

On some Ramanujan equations concerning the continued fractions. Further possible mathematical connections with some parameters of Particle Physics and Cosmology V.

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Abstract

In this research thesis, we have analyzed and deepened some equations concerning the Ramanujan continued fractions. Further possible mathematical connections with some parameters of Particle Physics and Cosmology.

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 If we consider a function $\phi(y)$ (1)
 the transformable $\phi(y) = \sum_{n=0}^{\infty} a_n y^n$
 (A) $1 + \frac{y}{(1-y)^2} + \frac{y^2}{(1-y)^2(1-y^2)} + \frac{y^3}{(1-y)^2(1-y^2)^2}$
 (B) $1 + \frac{y}{1-y} + \frac{y^2}{(1-y)^2(1-y^2)} + \frac{y^3}{(1-y)^2(1-y^2)^2}$
 and consider determine the values of
 the singularities at the points $y=1$,
 $y=-1$, $y=i$, $y=-i$, ... We know how
 beautifully the asymptotic nature
 form of the function can be expressed
 in a neat and closed form as-
 follows when $y = e^{-t}$ and $t \rightarrow 0$
 (A) $= \sqrt{\frac{t}{2\pi}} e^{\frac{t}{2\pi} - \frac{t^2}{24}}$
 (B) $= \frac{e^{\frac{t}{2\pi} - \frac{t^2}{24}}}{\sqrt{2\pi t}} + o(1)$
 and similar results at other points
 - singularities. It is not necessary that
 there should be only one term but this
 may be many terms but the sum
 of them must be finite. Also $o(1)$
 means term out to be $O(1)$. That is all.
 In fact when $y \rightarrow 1$ the function
 $\frac{1}{(1-y)^2(1-y^2)} \sim \frac{1}{2(1-y)^3}$
 this is equivalent to the sum of five
 terms $O(1)$ together with $O(1)$ in-
 stead of $o(1)$.
 If we take a number of functions
 like (A) and (B) it is only in a limited
 number of cases the terms close as
 above; but in the majority of cases they
 never close as above. For instance,
 when $y = e^{-t}$ and $t \rightarrow 0$
 (C) $1 + \frac{y}{(1-y)^2} + \frac{y^2}{(1-y)^2(1-y^2)} + \frac{y^3}{(1-y)^2(1-y^2)^2}$
 $= \sqrt{\frac{t}{2\pi}} e^{\frac{t}{2\pi} + a_1 t + a_2 t^2 + \dots} + o(1)$
 where $a_1 = \frac{1}{24}$, and so on.



<https://news.cnrs.fr/articles/ramanujan-the-man-who-knew-infinity>

From:

<https://www.youtube.com/watch?v=IBWCm34QmjQ&t=1749s>

“17Aug18 Professor George E. Andrews – Ramanujan: The Man, The Movie and the Mathematics”

$$\begin{aligned} & \frac{1}{1+q} - \frac{q^2(1-q)}{(1+q)(1+q^2)(1+q^3)} + \frac{q^6(1-q)(1-q^3)}{(1+q)(1+q^2)\dots(1+q^5)} + \dots \\ & = 1 - q + q^3 - q^6 + q^{10} - q^{15} + \dots := F(q) \\ & \frac{1}{1+q} + \frac{q(1-q)^2}{(1+q)(1+q^2)(1+q^3)} + \frac{q^2(1-q)^2(1-q^3)^2}{(1+q)(1+q^2)\dots(1+q^5)} + \dots \\ & = F(q^2) \\ & \frac{1}{1+q} + \frac{q(1-q)}{(1+q)(1+q^2)(1+q^3)} + \frac{q^2(1-q)(1-q^3)}{(1+q)(1+q^2)\dots(1+q^5)} + \dots \\ & = F(q^3) \\ & \frac{1}{1+q} + \frac{q(1-q)}{(1+q)(1+q^3)} + \frac{q^2(1-q)(1-q^3)}{(1+q)(1+q^3)(1+q^5)} + \dots \\ & = F(q^4) \\ & \frac{1}{1+q} + \frac{q(1-q)}{(1+q)(1+q^3)} + \frac{q^2(1-q)(1+q^2)}{(1+q)(1+q^3)(1+q^5)} + \dots \\ & = F(q^6) \end{aligned}$$

George E. Andrews Ramanujan: The Man, The Movie, and the Mathematics

For $q = e^{-2\pi i \tau}$ where $i\tau > 0$; $i\tau = 1$; $q = 0.0018674427317\dots \approx 0.00186744\dots$

(a)

$$\begin{aligned} & \frac{1}{1+q} - \frac{q^2(1-q)}{(1+q)(1+q^2)(1+q^3)} + \frac{q^6(1-q)(1-q^3)}{(1+q)(1+q^2)\dots(1+q^5)} + \dots \\ & = 1 - q + q^3 - q^6 + q^{10} - q^{15} + \dots := F(q) \end{aligned}$$

(b)

$$\frac{1}{1+q} + \frac{q(1-q)^2}{(1+q)(1+q^2)(1+q^3)} + \frac{q^2(1-q)^2(1-q^3)^2}{(1+q)(1+q^2)\dots(1+q^5)} + \dots$$
$$= F(q^2)$$

(c)

$$\frac{1}{1+q} + \frac{q(1-q)}{(1+q)(1+q^2)(1+q^3)} + \frac{q^2(1-q)(1-q^3)}{(1+q)(1+q^2)\dots(1+q^5)} + \dots$$
$$= F(q^3)$$

(d)

$$\frac{1}{1+q} + \frac{q(1-q)}{(1+q)(1+q^3)} + \frac{q^2(1-q)(1-q^3)}{(1+q)(1+q^3)(1+q^5)} + \dots$$
$$= F(q^4)$$

(e)

$$\frac{1}{1+q} + \frac{q(1-q)}{(1+q)(1+q^3)} + \frac{q^2(1-q)(1+q^2)}{(1+q)(1+q^3)(1+q^5)} + \dots$$
$$= F(q^6)$$

From (a)

$$\frac{1}{1+q} - \frac{q^2(1-q)}{(1+q)(1+q^2)(1+q^3)} + \frac{q^6(1-q)(1-q^3)}{(1+q)(1+q^2)\dots(1+q^5)} + \dots$$

$$= 1 - q + q^3 - q^6 + q^{10} - q^{15} + \dots := F(q)$$

we obtain, for $q = 0.00186744$:

$$1/(1+0.00186744) - (((0.00186744^2)(1-0.00186744))/(((1+0.00186744)(1+0.00186744^2)(1+0.00186744^3))))$$

Input interpretation:

$$\frac{1}{1+0.00186744} - \frac{0.00186744^2(1-0.00186744)}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)}$$

Result:

0.998132566512383472254757981308636609823513562654449979220...

0.9981325...

Partial Result

$$(((0.00186744^6(1-0.00186744)(1-0.00186744^3))))/$$

$$(((1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)(1+0.00186744^4)(1+0.00186744^5))))$$

Input interpretation:

$$\frac{(0.00186744^6(1-0.00186744)(1-0.00186744^3))}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)(1+0.00186744^4)(1+0.00186744^5)}$$

Result:

4.2252886426780994880386059804784711267113625543227267... $\times 10^{-17}$

4.225288642... $\times 10^{-17}$ Partial result

Thence:

Input interpretation:

$$\frac{1}{1 + 0.00186744} - \frac{0.00186744^2 (1 - 0.00186744)}{(1 + 0.00186744)(1 + 0.00186744^2)(1 + 0.00186744^3) + \dots} + 4.2252886426780994880386059804784711267113625543227267 \times 10^{-17}$$

Result:

0.998132566512383514507644408089631490209573367439161246333...

0.99813256651238... Final Result

This result is practically equal to the following Ramanujan generalized continued fraction:

$$\frac{1}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \dots}}}}} = e^{2\pi/5} \left(\sqrt{\phi \sqrt{5}} - \phi \right) = 0,9981360456 \dots$$

$e^{(2\pi/5)} (((\text{sqrt}(\text{golden ratio})\text{sqrt}5)-\text{golden ratio}))$

Input:

$$e^{2\pi/5} \left(\sqrt{\phi \sqrt{5}} - \phi \right)$$

ϕ is the golden ratio

Exact result:

$$e^{(2\pi/5)} \left(\sqrt[4]{5} \sqrt{\phi} - \phi \right)$$

Decimal approximation:

0.998136044598509332150024459047074735311382994763043982185...

0.998136044598....

Property:

$e^{(2\pi/5)} \left(\sqrt[4]{5} \sqrt{\phi} - \phi \right)$ is a transcendental number

$\binom{n}{m}$ is the binomial coefficient

$n!$ is the factorial function

$(\alpha)_n$ is the Pochhammer symbol (rising factorial)

\mathbb{R} is the set of real numbers

From (b)

$$\frac{1}{1+q} + \frac{q(1-q)^2}{(1+q)(1+q^2)(1+q^3)} + \frac{q^2(1-q)^2(1-q^3)^2}{(1+q)(1+q^2)\dots(1+q^5)} + \dots$$

$= F(q^2)$

$$\frac{1}{1+0.00186744} + \frac{(0.00186744(1-0.00186744)^2)}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)}$$

Input interpretation:

$$\frac{1}{1+0.00186744} + \frac{0.00186744(1-0.00186744)^2}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)}$$

Result:

0.999993038348366349082272561050573688109381291311847896576...

0.999993038348... Partial result

$$\frac{(((0.00186744^2(1-0.00186744)^2*(1-0.00186744^3)^2)))}{(((1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)(1+0.00186744^4)(1+0.00186744^5)))}$$

Input interpretation:

$$\frac{(0.00186744^2(1-0.00186744)^2(1-0.00186744^3)^2)}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)(1+0.00186744^4)(1+0.00186744^5)}$$

Result:

3.4678313969234236753964573799127696371490912532034236... × 10⁻⁶

3.4678313969... * 10⁻⁶ partial result

Thence:

1/(1+0.00186744) + ((0.00186744(1-0.00186744)²)/((1+0.00186744)(1+0.00186744²)(1+0.00186744³))+3.4678313969234236753964573799127696371490912532034236 × 10⁻⁶

Input interpretation:

$$\frac{1}{1 + 0.00186744} + \frac{0.00186744(1 - 0.00186744)^2}{(1 + 0.00186744)(1 + 0.00186744^2)(1 + 0.00186744^3)} + 3.4678313969234236753964573799127696371490912532034236 \times 10^{-6}$$

Result:

0.999996506179763272505947957507953600879018440403101100000...

0.9999965061797632.... Final Result

From (c)

$$\frac{1}{1 + q} + \frac{q(1 - q)}{(1 + q)(1 + q^2)(1 + q^3)} + \frac{q^2(1 - q)(1 - q^3)}{(1 + q)(1 + q^2) \dots (1 + q^5)} + \dots = F(q^3)$$

1/(1+0.00186744)+(0.00186744(1-0.00186744))/((1+0.00186744)(1+0.00186744²)(1+0.00186744³))+((0.00186744²(1-0.00186744)(1-0.00186744³))/((1+0.00186744)(1+0.00186744²)(1+0.00186744⁵)))

Input interpretation:

$$\frac{1}{1 + 0.00186744} + \frac{0.00186744(1 - 0.00186744)}{(1 + 0.00186744)(1 + 0.00186744^2)(1 + 0.00186744^3)} + \frac{0.00186744^2(1 - 0.00186744)(1 - 0.00186744^3)}{(1 + 0.00186744)(1 + 0.00186744^2)(1 + 0.00186744^5)}$$

Result:

0.999999986987417124730226028110134970079028870967751202815...

0.99999998698741712473.....

From (d)

$$\frac{1}{1 + q} + \frac{q(1 - q)}{(1 + q)(1 + q^3)} + \frac{q^2(1 - q)(1 - q^3)}{(1 + q)(1 + q^3)(1 + q^5)} + \dots = F(q^4)$$

$$\frac{1/(1+0.00186744) + (0.00186744(1-0.00186744)) / ((1+0.00186744)(1+0.00186744^3)) + (0.00186744^2(1-0.00186744)(1-0.00186744^3)) / ((1+0.00186744)(1+0.00186744^3)(1+0.00186744^5))}{1}$$

Input interpretation:

$$\frac{1}{1 + 0.00186744} + \frac{0.00186744(1 - 0.00186744)}{(1 + 0.00186744)(1 + 0.00186744^3)} + \frac{0.00186744^2(1 - 0.00186744)(1 - 0.00186744^3)}{(1 + 0.00186744)(1 + 0.00186744^3)(1 + 0.00186744^5)}$$

Result:

0.999999993487593859233196962292120734929897206065448414039...

0.99999999348759385923.....

From (e)

$$\frac{1}{1+q} + \frac{q(1-q)}{(1+q)(1+q^3)} + \frac{q^2(1-q)(1+q^2)}{(1+q)(1+q^3)(1+q^5)} + \dots$$

$$= F(q^6)$$

$$\frac{1}{(1+0.00186744)} + \frac{(0.00186744(1-0.00186744))}{((1+0.00186744)(1+0.00186744^3))} + \frac{(0.00186744^2(1-0.00186744)(1+0.00186744^2))}{((1+0.00186744)(1+0.00186744^3)(1+0.00186744^5))}$$

Input interpretation:

$$\frac{1}{1+0.00186744} + \frac{0.00186744(1-0.00186744)}{(1+0.00186744)(1+0.00186744^3)} + \frac{0.00186744^2(1-0.00186744)(1+0.00186744^2)}{(1+0.00186744)(1+0.00186744^3)(1+0.00186744^5)}$$

Result:

0.999999993499732633859102125517180322594693350809522240082...
0.9999999934997326338591.....

