt255)^2 ((sqrt(((22+3sqrt51)/4))-sqrt(((18+2sqrt51)/4))))))^12 (((sqrt(((10+sqrt51)/4))-sqrt((6+sqrt51)/4))))^12)))]

Input interpretation:

$$\log_{0.983883548} \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \\ \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \\ \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right)$$

$\log_b(x)$ is the base- b logarithm

Result:

4095.999962122277448960173118305862840676373851901832178996...

4095.99996212... \approx 4096

Alternative representation:

$$\log_{0.983884} \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \\ \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \\ \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) = \\ \frac{1}{\log(0.983884)} \log \left((-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 \left(\frac{1}{2} (-9 + \sqrt{85}) \right)^6 \right. \\ \left. (16 - \sqrt{255})^2 \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \\ \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \sqrt{765} \right)$$

Series representations:

$$\begin{aligned} & \log_{0.983884} \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \\ & \quad \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \\ & \quad \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) = \\ & - \frac{1}{\log(0.983884)} \left(\sum_{k=1}^{\infty} \frac{1}{k} (-1)^k \left(-1 + \frac{1}{64} (-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 \right. \right. \\ & \quad \left. \left. (16 - \sqrt{255})^2 \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \right. \\ & \quad \left. \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right)^k \right) \end{aligned}$$

$$\begin{aligned} & \log_{0.983884} \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \\ & \quad \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \\ & \quad \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) = \\ & -61.5484 \log \left(\frac{1}{64} (-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 (16 - \sqrt{255})^2 \right. \\ & \quad \left. \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \\ & \quad \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right) - \\ & \log \left(\frac{1}{64} (-2 + \sqrt{5})^8 (4 - \sqrt{15})^6 (-9 + \sqrt{85})^6 (16 - \sqrt{255})^2 \right. \\ & \quad \left. \sqrt{765} \left(-\sqrt{\frac{1}{4} (6 + \sqrt{51})} + \sqrt{\frac{1}{4} (10 + \sqrt{51})} \right)^{12} \right. \\ & \quad \left. \left(-\sqrt{\frac{1}{4} (18 + 2\sqrt{51})} + \sqrt{\frac{1}{4} (22 + 3\sqrt{51})} \right)^{12} \right) \sum_{k=0}^{\infty} (-0.0161165)^k G(k) \\ & \text{for } \left(G(0) = 0 \text{ and } \frac{(-1)^k k}{2(1+k)(2+k)} + G(k) = \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right) \end{aligned}$$

$$\begin{aligned}
& \log_{0.983884} \left(\sqrt{765} (\sqrt{5} - 2)^8 \left(\frac{1}{2} (\sqrt{85} - 9) \right)^6 (4 - \sqrt{15})^6 \right. \\
& \quad \left. (16 - \sqrt{255})^2 \left(\sqrt{\frac{1}{4} (22 + 3\sqrt{51})} - \sqrt{\frac{1}{4} (18 + 2\sqrt{51})} \right)^{12} \right. \\
& \quad \left. \left(\sqrt{\frac{1}{4} (10 + \sqrt{51})} - \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right)^{12} \right) = \\
& \log_{0.983884} \left(\frac{1}{64} \sqrt{764} \left(-2 + \sqrt{4} \sum_{k=0}^{\infty} 4^{-k} \binom{\frac{1}{2}}{k} \right)^8 \left(4 - \sqrt{14} \sum_{k=0}^{\infty} 14^{-k} \binom{\frac{1}{2}}{k} \right)^6 \right. \\
& \quad \left(-9 + \sqrt{84} \sum_{k=0}^{\infty} 84^{-k} \binom{\frac{1}{2}}{k} \right)^6 \left(16 - \sqrt{254} \sum_{k=0}^{\infty} 254^{-k} \binom{\frac{1}{2}}{k} \right)^2 \left(\sum_{k=0}^{\infty} 764^{-k} \binom{\frac{1}{2}}{k} \right) \\
& \quad \left(\sum_{k=0}^{\infty} 4^k \binom{\frac{1}{2}}{k} \left(-(2 + \sqrt{51})^{-k} \sqrt{\frac{1}{4} (2 + \sqrt{51})} + (6 + \sqrt{51})^{-k} \sqrt{\frac{1}{4} (6 + \sqrt{51})} \right) \right)^{12} \\
& \quad \left(\sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} \left(\left(\frac{4}{3} \right)^k (6 + \sqrt{51})^{-k} \sqrt{\frac{3}{4} (6 + \sqrt{51})} - \right. \right. \\
& \quad \quad \left. \left. 2^k (7 + \sqrt{51})^{-k} \sqrt{\frac{1}{2} (7 + \sqrt{51})} \right) \right)^{12} \Big)
\end{aligned}$$

Integral representations:

$$\log(z) = \int_1^z \frac{1}{t} dt$$

$$\log(1+z) = \frac{1}{2\pi i} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s+1)\Gamma(-s)^2}{\Gamma(1-s)z^s} ds \text{ for } (-1 < \gamma < 0 \text{ and } |\arg(z)| < \pi)$$

$$2*\sqrt{4095.99996212227}-\text{Pi}+1/\text{golden ratio}$$

Input interpretation:

$$2\sqrt{4095.99996212227} - \pi + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

125.476440743321...

