

Mathematical connections between the formula concerning the coefficients of the '5th order' Ramanujan's mock theta function, the mass of mesons in string model, various parameters of Particle Physics and Cosmology.

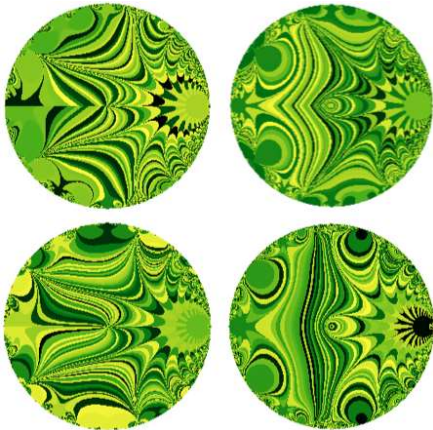
Michele Nardelli¹, Antonio Nardelli

Abstract

In this research thesis, we have described new possible mathematical connections between the formula concerning the coefficients of the '5th order' Ramanujan's mock theta function, the mass of mesons in string model, various parameters of Particle Physics and Cosmology.

¹ M.Nardelli have studied by Dipartimento di Scienze della Terra Università degli Studi di Napoli Federico II, Largo S. Marcellino, 10 - 80138 Napoli, Dipartimento di Matematica ed Applicazioni "R. Caccioppoli" - Università degli Studi di Napoli "Federico II" – Polo delle Scienze e delle Tecnologie Monte S. Angelo, Via Cintia (Fuorigrotta), 80126 Napoli, Italy

<https://royalsocietypublishing.org/toc/rsta/2020/378/2163>



<https://blog.wolfram.com/2013/05/01/after-100-years-ramanujan-gap-filled/>

From:

Masses and internal structure of mesons in the string quark model

L.D. Soloviev

*Department of Physics, University of Michigan, Ann Arbor, MI 48109-1120, USA,
And Institute for High Energy Physics, 142284, Protvino, Russia - (20 February 1999)*

The strange mesons $K_0^*(1430), 0^+$ and $K^*(1680), 1^-$ are not described by the same wave function Ψ_+ (with different j). It seems probable that a new strange 1^- meson exists with mass 1900 MeV which is a partner of $K_0^*(1430)$, see Table VI in Appendix C. On the other hand, the $K^*(1680)$ -mass, 1717 ± 17 MeV, is only half of its width, 322 ± 110 MeV, lower than the SQM value 1910 MeV.

We have the following Table:

TABLE I. Energy distribution inside mesons at rest. $v_i(E_i)$ is velocity in c (energy in MeV) of the i -th quark, E_0 is energy of the gluon string in MeV and $m_E = m - m_1 - m_2$.

Particle, quark content	v_1	v_2	E_1	E_2	E_0	$E_0/m, \%$	$E_0/m_E, \%$
$\rho^+, d\bar{u}$	0,98	0,99	53	39	679	88	90
$\pi^+, d\bar{u}$	0,88	0,93	23	16	99	72	82
$B^+, b\bar{u}$	0,07	0,99	4727	46	507	9.6	91
$J/\psi(1S), c\bar{c}$	0,22	0,22	1476	1476	146	4.7	67
$\Upsilon(1S), b\bar{b}$	0,05	0,05	4720	4720	22	0.2	67
$\chi_{b2}(1P), b\bar{b}$	0,18	0,18	4795	4795	324	3.3	67

We see that the light quarks are relativistic and give noticeable contributions to the meson masses. The main contribution to the mass "excess" of mesons $m_E = m - m_1 - m_2$ is given by the gluon string.

We have that:

$$53+39+679 = 771$$

$$23+16+99 = 138$$

$$4727+46+507 = 5280$$

$$1476+1476+146 = 3098$$

$$4720+4720+22 = 9462$$

$$4795+4795+324 = 9914$$

We take the value of E_1 , E_2 and E_0 and we make some calculations. From the formula of the coefficients of the "5th order" mock theta function $\psi_1(q)$

$$a(n) \sim \sqrt{\phi} * \exp(\pi * \sqrt{n/15}) / (2 * 5^{(1/4)} * \sqrt{n})$$

we obtain, for $n = 248$:

$$\sqrt{\text{golden ratio}} * \exp(\pi * \sqrt{248/15}) / (2 * 5^{(1/4)} * \sqrt{248}) - 76 + 4 + 2$$

where 76, 4 and 2 are a Lucas numbers

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{248}{15}}\right)}{2^4 \sqrt{5} \sqrt{248}} - 76 + 4 + 2$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{2\sqrt{62/15} \pi} \sqrt{\frac{\phi}{62}}}{4^4 \sqrt{5}} - 70$$

Decimal approximation:

9462.651386770605179169703337982742267241147864888158522697...

9462.6513867..... result very near to the rest mass of Upsilon meson 9460.30 MeV

Property:

$$-70 + \frac{e^{2\sqrt{62/15} \pi} \sqrt{\frac{\phi}{62}}}{4^4 \sqrt{5}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{1}{8} \sqrt{\frac{1}{155} (5 + \sqrt{5})} e^{2\sqrt{62/15} \pi} - 70$$

$$\frac{\sqrt{\frac{1}{31} (1 + \sqrt{5})} e^{2\sqrt{62/15} \pi}}{8^4 \sqrt{5}} - 70$$

$$\frac{5^{3/4} \sqrt{31 (1 + \sqrt{5})} e^{2\sqrt{62/15} \pi} - 86\,800}{1240}$$