The sum of the five results is:

$$(0.99813256651238+0.9999965061797632+0.9999998698741712473+0.99999999348759385923+0.9999999934997326338591)$$

Input interpretation:

$$0.99813256651238 + 0.9999965061797632 + 0.9999998698741712473 + 0.99999999348759385923 + 0.9999999934997326338591$$

Result:

4.9981290466668868178191
 4.9981290466668868178191

$(0.99813256651238+0.9999965061797632+0.9999998698741712473+0.99999999348759385923+0.9999999934997326338591)^3+1/\text{golden ratio}$

Input interpretation:

$$(0.99813256651238 + 0.9999965061797632 + 0.9999998698741712473 + 0.99999999348759385923 + 0.9999999934997326338591)^3 + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

125.47776498921...

125.477764.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

Alternative representations:

$$(0.998132566512380000 + 0.99999650617976320000 + 0.99999986987417124730000 + 0.999999993487593859230000 + 0.99999999349973263385910000)^3 + \frac{1}{\phi} = 4.99812904666688682^3 + \frac{1}{2 \sin(54^\circ)}$$

$$(0.998132566512380000 + 0.99999650617976320000 + 0.99999986987417124730000 + 0.999999993487593859230000 + 0.99999999349973263385910000)^3 + \frac{1}{\phi} = 4.99812904666688682^3 + -\frac{1}{2 \cos(216^\circ)}$$

$$(0.998132566512380000 + 0.99999650617976320000 + 0.99999986987417124730000 + 0.999999993487593859230000 + 0.99999999349973263385910000)^3 + \frac{1}{\phi} = 4.99812904666688682^3 + -\frac{1}{2 \sin(666^\circ)}$$

$(0.99813256651238+0.9999965061797632+0.9999998698741712473+0.99999999348759385923+0.9999999934997326338591)^3+13+\text{golden ratio}$

where 13 is a Fibonacci number

Input interpretation:

$$(0.99813256651238 + 0.9999965061797632 + 0.9999998698741712473 + 0.99999999348759385923 + 0.9999999934997326338591)^3 + 13 + \phi$$

ϕ is the golden ratio

Result:

139.47776498921...

139.477764.... result practically equal to the rest mass of Pion meson 139.57 MeV

Alternative representations:

$$(0.998132566512380000 + 0.99999650617976320000 + 0.99999986987417124730000 + 0.999999993487593859230000 + 0.99999999349973263385910000)^3 + 13 + \phi = 13 + 4.99812904666688682^3 + 2 \sin(54^\circ)$$

$$(0.998132566512380000 + 0.99999650617976320000 + 0.99999986987417124730000 + 0.999999993487593859230000 + 0.99999999349973263385910000)^3 + 13 + \phi = 13 - 2 \cos(216^\circ) + 4.99812904666688682^3$$

$$(0.998132566512380000 + 0.99999650617976320000 + 0.99999986987417124730000 + 0.999999993487593859230000 + 0.99999999349973263385910000)^3 + 13 + \phi = 13 + 4.99812904666688682^3 - 2 \sin(666^\circ)$$

The mean of the five results is:

$$(0.99813256651238+0.9999965061797632+0.9999998698741712473+0.99999999348759385923+0.9999999934997326338591)/5$$

Input interpretation:

$$\frac{1}{5} (0.99813256651238 + 0.9999965061797632 + 0.9999998698741712473 + 0.99999999348759385923 + 0.9999999934997326338591)$$

Result:

0.99962580933337736356382

Repeating decimal:

0.999625809333377363563820

0.999625809333377363563820

We know that:

Leaving aside the need for further contributions to the potential that are needed to comply with well-known bounds on the tensor-to-scalar ratio r [35], when combining in four dimensions a “hard” exponential with a “mild” term one stumbles on some amusing numerology. The values of $\tilde{\gamma}$ translate indeed into the spectral index for primordial scalar perturbations, according to

$$n_S = \frac{\gamma^{(c)2} - 9\gamma_d^2}{\gamma^{(c)2} - 3\gamma_d^2}, \quad (8.22)$$

and $\frac{\gamma_d}{\gamma^{(c)}} = \frac{1}{12}$ would yield $n_S \simeq 0.96$. According to eq. (8.21), this result would obtain for $\alpha = 2$ and $p = 4$, *i.e.* for an NS five-brane wrapped around a small defect in the extra dimensions, which would make it effectively look like a four-dimensional extended object. This would be naturally available only for the $SO(16) \times SO(16)$ heterotic string of [9], which motivates us to take a closer look at dualities for these non-supersymmetric strings, starting from the original work in [41].

The scalar *spectral index* describes how the density fluctuations vary with scale. As the size of these fluctuations depends upon the inflaton's motion when these quantum fluctuations are becoming super-horizon sized, different inflationary potentials predict different spectral indices. These depend upon the slow roll parameters, in particular the gradient and curvature of the potential. Models such as monomial potentials predict a red spectral index $n_S < 1$. Planck provides a value of n_S of 0.96.

$$n_S \cong 0.96$$

From (c), we have that:

$$\left(\frac{1}{(1+0.00186744)} + \frac{0.00186744(1-0.00186744)}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)} + \frac{0.00186744^2(1-0.00186744)(1-0.00186744^3)}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^5)} \right)^{2097152}$$

Where $2097152 = 64^3 * 8$

Input interpretation:

$$\left(\frac{1}{1+0.00186744} + \frac{0.00186744(1-0.00186744)}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)} + \frac{0.00186744^2(1-0.00186744)(1-0.00186744^3)}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^5)} \right)^{2097152}$$

Result:

0.973079626199252766745687805129759260286022723358251534260...

[0.973079626199.....](#)

From (a), we obtain:

$$\left(\frac{1}{(1+0.00186744)} - \frac{((0.00186744^2)(1-0.00186744))}{((1+0.00186744)(1+0.00186744^2)(1+0.00186744^3))} + 4.2252886426780994880386059804784711267113625543227267 \times 10^{-17} \right)^{24}$$

Input interpretation:

$$\left(\frac{1}{1+0.00186744} - \frac{0.00186744^2(1-0.00186744)}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)} + \frac{4.2252886426780994880386059804784711267113625543227267 \times 10^{-17}}{1} \right)^{24}$$

Result:

0.956131040598589094149566082593776598590362040483222440035...

[0.95613104059.....](#)

Or:

$$\left(\left(\left(\frac{1}{1+0.00186744} - \left(\left(\left(0.00186744^2 \right) \left(1 - 0.00186744 \right) \right) \right) \right) \right) \right) \left(\left(\left(1 + 0.00186744 \right) \left(1 + 0.00186744^2 \right) \left(1 + 0.00186744^3 \right) \right) \right) + 4.2252886426780994880386059804784711267113625543227267 \times 10^{-17} \right)^{21}$$

Input interpretation:

$$\left(\frac{1}{1+0.00186744} - \frac{0.00186744^2 (1 - 0.00186744)}{(1+0.00186744)(1+0.00186744^2)(1+0.00186744^3)} + 4.2252886426780994880386059804784711267113625543227267 \times 10^{-17} \right)^{21}$$

Result:

0.961507642350613014002244052490243503931743205758750009026...

0.961507642350613.....

These three results are very near to the spectral index n_s , to the mesonic Regge slope, to the inflaton value at the end of the inflation 0.9402 and to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1)\sqrt{5}} - \varphi + 1} = 1 - \frac{e^{-\pi}}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-3\pi}}{1 + \frac{e^{-4\pi}}{1 + \dots}}}} \approx 0.9568666373$$

From the product of the inverse of the five results, we obtain:

$$\left(\frac{1}{0.99813256651238} \times \frac{1}{0.9999965061797632} \times \frac{1}{0.9999998698741712473} \times \frac{1}{0.999999348759385923} \times \frac{1}{0.9999999934997326338591} \right)$$

Input interpretation:

$$\frac{1}{0.99813256651238} \times \frac{1}{0.9999965061797632} \times \frac{1}{0.9999998698741712473} \times \frac{1}{0.99999999348759385923} \times \frac{1}{0.9999999934997326338591}$$

Result:

1.001874453763139680583361610568262773169221365324011909621...

1.0018744537631... result practically equal to the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{2\pi}{5}}}{\sqrt{\varphi\sqrt{5} - \varphi}} = 1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \frac{e^{-8\pi}}{1 + \dots}}}} \approx 1.0018674362$$

From which:

$$\frac{1}{10^{52}} \left[\frac{1}{0.99813256651238} \times \frac{1}{0.9999965061797632} \times \frac{1}{0.999999869874171247} \times \frac{1}{0.99999999348759385923} \times \frac{1}{0.9999999934997326338591} + \frac{10}{10^2} + \left(76 \times \frac{1}{2}\right) \times \frac{1}{10^4} \right]$$

where 76 is a Lucas number

Input interpretation:

$$\frac{1}{10^{52}} \left(\frac{1}{0.99813256651238} \times \frac{1}{0.9999965061797632} \times \frac{1}{0.9999998698741712473} \times \frac{1}{0.99999999348759385923} \times \frac{1}{0.9999999934997326338591} + \frac{10}{10^2} + \left(76 \times \frac{1}{2}\right) \times \frac{1}{10^4} \right)$$

Result:

1.1056744537631396805833616105682627731692213653240119... × 10⁻⁵²

1.105674453... * 10⁻⁵²

result practically equal to the value of Cosmological Constant 1.1056 * 10⁻⁵² m⁻²

From (a)

$$\frac{1}{1+q} - \frac{q^2(1-q)}{(1+q)(1+q^2)(1+q^3)} + \frac{q^6(1-q)(1-q^3)}{(1+q)(1+q^2)\dots(1+q^5)} + \dots$$

$$= 1 - q + q^3 - q^6 + q^{10} - q^{15} + \dots := F(q)$$

we obtain, for $q = 0.5$:

$$1/(1+0.5) - (((0.5^2)(1-0.5))/(((1+0.5)(1+0.5^2)(1+0.5^3)))+(((0.5^6(1-0.5)(1-0.5^3)))/ (((1+0.5)(1+0.5^2)(1+0.5^5))))$$

Input:

$$\frac{1}{1+0.5} - \frac{0.5^2(1-0.5)}{(1+0.5)(1+0.5^2)(1+0.5^3)} + \frac{0.5^6(1-0.5)(1-0.5^3)}{(1+0.5)(1+0.5^2)(1+0.5^5)}$$

Result:

0.610942760942760942760942760942760942760942760942760942760942760942760...

0.61094276...

From which:

$$1/10^{52}[1/(1+0.5) - (((0.5^2)(1-0.5))/(((1+0.5)(1+0.5^2)(1+0.5^3)))+(((0.5^6(1-0.5)(1-0.5^3)))/ (((1+0.5)(1+0.5^2)(1+0.5^5))))+(47+2)/10^2+47/10^4]$$

where 47 and 2 are Lucas numbers

Input:

$$\frac{1}{10^{52}} \left(\frac{1}{1+0.5} - \frac{0.5^2(1-0.5)}{(1+0.5)(1+0.5^2)(1+0.5^3)} + \frac{0.5^6(1-0.5)(1-0.5^3)}{(1+0.5)(1+0.5^2)(1+0.5^5)} + \frac{47+2}{10^2} + \frac{47}{10^4} \right)$$

Result:

1.1056427609427609427609427609427609427609427609427609427609... $\times 10^{-52}$

1.1056427609... $\times 10^{-52}$

result practically equal to the value of Cosmological Constant $1.1056 \times 10^{-52} \text{ m}^{-2}$

Note that:

Input interpretation:

0.610942760942760942760942760942760942760942760942760942760942760

Rational approximation:

$\frac{109\,096\,921\,597\,139\,930\,287\,905\,828\,168\,194\,904\,420\,417\,804\,016\,025\,801}{178\,571\,428\,571\,785\,942\,659\,179\,007\,803\,548\,562\,209\,226\,165\,846\,016\,329}$

Continued fraction:

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{3 + \frac{1}{18 + \frac{1}{18 + \frac{1}{\dots}}}}}}}}$$

Possible closed forms:

$$\frac{3629 \mathcal{W}_{\text{Wad}}}{1782} \approx 0.61094276094276094276094276094276094276094276094276094276094276$$

$$\frac{3629}{5940} \approx 0.61094276094276094276094276094276094276094276094276094276094276$$

$$\sqrt{\frac{1}{546} (-134 - 163 e + 790 \pi - 2454 \log(2))} \approx 0.61094276094276094242531$$

\mathcal{W}_{Wad} is the Wadsworth constant

$\log(x)$ is the natural logarithm

From the following closed form

$$\sqrt{\frac{1}{546} (-134 - 163 e + 790 \pi - 2454 \log(2))} \approx 0.61094276094276094242531$$

we obtain:

$$\text{sqrt}((1/546(-134 - 163e + (x+8)\pi - 2454\log(2)))) = 0.61094276094276$$

Input interpretation:

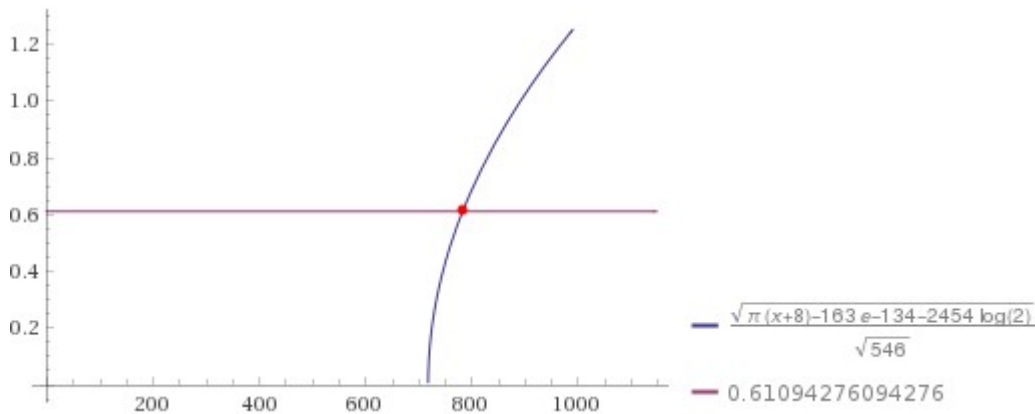
$$\sqrt{\frac{1}{546} (-134 - 163 e + (x + 8) \pi - 2454 \log(2))} = 0.61094276094276$$

$\log(x)$ is the natural logarithm

Result:

$$\frac{\sqrt{\pi(x+8) - 163e - 134 - 2454 \log(2)}}{\sqrt{546}} = 0.61094276094276$$

Plot:



Alternate form:

$$\frac{\sqrt{\pi x + 8 \pi - 163 e - 134 - 2454 \log(2)}}{\sqrt{546}} = 0.61094276094276$$

Alternate form assuming x is positive:

$$1.00000000000000 \sqrt{\pi(x+8) - 163 e - 2(67 + 1227 \log(2))} = 14.275681321850$$

Solution:

$$x = \frac{\frac{1986437731}{5880600} + 163 e + 2454 \log(2)}{\pi} - 8$$

Input:

$$-8 + \frac{\frac{1986437731}{5880600} + 163 e + 2454 \log(2)}{\pi}$$

$\log(x)$ is the natural logarithm

Decimal approximation:

782.000000000000000000000712743824136385362804856560606291673660...