125.476440743321... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

Series representations:

$$2\sqrt{4095.999962122270000} - \pi + \frac{1}{\phi} = \frac{1}{\phi} - \pi + 2\sqrt{4094.999962122270000} \sum_{k=0}^{\infty} e^{-8.317521987037418840k} \binom{\frac{1}{2}}{k}$$

$$2\sqrt{4095.999962122270000} - \pi + \frac{1}{\phi} = \frac{1}{\phi} - \pi + 2\sqrt{4094.999962122270000} \sum_{k=0}^{\infty} \frac{(-0.0002442002464590356536)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$2\sqrt{4095.999962122270000} - \pi + \frac{1}{\phi} = \frac{1}{\phi} - \pi + \frac{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} e^{-8.317521987037418840s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}}$$

$2*\text{sqrt}(4095.99996212227)+11+1/\text{golden ratio}$

Input interpretation:

$$2\sqrt{4095.99996212227} + 11 + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

139.618033396910...

139.61803339691... result practically equal to the rest mass of Pion meson 139.57 MeV

Series representations:

$$2\sqrt{4095.999962122270000} + 11 + \frac{1}{\phi} = 11 + \frac{1}{\phi} + 2\sqrt{4094.999962122270000} \sum_{k=0}^{\infty} e^{-8.317521987037418840k} \binom{\frac{1}{2}}{k}$$

$$2\sqrt{4095.999962122270000} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + 2\sqrt{4094.999962122270000} \sum_{k=0}^{\infty} \frac{(-0.0002442002464590356536)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$2\sqrt{4095.999962122270000} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} e^{-8.317521987037418840 s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}}$$

$$27 * \text{sqrt}(4095.99996212227) + 1$$

Input interpretation:

$$27\sqrt{4095.99996212227} + 1$$

Result:

1728.99999201017...

1728.99999201017... \approx 1729

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

From Wikipedia:

“The fundamental group of the complex form, compact real form, or any algebraic version of E_6 is the cyclic group $\mathbf{Z}/3\mathbf{Z}$, and its outer automorphism group is the cyclic group $\mathbf{Z}/2\mathbf{Z}$. Its fundamental representation is 27-dimensional (complex), and a basis is given by the 27 lines on a cubic surface. The dual representation, which is inequivalent, is also 27-dimensional. In particle physics, E_6 plays a role in some grand unified theories”.

We have that (page 330):

The image shows a handwritten mathematical derivation for the sum of reciprocals of squares. The formula is:
$$C + \frac{\pi}{3} \log x + \frac{1}{2x} - \frac{1}{4\pi x^2} + 2 \left(\frac{1}{e^{2\pi} - 1} \cdot \frac{1}{1-x} + \frac{2}{e^{4\pi} - 1} \cdot \frac{1}{4-x^2} + \dots \right)$$

$$+ \frac{\pi \cot \pi x}{e^{2\pi x} - 1} + \frac{4\pi \log(2 \sin \pi x)}{(e^{\pi x} - e^{-\pi x})^2} - 2\pi \left\{ \frac{\log(1-x^2)}{(e^{\pi} - e^{-\pi})^2} + \frac{\log(e^4 - x^2)}{(e^{2\pi} - e^{-2\pi})^2} + \dots \right\}$$

$$- 2\pi \sum_{n=1}^{\infty} e^{-2\pi n x} \left[\pi^2 \left\{ \frac{\sin 2\pi n x}{1+n^2} + \frac{\sin 4\pi n x}{2^2+n^2} + \dots \right\} \right.$$

$$\left. - \pi^3 \left\{ \frac{\cos 2\pi n x}{1(1+n^2)} + \frac{\cos 4\pi n x}{2(2^2+n^2)} + \dots \right\} \right]$$

$$= 1 + \frac{1}{4} + \frac{1}{9} + \dots + \frac{1}{x^2}$$

This image shows a partial view of the handwritten formula from the previous image, focusing on the first few terms:
$$C + \frac{\pi}{3} \log x + \frac{1}{2x} - \frac{1}{4\pi x^2} + 2 \left(\frac{1}{e^{2\pi} - 1} \cdot \frac{1}{1-x} + \frac{2}{e^{4\pi} - 1} \cdot \frac{1}{4-x^2} + \dots \right)$$

For $x = 1/2 = 0.5$ and $C = 3$

$$C + \frac{\pi}{3} \ln 0.5 + \frac{1}{2 \times 0.5} - \frac{1}{4\pi \times 0.5^2} + 2 \left(\left(\frac{1}{e^{2\pi} - 1} \right) \times \frac{1}{1 - 0.5^2} + \frac{2}{e^{4\pi} - 1} \times \frac{1}{4 - 0.5^2} \right)$$

Input:

$$3 + \frac{\pi}{3} \log(0.5) + \frac{1}{2 \times 0.5} - \frac{1}{4\pi \times 0.5^2} + 2 \left(\frac{1}{e^{2\pi} - 1} \times \frac{1}{1 - 0.5^2} + \frac{2}{e^{4\pi} - 1} \times \frac{1}{4 - 0.5^2} \right)$$

log(x) is the natural logarithm

Result:

2.96082...

2.96082...