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{248}{15}}\right)}{2 \sqrt[4]{5} \sqrt{248}} - 76 + 4 + 2 = \left(-700 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (248 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right. \\ \left. \exp\left[\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{248}{15} - z_0\right)^k z_0^{-k}}{k!} \right] \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (248 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{248}{15}}\right)}{2 \sqrt[4]{5} \sqrt{248}} - 76 + 4 + 2 = \\ \left(-700 \exp\left(i \pi \left[\frac{\arg(248 - x)}{2 \pi} \right] \right) \sum_{k=0}^{\infty} \frac{(-1)^k (248 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\ \left. 5^{3/4} \exp\left(i \pi \left[\frac{\arg(\phi - x)}{2 \pi} \right] \right) \exp\left[\pi \exp\left(i \pi \left[\frac{\arg\left(\frac{248}{15} - x\right)}{2 \pi} \right] \right) \sqrt{x} \right. \right. \\ \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{248}{15} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right] \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\ \left(10 \exp\left(i \pi \left[\frac{\arg(248 - x)}{2 \pi} \right] \right) \sum_{k=0}^{\infty} \frac{(-1)^k (248 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{248}{15}}\right)}{2^{4\sqrt{5}} \sqrt{248}} - 76 + 4 + 2 =$$

$$\left(\left(\frac{1}{z_0}\right)^{-1/2 [\arg(248-z_0)/(2\pi)]} z_0^{-1/2 [\arg(248-z_0)/(2\pi)]} \left[-700 \left(\frac{1}{z_0}\right)^{1/2 [\arg(248-z_0)/(2\pi)]} \right. \right.$$

$$\left. z_0^{1/2 [\arg(248-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (248-z_0)^k z_0^{-k}}{k!} + \right.$$

$$\left. 5^{3/4} \exp\left[\pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(\frac{248}{15}-z_0)/(2\pi)]} z_0^{1/2 (1+[\arg(\frac{248}{15}-z_0)/(2\pi)])} \right. \right.$$

$$\left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{248}{15}-z_0\right)^k z_0^{-k}}{k!} \right] \left(\frac{1}{z_0}\right)^{1/2 [\arg(\phi-z_0)/(2\pi)]}$$

$$\left. z_0^{1/2 [\arg(\phi-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \Bigg/$$

$$\left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (248-z_0)^k z_0^{-k}}{k!} \right)$$

For n = 224, we obtain:

$$\text{sqrt}(\text{golden ratio}) * \exp(\text{Pi} * \text{sqrt}(224/15)) / (2 * 5^{(1/4)} * \text{sqrt}(224)) - 29 - 7 - 4 - 2$$

where 29, 7, 4 and 2 are Lucas numbers

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{224}{15}}\right)}{2^{4\sqrt{5}} \sqrt{224}} - 29 - 7 - 4 - 2$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{4\sqrt{14/15} \pi} \sqrt{\frac{\phi}{14}}}{8^{4\sqrt{5}}} - 42$$

Decimal approximation:

5279.676272893316178518269411552302582626123629475691238192...

5279.67627.... result practically equal to the rest mass of B meson 5279.53 MeV

Property:

$$-42 + \frac{e^{4\sqrt{14/15}\pi} \sqrt{\frac{\phi}{14}}}{8\sqrt[4]{5}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{1}{16} \sqrt{\frac{1}{35} (5 + \sqrt{5})} e^{4\sqrt{14/15}\pi} - 42$$

$$\frac{\sqrt{\frac{1}{7} (1 + \sqrt{5})} e^{4\sqrt{14/15}\pi}}{16\sqrt[4]{5}} - 42$$

$$\frac{1}{560} \left(5^{3/4} \sqrt{7(1 + \sqrt{5})} e^{4\sqrt{14/15}\pi} - 23520 \right)$$

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{224}{15}}\right)}{2\sqrt[4]{5} \sqrt{224}} - 29 - 7 - 4 - 2 = \left(-420 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (224 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right. \\ \left. \exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{224}{15} - z_0\right)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (224 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{224}{15}}\right)}{2 \sqrt[4]{5} \sqrt{224}} - 29 - 7 - 4 - 2 = \\
& \left(-420 \exp\left(i \pi \left\lfloor \frac{\arg(224-x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (224-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\
& \quad 5^{3/4} \exp\left(i \pi \left\lfloor \frac{\arg(\phi-x)}{2 \pi} \right\rfloor\right) \exp\left(\pi \exp\left(i \pi \left\lfloor \frac{\arg\left(\frac{224}{15}-x\right)}{2 \pi} \right\rfloor\right)\right) \sqrt{x} \\
& \quad \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{224}{15}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \sum_{k=0}^{\infty} \frac{(-1)^k (\phi-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\
& \left(10 \exp\left(i \pi \left\lfloor \frac{\arg(224-x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (224-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)
\end{aligned}$$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{224}{15}}\right)}{2 \sqrt[4]{5} \sqrt{224}} - 29 - 7 - 4 - 2 = \\
& \left(\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(224-z_0)/(2 \pi) \rfloor} z_0^{-1/2 \lfloor \arg(224-z_0)/(2 \pi) \rfloor} \left(-420 \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(224-z_0)/(2 \pi) \rfloor} \right. \right. \\
& \quad \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (224-z_0)^k z_0^{-k}}{k!} + \right. \\
& \quad 5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg\left(\frac{224}{15}-z_0\right)/(2 \pi) \rfloor} z_0^{1/2 (1 + \lfloor \arg\left(\frac{224}{15}-z_0\right)/(2 \pi) \rfloor)} \right. \\
& \quad \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{224}{15}-z_0\right)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(\phi-z_0)/(2 \pi) \rfloor} \\
& \quad \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \right) / \\
& \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (224-z_0)^k z_0^{-k}}{k!} \right)
\end{aligned}$$

For $n = 203$, we obtain:

$$\sqrt{\phi} \times \frac{\exp(\pi \sqrt{\frac{203}{15}})}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7$$

where 29 and 7 are Lucas numbers

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{\sqrt{203/15} \pi} \sqrt{\frac{\phi}{203}}}{2 \sqrt[4]{5}} - 22$$

Decimal approximation:

3098.306470397246116418734540645508975568045288431783102611...