782

From which:

$$-8 + (1986437731/5880600 + 163 e + 2454 \log(2))/\pi + 1/\text{golden ratio}$$

where 8 is a Fibonacci number

Input:

$$-8 + \frac{\frac{1986437731}{5880600} + 163 e + 2454 \log(2)}{\pi} + \frac{1}{\phi}$$

$\log(x)$ is the natural logarithm

ϕ is the golden ratio

Decimal approximation:

782.6180339887498949194789692480041743982059652404349302281...

782.6180339887.... result practically equal to the rest mass of Omega meson 782.65

$$\sqrt{\frac{1}{546}(-x-5) - 163e + 790\pi - 2454\log(2)}} = 0.61094276094276$$

Input interpretation:

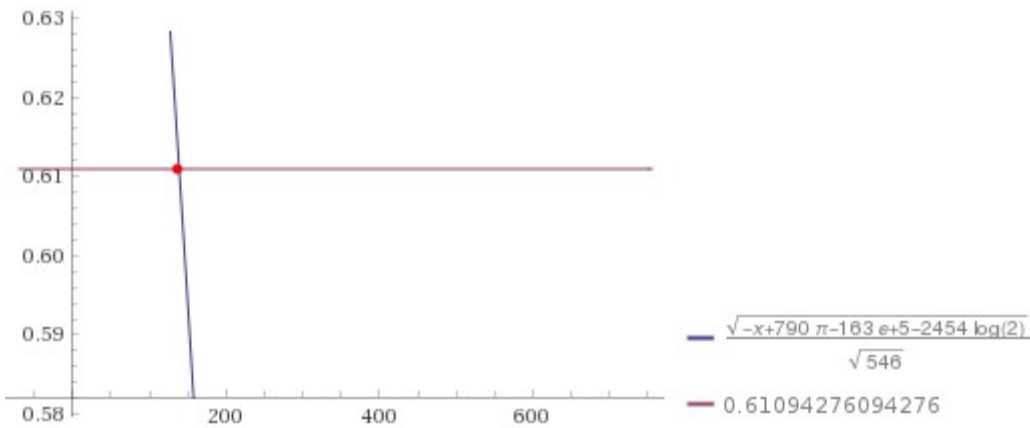
$$\sqrt{\frac{1}{546}(-x-5) - 163 e + 790 \pi - 2454 \log(2)} = 0.61094276094276$$

$\log(x)$ is the natural logarithm

Result:

$$\frac{\sqrt{-x + 790 \pi - 163 e + 5 - 2454 \log(2)}}{\sqrt{546}} = 0.61094276094276$$

Plot:



Alternate form assuming x is positive:

$$1.000000000000000 \sqrt{-x + 790 \pi - 163 e + 5 - 2454 \log(2)} = 14.275681321850$$

Solution:

$$x = -\frac{1\ 169\ 034\ 331}{5\ 880\ 600} - 163 e + 790 \pi - 2454 \log(2)$$

from which:

$$-1169034331/5880600 - 163 e + 790 \pi - 2454 \log(2) + 1/\text{golden ratio}$$

Input:

$$-\frac{1\ 169\ 034\ 331}{5\ 880\ 600} - 163 e + 790 \pi - 2454 \log(2) + \frac{1}{\phi}$$

log(x) is the natural logarithm

φ is the golden ratio

Decimal approximation:

139.6180339887498946242895106545292567181078757323973035890...

139.6180339887... result practically equal to the rest mass of Pion meson 139.57 MeV

$$\sqrt{\frac{1}{546}(-x+9) - 163e + 790\pi - 2454\log(2))} = 0.61094276094276$$

Input interpretation:

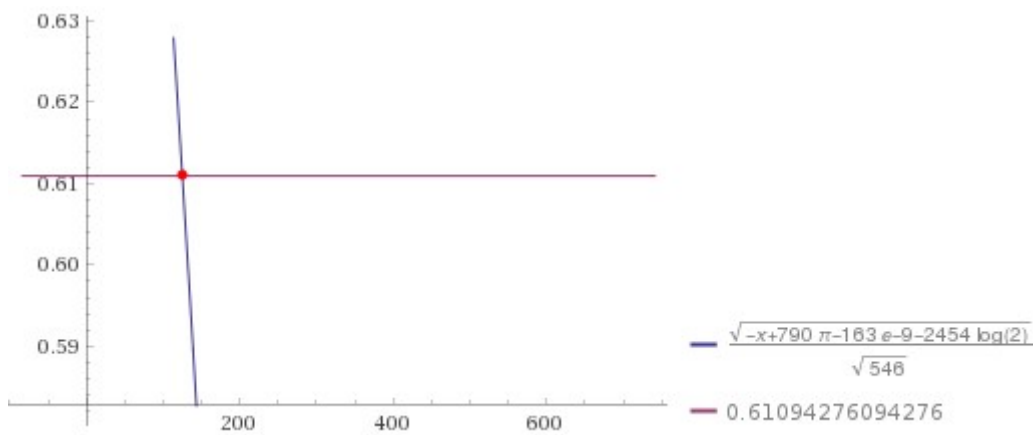
$$\sqrt{\frac{1}{546}(-x+9) - 163e + 790\pi - 2454\log(2)} = 0.61094276094276$$

log(x) is the natural logarithm

Result:

$$\frac{\sqrt{-x + 790\pi - 163e - 9 - 2454\log(2)}}{\sqrt{546}} = 0.61094276094276$$

Plot:



Alternate form assuming x is positive:

$$1.0000000000000000 \sqrt{-x + 790\pi - 163e - 9 - 2454\log(2)} = 14.275681321850$$

Solution:

$$x = -\frac{1251362731}{5880600} - 163e + 790\pi - 2454\log(2)$$

From which:

$$-1251362731/5880600 - 163e + 790\pi - 2454\log(2) + 1/\text{golden ratio}$$

Input:

$$-\frac{1251362731}{5880600} - 163e + 790\pi - 2454\log(2) + \frac{1}{\phi}$$

log(x) is the natural logarithm

ϕ is the golden ratio

Decimal approximation:

125.6180339887498946242895106545292567181078757323973035890...

125.6180339887.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

$$\text{sqrt}((1/546(-134 - 163e + 790\pi - x\log(2)))) = 0.61094276094276$$

Input interpretation:

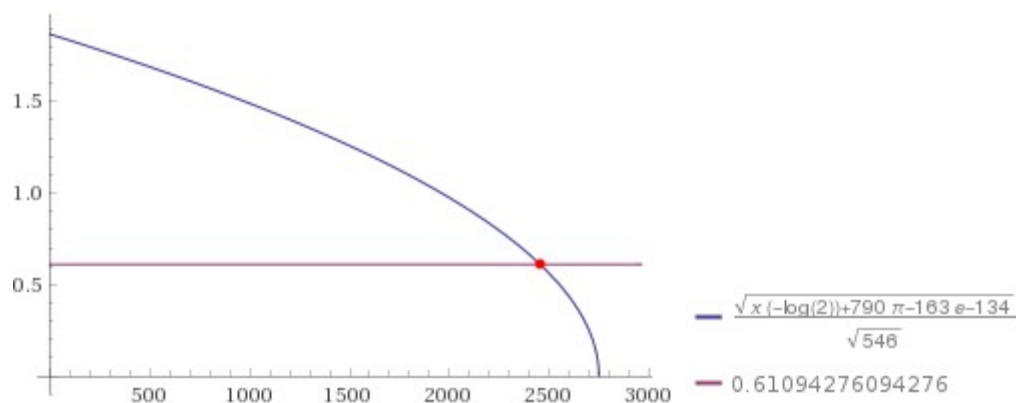
$$\sqrt{\frac{1}{546} (-134 - 163 e + 790 \pi - x \log(2))} = 0.61094276094276$$

$\log(x)$ is the natural logarithm

Result:

$$\frac{\sqrt{x(-\log(2)) + 790\pi - 163e - 134}}{\sqrt{546}} = 0.61094276094276$$

Plot:



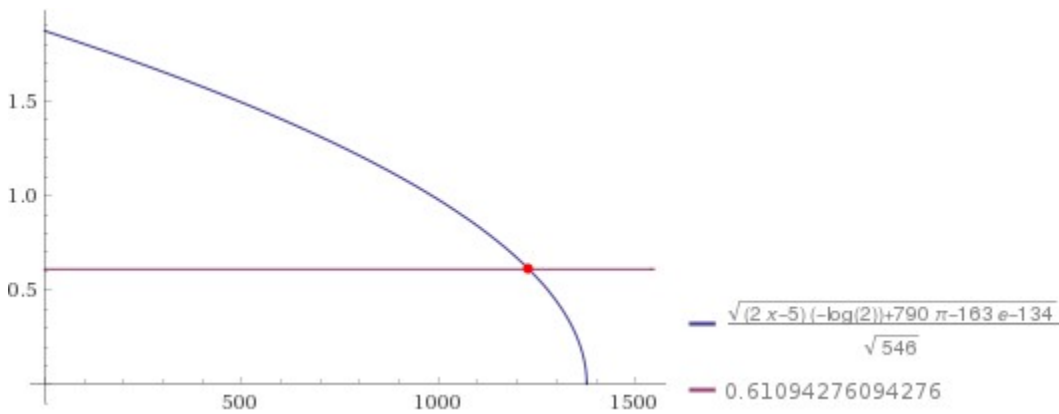
Alternate form assuming x is positive:

$$1.00000000000000 \sqrt{x(-\log(2)) + 790\pi - 163e - 134} = 14.275681321850$$

Solution:

$$x = -\frac{1986437731}{5880600 \log(2)} - \frac{163e}{\log(2)} + \frac{790\pi}{\log(2)}$$

Plot:



Alternate forms:

$$\frac{\sqrt{x(-\log(4)) + 790\pi - 163e - 134 + \log(32)}}{\sqrt{546}} = 0.61094276094276$$

$$\frac{\sqrt{-2x\log(2) + 790\pi - 163e - 134 + 5\log(2)}}{\sqrt{546}} = 0.61094276094276$$

Alternate form assuming x is positive:

$$1.00000000000000 \sqrt{x(-\log(4)) + 790\pi - 163e - 134 + \log(32)} = 14.275681321850$$

Solution:

$$x = \frac{5}{2} - \frac{1986437731}{11761200 \log(2)} + \frac{395\pi}{\log(2)} - \frac{163e}{\log(4)}$$

From which:

$$5/2 - 1986437731/(11761200 \log(2)) + (395 \pi)/\log(2) - (163 e)/\log(4) + \text{golden ratio}^2$$

Input:

$$\frac{5}{2} - \frac{1986437731}{11761200 \log(2)} + \frac{395\pi}{\log(2)} - \frac{163e}{\log(4)} + \phi^2$$

$\log(x)$ is the natural logarithm

ϕ is the golden ratio

Decimal approximation:

1232.118033988749894686684001841903435849293523012806178528...