Alternative representations:

$$3 + \frac{1}{3} \log(0.5) \pi + \frac{1}{2 \times 0.5} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(e^{2\pi}-1)} + \frac{2}{(4-0.5^2)(e^{4\pi}-1)} \right) =$$

$$3 + \frac{\pi \log_e(0.5)}{3} + \frac{1}{1} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(-1+e^{2\pi})} + \frac{2}{(4-0.5^2)(-1+e^{4\pi})} \right)$$

$$3 + \frac{1}{3} \log(0.5) \pi + \frac{1}{2 \times 0.5} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(e^{2\pi}-1)} + \frac{2}{(4-0.5^2)(e^{4\pi}-1)} \right) = 3 +$$

$$\frac{1}{3} \pi \log(a) \log_a(0.5) + \frac{1}{1} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(-1+e^{2\pi})} + \frac{2}{(4-0.5^2)(-1+e^{4\pi})} \right)$$

$$3 + \frac{1}{3} \log(0.5) \pi + \frac{1}{2 \times 0.5} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(e^{2\pi}-1)} + \frac{2}{(4-0.5^2)(e^{4\pi}-1)} \right) =$$

$$3 - \frac{\pi \text{Li}_1(0.5)}{3} + \frac{1}{1} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(-1+e^{2\pi})} + \frac{2}{(4-0.5^2)(-1+e^{4\pi})} \right)$$

Series representations:

$$3 + \frac{1}{3} \log(0.5) \pi + \frac{1}{2 \times 0.5} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(e^{2\pi}-1)} + \frac{2}{(4-0.5^2)(e^{4\pi}-1)} \right) =$$

$$4 + \frac{2.66667}{-1+e^{2\pi}} + \frac{1.06667}{-1+e^{4\pi}} - \frac{1}{\pi} - \frac{1}{3} \pi \sum_{k=1}^{\infty} \frac{(-1)^k (-0.5)^k}{k}$$

$$3 + \frac{1}{3} \log(0.5) \pi + \frac{1}{2 \times 0.5} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(e^{2\pi}-1)} + \frac{2}{(4-0.5^2)(e^{4\pi}-1)} \right) =$$

$$4 + \frac{2.66667}{-1+e^{2\pi}} + \frac{1.06667}{-1+e^{4\pi}} - \frac{1}{\pi} - \frac{1}{3} \pi \sum_{k=1}^{\infty} \frac{(-1)^k (-0.5)^k}{k}$$

$$3 + \frac{1}{3} \log(0.5) \pi + \frac{1}{2 \times 0.5} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(e^{2\pi}-1)} + \frac{2}{(4-0.5^2)(e^{4\pi}-1)} \right) =$$

$$4 + \frac{2.66667}{-1+e^{2\pi}} + \frac{1.06667}{-1+e^{4\pi}} - \frac{1}{\pi} + \frac{2}{3} i \pi^2 \left[\frac{\arg(0.5-x)}{2\pi} \right] +$$

$$\frac{1}{3} \pi \log(x) - \frac{1}{3} \pi \sum_{k=1}^{\infty} \frac{(-1)^k (0.5-x)^k x^{-k}}{k} \quad \text{for } x < 0$$

Integral representation:

$$3 + \frac{1}{3} \log(0.5) \pi + \frac{1}{2 \times 0.5} - \frac{1}{4 \pi 0.5^2} + 2 \left(\frac{1}{(1-0.5^2)(e^{2\pi}-1)} + \frac{2}{(4-0.5^2)(e^{4\pi}-1)} \right) =$$

$$4 + \frac{2.66667}{-1+e^{2\pi}} + \frac{1.06667}{-1+e^{4\pi}} - \frac{1}{\pi} + \frac{\pi}{3} \int_1^{0.5} \frac{1}{t} dt$$

$$+ \frac{\pi \cot \pi x}{e^{2\pi x} - 1} + \frac{2\pi \log(2 \sin \pi x)}{(e^{\pi x} - e^{-\pi x})^2} - 2\pi \left\{ \frac{\log(1-x^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16-x^4)}{(e^{2\pi} - e^{-2\pi})^2} \right\}$$

For $x = 1/2$

$$\pi \cot(\pi \cdot 0.5) / (e^{2\pi \cdot 0.5} - 1) + 2\pi \ln(2 \sin(\pi \cdot 0.5)) / (e^{\pi \cdot 0.5} - e^{-\pi \cdot 0.5})^2 - 2\pi \left(\frac{\ln(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\ln(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right)$$

Input:

$$\pi \times \frac{\cot(\pi \times 0.5)}{e^{2\pi \times 0.5} - 1} + 2\pi \times \frac{\log(2 \sin(\pi \times 0.5))}{(e^{\pi \times 0.5} - e^{-\pi \times 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right)$$

$\cot(x)$ is the cotangent function

$\log(x)$ is the natural logarithm

Result:

0.206288...

0.206288...

Alternative representations:

$$\frac{\pi \cot(\pi \cdot 0.5)}{e^{2\pi \cdot 0.5} - 1} + \frac{(2\pi) \log(2 \sin(\pi \cdot 0.5))}{(e^{\pi \cdot 0.5} - e^{-\pi \cdot 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right) =$$

$$\frac{\pi \left(i + \frac{2i}{-1 + e^{i\pi}} \right)}{-1 + e^\pi} + \frac{2\pi \log(2 \cos(0))}{(-e^{-0.5\pi} + e^{0.5\pi})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(-e^{-\pi} + e^\pi)^2} + \frac{\log(16 - 0.5^4)}{(-e^{-2\pi} + e^{2\pi})^2} \right)$$

$$\frac{\pi \cot(\pi \cdot 0.5)}{e^{2\pi \cdot 0.5} - 1} + \frac{(2\pi) \log(2 \sin(\pi \cdot 0.5))}{(e^{\pi \cdot 0.5} - e^{-\pi \cdot 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right) =$$