3098.30647..... result very near to the rest mass of J/Psi meson 3096.916

Property:

$$-22 + \frac{e^{\sqrt{203/15} \pi} \sqrt{\frac{\phi}{203}}}{2 \sqrt[4]{5}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{2030}} e^{\sqrt{203/15} \pi} - 22$$

$$\frac{\sqrt{\frac{1}{406} (1 + \sqrt{5})} e^{\sqrt{203/15} \pi}}{2 \sqrt[4]{5}} - 22$$

$$\frac{5^{3/4} \sqrt{406(1+\sqrt{5})} e^{\sqrt{203/15} \pi} - 89320}{4060}$$

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7 = \left(-220 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (203 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right. \\ \left. \exp\left[\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{203}{15} - z_0\right)^k z_0^{-k}}{k!} \right] \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (203 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7 = \\ \left(-220 \exp\left(i \pi \left[\frac{\arg(203 - x)}{2 \pi} \right]\right) \sum_{k=0}^{\infty} \frac{(-1)^k (203 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\ \left. 5^{3/4} \exp\left(i \pi \left[\frac{\arg(\phi - x)}{2 \pi} \right]\right) \exp\left[\pi \exp\left(i \pi \left[\frac{\arg\left(\frac{203}{15} - x\right)}{2 \pi} \right]\right) \sqrt{x} \right. \right. \\ \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{203}{15} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right] \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\ \left(10 \exp\left(i \pi \left[\frac{\arg(203 - x)}{2 \pi} \right]\right) \sum_{k=0}^{\infty} \frac{(-1)^k (203 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7 =$$

$$\left(\left(\frac{1}{z_0}\right)^{-1/2 [\arg(203-z_0)/(2\pi)]} z_0^{-1/2 [\arg(203-z_0)/(2\pi)]} \left[-220 \left(\frac{1}{z_0}\right)^{1/2 [\arg(203-z_0)/(2\pi)]} \right. \right.$$

$$\left. z_0^{1/2 [\arg(203-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (203-z_0)^k z_0^{-k}}{k!} + \right.$$

$$5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(\frac{203}{15}-z_0)/(2\pi)]} z_0^{1/2 (1+[\arg(\frac{203}{15}-z_0)/(2\pi)])} \right.$$

$$\left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{203}{15}-z_0\right)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 [\arg(\phi-z_0)/(2\pi)]}$$

$$\left. z_0^{1/2 [\arg(\phi-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \Bigg/$$

$$\left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (203-z_0)^k z_0^{-k}}{k!} \right)$$

For n = 152, we obtain:

$$\text{sqrt(golden ratio)} * \exp(\text{Pi} * \text{sqrt}(152/15)) / (2 * 5^{(1/4)} * \text{sqrt}(152)) + 11$$

where 11 is a Lucas number

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{152}{15}}\right)}{2 \sqrt[4]{5} \sqrt{152}} + 11$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{2\sqrt{38/15} \pi} \sqrt{\frac{\phi}{38}}}{4 \sqrt[4]{5}} + 11$$

Decimal approximation:

771.3345537208618611087728575016654588295858015934328676629...

771.33455372... result very near to the rest mass of Charged rho meson 775.4 MeV

Property:

$$11 + \frac{e^{2\sqrt{38/15}\pi} \sqrt{\frac{\phi}{38}}}{4\sqrt[4]{5}} \text{ is a transcendental number}$$

Alternate forms:

$$11 + \frac{1}{8} \sqrt{\frac{1}{95} (5 + \sqrt{5})} e^{2\sqrt{38/15}\pi}$$

$$11 + \frac{\sqrt{\frac{1}{19} (1 + \sqrt{5})} e^{2\sqrt{38/15}\pi}}{8\sqrt[4]{5}}$$

$$\frac{1}{760} \left(8360 + 5^{3/4} \sqrt{19(1 + \sqrt{5})} e^{2\sqrt{38/15}\pi} \right)$$

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{152}{15}}\right)}{2\sqrt[4]{5} \sqrt{152}} + 11 = \left(110 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (152 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right. \\ \left. \exp\left[\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{152}{15} - z_0\right)^k z_0^{-k}}{k!}\right] \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (152 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{152}{15}}\right)}{2 \sqrt[4]{5} \sqrt{152}} + 11 = \left(110 \exp\left(i \pi \left[\frac{\arg(152-x)}{2\pi} \right]\right) \sum_{k=0}^{\infty} \frac{(-1)^k (152-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\ \left. 5^{3/4} \exp\left(i \pi \left[\frac{\arg(\phi-x)}{2\pi} \right]\right) \exp\left(\pi \exp\left(i \pi \left[\frac{\arg\left(\frac{152}{15}-x\right)}{2\pi} \right]\right)\right) \sqrt{x} \right. \\ \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{152}{15}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \sum_{k=0}^{\infty} \frac{(-1)^k (\phi-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\ \left(10 \exp\left(i \pi \left[\frac{\arg(152-x)}{2\pi} \right]\right) \sum_{k=0}^{\infty} \frac{(-1)^k (152-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{152}{15}}\right)}{2 \sqrt[4]{5} \sqrt{152}} + 11 = \left(\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(152-z_0)/(2\pi) \rfloor} z_0^{-1/2 \lfloor \arg(152-z_0)/(2\pi) \rfloor} \right. \\ \left(110 \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(152-z_0)/(2\pi) \rfloor} z_0^{1/2 \lfloor \arg(152-z_0)/(2\pi) \rfloor} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (152-z_0)^k z_0^{-k}}{k!} + \right. \\ \left. 5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg\left(\frac{152}{15}-z_0\right)/(2\pi) \rfloor} z_0^{1/2 (1+\lfloor \arg\left(\frac{152}{15}-z_0\right)/(2\pi) \rfloor)} \right. \right. \\ \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{152}{15}-z_0\right)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(\phi-z_0)/(2\pi) \rfloor} \\ \left. z_0^{1/2 \lfloor \arg(\phi-z_0)/(2\pi) \rfloor} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \right) / \\ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (152-z_0)^k z_0^{-k}}{k!} \right)$$

For $n = 99$, we obtain:

$$\text{sqrt(golden ratio)} * \exp(\text{Pi} * \text{sqrt}(99/15)) / (2 * 5^{(1/4)} * \text{sqrt}(99)) + \text{sqrt}7$$

where 7 is a Lucas number

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{99}{15}}\right)}{2 \sqrt[4]{5} \sqrt{99}} + \sqrt{7}$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{\sqrt{33/5} \pi} \sqrt{\frac{\phi}{11}}}{6 \sqrt[4]{5}} + \sqrt{7}$$

Decimal approximation:

139.4343952159257987947932448542685258194523119145374368647...