1232.1180339887....result practically equal to the rest mass of Delta baryon 1232

$$\text{sqrt}((1/546(-134 -163e + 790\pi - (x+521+199)\log(2)))) = 0.61094276094276$$

where 521 and 199 are Lucas numbers

Input interpretation:

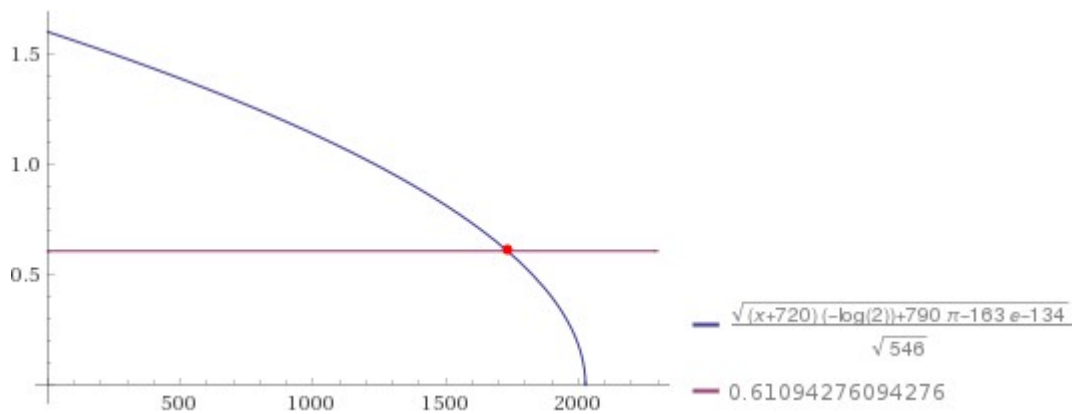
$$\sqrt{\frac{1}{546} (-134 - 163 e + 790 \pi - (x + 521 + 199) \log(2))} = 0.61094276094276$$

log(x) is the natural logarithm

Result:

$$\frac{\sqrt{(x + 720) (-\log(2)) + 790 \pi - 163 e - 134}}{\sqrt{546}} = 0.61094276094276$$

Plot:



Alternate form:

$$\frac{\sqrt{x(-\log(2)) + 790 \pi - 163 e - 134 - 720 \log(2)}}{\sqrt{546}} = 0.61094276094276$$

Alternate form assuming x is positive:

$$1.00000000000000 \sqrt{(x + 720) (-\log(2)) + 790 \pi - 163 e - 134} = 14.27568132185$$

we obtain:

$$3629 \cdot (3/10) \cdot 1/1782 \quad \text{where } W_{\text{wad}} = 3/10$$

Input:

$$3629 \times \frac{3}{10} \times \frac{1}{1782}$$

Exact result:

$$\frac{3629}{5940}$$

Decimal approximation:

0.610942760942760942760942760942760942760942760942760942760942760942760...

$$3629 \cdot (3/10) \cdot 1/x = 0.610942760942769$$

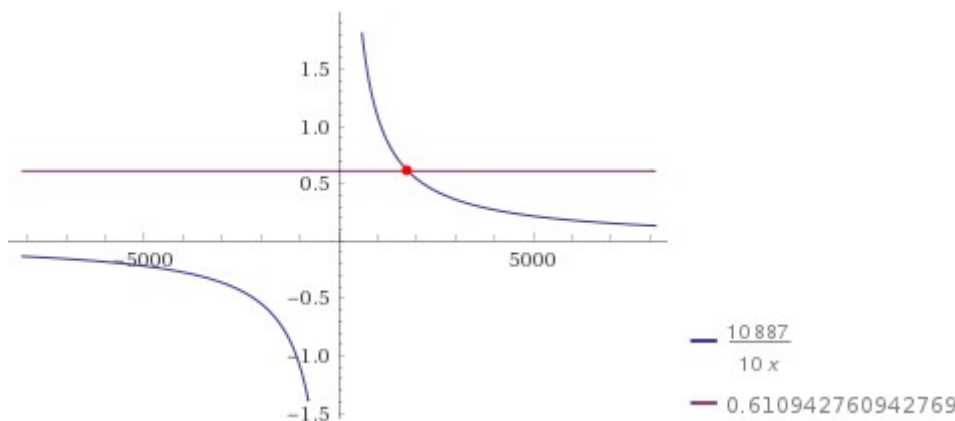
Input interpretation:

$$3629 \times \frac{3}{10} \times \frac{1}{x} = 0.610942760942769$$

Result:

$$\frac{10887}{10x} = 0.610942760942769$$

Plot:



Alternate form assuming x is real:

$$\frac{1781.9999999999998}{x} = 1.0000000000000000$$

Alternate form assuming x is positive:

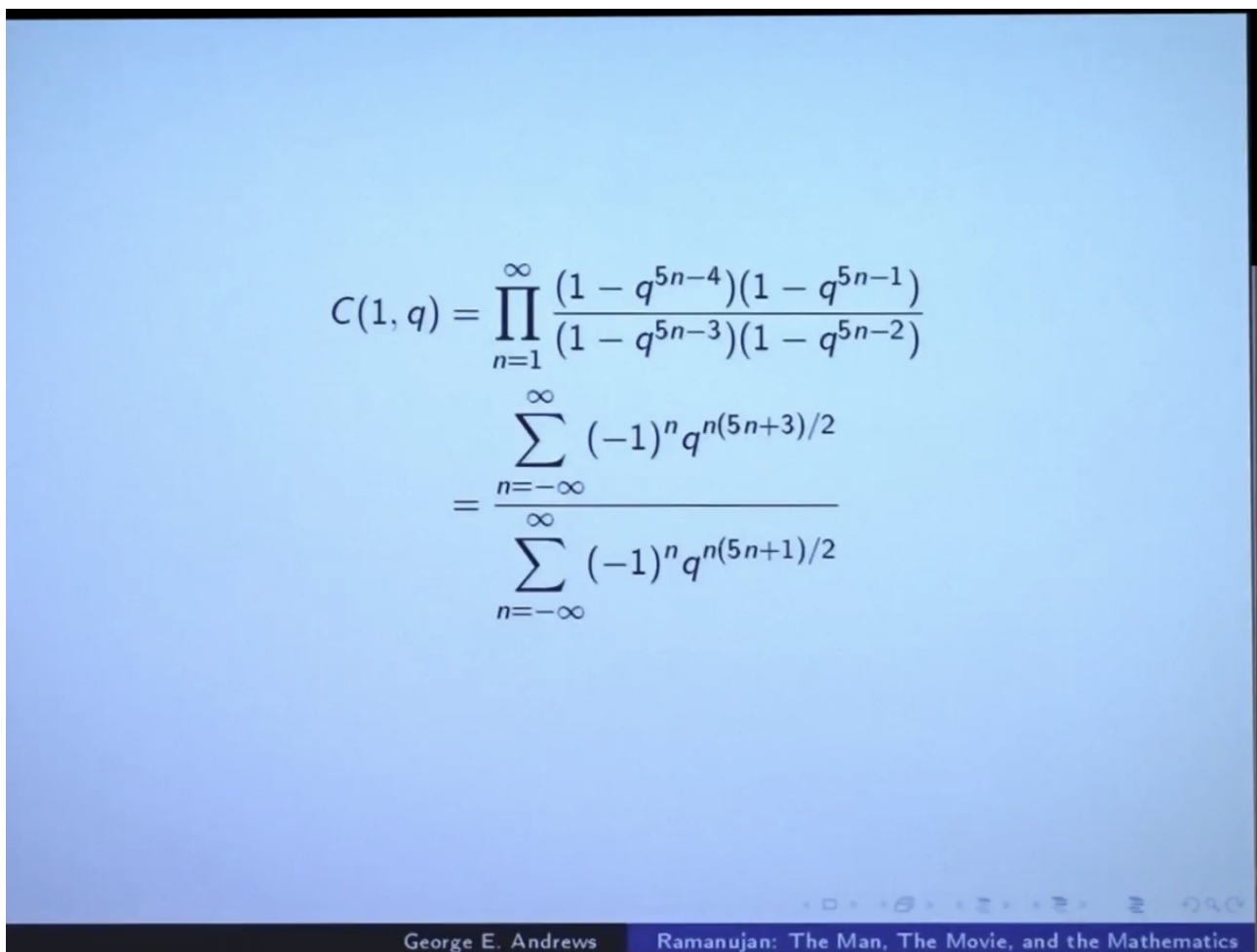
$$1.0000000000000000 x = 1781.9999999999998 \quad (\text{for } x \neq 0)$$

Solution:

$$x \approx 1782.0000000000$$

1782 result in the range of the hypothetical mass of Gluino (gluino = 1785.16 GeV).

We have that:


$$\begin{aligned} C(1, q) &= \prod_{n=1}^{\infty} \frac{(1 - q^{5n-4})(1 - q^{5n-1})}{(1 - q^{5n-3})(1 - q^{5n-2})} \\ &= \frac{\sum_{n=-\infty}^{\infty} (-1)^n q^{n(5n+3)/2}}{\sum_{n=-\infty}^{\infty} (-1)^n q^{n(5n+1)/2}} \end{aligned}$$

For $q = 0.5$, and $n = 2$, we obtain:

$$\frac{((-1)^2 * 0.5^{((2((5*2+3)/2)))))}{((-1)^2 * 0.5^{((2((5*2+1)/2)))))}$$

Input:

$$\frac{(-1)^2 \times 0.5^{2(1/2(5 \times 2 + 3))}}{(-1)^2 \times 0.5^{2(1/2(5 \times 2 + 1))}}$$

Result:

0.25

0.25

Rational form:

$$\frac{1}{4}$$

For n = 3, we obtain:

$$\frac{((((-1)^3 * 0.5^{((3((5*3+3)/2))))))}{((((-1)^3 * 0.5^{((3((5*3+1)/2))))))}}$$

Input:

$$\frac{(-1)^3 \times 0.5^{3(1/2(5 \times 3 + 3))}}{(-1)^3 \times 0.5^{3(1/2(5 \times 3 + 1))}}$$

Result:

0.125

0.125

Rational form:

$$\frac{1}{8}$$

We take n = 3 and obtain:

$$2 * \left(\frac{1}{\left(\frac{((-1)^3 * 0.5^{((3((5*3+3)/2))))}{((-1)^3 * 0.5^{((3((5*3+1)/2))))}} \right)^2} \right) - 3 + \frac{1}{\text{golden ratio}}$$

where 3 is a Fibonacci number

Input:

$$2 \times \frac{1}{\left(\frac{(-1)^3 \times 0.5^{3(1/2(5 \times 3 + 3))}}{(-1)^3 \times 0.5^{3(1/2(5 \times 3 + 1))}} \right)^2} - 3 + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

125.618...

125.618.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

Alternative representations:

$$\frac{2}{\left(\frac{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 3)}{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 1)}\right)^2} - 3 + \frac{1}{\phi} = -3 + \frac{2}{\left(\frac{-0.5^{27}}{-0.5^{24}}\right)^2} + \frac{1}{2 \sin(54^\circ)}$$

$$\frac{2}{\left(\frac{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 3)}{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 1)}\right)^2} - 3 + \frac{1}{\phi} = -3 + -\frac{1}{2 \cos(216^\circ)} + \frac{2}{\left(\frac{-0.5^{27}}{-0.5^{24}}\right)^2}$$

$$\frac{2}{\left(\frac{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 3)}{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 1)}\right)^2} - 3 + \frac{1}{\phi} = -3 + \frac{2}{\left(\frac{-0.5^{27}}{-0.5^{24}}\right)^2} + -\frac{1}{2 \sin(666^\circ)}$$

And:

$$2 * \left(\frac{1}{\left(\frac{((-1)^3 * 0.5^{((3 * (5 * 3 + 3) / 2))})}{((-1)^3 * 0.5^{((3 * (5 * 3 + 1) / 2))})} \right)^2} \right) / \left(\left(\frac{((-1)^3 * 0.5^{((3 * (5 * 3 + 1) / 2))})}{((-1)^3 * 0.5^{((3 * (5 * 3 + 1) / 2))})} \right)^2} \right) + 11 + 1 / \text{golden ratio}$$

where 11 is a Lucas number

Input:

$$2 \times \frac{1}{\left(\frac{(-1)^3 \cdot 0.5^{3(1/2(5 \times 3 + 3))}}{(-1)^3 \cdot 0.5^{3(1/2(5 \times 3 + 1))}}\right)^2} + 11 + \frac{1}{\phi}$$

φ is the golden ratio

Result:

139.618...

139.618... result practically equal to the rest mass of Pion meson 139.57 MeV

Alternative representations:

$$\frac{2}{\left(\frac{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 3)}{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 1)}\right)^2} + 11 + \frac{1}{\phi} = 11 + \frac{2}{\left(\frac{-0.5^{27}}{-0.5^{24}}\right)^2} + \frac{1}{2 \sin(54^\circ)}$$

$$\frac{2}{\left(\frac{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 3)}{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 1)}\right)^2} + 11 + \frac{1}{\phi} = 11 + -\frac{1}{2 \cos(216^\circ)} + \frac{2}{\left(\frac{-0.5^{27}}{-0.5^{24}}\right)^2}$$

$$\frac{2}{\left(\frac{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 3)}{(-1)^3 \cdot 0.5^{3/2} (5 \times 3 + 1)}\right)^2} + 11 + \frac{1}{\phi} = 11 + \frac{2}{\left(\frac{-0.5^{27}}{-0.5^{24}}\right)^2} + -\frac{1}{2 \sin(666^\circ)}$$

27*(((1/[((((-1)^3 * 0.5^(((3((5*3+3)/2)))))))/ ((((-1)^3 * 0.5^(((3((5*3+1)/2)))))))]^2)))+1/golden ratio

where 27 is equal to $\sqrt{729}$

Input:

$$27 \times \frac{1}{\left(\frac{(-1)^3 \cdot 0.5^{3/2} (1/2 (5 \times 3 + 3))}{(-1)^3 \cdot 0.5^{3/2} (1/2 (5 \times 3 + 1))}\right)^2} + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

1728.618033988749894848204586834365638117720309179805762862...