$$- \frac{i(\pi \coth((-0.5i)\pi))}{-1 + e^\pi} + \frac{2\pi \log(a) \log_a(2 \sin(0.5\pi))}{(-e^{-0.5\pi} + e^{0.5\pi})^2} - 2\pi \left(\frac{\log(a) \log_a(1 - 0.5^4)}{(-e^{-\pi} + e^\pi)^2} + \frac{\log(a) \log_a(16 - 0.5^4)}{(-e^{-2\pi} + e^{2\pi})^2} \right)$$

$$\begin{aligned} & \frac{\pi \cot(\pi 0.5)}{e^{2\pi 0.5} - 1} + \frac{(2\pi) \log(2 \sin(\pi 0.5))}{(e^{\pi 0.5} - e^{-\pi 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right) = \\ & \frac{\pi \left(i + \frac{2i}{-1 + e^\pi} \right)}{-1 + e^\pi} + \frac{2\pi \log(a) \log_a(2 \sin(0.5\pi))}{(-e^{-0.5\pi} + e^{0.5\pi})^2} - \\ & 2\pi \left(\frac{\log(a) \log_a(1 - 0.5^4)}{(-e^{-\pi} + e^\pi)^2} + \frac{\log(a) \log_a(16 - 0.5^4)}{(-e^{-2\pi} + e^{2\pi})^2} \right) \end{aligned}$$

Integral representations:

$$\begin{aligned} & \frac{\pi \cot(\pi 0.5)}{e^{2\pi 0.5} - 1} + \frac{(2\pi) \log(2 \sin(\pi 0.5))}{(e^{\pi 0.5} - e^{-\pi 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right) = \\ & - \frac{\pi}{-1 + e^\pi} \int_{\frac{\pi}{2}}^{0.5\pi} \csc^2(t) dt - \frac{2\pi \log(0.9375)}{(-e^{-\pi} + e^\pi)^2} - \\ & \frac{2\pi \log(15.9375)}{(-e^{-2\pi} + e^{2\pi})^2} + \frac{2\pi \log(\pi \int_0^1 \cos(0.5\pi t) dt)}{(-e^{-0.5\pi} + e^{0.5\pi})^2} \end{aligned}$$

$$\begin{aligned} & \frac{\pi \cot(\pi 0.5)}{e^{2\pi 0.5} - 1} + \frac{(2\pi) \log(2 \sin(\pi 0.5))}{(e^{\pi 0.5} - e^{-\pi 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right) = \\ & - \frac{\pi}{-1 + e^\pi} \int_{\frac{\pi}{2}}^{0.5\pi} \csc^2(t) dt - \frac{2\pi \log(0.9375)}{(-e^{-\pi} + e^\pi)^2} - \frac{2\pi \log(15.9375)}{(-e^{-2\pi} + e^{2\pi})^2} + \\ & \frac{2\pi \log\left(\frac{0.25\sqrt{\pi}}{i} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\mathcal{A}^{-(0.0625\pi^2)/s+s}}{s^{3/2}} ds\right)}{(-e^{-0.5\pi} + e^{0.5\pi})^2} \quad \text{for } \gamma > 0 \end{aligned}$$

$$\begin{aligned} & \frac{\pi \cot(\pi 0.5)}{e^{2\pi 0.5} - 1} + \frac{(2\pi) \log(2 \sin(\pi 0.5))}{(e^{\pi 0.5} - e^{-\pi 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right) = \\ & - \frac{\pi}{-1 + e^\pi} \int_{\frac{\pi}{2}}^{0.5\pi} \csc^2(t) dt - \frac{2\pi \log(0.9375)}{(-e^{-\pi} + e^\pi)^2} - \frac{2\pi \log(15.9375)}{(-e^{-2\pi} + e^{2\pi})^2} + \\ & \frac{2\pi \log\left(\frac{\sqrt{\pi}}{i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{0.25 e^{2.77259s} \pi^{1-2s} \Gamma(s)}{\Gamma\left(\frac{3}{2}-s\right)} ds\right)}{(-e^{-0.5\pi} + e^{0.5\pi})^2} \quad \text{for } 0 < \gamma < 1 \end{aligned}$$

Multiple-argument formulas:

$$\begin{aligned} & \frac{\pi \cot(\pi 0.5)}{e^{2\pi 0.5} - 1} + \frac{(2\pi) \log(2 \sin(\pi 0.5))}{(e^{\pi 0.5} - e^{-\pi 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right) = \\ & - 2\pi \left(\frac{\log(0.9375)}{(-e^{-\pi} + e^\pi)^2} + \frac{\log(15.9375)}{(-e^{-2\pi} + e^{2\pi})^2} \right) + \\ & \frac{2\pi (\log(2) + \log(\sin(0.5\pi)))}{(-e^{-0.5\pi} + e^{0.5\pi})^2} + \frac{\pi (\cot(0.25\pi) - \tan(0.25\pi))}{2(-1 + e^\pi)} \end{aligned}$$

$$\frac{\pi \cot(\pi 0.5)}{e^{2\pi 0.5} - 1} + \frac{(2\pi) \log(2 \sin(\pi 0.5))}{(e^{\pi 0.5} - e^{-\pi 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right) =$$