139.4343952... result practically equal to the rest mass of Pion meson 139.57 MeV

Property:

$$\sqrt{7} + \frac{e^{\sqrt{33/5} \pi} \sqrt{\frac{\phi}{11}}}{6 \sqrt[4]{5}} \text{ is a transcendental number}$$

Alternate forms:

$$\sqrt{7} + \frac{1}{6} \sqrt{\frac{1}{110} (5 + \sqrt{5})} e^{\sqrt{33/5} \pi}$$

$$\sqrt{7} + \frac{\sqrt{\frac{1}{22} (1 + \sqrt{5})} e^{\sqrt{33/5} \pi}}{6 \sqrt[4]{5}}$$

$$\frac{1}{660} \left(660 \sqrt{7} + 5^{3/4} \sqrt{22 (1 + \sqrt{5})} e^{\sqrt{33/5} \pi} \right)$$

Series representations:

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{\infty}{15}}\right)}{2 \sqrt[4]{5} \sqrt{99}} + \sqrt{7} = \\
& \left(5^{3/4} \exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{33}{5} - z_0\right)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} + \right. \\
& \left. 10 \sqrt{z_0} \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{(-1)^{k_1+k_2} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} (7 - z_0)^{k_1} (99 - z_0)^{k_2} z_0^{-k_1-k_2}}{k_1! k_2!} \right) / \\
& \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (99 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))
\end{aligned}$$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{\infty}{15}}\right)}{2 \sqrt[4]{5} \sqrt{99}} + \sqrt{7} = \left(5^{3/4} \exp\left(i \pi \left\lfloor \frac{\arg(\phi - x)}{2 \pi} \right\rfloor \right) \right. \\
& \exp\left(\pi \exp\left(i \pi \left\lfloor \frac{\arg\left(\frac{33}{5} - x\right)}{2 \pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{33}{5} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \\
& \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + 10 \exp\left(i \pi \left\lfloor \frac{\arg(7 - x)}{2 \pi} \right\rfloor\right) \exp\left(i \pi \left\lfloor \frac{\arg(99 - x)}{2 \pi} \right\rfloor\right) \\
& \left. \sqrt{x} \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{(-1)^{k_1+k_2} (7 - x)^{k_1} (99 - x)^{k_2} x^{-k_1-k_2} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2}}{k_1! k_2!} \right) / \\
& \left(10 \exp\left(i \pi \left\lfloor \frac{\arg(99 - x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (99 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)
\end{aligned}$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{\infty}{15}}\right)}{2 \sqrt[4]{5} \sqrt{99}} + \sqrt{7} =$$

$$\left(\left(\frac{1}{z_0}\right)^{-1/2 [\arg(\infty - z_0)/(2\pi)]} z_0^{-1/2 [\arg(\infty - z_0)/(2\pi)]} \left[5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(\frac{33}{5} - z_0)/(2\pi)]}\right) \right. \right.$$

$$\left. \left. z_0^{1/2 (1 + [\arg(\frac{33}{5} - z_0)/(2\pi)])} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{33}{5} - z_0\right)^k z_0^{-k}}{k!} \right. \right.$$

$$\left. \left. \left(\frac{1}{z_0}\right)^{1/2 [\arg(\phi - z_0)/(2\pi)]} z_0^{1/2 [\arg(\phi - z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} + \right. \right.$$

$$\left. \left. 10 \left(\frac{1}{z_0}\right)^{1/2 [\arg(7 - z_0)/(2\pi)] + 1/2 [\arg(\infty - z_0)/(2\pi)]} z_0^{1/2 + 1/2 [\arg(7 - z_0)/(2\pi)] + 1/2 [\arg(\infty - z_0)/(2\pi)]} \right. \right.$$

$$\left. \left. \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{(-1)^{k_1 + k_2} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} (7 - z_0)^{k_1} (99 - z_0)^{k_2} z_0^{-k_1 - k_2}}{k_1! k_2!} \right) \right) \Bigg/$$

$$\left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (99 - z_0)^k z_0^{-k}}{k!} \right)$$

For n = 250, we obtain:

$$\text{sqrt(golden ratio)} * \exp(\text{Pi} * \text{sqrt}(250/15)) / (2 * 5^{(1/4)} * \text{sqrt}(250)) - 76 - 3 - 2$$

where 76, 3 and 2 are Lucas numbers

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{250}{15}}\right)}{2 \sqrt[4]{5} \sqrt{250}} - 76 - 3 - 2$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{5 \sqrt{2/3} \pi} \sqrt{\frac{\phi}{2}}}{10 \times 5^{3/4}} - 81$$

Decimal approximation:

9914.268365498153413336980122900378848161885661704798611997...

9914.2683654....

Property:

$-81 + \frac{e^{5\sqrt{2/3}\pi} \sqrt{\frac{\phi}{2}}}{10 \times 5^{3/4}}$ is a transcendental number

Alternate forms:

$$\frac{1}{100} \sqrt{5 + \sqrt{5}} e^{5\sqrt{2/3}\pi} - 81$$

$$\frac{\sqrt{1 + \sqrt{5}} e^{5\sqrt{2/3}\pi}}{20 \times 5^{3/4}} - 81$$

$$\frac{1}{100} \left(\sqrt[4]{5} \sqrt{1 + \sqrt{5}} e^{5\sqrt{2/3}\pi} - 8100 \right)$$

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{250}{15}}\right)}{2 \sqrt[4]{5} \sqrt{250}} - 76 - 3 - 2 = \left(-810 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (250 - z_0)^k z_0^{-k}}{k!} + \right.$$

$$\left. 5^{3/4} \exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{50}{3} - z_0\right)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) /$$

$$\left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (250 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{250}{15}}\right)}{2 \sqrt[4]{5} \sqrt{250}} - 76 - 3 - 2 = \\
& \left(-810 \exp\left(i \pi \left\lfloor \frac{\arg(250-x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (250-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\
& \quad 5^{3/4} \exp\left(i \pi \left\lfloor \frac{\arg(\phi-x)}{2 \pi} \right\rfloor\right) \exp\left(\pi \exp\left(i \pi \left\lfloor \frac{\arg\left(\frac{50}{3}-x\right)}{2 \pi} \right\rfloor\right) \sqrt{x}\right) \\
& \quad \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{50}{3}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \sum_{k=0}^{\infty} \frac{(-1)^k (\phi-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \Bigg/ \\
& \left(10 \exp\left(i \pi \left\lfloor \frac{\arg(250-x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (250-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)
\end{aligned}$$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{250}{15}}\right)}{2 \sqrt[4]{5} \sqrt{250}} - 76 - 3 - 2 = \\
& \left(\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(250-z_0)/(2\pi) \rfloor} z_0^{-1/2 \lfloor \arg(250-z_0)/(2\pi) \rfloor} \left(-810 \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(250-z_0)/(2\pi) \rfloor} \right. \right. \\
& \quad \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (250-z_0)^k z_0^{-k}}{k!} + \right. \right. \\
& \quad \left. \left. 5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg\left(\frac{50}{3}-z_0\right)/(2\pi) \rfloor} z_0^{-1/2 (1+\lfloor \arg\left(\frac{50}{3}-z_0\right)/(2\pi) \rfloor)} \right) \right. \right. \\
& \quad \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{50}{3}-z_0\right)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(\phi-z_0)/(2\pi) \rfloor} z_0^{-1/2 \lfloor \arg(\phi-z_0)/(2\pi) \rfloor} \right. \\
& \quad \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \right) \Bigg/ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (250-z_0)^k z_0^{-k}}{k!} \right)
\end{aligned}$$