1728.6180339887...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Alternative representations:

$$\frac{27}{\left(\frac{(-1)^3 0.5^{3/2} (5 \times 3+3)}{(-1)^3 0.5^{3/2} (5 \times 3+1)}\right)^2} + \frac{1}{\phi} = \frac{27}{\left(\frac{-0.5^{27}}{-0.5^{24}}\right)^2} + \frac{1}{2 \sin(54^\circ)}$$

$$\frac{27}{\left(\frac{(-1)^3 0.5^{3/2} (5 \times 3+3)}{(-1)^3 0.5^{3/2} (5 \times 3+1)}\right)^2} + \frac{1}{\phi} = -\frac{1}{2 \cos(216^\circ)} + \frac{27}{\left(\frac{-0.5^{27}}{-0.5^{24}}\right)^2}$$

$$\frac{27}{\left(\frac{(-1)^3 0.5^{3/2} (5 \times 3+3)}{(-1)^3 0.5^{3/2} (5 \times 3+1)}\right)^2} + \frac{1}{\phi} = \frac{27}{\left(\frac{-0.5^{27}}{-0.5^{24}}\right)^2} + \frac{1}{2 \sin(666^\circ)}$$

We have that:

$$\frac{q^{1/5}}{C(1, q)} = \frac{\sqrt{5} - 1}{2} e^{\left\{ -\frac{1}{5} \int_q^1 \frac{(1-t)^5 (1-t)^5 \dots dt}{(1-t^5)(1-t^{10}) \dots t} \right\}}$$

For $q = 0.5$ and $C(1, q) = 0.125$, we obtain:

$$0.5^{(1/5)} / 0.125$$

Input:

$$\frac{\sqrt[5]{0.5}}{0.125}$$

Result:

6.964404506368993113090160139837968791833003394784024385934...

6.9644045063689....

From which:

$$(((0.5^{(1/5)} / 0.125))) = [1/2(\sqrt{5}-1)]e^x$$

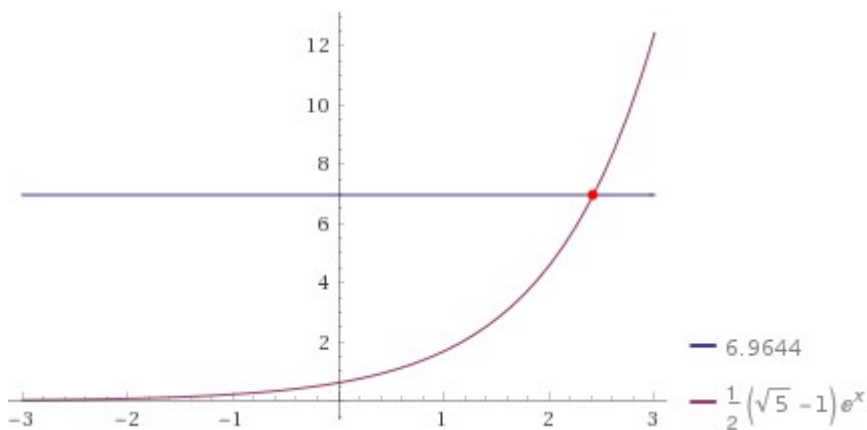
Input:

$$\frac{\sqrt[5]{0.5}}{0.125} = \left(\frac{1}{2}(\sqrt{5}-1)\right)e^x$$

Result:

$$6.9644 = \frac{1}{2}(\sqrt{5}-1)e^x$$

Plot:



Alternate form:

$$e^x = 11.2686$$

Alternate form assuming x is positive:

$$e^x = 11.2686$$

Expanded form:

$$6.9644 = \frac{\sqrt{5} e^x}{2} - \frac{e^x}{2}$$

Real solution:

$$x \approx 2.42202$$

$$2.42202$$

Solution:

$$x \approx i(6.28319 n + (-2.42202 i)), \quad n \in \mathbb{Z}$$

\mathbb{Z} is the set of integers

Thence:

$$-\frac{1}{5} \int_q^1 \frac{(1-t)^5(1-t)^5 \dots dt}{(1-t)^5(1-t)^{10} \dots t} = 2.42202$$

Indeed:

$$[1/2(\sqrt{5}-1)]e^{(2.42202)}$$

Input interpretation:

$$\left(\frac{1}{2}(\sqrt{5}-1)\right)e^{2.42202}$$

Result:

6.964377131943264659382763889136746065135256464569946022273...

6.9643771319....

Series representations:

$$\frac{1}{2} e^{2.42202} (\sqrt{5} - 1) = -\frac{e^{2.42202}}{2} + \frac{1}{2} e^{2.42202} \sqrt{4} \sum_{k=0}^{\infty} 4^{-k} \binom{\frac{1}{2}}{k}$$

$$\frac{1}{2} e^{2.42202} (\sqrt{5} - 1) = -\frac{e^{2.42202}}{2} + \frac{1}{2} e^{2.42202} \sqrt{4} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{4}\right)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$\frac{1}{2} e^{2.42202} (\sqrt{5} - 1) = -\frac{e^{2.42202}}{2} + \frac{e^{2.42202} \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 4^{-s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)}{4 \sqrt{\pi}}$$

$\binom{n}{m}$ is the binomial coefficient

$n!$ is the factorial function

$(\alpha)_n$ is the Pochhammer symbol (rising factorial)

$\Gamma(x)$ is the gamma function

$\text{Res}_{z=z_0} f$ is a complex residue

Now, we have that:

$$\left(\left(\frac{0.5^{1/5}}{0.125}\right)^4 + 76 + 29 - \phi^3\right)$$

where 76 and 29 are Lucas numbers

Input:

$$\left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 + 76 + 29 - \phi^3$$

ϕ is the golden ratio

Result:

2453.30...

2453.30... result practically equal to the rest mass of charmed Sigma baryon 2453.74

Alternative representations:

$$\left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 + 76 + 29 - \phi^3 = 105 + \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 - (2 \sin(54^\circ))^3$$

$$\left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 + 76 + 29 - \phi^3 = 105 - (-2 \cos(216^\circ))^3 + \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4$$

$$\left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 + 76 + 29 - \phi^3 = 105 + \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 - (-2 \sin(666^\circ))^3$$

$((0.5^{1/5} / 0.125))^4 - 521 - 76 - 29 + \text{golden ratio}$

where 521 is a Lucas number

Input:

$$\left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 - 521 - 76 - 29 + \phi$$

ϕ is the golden ratio

Result:

1728.15...

1728.15...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Alternative representations:

$$\left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 - 521 - 76 - 29 + \phi = -626 + \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 + 2 \sin(54^\circ)$$

$$\left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 - 521 - 76 - 29 + \phi = -626 + 2 \cos\left(\frac{\pi}{5}\right) + \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4$$

$$\left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4 - 521 - 76 - 29 + \phi = -626 - 2 \cos(216^\circ) + \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^4$$

$1/2(((0.5^{(1/5)} / 0.125)))^3 - 29 - 1/\text{golden ratio}$

where 29 is a Lucas number

Input:

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^3 - 29 - \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

139.279...

139.279... result practically equal to the rest mass of Pion meson 139.57 MeV

Alternative representations:

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^3 - 29 - \frac{1}{\phi} = -29 + \frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^3 - \frac{1}{2 \sin(54^\circ)}$$

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^3 - 29 - \frac{1}{\phi} = -29 - \frac{1}{2 \cos(216^\circ)} + \frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^3$$

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^3 - 29 - \frac{1}{\phi} = -29 + \frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125}\right)^3 - \frac{1}{2 \sin(666^\circ)}$$

$$1/2(((0.5^{(1/5)} / 0.125)))^3 - 47 + \pi + 1/\text{golden ratio}$$

where 47 is a Lucas number

Input:

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

125.657...

125.657... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

Alternative representations:

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi} = -47 + \pi + -\frac{1}{2 \cos(216^\circ)} + \frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3$$

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi} = -47 + \pi + \frac{1}{2 \cos(\frac{\pi}{5})} + \frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3$$

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi} = -47 + 180^\circ + -\frac{1}{2 \cos(216^\circ)} + \frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3$$

Series representations:

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi} = 121.897 + \frac{1}{\phi} + 4 \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi} = 119.897 + \frac{1}{\phi} + 2 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi} = 121.897 + \frac{1}{\phi} + \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}}$$

Integral representations:

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi} = 121.897 + \frac{1}{\phi} + 2 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi} = 121.897 + \frac{1}{\phi} + 4 \int_0^1 \sqrt{1-t^2} dt$$

$$\frac{1}{2} \left(\frac{\sqrt[5]{0.5}}{0.125} \right)^3 - 47 + \pi + \frac{1}{\phi} = 121.897 + \frac{1}{\phi} + 2 \int_0^{\infty} \frac{\sin(t)}{t} dt$$

Now, we have that:

$$1 + q^9 (1 + q^2 (1 + q^2 (1 + q^2) (1 + q^4 (1 + q + q^4 + 2 q^5 - q^7 + 3 q^9 - q^{11} + q^{12} + 4 q^{13} + q^{14} - q^{15} + 4 q^{17} + 2 q^{18} - 2 q^{19} + 4 q^{21} + 2 q^{22} - 2 q^{23} + q^{24} + 3 q^{25} + 2 q^{26} - 2 q^{27} + q^{28} + 3 q^{29} + 2 q^{30} - 2 q^{31} + q^{32} + 3 q^{33} + 2 q^{34} - q^{35} + 2 q^{37} + q^{38} - q^{39} + 2 q^{41} + q^{45} + q^{49}))))))$$

Schur's polynomials generalized $d_n(x)$

$$\sqrt[n]{\quad}$$

For $q = 0.5$, we obtain:

$$\begin{aligned}
 & 1+0.5^9(1+0.5^2(1+0.5^2(1+0.5^2)(1+0.5^4(1+0.5+0.5^4+2*0.5^5-0.5^7+3*0.5^9- \\
 & 0.5^{11}+0.5^{12}+4*0.5^{13}+0.5^{14}-0.5^{15}+4*0.5^{17}+2*0.5^{18}- \\
 & 2*0.5^{19}+4*0.5^{21}+2*0.5^{22}-2*0.5^{23}+0.5^{24}+3*0.5^{25}+2*0.5^{26}- \\
 & 2*0.5^{27}+0.5^{28}+3*0.5^{29}+2*0.5^{30}-2*0.5^{31}+0.5^{32}+3*0.5^{33}+2*0.5^{34}- \\
 & 0.5^{35}+2*0.5^{37}+0.5^{38}-0.5^{39}+2*0.5^{41}+0.5^{45}+0.5^{49}))) = \\
 & = 1.002609475690709
 \end{aligned}$$

$$\begin{aligned}
 & ((1+0.5^9(1+0.5^2(1+0.5^2(1+0.5^2)(1+0.5^4(1+0.5+0.5^4+2*0.5^5- \\
 & 0.5^7+3*0.5^9-0.5^{11}+0.5^{12}+4*0.5^{13}+0.5^{14}-0.5^{15}+4*0.5^{17}+2*0.5^{18})- \\
 & 6.1353084976900618 \times 10^{-6}))))))
 \end{aligned}$$

Input interpretation:

$$\begin{aligned}
 & 1 + 0.5^9 \left(1 + 0.5^2 \left(1 + 0.5^2 \left(1 + 0.5^2 \left(1 + 0.5^4 \left(1 + 0.5 + 0.5^4 + 2 \times 0.5^5 - 0.5^7 + 3 \times 0.5^9 - 0.5^{11} + 0.5^{12} + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 4 \times 0.5^{13} + 0.5^{14} - 0.5^{15} + 4 \times 0.5^{17} + 2 \times 0.5^{18} \right) - \right. \right. \\
 & \quad \left. \left. 6.1353084976900618 \times 10^{-6} \right) \right) \right) \right)
 \end{aligned}$$

Result:

1.0026094747687839490719700927734375

1.00260947476... result near to the following Rogers-Ramanujan continued fraction:

$$\frac{e^{\frac{2\pi}{5}}}{\sqrt{\varphi}\sqrt{5} - \varphi} = 1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \frac{e^{-8\pi}}{1 + \dots}}}}} \approx 1.0018674362$$

and:

$$\begin{aligned}
 & 1/((((((1+0.5^9(1+0.5^2(1+0.5^2(1+0.5^2)(1+0.5^4(1+0.5+0.5^4+2*0.5^5- \\
 & 0.5^7+3*0.5^9-0.5^{11}+0.5^{12}+4*0.5^{13}+0.5^{14}-0.5^{15}+4*0.5^{17}+2*0.5^{18})- \\
 & 6.1353084976900618 \times 10^{-6}))))))))^16
 \end{aligned}$$

Input interpretation:

$$1 / \left((1 + 0.5^9 (1 + 0.5^2 (1 + 0.5^2 (1 + 0.5^2 (1 + 0.5^4 (1 + 0.5 + 0.5^4 + 2 \times 0.5^5 - 0.5^7 + 3 \times 0.5^9 - 0.5^{11} + 0.5^{12} + 4 \times 0.5^{13} + 0.5^{14} - 0.5^{15} + 4 \times 0.5^{17} + 2 \times 0.5^{18}) - 6.1353084976900618 \times 10^{-6}))) \right)^{16}$$

Result:

0.959160154944736681097552698173659147572693523282288390554...

0.959160154...

result very near to the spectral index n_s , to the mesonic Regge slope, to the inflaton value at the end of the inflation 0.9402 (see Appendix) and to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1)\sqrt{5}} - \varphi + 1} = 1 - \frac{e^{-\pi}}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-3\pi}}{1 + \frac{e^{-4\pi}}{1 + \dots}}}} \approx 0.9568666373$$

From:

Astronomy & Astrophysics manuscript no. ms c ESO 2019 - September 24, 2019
Planck 2018 results. VI. Cosmological parameters

The primordial fluctuations are consistent with Gaussian purely adiabatic scalar perturbations characterized by a power spectrum with a spectral index $n_s = 0.965 \pm 0.004$, consistent with the predictions of slow-roll, single-field, inflation.