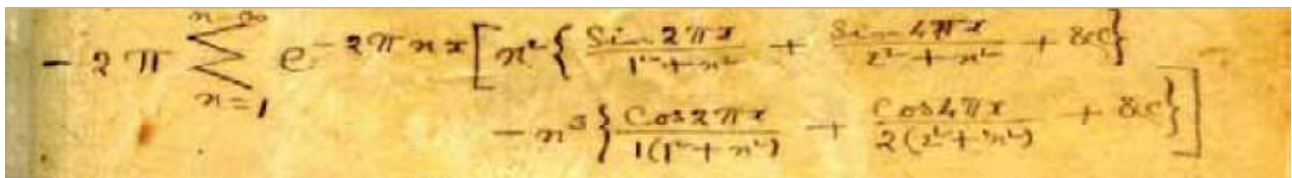
$$\frac{\pi(-3 \cot(0.166667\pi) + \cot^3(0.166667\pi))}{(-1 + e^\pi)(-1 + 3 \cot^2(0.166667\pi))} -$$

$$2\pi \left(\frac{\log(0.9375)}{(-e^{-\pi} + e^\pi)^2} + \frac{\log(15.9375)}{(-e^{-2\pi} + e^{2\pi})^2} \right) + \frac{2\pi(\log(2) + \log(\sin(0.5\pi)))}{(-e^{-0.5\pi} + e^{0.5\pi})^2}$$

$$\frac{\pi \cot(\pi 0.5)}{e^{2\pi 0.5} - 1} + \frac{(2\pi) \log(2 \sin(\pi 0.5))}{(e^{\pi 0.5} - e^{-\pi 0.5})^2} - 2\pi \left(\frac{\log(1 - 0.5^4)}{(e^\pi - e^{-\pi})^2} + \frac{\log(16 - 0.5^4)}{(e^{2\pi} - e^{-2\pi})^2} \right) =$$

$$\frac{\pi(-1 + \cot(-0.5\pi) \cot(\pi))}{(-1 + e^\pi)(\cot(-0.5\pi) + \cot(\pi))} -$$

$$2\pi \left(\frac{\log(0.9375)}{(-e^{-\pi} + e^\pi)^2} + \frac{\log(15.9375)}{(-e^{-2\pi} + e^{2\pi})^2} \right) + \frac{2\pi(\log(2) + \log(\sin(0.5\pi)))}{(-e^{-0.5\pi} + e^{0.5\pi})^2}$$



For $x = 1/2$ and $n = 2$

$$-2\pi \cdot (e^{(-2\pi \cdot 2 \cdot 0.5)}) \cdot (2^2 \cdot (\sin(2\pi \cdot 1/2)/(1+4) + \sin(4\pi \cdot 0.5)/(4+4)) - 8 \cdot (((\cos(2\pi \cdot 0.5)/(1(1+4))) + (((\cos(4\pi \cdot 0.5)/(2(4+4))))))))))$$

Input:

$$-2\pi e^{-2\pi \cdot 2 \cdot 0.5} \left(2^2 \left(\frac{\sin\left(2\pi \times \frac{1}{2}\right)}{1+4} + \frac{\sin(4\pi \times 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi \times 0.5)}{1(1+4)} + \frac{\cos(4\pi \times 0.5)}{2(4+4)} \right) \right) \right)$$

Result:

-0.0516274...

-0.05162735042901456149533991271596422600729620248329024148...

-0.0516273504...

Alternative representations:

$$-2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi \cdot 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi \cdot 0.5)}{1(1+4)} + \frac{\cos(4\pi \cdot 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi \cdot 2 \cdot 0.5} =$$

$$-8\pi \left(\frac{1}{5} \cos\left(-\frac{\pi}{2}\right) + \frac{1}{8} \cos(-1.5\pi) - 8 \left(\frac{1}{5} \cosh(i\pi) + \frac{1}{16} \cosh(2i\pi) \right) \right) e^{-2\pi}$$

$$-2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi 0.5)}{1(1+4)} + \frac{\cos(4\pi 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi 2 \times 0.5} =$$

$$-8\pi \left(\frac{1}{5} \cos\left(-\frac{\pi}{2}\right) + \frac{1}{8} \cos(-1.5\pi) - 8 \left(\frac{1}{5} \cosh(-i\pi) + \frac{1}{16} \cosh((-2i)\pi) \right) \right) e^{-2\pi}$$

$$-2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi 0.5)}{1(1+4)} + \frac{\cos(4\pi 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi 2 \times 0.5} =$$

$$-8\pi \left(-\frac{1}{5} \cos\left(\frac{3\pi}{2}\right) - \frac{1}{8} \cos(2.5\pi) - 8 \left(\frac{1}{5} \cosh(-i\pi) + \frac{1}{16} \cosh((-2i)\pi) \right) \right) e^{-2\pi}$$