For n = 181, we obtain:

$$\sqrt{\text{golden ratio}} * \exp(\text{Pi} * \sqrt{181/15}) / (2 * 5^{(1/4)} * \sqrt{181}) - 18$$

where 18 is a Lucas number

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{181}{15}}\right)}{2^4 \sqrt{5} \sqrt{181}} - 18$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{\sqrt{181/15} \pi} \sqrt{\frac{\phi}{181}}}{2^4 \sqrt{5}} - 18$$

Decimal approximation:

1717.125533153011008619695955154105542578248297442381526157...

1717.12553... result in the range of the mass of candidate “glueball” $f_0(1710)$ (“glueball” = 1760 ± 15 MeV).

Property:

$$-18 + \frac{e^{\sqrt{181/15} \pi} \sqrt{\frac{\phi}{181}}}{2^4 \sqrt{5}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{1810}} e^{\sqrt{181/15} \pi} - 18$$

$$\frac{\sqrt{\frac{1}{362} (1 + \sqrt{5})} e^{\sqrt{181/15} \pi}}{2^4 \sqrt{5}} - 18$$

$$\frac{5^{3/4} \sqrt{362 (1 + \sqrt{5})} e^{\sqrt{181/15} \pi} - 65160}{3620}$$

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{181}{15}}\right)}{2 \sqrt[4]{5} \sqrt{181}} - 18 = \left(-180 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (181 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right. \\ \left. \exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{181}{15} - z_0\right)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (181 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{181}{15}}\right)}{2 \sqrt[4]{5} \sqrt{181}} - 18 = \left(-180 \exp\left(i \pi \left\lfloor \frac{\arg(181 - x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (181 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\ \left. 5^{3/4} \exp\left(i \pi \left\lfloor \frac{\arg(\phi - x)}{2 \pi} \right\rfloor\right) \exp\left(\pi \exp\left(i \pi \left\lfloor \frac{\arg\left(\frac{181}{15} - x\right)}{2 \pi} \right\rfloor\right) \sqrt{x}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{181}{15} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\ \left(10 \exp\left(i \pi \left\lfloor \frac{\arg(181 - x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (181 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{181}{15}}\right)}{2^{\frac{4}{\sqrt{5}}} \sqrt{181}} - 18 = \\
& \left(\left(\frac{1}{z_0}\right)^{-1/2 [\text{arg}(181-z_0)/(2\pi)]} z_0^{-1/2 [\text{arg}(181-z_0)/(2\pi)]} \left[-180 \left(\frac{1}{z_0}\right)^{1/2 [\text{arg}(181-z_0)/(2\pi)]} \right. \right. \\
& \quad \left. \left. z_0^{1/2 [\text{arg}(181-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (181-z_0)^k z_0^{-k}}{k!} + \right. \right. \\
& \quad \left. \left. 5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 [\text{arg}(\frac{181}{15}-z_0)/(2\pi)]} z_0^{1/2 (1+[\text{arg}(\frac{181}{15}-z_0)/(2\pi)])} \right. \right. \right. \\
& \quad \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{181}{15}-z_0\right)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 [\text{arg}(\phi-z_0)/(2\pi)]} \right. \\
& \quad \left. \left. z_0^{1/2 [\text{arg}(\phi-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \right) / \\
& \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (181-z_0)^k z_0^{-k}}{k!} \right)
\end{aligned}$$

We note that all seven results are transcendental numbers. We ask ourselves: is there a reason for this?

In [mathematics](#), a **transcendental number** is a [real number](#) or [complex number](#) that is not an [algebraic number](#)—that is, not a [root](#) (i.e., solution) of a nonzero [polynomial equation](#) with [integer coefficients](#).

The best-known transcendental numbers are π and e

It is conjectured that all [infinite continued fractions with bounded terms that are not eventually periodic](#) are transcendental. The [number](#) π is transcendental. The set of transcendental numbers is [uncountable](#), meaning that there are [infinitely more transcendental numbers than algebraic ones](#). This result was demonstrated by Georg Cantor at the end of the nineteenth century. In mathematics, an [uncountable set](#) (or uncountable infinite set) is an infinite set that contains too many elements to be countable.

If the number is irrational, the representation in continuous fraction is infinite and unique; vice versa, each continuous infinite fraction represents an irrational number. Irrational numbers are exactly those numbers whose expansion in any base (decimal, binary, etc.) never ends and does not form a periodic sequence. Some irrational numbers are algebraic numbers like the square root of 2 and the cube root of 5); others are transcendental numbers like π and e .

So if the values of the masses of the analyzed mesons are all transcendental numbers, which are part of an uncountable infinite set, this could mean that there is the infinite in between. It could therefore mean that the set of mesons in a bubble of an inflationary universe like ours, is an uncountable infinity.

If we take, for example the mass of $J/\psi = 3098$, we note that:

$$\text{sqrt}(\text{golden ratio}) * \exp(\text{Pi} * \text{sqrt}(203/15)) / (2 * 5^{(1/4)} * \text{sqrt}(203)) - 29 + 7$$

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7$$

$$\frac{e^{\sqrt{203/15} \pi} \sqrt{\frac{\phi}{203}}}{2 \sqrt[4]{5}} - 22$$

3098.306470397246116418734540645508975568045288431783102611...