We know that α' is the Regge slope (string tension). With regard the Omega mesons, the values are:

$$\omega \quad | \quad 6 \quad | \quad m_{u/d} = 0 - 60 \quad | \quad 0.910 - 0.918$$

$$\omega/\omega_3 \quad | \quad 5 + 3 \quad | \quad m_{u/d} = 255 - 390 \quad | \quad 0.988 - 1.18$$


$$\omega/\omega_3 \mid 5 + 3 \mid m_{u/d} = 240 - 345 \mid 0.937 - 1.000$$

Now, we have that:

FIRST ROGERS-RAMANUJAN IDENTITY

$$1 + \frac{q}{1-q} + \frac{q^4}{(1-q)(1-q^2)} + \frac{q^9}{(1-q)(1-q^2)(1-q^3)} + \dots$$

$$= \frac{1}{(1-q)(1-q^4)(1-q^6)(1-q^9)(1-q^{11})(1-q^{14}) \dots}$$



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For $q = 0.5$, we obtain:

$$1/10^{27}[1/(((1-0.5)(1-0.5^4)(1-0.5^6)(1-0.5^9)(1-0.5^{11})(1-0.5^{14}))) - 0.5]$$

Input:

$$\frac{1}{10^{27}} \left(\frac{1}{(1-0.5)(1-0.5^4)(1-0.5^6)(1-0.5^9)(1-0.5^{11})(1-0.5^{14})} - 0.5 \right)$$

Result:

$$1.6726302514952381357587893645500581702030062401735769... \times 10^{-27}$$

1.672630251495238... * 10⁻²⁷ result practically equal to the proton mass in kg

We have also that:

$$(((1+0.5/(1-0.5)+0.5^4/(((1-0.5)(1-0.5^2))))+0.5^9/(((1-0.5)(1-0.5^2)(1-0.5^3))))))^6+34+1/\text{golden ratio}$$

where 34 is a Fibonacci number

Input:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)} \right)^6 + 34 + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

$$139.790...$$

139.790... result practically equal to the rest mass of Pion meson 139.57 MeV

Alternative representations:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)} \right)^6 + 34 + \frac{1}{\phi} = 34 + \left(1 + \frac{0.5}{0.5} + \frac{0.5^4}{0.5(1-0.5^2)} + \frac{0.5^9}{0.5(1-0.5^2)(1-0.5^3)} \right)^6 + \frac{1}{2 \sin(54^\circ)}$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^6 + 34 + \frac{1}{\phi} =$$

$$34 + \frac{1}{2 \cos(216^\circ)} + \left(1 + \frac{0.5}{0.5} + \frac{0.5^4}{0.5(1-0.5^2)} + \frac{0.5^9}{0.5(1-0.5^2)(1-0.5^3)}\right)^6$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^6 + 34 + \frac{1}{\phi} =$$

$$34 + \left(1 + \frac{0.5}{0.5} + \frac{0.5^4}{0.5(1-0.5^2)} + \frac{0.5^9}{0.5(1-0.5^2)(1-0.5^3)}\right)^6 + \frac{1}{2 \sin(666^\circ)}$$

$$\left(\left(\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)\right)^6 + 18 + \text{golden ratio}^2\right)$$

where 18 is a Lucas number

Input:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^6 + 18 + \phi^2$$

ϕ is the golden ratio

Result:

125.790...

125.790... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

Alternative representations:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^6 + 18 + \phi^2 =$$

$$18 + \left(1 + \frac{0.5}{0.5} + \frac{0.5^4}{0.5(1-0.5^2)} + \frac{0.5^9}{0.5(1-0.5^2)(1-0.5^3)}\right)^6 + (2 \sin(54^\circ))^2$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^6 + 18 + \phi^2 =$$

$$18 + (-2 \cos(216^\circ))^2 + \left(1 + \frac{0.5}{0.5} + \frac{0.5^4}{0.5(1-0.5^2)} + \frac{0.5^9}{0.5(1-0.5^2)(1-0.5^3)}\right)^6$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^6 + 18 + \phi^2 =$$

$$18 + \left(1 + \frac{0.5}{0.5} + \frac{0.5^4}{0.5(1-0.5^2)} + \frac{0.5^9}{0.5(1-0.5^2)(1-0.5^3)}\right)^6 + (-2 \sin(666^\circ))^2$$

$$(((1+0.5/(1-0.5)+0.5^4/(((1-0.5)(1-0.5^2))))+0.5^9/(((1-0.5)(1-0.5^2)(1-0.5^3))))))^9+729-76-\pi$$

Where 76 is a Lucas number and $729 = 9^3$ (see Ramanujan cubes)

Input:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi$$

Result:

1728.44...

1728.44...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Alternative representations:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi =$$

$$653 - 180^\circ + \left(1 + \frac{0.5}{0.5} + \frac{0.5^4}{0.5(1-0.5^2)} + \frac{0.5^9}{0.5(1-0.5^2)(1-0.5^3)}\right)^9$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi =$$

$$653 + i \log(-1) + \left(1 + \frac{0.5}{0.5} + \frac{0.5^4}{0.5(1-0.5^2)} + \frac{0.5^9}{0.5(1-0.5^2)(1-0.5^3)}\right)^9$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi =$$

$$653 - \cos^{-1}(-1) + \left(1 + \frac{0.5}{0.5} + \frac{0.5^4}{0.5(1-0.5^2)} + \frac{0.5^9}{0.5(1-0.5^2)(1-0.5^3)}\right)^9$$

Series representations:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi =$$

$$1731.58 - 4 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi =$$

$$1733.58 - 2 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi =$$

$$1731.58 - \sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}$$

Integral representations:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi =$$

$$1731.58 - 2 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi =$$

$$1731.58 - 4 \int_0^1 \sqrt{1-t^2} dt$$

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 76 - \pi = 1731.58 - 2 \int_0^\infty \frac{\sin(t)}{t} dt$$

$$\left(\left(\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 18 - 7\right)\right)$$

where 18 and 7 are Lucas numbers

Input:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + 729 - 18 - 7$$

Result:

1782.579706019089110335168460402380716828232902029615740744...

1782.579706.... result in the range of the hypothetical mass of Gluino (gluino = 1785.16 GeV).

$$\left(\left(\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + (x - 47 + \frac{1}{\text{golden ratio}}) - 76 - \pi\right)\right) = 1728.44$$

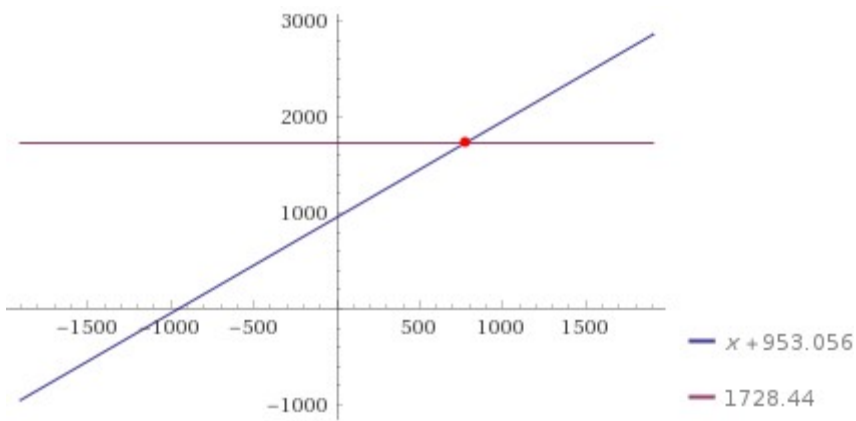
Input interpretation:

$$\left(1 + \frac{0.5}{1-0.5} + \frac{0.5^4}{(1-0.5)(1-0.5^2)} + \frac{0.5^9}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^9 + \left(x - 47 + \frac{1}{\phi}\right) - 76 - \pi = 1728.44$$

ϕ is the golden ratio

Result:

$$x + 953.056 = 1728.44$$

Plot:**Alternate forms:**

$$x - 775.384 = 0$$

$$x + 953.056 = 1728.44$$

Solution:

$$x \approx 775.384$$

775.384 result practically equal to the rest mass of Neutral rho meson 775.26

Now, we have that:

SECOND ROGERS-RAMANUJAN IDENTITY

$$\frac{1 + \frac{q^2}{1-q} + \frac{q^6}{(1-q)(1-q^2)} + \frac{q^{12}}{(1-q)(1-q^2)(1-q^3)} + \dots}{(1-q^2)(1-q^3)(1-q^7)(1-q^8)(1-q^{12})(1-q^{13})\dots}$$

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$$1 + 0.5^2 / (1 - 0.5) + 0.5^6 / (((1 - 0.5)(1 - 0.5^2))) + 0.5^{12} / (((1 - 0.5)(1 - 0.5^2)(1 - 0.5^3)))$$

Input:

$$1 + \frac{0.5^2}{1 - 0.5} + \frac{0.5^6}{(1 - 0.5)(1 - 0.5^2)} + \frac{0.5^{12}}{(1 - 0.5)(1 - 0.5^2)(1 - 0.5^3)}$$

Result:

1.542410714285714285714285714285714285714285714285714285714...

1.5424107142857...

Repeating decimal:

1.542410714285̄ (period 6)

$$1/10^{27}[1+0.5^2/(1-0.5)+0.5^6/(((1-0.5)(1-0.5^2)))+0.5^{12}/(((1-0.5)(1-0.5^2)(1-0.5^3)))+13/10^2]$$

where 13 is a Fibonacci number

Input:

$$\frac{1}{10^{27}} \left(1 + \frac{0.5^2}{1-0.5} + \frac{0.5^6}{(1-0.5)(1-0.5^2)} + \frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)} + \frac{13}{10^2} \right)$$

Result:

$$1.6724107142857142857142857142857142857142857142857142... \times 10^{-27}$$

1.6724107142857... * 10⁻²⁷ result practically equal to the proton mass in kg

$$1/(((1-0.5^2)(1-0.5^3)(1-0.5^7)(1-0.5^8)(1-0.5^{12})(1-0.5^{13})))$$

Input:

$$\frac{1}{(1-0.5^2)(1-0.5^3)(1-0.5^7)(1-0.5^8)(1-0.5^{12})(1-0.5^{13})}$$

Result:

$$1.542395596732198841370048143776104434738164036727347745386...$$

$$1.542395596732...$$

$$1/10^{27}[1/(((1-0.5^2)(1-0.5^3)(1-0.5^7)(1-0.5^8)(1-0.5^{12})(1-0.5^{13}))) + 13/10^2]$$

Input:

$$\frac{1}{10^{27}} \left(\frac{1}{(1-0.5^2)(1-0.5^3)(1-0.5^7)(1-0.5^8)(1-0.5^{12})(1-0.5^{13})} + \frac{13}{10^2} \right)$$

Result:

$$1.6723955967321988413700481437761044347381640367273477... \times 10^{-27}$$

1.6723955967... * 10⁻²⁷ result practically equal to the proton mass in kg

We have also that:

$$\left(\left(\left(1+\frac{0.5^2}{1-0.5}+\frac{0.5^6}{(1-0.5)(1-0.5^2)}\right)+\frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)\right)^{16-7}$$

where 7 is a Lucas number

Input:

$$\left(1 + \frac{0.5^2}{1-0.5} + \frac{0.5^6}{(1-0.5)(1-0.5^2)} + \frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^{16} - 7$$

Result:

1019.125626936426527138045843785105594041168531938759483884...

1019.1256269... result practically equal to the rest mass of Phi meson 1019.445

$$\left(\left(\left(1+\frac{0.5^2}{1-0.5}+\frac{0.5^6}{(1-0.5)(1-0.5^2)}\right)+\frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)\right)^{16+3^6-3^3}$$

where 3 is a Fibonacci number

Input:

$$\left(1 + \frac{0.5^2}{1-0.5} + \frac{0.5^6}{(1-0.5)(1-0.5^2)} + \frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^{16} + 3^6 - 3^3$$

Result:

1728.125626936426527138045843785105594041168531938759483884...

1728.1256269364.....

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$\left(\left(\left(\left(1+\frac{0.5^2}{1-0.5}+\frac{0.5^6}{(1-0.5)(1-0.5^2)}\right)+\frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)\right)\right)^{16}+3^6+3^3$$

Input:

$$\left(1+\frac{0.5^2}{1-0.5}+\frac{0.5^6}{(1-0.5)(1-0.5^2)}+\frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^{16}+3^6+3^3$$

Result:

1782.125626936426527138045843785105594041168531938759483884...

1782.1256269.... result in the range of the hypothetical mass of Gluino (gluino = 1785.16 GeV).

$$\left(\left(\left(\left(1+\frac{0.5^2}{1-0.5}+\frac{0.5^6}{(1-0.5)(1-0.5^2)}\right)+\frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)\right)\right)^{11+29-7}$$

where 29 and 7 are Lucas numbers

Input:

$$\left(1+\frac{0.5^2}{1-0.5}+\frac{0.5^6}{(1-0.5)(1-0.5^2)}+\frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^{11}+29-7$$

Result:

139.5439733534701919006018363881289308202786724799000192200...

139.54397335... result practically equal to the rest mass of Pion meson 139.57 MeV

$$\left(\left(\left(\left(1+\frac{0.5^2}{1-0.5}+\frac{0.5^6}{(1-0.5)(1-0.5^2)}\right)+\frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)\right)\right)^{11+11-3}$$

where 11 and 3 are Lucas numbers

Input:

$$\left(1+\frac{0.5^2}{1-0.5}+\frac{0.5^6}{(1-0.5)(1-0.5^2)}+\frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right)^{11}+11-3$$

Result:

125.5439733534701919006018363881289308202786724799000192200...