Series representations:

$$-2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi 0.5)}{1(1+4)} + \frac{\cos(4\pi 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi 2 \times 0.5} =$$

$$\sum_{k=0}^{\infty} \frac{(-1)^k e^{-2\pi} \pi^{1+2k} \left((-1.6 - 2e^{1.38629k}) \pi (2k)! + (12.8 + 4e^{1.38629k}) (1+2k)! \right)}{(2k)! (1+2k)!}$$

$$-2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi 0.5)}{1(1+4)} + \frac{\cos(4\pi 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi 2 \times 0.5} =$$

$$\sum_{k=0}^{\infty} \frac{(-1)^k e^{-2\pi} \pi \left((12.8 + 4e^{1.38629k}) \pi^{2k} - 3.2 J_{1+2k}(\pi) (2k)! - 2 J_{1+2k}(2\pi) (2k)! \right)}{(2k)!}$$

$$-2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi 0.5)}{1(1+4)} + \frac{\cos(4\pi 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi 2 \times 0.5} =$$

$$\sum_{k=0}^{\infty} \frac{1}{5k!} 2 e^{-2\pi} \pi$$

$$\left((-1)^{1+k} (8 J_{1+2k}(\pi) + 5 J_{1+2k}(2\pi)) k! + 2 \cos\left(\frac{k\pi}{2} + z_0\right) \left(16 (\pi - z_0)^k + 5 (2\pi - z_0)^k \right) \right)$$

Integral representations:

$$-2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi 0.5)}{1(1+4)} + \frac{\cos(4\pi 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi 2 \times 0.5} =$$

$$16.8 e^{-2\pi} \pi + \int_0^1 e^{-2\pi} \pi^2 (-1.6 \cos(\pi t) - 2 \cos(2\pi t) - 12.8 \sin(\pi t) - 8 \sin(2\pi t)) dt$$

$$\begin{aligned}
& -2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi \cdot 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi \cdot 0.5)}{1(1+4)} + \frac{\cos(4\pi \cdot 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi \cdot 2 \times 0.5} = \\
& \int_{\frac{\pi}{2}}^{2\pi} e^{-2\pi} \pi (-1.06667 \cos(0 - 0.333333 \pi + 0.666667 t) - \\
& \quad 1.33333 \cos(0 - 0.666667 \pi + 1.33333 t) - \\
& \quad 4.26667 \sin(0 + 0.333333 \pi + 0.333333 t) - 4 \sin(t)) dt
\end{aligned}$$

$$\begin{aligned}
& -2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi \cdot 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi \cdot 0.5)}{1(1+4)} + \frac{\cos(4\pi \cdot 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi \cdot 2 \times 0.5} = \\
& \int_0^1 e^{-2\pi} \pi^2 (-1.6 \cos(\pi t) - 2 \cos(2\pi t)) dt + \\
& \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{e^{-2\pi} \mathcal{A}^{-(1.25\pi^2)/s+s} \left(2 \mathcal{A}^{(0.25\pi^2)/s} + 6.4 \mathcal{A}^{\pi^2/s} \right) \sqrt{\pi}}{i\sqrt{s}} ds \text{ for } \gamma > 0
\end{aligned}$$

Multiple-argument formulas:

$$\begin{aligned}
& -2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi \cdot 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi \cdot 0.5)}{1(1+4)} + \frac{\cos(4\pi \cdot 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi \cdot 2 \times 0.5} = \\
& \frac{1}{5} e^{-2\pi} \pi (-84 + 128 \cos^2(0.5\pi) + 40 \cos^2(\pi) - 8 \sin(\pi) - 5 U_1(\cos(\pi)) \sin(\pi))
\end{aligned}$$

$$\begin{aligned}
& -2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi \cdot 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi \cdot 0.5)}{1(1+4)} + \frac{\cos(4\pi \cdot 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi \cdot 2 \times 0.5} = \\
& \frac{2}{5} e^{-2\pi} \pi \left(-42 + 64 \cos^2(0.5\pi) + 20 \cos^2(\pi) - 8 \cos\left(\frac{\pi}{2}\right) \sin\left(\frac{\pi}{2}\right) - 5 \cos(\pi) \sin(\pi) \right)
\end{aligned}$$

$$\begin{aligned}
& -2 \times 2^2 \left(\frac{\sin\left(\frac{2\pi}{2}\right)}{1+4} + \frac{\sin(4\pi \cdot 0.5)}{4+4} - 8 \left(\frac{\cos(2\pi \cdot 0.5)}{1(1+4)} + \frac{\cos(4\pi \cdot 0.5)}{2(4+4)} \right) \right) \pi e^{-2\pi \cdot 2 \times 0.5} = \\
& -\frac{2}{5} e^{-2\pi} \pi \left(-42 + 64 \sin^2(0.5\pi) + 8 \cos\left(\frac{\pi}{2}\right) \sin\left(\frac{\pi}{2}\right) + 5 \cos(\pi) \sin(\pi) + 20 \sin^2(\pi) \right)
\end{aligned}$$

Thence, we obtain:

$$(2.96082096782292266455507130109+0.20628814922463399289199102-0.051627350429014561495339)$$

Input interpretation:

$$2.96082096782292266455507130109 + 0.20628814922463399289199102 - 0.051627350429014561495339$$

Result:

$$3.11548176661854209595172332109$$

3.1154817666....

$$1+1/((1/2(2.960820967822+0.206288149224-0.051627350429)))$$

Input interpretation:

$$1 + \frac{1}{\frac{1}{2}(2.960820967822 + 0.206288149224 - 0.051627350429)}$$

Result:

$$1.641955289685978404876901251679786569392353711077671497521...$$

$$1.64195528... \approx \zeta(2) = \frac{\pi^2}{6} = 1.644934 ...$$

$$1/2(((2.960820967822+0.206288149224-0.051627350429)))^5-7$$

Input interpretation:

$$\frac{1}{2} (2.960820967822 + 0.206288149224 - 0.051627350429)^5 - 7$$

Result:

$$139.7560701878362354517579208507929104665428556881136454226...$$

139.75607018... result practically equal to the rest mass of Pion meson 139.57 MeV

$$1/2(((2.960820967822+0.206288149224-0.051627350429)))^5-21$$

Input interpretation:

$$\frac{1}{2} (2.960820967822 + 0.206288149224 - 0.051627350429)^5 - 21$$

Result:

125.7560701878362354517579208507929104665428556881136454226...