3098.30647...

$$-22 + \frac{e^{\sqrt{203/15} \pi} \sqrt{\frac{\phi}{203}}}{2 \sqrt[4]{5}} \text{ is a transcendental number}$$

Thence, 3098.30647.... is a transcendental number and must be expressed from an infinite continued fraction. Indeed:

Continued fraction

$$\begin{array}{c}
 3098 + \cfrac{1}{3 + \cfrac{1}{3 + \cfrac{1}{1 + \cfrac{1}{4 + \cfrac{1}{13 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{3 + \cfrac{1}{2 + \cfrac{1}{2 + \cfrac{1}{5 + \cfrac{1}{7 + \cfrac{1}{6 + \cfrac{1}{1 + \cfrac{1}{31 + \cfrac{1}{5 + \cfrac{1}{1 + \cfrac{1}{84 + \cfrac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}
 \end{array}$$

We observe that, from the above expression, we obtain:

Input interpretation:

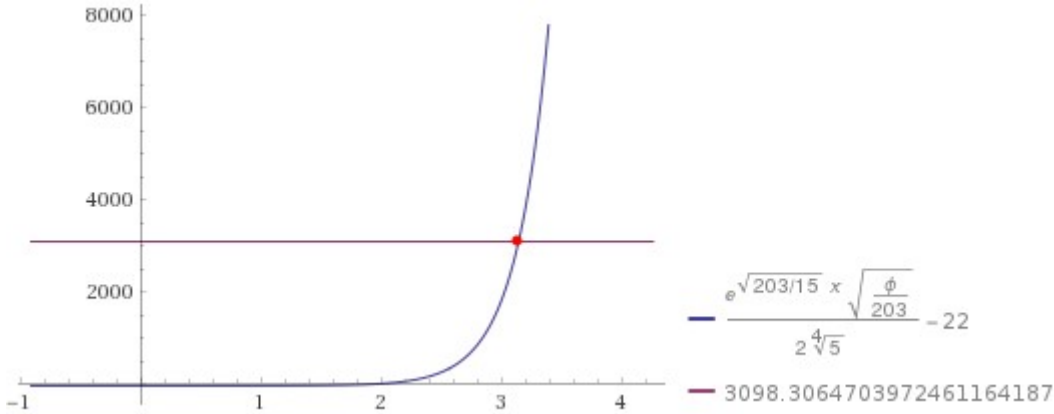
$$\sqrt{\phi} \times \frac{\exp\left(x \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7 = 3098.3064703972461164187$$

phi is the golden ratio

Result:

$$\frac{e^{\sqrt{203/15} x} \sqrt{\frac{\phi}{203}}}{2 \sqrt[4]{5}} - 22 = 3098.3064703972461164187$$

Plot:



Alternate forms:

$$e^{\sqrt{203/15} x} = 104525.90760556640926415$$

$$\frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{2030}} e^{\sqrt{203/15} x} - 22 = 3098.3064703972461164187$$

$$\frac{\sqrt{\frac{1}{406} (1 + \sqrt{5})} e^{\sqrt{203/15} x}}{2 \sqrt[4]{5}} - 22 = 3098.3064703972461164187$$

$$1.000000000000000000000000 e^{\sqrt{203/15} x} = 104525.90760556640926415$$

Real solution:

$$x \approx 3.1415926535897932384626$$

$$3.14159...$$

Thence, we obtain π that is a transcendental number. If instead of π , insert in the principal formula the number 3, we obtain:

$$\text{sqrt(golden ratio)} * \exp(3 * \text{sqrt}(203/15)) / (2 * 5^{(1/4)} * \text{sqrt}(203)) + 11$$

Input:

$$\sqrt{\phi} \times \frac{\exp\left(3 \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} + 11$$

$$\frac{e^{\sqrt{609/5}} \sqrt{\frac{\phi}{203}}}{2 \sqrt[4]{5}} + 11$$

$$1864.442488282617403318876228810194678643298431300428782619...$$

1864.4424882826..... result practically to the rest mass of D meson 1864.84, that is a transcendental number and can be expressed from an infinite continued fraction. Indeed:

Property:

$$11 + \frac{e^{\sqrt{609/5}} \sqrt{\frac{\phi}{203}}}{2 \sqrt[4]{5}} \text{ is a transcendental number}$$

Alternate forms:

$$11 + \frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{2030}} e^{\sqrt{609/5}}$$

$$11 + \frac{\sqrt{\frac{1}{406}(1 + \sqrt{5})} e^{\sqrt{609/5}}}{2 \sqrt[4]{5}}$$

$$\frac{44660 + 5^{3/4} \sqrt{406(1 + \sqrt{5})} e^{\sqrt{609/5}}}{4060}$$

- **Fraction form**

[1864; 2, 3, 1, 5, 1, 1, 6, 1, 69, 26, 2, 23, 1, 2, 1, 5, 18, 4, 1, 1, 1, 1, 1, 1, 2, 3, 42, ...]

$$1864 + \frac{1}{2 + \frac{1}{3 + \frac{1}{1 + \frac{1}{5 + \frac{1}{1 + \frac{1}{1 + \frac{1}{6 + \frac{1}{1 + \frac{1}{69 + \frac{1}{26 + \frac{1}{2 + \frac{1}{23 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{5 + \frac{1}{18 + \frac{1}{4 + \frac{1}{1 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

$$\frac{\sqrt{\phi} \exp\left(3 \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} + 11 = \left(110 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (203 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right.$$

$$\left. \exp\left(3 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{203}{15} - z_0\right)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) /$$