125.54397335.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

$$1/10^{52}(((((((1+0.5^2/(1-0.5)+0.5^6/(((1-0.5)(1-0.5^2))))+0.5^{12}/(((1-0.5)(1-0.5^2)(1-0.5^3)))))))-1/\text{golden ratio}+(21-3)/10^2+13/10^4))$$

where 3, 21 and 13 are Fibonacci numbers

Input:

$$\frac{1}{10^{52}} \left(\left(1 + \frac{0.5^2}{1-0.5} + \frac{0.5^6}{(1-0.5)(1-0.5^2)} + \frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)} \right) - \frac{1}{\phi} + \frac{21-3}{10^2} + \frac{13}{10^4} \right)$$

φ is the golden ratio

Result:

$$1.10568... \times 10^{-52}$$

1.10568... * 10⁻⁵² result practically equal to the value of Cosmological Constant
1.1056 * 10⁻⁵² m⁻²

Alternative representations:

$$\frac{\left(1 + \frac{0.5^2}{1-0.5} + \frac{0.5^6}{(1-0.5)(1-0.5^2)} + \frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)} \right) - \frac{1}{\phi} + \frac{21-3}{10^2} + \frac{13}{10^4}}{10^{52}} = \frac{1 + \frac{0.5^2}{0.5} + \frac{0.5^6}{0.5(1-0.5^2)} + \frac{0.5^{12}}{0.5(1-0.5^2)(1-0.5^3)} + \frac{18}{10^2} + \frac{13}{10^4} - \frac{1}{2 \sin(54^\circ)}}{10^{52}}$$

$$\frac{\left(1 + \frac{0.5^2}{1-0.5} + \frac{0.5^6}{(1-0.5)(1-0.5^2)} + \frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right) - \frac{1}{\phi} + \frac{21-3}{10^2} + \frac{13}{10^4}}{10^{52}} =$$

$$\frac{1 + \frac{0.5^2}{0.5} - \frac{1}{2 \cos(216^\circ)} + \frac{0.5^6}{0.5(1-0.5^2)} + \frac{0.5^{12}}{0.5(1-0.5^2)(1-0.5^3)} + \frac{18}{10^2} + \frac{13}{10^4}}{10^{52}}$$

$$\frac{\left(1 + \frac{0.5^2}{1-0.5} + \frac{0.5^6}{(1-0.5)(1-0.5^2)} + \frac{0.5^{12}}{(1-0.5)(1-0.5^2)(1-0.5^3)}\right) - \frac{1}{\phi} + \frac{21-3}{10^2} + \frac{13}{10^4}}{10^{52}} =$$

$$\frac{1 + \frac{0.5^2}{0.5} + \frac{0.5^6}{0.5(1-0.5^2)} + \frac{0.5^{12}}{0.5(1-0.5^2)(1-0.5^3)} + \frac{18}{10^2} + \frac{13}{10^4} - \frac{1}{2 \sin(666^\circ)}}{10^{52}}$$

Now, we have that:

$$\sum_{n=0}^{\infty} p(n)q^n$$

$$= (1 + q^1 + q^{2 \times 1} + q^{3 \times 1} + \dots)$$

$$\times (1 + q^2 + q^{2 \times 2} + q^{3 \times 2} + \dots)$$

$$\times (1 + q^3 + q^{2 \times 3} + q^{3 \times 3} + \dots)$$

$$\vdots$$

$$= \frac{1}{1-q} \times \frac{1}{1-q^2} \times \frac{1}{1-q^3} \times \dots$$

$$= \prod_{n=1}^{\infty} \frac{1}{1-q^n}$$

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product $(1/(1-q^n))$, $n=1$ to infinity

Input interpretation:

$$\prod_{n=1}^{\infty} \frac{1}{1-q^n}$$

Infinite product:

$$\prod_{n=1}^{\infty} \frac{1}{1-q^n} = \frac{1}{(q; q)_{\infty}}$$

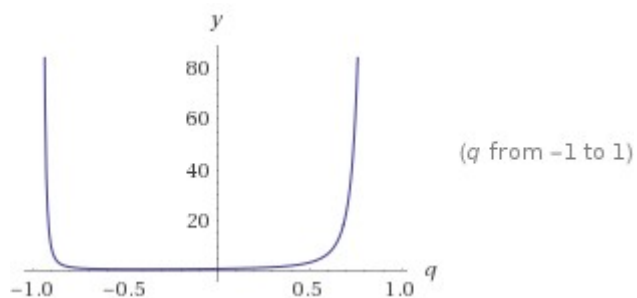
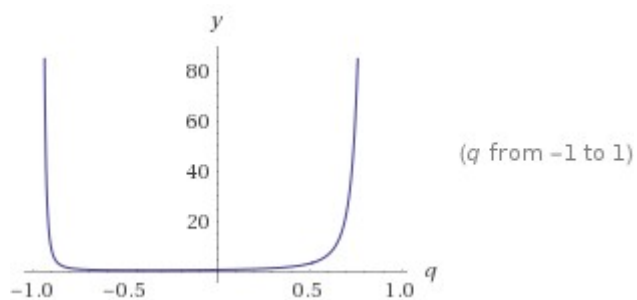
$(a; q)_n$ gives the q -Pochhammer symbol

Partial product formula:

$$\prod_{n=1}^m \frac{1}{1-q^n} = \frac{1}{(q; q)_m}$$

$(a; q)_n$ gives the q -Pochhammer symbol

Plots:



For $q = 0.5$, we obtain.

product $(1/(1-0.5^n))$, $n=1$ to infinity

Input interpretation:

$$\prod_{n=1}^{\infty} \frac{1}{1 - 0.5^n}$$

Infinite product:

$$\prod_{n=1}^{\infty} \frac{1}{1 - 0.5^n} = 3.462746619455064$$

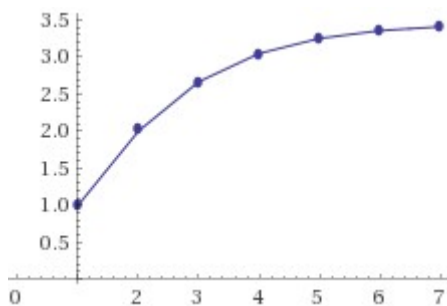
3.462746619455064

Partial product formula:

$$\prod_{n=1}^m \frac{1}{1 - 0.5^n} = \frac{1}{(0.5; 0.5)_m}$$

$(a; q)_n$ gives the q -Pochhammer symbol

Partial products:



We have that:

$$\left(\left(\left(\left(\text{product } (1/(1-0.5^n)), n=1 \text{ to infinity}\right)\right)\right)\right)^5$$

Input interpretation:

$$\left(\prod_{n=1}^{\infty} \frac{1}{1-0.5^n}\right)^5$$

Result:

497.855798606219

497.855798606219 result practically equal to the rest mass of Kaon meson 497.614

$$\left(\left(\left(\left(\text{product } (1/(1-0.5^n)), n=1 \text{ to infinity}\right)\right)\right)\right)^4 - 4$$

where 4 is a Lucas number

Input interpretation:

$$\left(\prod_{n=1}^{\infty} \frac{1}{1-0.5^n}\right)^4 - 4$$

Result:

139.7748277073093

139.7748277073093 result practically equal to the rest mass of Pion meson 139.57 MeV

$$\left(\left(\left(\left(\text{product } (1/(1-0.5^n)), n=1 \text{ to infinity}\right)\right)\right)\right)^4 - 18$$

where 18 is a Lucas number

Input interpretation:

$$\left(\prod_{n=1}^{\infty} \frac{1}{1-0.5^n}\right)^4 - 18$$

Result:

125.7748277073093

125.7748277073093 result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

$$27 \times \frac{1}{2} \left(\left(\left(\left(\left(\prod_{n=1}^{\infty} \frac{1}{1-0.5^n} \right) \right)^4 - 18 + \phi^2 \right) \right) \right) - 4$$

where 4 and 18 are Lucas numbers

Input interpretation:

$$27 \times \frac{1}{2} \left(\left(\left(\left(\prod_{n=1}^{\infty} \frac{1}{1-0.5^n} \right) \right)^4 - 18 + \phi^2 \right) \right) - 4$$

ϕ is the golden ratio

Result:

1729.303632896798

1729.303632... This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$27 \times \frac{1}{2} \left(\left(\left(\left(\left(\prod_{n=1}^{\infty} \frac{1}{1-0.5^n} \right) \right)^4 - 18 + \phi^2 \right) \right) \right) + 47 + \pi$$

where 47 is a Lucas number

Input interpretation:

$$27 \times \frac{1}{2} \left(\left(\left(\left(\prod_{n=1}^{\infty} \frac{1}{1-0.5^n} \right) \right)^4 - 18 + \phi^2 \right) \right) + 47 + \pi$$

ϕ is the golden ratio

Result:

1783.445225550388

1783.445225.... result in the range of the hypothetical mass of Gluino (gluino = 1785.16 GeV).

Now, we have that:

THESE ALL FOLLOWS FROM

$$\sum_{n=0}^{\infty} \frac{t^n q^{n(n-1)/2}}{(1+t)(1+tq)\dots(1+tq^n)} = 1$$

Proof.

CALL L.H.S. $f(t)$

$$\begin{aligned} f(t) &= \frac{1}{1+t} + \sum_{n=1}^{\infty} \frac{t^n q^{n(n-1)/2}}{(1+t)(1+tq)\dots(1+tq^n)} \\ &= \frac{1}{1+t} + \frac{t}{1+t} \sum_{n=0}^{\infty} \frac{t^n q^{n(n+1)/2}}{(1+tq)\dots(1+tq^{n+1})} \\ &= \frac{1}{1+t} + \frac{t}{1+t} f(tq) \end{aligned}$$

BUT THE CONSTANT F'N 1 SATISFIES THE SAME DEFINING EQUATION □

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For $q = 0.5$ and $t = 8$, we obtain

$$\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n(n-1)/2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)},$$

Input interpretation:

$$\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n \times (n-1) / 2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)}$$

Result:

2.79218

2.79218

$$\frac{1}{10^{27}} \left(\left(\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n(n-1)/2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)} \right) \right)^{1/2}$$

Input interpretation:

$$\frac{1}{10^{27}} \sqrt{\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n \times (n-1) / 2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)}}$$

Result:

1.67098×10^{-27}

1.67098×10^{-27} result practically equal to the value of the formula:

$$m_{p'} = 2 \times \frac{\eta}{R} m_P = 1.6714213 \times 10^{-27} \text{ kg}$$

that is the holographic proton mass (N. Haramein)

$$\frac{1}{2} \left(\left(\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n(n-1)/2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)} \right) \right)^8 + 21 + \text{golden ratio}$$

where 21 is a Fibonacci number

Input interpretation:

$$\frac{1}{2} \left(\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n \times (n-1)/2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)} \right)^8 + 21 + \phi$$

φ is the golden ratio

Result:

1869.84

1869.84 result practically equal to the rest mass of D meson 1869.61

$$\frac{1}{2} \left(\left(\frac{1}{1+8} + \sum_{n=1}^{\infty} \left(\frac{8^n * 0.5^{(n(n-1)/2)}}{(1+8)(1+8*0.5)(1+8*0.5^n)} \right) \right) \right)^8 - 123 + \pi + \text{golden ratio}$$

where 123 is a Lucas number

Input interpretation:

$$\frac{1}{2} \left(\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n \times (n-1)/2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)} \right)^8 - 123 + \pi + \phi$$

φ is the golden ratio

Result:

1728.98

1728.98

This result is very near to the mass of candidate glueball f₀(1710) meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$\left(\left(\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n(n-1)/2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)} \right) \right)^5 - 34 + 2 + \phi$$

where 34 and 2 are Fibonacci numbers

Input interpretation:

$$\left(\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n(n-1)/2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)} \right)^5 - 34 + 2 + \phi$$

ϕ is the golden ratio

Result:

139.332

139.332 result practically equal to the rest mass of Pion meson 139.57 MeV

$$\left(\left(\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n(n-1)/2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)} \right) \right)^5 - 55 + 13 - \phi^2$$

where 13 and 55 are Fibonacci numbers

Input interpretation:

$$\left(\frac{1}{1+8} + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n(n-1)/2}}{(1+8)(1+8 \times 0.5)(1+8 \times 0.5^n)} \right)^5 - 55 + 13 - \phi^2$$

ϕ is the golden ratio

Result:

125.096

125.096 result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

Now, we have that:

$$\begin{aligned}
 & 1 + \sum_{n=0}^{\infty} \frac{(-1)^n q^{n(n-1)/2}}{(1-q)(1-q^2)\cdots(1-q^n)} = \\
 & 1 + \sum_{n=0}^{\infty} \frac{(-1)^n q^{n^2}}{(1-q)(1-q^3)\cdots(1-q^{2n+1})} = \\
 & 1 + \sum_{n=0}^{\infty} \frac{(-1)^n q^{n(n-1)/2}}{(1+q)(1+q^2)\cdots(1+q^n)} =
 \end{aligned}$$

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For q = -0.5

$$1 + \sum_{n=0}^{\infty} \frac{((-1)^n * -0.5^{(n(n-1)/2)})}{((1-(-0.5))(1-(-0.5^2))(1-(-0.5^n))...)},$$

Input interpretation:

$$1 + \sum_{n=0}^{\infty} \frac{(-1)^n \times (-1) \times 0.5^{n \times (n-1)/2}}{1 - -0.5 (1 - -0.5^2 (1 - -0.5^n))}$$

Result:

0.786479

0.786479

For $q = 0.5$

$$1 + \sum_{n=0}^{\infty} \frac{((-1)^n * 0.5^{(n^2)})}{((1-0.5)(1-0.5^3)(1-0.5^{(2n+1)}))}, n=0..infinity$$

Input interpretation:

$$1 + \sum_{n=0}^{\infty} \frac{(-1)^n \times 0.5^{n^2}}{(1 - 0.5)(1 - 0.5^3)(1 - 0.5^{2n+1})}$$

Result:

4.40831

4.40831

$$1 + \sum_{n=0}^{\infty} \frac{((-1)^n * 0.5^{(n(n-1)/2)})}{(((1+0.5)(1+0.5^2)(1+0.5^n)))}, n=0..infinity$$

Input interpretation:

$$1 + \sum_{n=0}^{\infty} \frac{(-1)^n \times 0.5^{n \times (n-1) / 2}}{(1 + 0.5)(1 + 0.5^2)(1 + 0.5^n)}$$

Result:

1.07254

1.07254

we have that:

$$(0.786479 + 4.40831 + 1.07254)$$

Input interpretation:

$$0.786479 + 4.40831 + 1.07254$$

Result:

6.267329

6.267329

$$(2\pi)/(0.786479 + 4.40831 + 1.07254)$$

Input interpretation:

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254}$$

Result:

1.002529994385101927300335879376845506019284897721216110076...