125.75607018... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

$$27 * 1/2((1/2(((2.960820967822+0.206288149224-0.051627350429)))^5-18))-8-1/\text{golden ratio}$$

Input interpretation:

$$27 \times \frac{1}{2} \left(\frac{1}{2} (2.960820967822 + 0.206288149224 - 0.051627350429)^5 - 18 \right) - 8 - \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

1729.58891355...

1729.58891355...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Alternative representations:

$$\frac{27}{2} \left(\frac{1}{2} (2.9608209678220000 + 0.2062881492240000 - 0.0516273504290000)^5 - 18 \right) - 8 - \frac{1}{\phi} = -8 + \frac{27}{2} \left(-18 + \frac{3.115481766617000^5}{2} \right) - \frac{1}{2 \sin(54^\circ)}$$

Now, we have that (page 331):

$$\sqrt{505} (\sqrt{5}-2)^{14} (\sqrt{101}-10)^6 \left(\frac{5\sqrt{5} + \sqrt{101}}{4} \pm \sqrt{\frac{105 + 5\sqrt{505}}{8}} \right)^{12}$$

$$\sqrt{505} (\sqrt{5}-2)^{14} (\sqrt{101}-10)^6$$

$$\left(\left(\left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{1}{8} (105 + 5\sqrt{505})} \right) \right) \right)^{12}$$

Input:

$$\sqrt{505} (\sqrt{5}-2)^{14} (\sqrt{101}-10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{1}{8} (105 + 5\sqrt{505})} \right)^{12}$$

Result:

$$\sqrt{505} (\sqrt{5}-2)^{14} (\sqrt{101}-10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{105}{8} + 5\sqrt{505}} \right)^{12}$$

Decimal approximation:

0.236775064412460098799348383170800838574530236659763229772...

0.23677506...

Alternate forms:

$$\frac{1}{16777216} \left(218643557581264400 - 97780371518819340\sqrt{5} - 21755847119317740\sqrt{101} + 9729510613377489\sqrt{505} \right)$$

$$\left(\sqrt{10(21+8\sqrt{505})} + 5\sqrt{5} + \sqrt{101} \right)^{12}$$

$$\frac{\sqrt{505} (\sqrt{5}-2)^{14} (\sqrt{101}-10)^6 \left(5\sqrt{5} + \sqrt{101} + \sqrt{10(21+8\sqrt{505})} \right)^{12}}{16777216}$$

$$\frac{1}{16777216} \sqrt{505} (\sqrt{5}-2)^{14} (\sqrt{101}-10)^6$$

$$\left(5\sqrt{5} + \sqrt{101} + \sqrt{105 - 5i\sqrt{31879}} + \sqrt{5i(\sqrt{31879} - 21i)} \right)^{12}$$

$$7 * (((\sqrt{505} (\sqrt{5}-2)^{14} (\sqrt{101}-10)^6 \\ (((1/4*(5\sqrt{5}+\sqrt{101})+\sqrt{(1/8*105+5\sqrt{505}}))))^12))))))$$

Input:

$$7 \left(\sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{1}{8} \times 105 + 5\sqrt{505}} \right)^{12} \right)$$

Result:

$$7 \sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{105}{8} + 5\sqrt{505}} \right)^{12}$$

Decimal approximation:

1.657425450887220691595438682195605870021711656618342608407...

1.657425450887... result very near to the 14th root of the following Ramanujan's class invariant $Q = (G_{505}/G_{101/5})^3 = 1164,2696$ i.e. 1,65578...

Alternate forms:

$$\frac{1}{16\,777\,216} \left(218\,643\,557\,581\,264\,400 - 97\,780\,371\,518\,819\,340 \sqrt{5} - \right. \\ \left. 21\,755\,847\,119\,317\,740 \sqrt{101} + 9\,729\,510\,613\,377\,489 \sqrt{505} \right) \\ \left(\sqrt{10(21 + 8\sqrt{505})} + 5\sqrt{5} + \sqrt{101} \right)^{12} \cdot 7 \\ \frac{7\sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(5\sqrt{5} + \sqrt{101} + \sqrt{10(21 + 8\sqrt{505})} \right)^{12}}{16\,777\,216} \\ \frac{1}{16\,777\,216} 7\sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \\ \left(5\sqrt{5} + \sqrt{101} + \sqrt{105 - 5i\sqrt{31879}} + \sqrt{5i(\sqrt{31879} - 21i)} \right)^{12}$$

$$729 * (((\sqrt{505} (\sqrt{5}-2)^{14} (\sqrt{101}-10)^6 \\ (((1/4*(5\sqrt{5}+\sqrt{101})+\sqrt{(1/8*105+5\sqrt{505}}))))^12))))))$$

Where $729 = 9^3$ (see Ramanujan cubes)

Input:

$$729 \left(\sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{1}{8} \times 105 + 5\sqrt{505}} \right)^{12} \right)$$

Result:

$$729 \sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{105}{8} + 5\sqrt{505}} \right)^{12}$$

Decimal approximation:

172.6090219566834120247249713315138113208325425249673945041...