$$\left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (203 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\frac{\sqrt{\phi} \exp\left(3\sqrt{\frac{203}{15}}\right)}{2\sqrt[4]{5}\sqrt{203}} + 11 = \left(110 \exp\left(i\pi \left\lfloor \frac{\arg(203-x)}{2\pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (203-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\ \left. 5^{3/4} \exp\left(i\pi \left\lfloor \frac{\arg(\phi-x)}{2\pi} \right\rfloor\right) \exp\left(3 \exp\left(i\pi \left\lfloor \frac{\arg\left(\frac{203}{15}-x\right)}{2\pi} \right\rfloor\right) \sqrt{x}\right) \right. \\ \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{203}{15}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \sum_{k=0}^{\infty} \frac{(-1)^k (\phi-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \Bigg/ \\ \left(10 \exp\left(i\pi \left\lfloor \frac{\arg(203-x)}{2\pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (203-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\frac{\sqrt{\phi} \exp\left(3\sqrt{\frac{203}{15}}\right)}{2\sqrt[4]{5}\sqrt{203}} + 11 = \left(\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(203-z_0)/(2\pi) \rfloor} z_0^{-1/2 \lfloor \arg(203-z_0)/(2\pi) \rfloor} \right. \\ \left(110 \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(203-z_0)/(2\pi) \rfloor} z_0^{1/2 \lfloor \arg(203-z_0)/(2\pi) \rfloor} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (203-z_0)^k z_0^{-k}}{k!} + \right. \\ \left. 5^{3/4} \exp\left(3 \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg\left(\frac{203}{15}-z_0\right)/(2\pi) \rfloor} z_0^{1/2 (1+\lfloor \arg\left(\frac{203}{15}-z_0\right)/(2\pi) \rfloor)} \right. \right. \\ \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{203}{15}-z_0\right)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(\phi-z_0)/(2\pi) \rfloor} \\ \left. z_0^{1/2 \lfloor \arg(\phi-z_0)/(2\pi) \rfloor} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \Bigg/ \\ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (203-z_0)^k z_0^{-k}}{k!} \right)$$

Therefore, it is not π that causes the result to be a transcendental number when the expression is developed. So is it the expression itself that, once developed, leads to results that are transcendental numbers? And why are the masses of the mesons under examination ALL values ascribable to transcendental numbers, expressible through infinite continued fractions? It would therefore seem that the strings that constitute the mesons are expressions of irrational and transcendental numbers (infinite continuous fractions like the Rogers-Ramanujan). Having the strings a frequency linked to their vibration, it is possible to hypothesize that the frequencies of the

strings / branes coincide with transcendental numbers and that they are also an uncountable infinite set

We note that, from the above six mesons mass, except the expression concerning the mass of the Pion, we obtain, performing several computations with Lucas numbers, the following interesting results:

For 9462.651..., we obtain:

$$\sqrt{\sqrt{\phi} \times \frac{\exp(\pi \sqrt{\frac{248}{15}})}{2 \sqrt[4]{5} \sqrt{248}} - 76 + 4 + 2} + 29 + 11 + 2$$

where 29, 11 and 2 are Lucas number

Input:

$$\sqrt{\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{248}{15}}\right)}{2 \sqrt[4]{5} \sqrt{248}} - 76 + 4 + 2} + 29 + 11 + 2$$

ϕ is the golden ratio

Exact result:

$$\sqrt{\frac{e^{2 \sqrt{62/15} \pi} \sqrt{\frac{\phi}{62}}}{4 \sqrt[4]{5}} - 70} + 42$$

Decimal approximation:

139.2761604236649812229311221955932569651879331468917939732...

139.2761604...

Property:

$$42 + \sqrt{-70 + \frac{e^{2 \sqrt{62/15} \pi} \sqrt{\frac{\phi}{62}}}{4 \sqrt[4]{5}}} \text{ is a transcendental number}$$

Alternate forms:

$$42 + \sqrt{\frac{1}{8} \sqrt{\frac{1}{155} (5 + \sqrt{5})} e^{2\sqrt{62/15} \pi} - 70}$$

$$42 + \sqrt{\frac{\sqrt{\frac{1}{31} (1 + \sqrt{5})} e^{2\sqrt{62/15} \pi}}{8 \sqrt[4]{5}} - 70}$$

$$\frac{1}{620} \left(26040 + \sqrt{310 \left(5^{3/4} \sqrt{31 (1 + \sqrt{5})} e^{2\sqrt{62/15} \pi} - 86800 \right)} \right)$$

Series representations:

$$\sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{248}{15}}\right)}{2 \sqrt[4]{5} \sqrt{248}} - 76 + 4 + 2 + 29 + 11 + 2 =}$$

$$42 + \sqrt{-71 + \frac{\exp\left(\pi \sqrt{\frac{248}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{248}} \sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} \left(-71 + \frac{\exp\left(\pi \sqrt{\frac{248}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{248}} \right)^{-k}}$$

$$\sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{248}{15}}\right)}{2 \sqrt[4]{5} \sqrt{248}} - 76 + 4 + 2 + 29 + 11 + 2 =}$$

$$42 + \sqrt{-71 + \frac{\exp\left(\pi \sqrt{\frac{248}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{248}} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k}{k!} \left(-71 + \frac{\exp\left(\pi \sqrt{\frac{248}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{248}} \right)^{-k}}$$

$$\sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{248}{15}}\right)}{2 \sqrt[4]{5} \sqrt{248}} - 76 + 4 + 2 + 29 + 11 + 2 =}$$

$$42 + \sqrt{z_0 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-70 + \frac{\exp\left(\pi \sqrt{\frac{248}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{248}} - z_0 \right)^k}{k!} z_0^{-k}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

For 5279.676..., we obtain:

$$2\sqrt{\left(\left(\sqrt{\text{golden ratio}}\right) * \exp\left(\pi * \sqrt{\frac{224}{15}}\right) / \left(2 * 5^{1/4} * \sqrt{224}\right) - 29 - 7 - 4 - 2\right) - 11 + 3 + 2}$$

Where 11, 3 and 2 are Lucas numbers

Input:

$$2\sqrt{\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{224}{15}}\right)}{2 \sqrt[4]{5} \sqrt{224}} - 29 - 7 - 4 - 2 - 11 + 3 + 2}$$

ϕ is the golden ratio

Exact result:

$$2\sqrt{\frac{e^{4\sqrt{14/15} \pi} \sqrt{\frac{\phi}{14}}}{8 \sqrt[4]{5}} - 42 - 6}$$

Decimal approximation:

139.3227617807109551977321779636908712011065133673118176353...

139.322761....