1.0025299943851.... result very near to the following Rogers-Ramanujan continued fraction:

$$\frac{e^{\frac{2\pi}{5}}}{\sqrt{\phi\sqrt{5} - \phi}} = 1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \frac{e^{-8\pi}}{1 + \dots}}}} \approx 1.0018674362$$

Alternative representations:

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254} = \frac{360^\circ}{6.26733}$$

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254} = -\frac{2i \log(-1)}{6.26733}$$

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254} = \frac{2 \cos^{-1}(-1)}{6.26733}$$

Series representations:

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254} = 1.27646 \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254} = -0.63823 + 0.63823 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254} = 0.319115 \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}}$$

Integral representations:

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254} = 0.63823 \int_0^\infty \frac{1}{1+t^2} dt$$

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254} = 1.27646 \int_0^1 \sqrt{1-t^2} dt$$

$$\frac{2\pi}{0.786479 + 4.40831 + 1.07254} = 0.63823 \int_0^\infty \frac{\sin(t)}{t} dt$$

Indeed, we have:

$$(0.786479 + 4.40831 + 1.07254) * 1.0025299943851019273003358793768455060192848977212161$$

Input interpretation:

$$(0.786479 + 4.40831 + 1.07254) \times 1.0025299943851019273003358793768455060192848977212161$$

Result:

6.283185307179586476925286766559005768394338798750211578796...

$$6.283185037179.... \approx 2\pi$$

$$1/2(0.786479 + 4.40831 + 1.07254)^3 + \pi - 1/\text{golden ratio}$$

Input interpretation:

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

125.612...

125.612... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

Alternative representations:

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi} = \pi + \frac{6.26733^3}{2} - \frac{1}{2 \cos(216^\circ)}$$

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi} = 180^\circ + \frac{6.26733^3}{2} - \frac{1}{2 \cos(216^\circ)}$$

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi} = \pi + \frac{6.26733^3}{2} - \frac{1}{2 \cos\left(\frac{\pi}{5}\right)}$$

Series representations:

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi} = 123.089 - \frac{1}{\phi} + 4 \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi} = 121.089 - \frac{1}{\phi} + 2 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi} = 123.089 - \frac{1}{\phi} + \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}}$$

Integral representations:

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi} = 123.089 - \frac{1}{\phi} + 2 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi} = 123.089 - \frac{1}{\phi} + 4 \int_0^1 \sqrt{1-t^2} dt$$

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + \pi - \frac{1}{\phi} = 123.089 - \frac{1}{\phi} + 2 \int_0^{\infty} \frac{\sin(t)}{t} dt$$

$1/2(0.786479 + 4.40831 + 1.07254)^3 + 18$ -golden ratio

where 18 is a Lucas number

Input interpretation:

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + 18 - \phi$$

ϕ is the golden ratio

Result:

139.470...

139.470... result practically equal to the rest mass of Pion meson 139.57 MeV

Alternative representations:

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + 18 - \phi = 18 + \frac{6.26733^3}{2} - 2 \sin(54^\circ)$$

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + 18 - \phi = 18 + 2 \cos(216^\circ) + \frac{6.26733^3}{2}$$

$$\frac{1}{2} (0.786479 + 4.40831 + 1.07254)^3 + 18 - \phi = 18 + \frac{6.26733^3}{2} + 2 \sin(666^\circ)$$

$(0.786479 + 4.40831 + 1.07254)^4 + 144 + 34 + 8$

where 144, 34 and 8 are Fibonacci numbers

Input interpretation:

$$(0.786479 + 4.40831 + 1.07254)^4 + 144 + 34 + 8$$

Result:

1728.872269460383563402766081

1728.87226946.....

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Now, we have that:

DEFINE

$$G(x, q) = 1 + \sum_{n=1}^{\infty} \frac{x^n q^{n^2}}{(1-q)(1-q^2)\dots(1-q^n)}$$

THE FIRST ROGERS-RAMANUJAN SERIES IS

$$G(1, q)$$

THE SECOND IS

$$G(q, q)$$

George E. Andrews Ramanujan: The Man, The Movie, and the Mathematics

For $q = 0.5$ and $x = 8$, we obtain:

$$1 + \sum_{n=1}^{\infty} \left(\frac{8^n \times 0.5^{(n^2)}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)} \right), n=1..infinity$$

Input interpretation:

$$1 + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n^2}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)}$$

Result:

89.084

89.084 \approx 89 that is a Fibonacci number

$$(55-5+1/\text{golden ratio}) + 1 + \sum_{n=1}^{\infty} \left(\frac{8^n \times 0.5^{(n^2)}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)} \right), n=1..infinity$$

where 55 and 5 are Fibonacci numbers

Input interpretation:

$$\left(55 - 5 + \frac{1}{\phi} \right) + 1 + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n^2}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)}$$

ϕ is the golden ratio

Result:

139.702

139.702 result practically equal to the rest mass of Pion meson 139.57 MeV

$$(34+\text{golden ratio}^2) + 1 + \sum_{n=1}^{\infty} \left(\frac{8^n \times 0.5^{(n^2)}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)} \right), n=1..infinity$$

where 34 is a Fibonacci number

Input interpretation:

$$(34 + \phi^2) + 1 + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n^2}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)}$$

ϕ is the golden ratio

Result:

125.702

125.702 result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

$$18 \left(\left(1 + \sum_{n=1}^{\infty} \left(\frac{8^n \times 0.5^{(n^2)}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)} \right) \right) \right) + 123 + \text{golden ratio}$$

where 18 and 123 are Lucas numbers

Input interpretation:

$$18 \left(1 + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n^2}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)} \right) + 123 + \phi$$

ϕ is the golden ratio

Result:

1728.13

1728.13

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$18 \left(\left(1 + \sum_{n=1}^{\infty} \left(\frac{8^n \times 0.5^{(n^2)}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)} \right) \right) \right) + 123 + 47 + 3\pi$$

where 47 is a Fibonacci number

Input interpretation:

$$18 \left(1 + \sum_{n=1}^{\infty} \frac{8^n \times 0.5^{n^2}}{(1-0.5)(1-0.5^2)(1 \times 0.5^n)} \right) + 123 + 47 + 3\pi$$

Result:

1782.94

1782.94 result in the range of the hypothetical mass of Gluino (gluino = 1785.16 GeV).

Now, we have that:

$$(C(1, q))^2 = \frac{\sum_{n=-\infty}^{\infty} \frac{q^{3n}}{1 - q^{5n+1}}}{\sum_{n=-\infty}^{\infty} \frac{q^n}{1 - q^{5n+1}}}$$

For $q = 0.5$ we obtain:

sum (((0.5^((3n))))/(1-0.5^(5n+1)) , n=-infinity..infinity

Approximated sum:

$$\sum_{n=-\infty}^{\infty} \frac{0.5^{3n}}{1 - 0.5^{5n+1}} \approx 1.4446$$

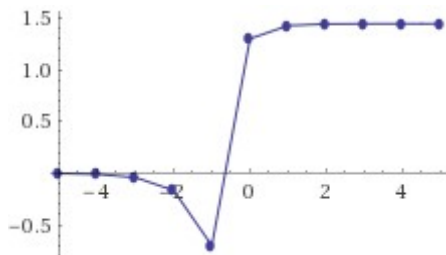
1.4446

Partial sum formula:

$$\begin{aligned} \sum_{n=0}^m \frac{0.5^{3n}}{1 - 0.5^{5n+1}} \approx & -0.577078 \left((0.61312 - 0.445458 i) \psi_2^{(0)}(m + (1.2 - 1.81294 i)) + \right. \\ & (0.61312 + 0.445458 i) \psi_2^{(0)}(m + (1.2 + 1.81294 i)) - \\ & (0.234191 - 0.720766 i) \psi_2^{(0)}(m + (1.2 - 3.62589 i)) - \\ & (0.234191 + 0.720766 i) \psi_2^{(0)}(m + (1.2 + 3.62589 i)) - \\ & \left. (6.22015 + 0 i) - 0.757858 \psi_2^{(0)}(m + 1.2) + (1.11022 \times 10^{-16} + 0 i) m \right) \end{aligned}$$

$\psi_q(z)$ gives the q-digamma function

Partial sums:



sum (((0.5)^n))/(1-0.5^(5n+1)) , n=-infinity..infinity

Approximated sum:

$$\sum_{n=-\infty}^{\infty} \frac{0.5^n}{1 - 0.5^{5n+1}} \approx 2.86638$$

2.86638

Partial sum formula:

$$\sum_{n=0}^m \frac{0.5^n}{1 - 0.5^{5n+1}} \approx$$

$$0.288539 \left((0.354967 - 1.09248 i) \left(\psi_2^{(0)}(m + (1.2 - 1.81294 i)) + m (-\log(2)) - \log(2) \right) + \right.$$

$$(0.354967 + 1.09248 i) \left(\psi_2^{(0)}(m + (1.2 + 1.81294 i)) + m (-\log(2)) - \log(2) \right) -$$

$$(0.929316 + 0.675188 i) \left(\psi_2^{(0)}(m + (1.2 - 3.62589 i)) + m (-\log(2)) - \log(2) \right) -$$

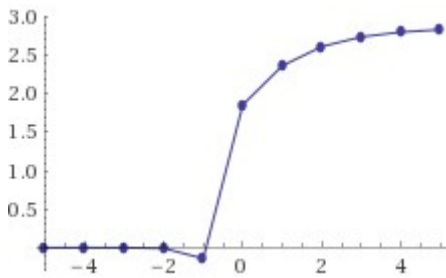
$$(0.929316 - 0.675188 i) \left(\psi_2^{(0)}(m + (1.2 + 3.62589 i)) + m (-\log(2)) - \log(2) \right) +$$

$$\left. (16.5647 + 0 i) + 1.1487 \left(\psi_2^{(0)}(m + 1.2) + m (-\log(2)) - \log(2) \right) \right)$$

$\log(x)$ is the natural logarithm

$\psi_q(z)$ gives the q -digamma function

Partial sums:



Thence:

$$(1.4446 / 2.86638)$$

Input interpretation:

$$\frac{1.4446}{2.86638}$$

Result:

0.503980630621201655049225852817839923527236444574690027142...

0.50398063...

$$76 \times \frac{1}{(1.4446 / 2.86638)} - 11$$

where 76 and 11 are Lucas numbers

Input interpretation:

$$76 \times \frac{1}{\frac{1.4446}{2.86638}} - 11$$

Result:

139.7994462134847016475148830125986432230375190364114633808...

139.79944621... result practically equal to the rest mass of Pion meson 139.57 MeV

$$76 \times \frac{1}{(1.4446 / 2.86638)} - 29 + \pi + \frac{1}{\text{golden ratio}}$$

where 29 is a Lucas number

Input interpretation:

$$76 \times \frac{1}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

125.559...

125.559... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

Alternative representations:

$$\frac{76}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi} = -29 + \pi + -\frac{1}{2 \cos(216^\circ)} + \frac{76}{2.86638}$$

$$\frac{76}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi} = -29 + 180^\circ + -\frac{1}{2 \cos(216^\circ)} + \frac{76}{2.86638}$$

$$\frac{76}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi} = -29 + \pi + \frac{1}{2 \cos\left(\frac{\pi}{5}\right)} + \frac{76}{2.86638}$$

Series representations:

$$\frac{76}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi} = 121.799 + \frac{1}{\phi} + 4 \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$\frac{76}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi} = 119.799 + \frac{1}{\phi} + 2 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{76}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi} = 121.799 + \frac{1}{\phi} + \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}}$$

Integral representations:

$$\frac{76}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi} = 121.799 + \frac{1}{\phi} + 2 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$\frac{76}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi} = 121.799 + \frac{1}{\phi} + 4 \int_0^1 \sqrt{1-t^2} dt$$

$$\frac{76}{\frac{1.4446}{2.86638}} - 29 + \pi + \frac{1}{\phi} = 121.799 + \frac{1}{\phi} + 2 \int_0^{\infty} \frac{\sin(t)}{t} dt$$

$$16 * 55 / (1.4446 / 2.86638) - 18$$

where 55 is Fibonacci number and 18 is a Lucas number

Input interpretation:

$$16 \times \frac{55}{\frac{1.4446}{2.86638}} - 18$$

Result:

1728.098850892980755918593382251142184687802852000553786515...

Repeating decimal:

1728.098850892980755918593382251142184687802852000553786515...

(period 3480)

1728.09885089....

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

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References

“17Aug18 Professor George E. Andrews”

George E. Andrews Tutte 100th distinguished Lecture Series -

<https://www.youtube.com/watch?v=IBWCm34QmjQ&t=1749s>