172.60902195... \approx 172 (Ramanujan taxicab number)

Alternate forms:

$$\frac{1}{16777216} \left(218643557581264400 - 97780371518819340\sqrt{5} - 21755847119317740\sqrt{101} + 9729510613377489\sqrt{505} \right)$$

$$\left(\sqrt{10(21 + 8\sqrt{505})} + 5\sqrt{5} + \sqrt{101} \right)^{12} 729$$

$$\frac{729 \sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(5\sqrt{5} + \sqrt{101} + \sqrt{10(21 + 8\sqrt{505})} \right)^{12}}{16777216}$$

$$\frac{1}{16777216} 729 \sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(5\sqrt{5} + \sqrt{101} + \sqrt{105 - 5i\sqrt{31879}} + \sqrt{5i(\sqrt{31879} - 21i)} \right)^{12}$$

$((729 * (((\sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6$
 $((\frac{1}{4} * (5\sqrt{5} + \sqrt{101}) + \sqrt{(\frac{1}{8} * 105 + 5\sqrt{505})}))))^{12})))) - 34 + \frac{1}{\phi}))$

Input:

$$729 \left(\sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{1}{8} \times 105 + 5\sqrt{505}} \right)^{12} \right) - 34 + \frac{1}{\phi}$$

ϕ is the golden ratio

Exact result:

$$\frac{1}{\phi} - 34 + 729 \sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{105}{8} + 5\sqrt{505}} \right)^{12}$$

Decimal approximation:

139.2270559454333068729295581658794494385528517047731573662...

139.227055945... result practically equal to the rest mass of Pion meson 139.57 MeV

$$(((729 * (((\sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 ((1/4 * (5\sqrt{5} + \sqrt{101}) + \sqrt{(1/8 * 105 + 5\sqrt{505}))))))^{12})))) - 47 - 2 + \text{golden ratio}))$$

Input:

$$729 \left(\sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{1}{8} \times 105 + 5\sqrt{505}} \right)^{12} \right) - 47 - 2 + \phi$$

ϕ is the golden ratio

Exact result:

$$\frac{1}{\phi} - 49 + 729 \sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{105}{8} + 5\sqrt{505}} \right)^{12}$$

Decimal approximation:

125.2270559454333068729295581658794494385528517047731573662...

125.227055945... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

$1/2*27*(((729*(((\sqrt{505}(\sqrt{5}-2)^{14}(\sqrt{101}-10)^6$
 $((1/4*(5\sqrt{5}+\sqrt{101})+\sqrt{(1/8*105+5\sqrt{505}))))^12))))-47+\text{golden}$
 $\text{ratio}^2))))-2$

Input:

$$\frac{1}{2} \times 27 \left(729 \left(\sqrt{505} (\sqrt{5} - 2)^{14} (\sqrt{101} - 10)^6 \right. \right. \\ \left. \left. \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{1}{8} \times 105 + 5\sqrt{505}} \right)^{12} \right) - 47 + \phi^2 \right) - 2$$

ϕ is the golden ratio

Exact result:

$$\frac{27}{2} \left(\phi^2 - 47 + 729 \sqrt{505} (\sqrt{5} - 2)^{14} \right. \\ \left. (\sqrt{101} - 10)^6 \left(\frac{1}{4} (5\sqrt{5} + \sqrt{101}) + \sqrt{\frac{105}{8} + 5\sqrt{505}} \right)^{12} \right) - 2$$

Decimal approximation:

1729.065255263349642784549035239372567420463498014437624444...

1729.06525526.....

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Conclusions

Note that:

$$g_{22} = \sqrt{(1 + \sqrt{2})}.$$

Hence

$$\begin{aligned} 64g_{22}^{24} &= e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} - \dots, \\ 64g_{22}^{-24} &= 4096e^{-\pi\sqrt{22}} + \dots, \end{aligned}$$

so that

$$64(g_{22}^{24} + g_{22}^{-24}) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots = 64\{(1 + \sqrt{2})^{12} + (1 - \sqrt{2})^{12}\}.$$

Hence

$$e^{\pi\sqrt{22}} = 2508951.9982\dots$$

Thence:

$$64g_{22}^{-24} = 4096e^{-\pi\sqrt{22}} + \dots$$

And

$$64(g_{22}^{24} + g_{22}^{-24}) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots = 64\{(1 + \sqrt{2})^{12} + (1 - \sqrt{2})^{12}\}$$

That are connected with 64, 128, 256, 512, 1024 and $4096 = 64^2$

(Modular equations and approximations to π - S. Ramanujan - Quarterly Journal of Mathematics, XLV, 1914, 350 – 372)

All the results of the most important connections are signed in blue throughout the drafting of the paper. We highlight as in the development of the various equations we use always the constants π , ϕ , $1/\phi$, the Fibonacci and Lucas numbers, linked to the golden ratio, that play a fundamental role in the development, and therefore, in the final results of the analyzed expressions.

“For this reason Ramanujan elaborated a theory of reality around Zero (representing absolute Reality) and Infinity (the manifold manifestations of that reality): their mathematical product represented all the numbers, each of which corresponded to individual acts of creation. For him, "the numbers and their mathematical ratios let us understand how everything was in harmony in the universe".”

(<https://www.cittanuova.it/ramanujanhardy-e-il-piacere-di-scoprire/?ms=006&se=007>)

References

Dark Spinors Hawking Radiation in String Theory Black Holes

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