Property:

$$-6 + 2\sqrt{-42 + \frac{e^{4\sqrt{14/15} \pi} \sqrt{\frac{\phi}{14}}}{8 \sqrt[4]{5}}} \text{ is a transcendental number}$$

Alternate forms:

$$2\sqrt{\frac{1}{16} \sqrt{\frac{1}{35} (5 + \sqrt{5})} e^{4\sqrt{14/15} \pi} - 42 - 6}$$

$$2 \sqrt{\frac{\sqrt{\frac{1}{7}(1+\sqrt{5})} e^{4\sqrt{14/15}\pi}}{16\sqrt[4]{5}} - 42 - 6}$$

$$\frac{1}{70} \left(\sqrt{35 \left(5^{3/4} \sqrt{7(1+\sqrt{5})} e^{4\sqrt{14/15}\pi} - 23520 \right)} - 420 \right)$$

Series representations:

$$2 \sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{224}{15}}\right)}{2\sqrt[4]{5} \sqrt{224}} - 29 - 7 - 4 - 2 - 11 + 3 + 2 =}$$

$$-6 + 2 \sqrt{-43 + \frac{\exp\left(\pi \sqrt{\frac{224}{15}}\right) \sqrt{\phi}}{2\sqrt[4]{5} \sqrt{224}} \sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} \left(-43 + \frac{\exp\left(\pi \sqrt{\frac{224}{15}}\right) \sqrt{\phi}}{2\sqrt[4]{5} \sqrt{224}} \right)^k}$$

$$2 \sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{224}{15}}\right)}{2\sqrt[4]{5} \sqrt{224}} - 29 - 7 - 4 - 2 - 11 + 3 + 2 =}$$

$$-6 + 2 \sqrt{-43 + \frac{\exp\left(\pi \sqrt{\frac{224}{15}}\right) \sqrt{\phi}}{2\sqrt[4]{5} \sqrt{224}} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-43 + \frac{\exp\left(\pi \sqrt{\frac{224}{15}}\right) \sqrt{\phi}}{2\sqrt[4]{5} \sqrt{224}} \right)^k}{k!}}$$

$$2 \sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{224}{15}}\right)}{2\sqrt[4]{5} \sqrt{224}} - 29 - 7 - 4 - 2 - 11 + 3 + 2 =}$$

$$-6 + 2 \sqrt{z_0 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-42 + \frac{\exp\left(\pi \sqrt{\frac{224}{15}}\right) \sqrt{\phi}}{2\sqrt[4]{5} \sqrt{224}} - z_0 \right)^k}{k!}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

For 3098.30647..., we obtain:

$$5/2\sqrt{((\sqrt{\text{golden ratio}}) * \exp(\text{Pi}*\sqrt{203/15})) / (2*5^{(1/4)}*\sqrt{203})-29+7))}$$

Input:

$$\frac{5}{2} \sqrt{\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7}$$

ϕ is the golden ratio

Exact result:

$$\frac{5}{2} \sqrt{\frac{e^{\sqrt{203/15} \pi} \sqrt{\frac{\phi}{203}}}{2 \sqrt[4]{5}} - 22}$$

Decimal approximation:

139.1560830146594354319465568452764690266115933026037262939...

139.156083....

Property:

$$\frac{5}{2} \sqrt{-22 + \frac{e^{\sqrt{203/15} \pi} \sqrt{\frac{\phi}{203}}}{2 \sqrt[4]{5}}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{5}{2} \sqrt{\frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{2030}} e^{\sqrt{203/15} \pi} - 22}$$

$$\frac{5}{2} \sqrt{\frac{\sqrt{\frac{1}{406} (1 + \sqrt{5})} e^{\sqrt{203/15} \pi}}{2 \sqrt[4]{5}} - 22}$$

$$\frac{1}{4} \sqrt{\frac{5}{203} \left(5^{3/4} \sqrt{406 (1 + \sqrt{5})} e^{\sqrt{203/15} \pi} - 89320 \right)}$$

Series representations:

$$\frac{1}{2} \sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7 \sqrt{5}} =$$

$$\frac{5}{2} \sqrt{-23 + \frac{\exp\left(\pi \sqrt{\frac{203}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{203}}} \sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} \left(-23 + \frac{\exp\left(\pi \sqrt{\frac{203}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{203}}\right)^{-k}$$

$$\frac{1}{2} \sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7 \sqrt{5}} =$$

$$\frac{5}{2} \sqrt{-23 + \frac{\exp\left(\pi \sqrt{\frac{203}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{203}}} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-23 + \frac{\exp\left(\pi \sqrt{\frac{203}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{203}}\right)^{-k}}{k!}$$

$$\frac{1}{2} \sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{203}{15}}\right)}{2 \sqrt[4]{5} \sqrt{203}} - 29 + 7 \sqrt{5}} =$$

$$\frac{5}{2} \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-22 + \frac{\exp\left(\pi \sqrt{\frac{203}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{203}} - z_0\right)^k}{k!} z_0^{-k}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

For 771.3345..., we obtain:

$$1/5(((\text{sqrt}(\text{golden ratio}) * \exp(\text{Pi} * \text{sqrt}(152/15))) / (2 * 5^{(1/4)} * \text{sqrt}(152)) + 11))) - 11 - 4$$

Where 11 and 4 are Lucas numbers

Input:

$$\frac{1}{5} \left(\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{152}{15}}\right)}{2 \sqrt[4]{5} \sqrt{152}} + 11 \right) - 11 - 4$$

ϕ is the golden ratio

Exact result:

$$\frac{1}{5} \left(\frac{e^{2 \sqrt{38/15} \pi} \sqrt{\frac{\phi}{38}}}{4 \sqrt[4]{5}} + 11 \right) - 15$$

Decimal approximation:

139.2669107441723722217545715003330917659171603186865735325...

139.26691....

Property:

$$-15 + \frac{1}{5} \left(11 + \frac{e^{2 \sqrt{38/15} \pi} \sqrt{\frac{\phi}{38}}}{4 \sqrt[4]{5}} \right) \text{ is a transcendental number}$$

Alternate forms:

$$\frac{e^{2 \sqrt{38/15} \pi} \sqrt{\frac{\phi}{38}}}{20 \sqrt[4]{5}} - \frac{64}{5}$$

$$\frac{5^{3/4} e^{2 \sqrt{38/15} \pi} \sqrt{38 \phi} + 8360}{3800} - 15$$

$$\frac{1}{40} \sqrt{\frac{1}{95} (5 + \sqrt{5})} e^{2 \sqrt{38/15} \pi} - \frac{64}{5}$$

Series representations:

$$\frac{1}{5} \left(\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{152}{15}}\right)}{2 \sqrt[4]{5} \sqrt{152}} + 11 \right) - 11 - 4 = \left(-640 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (152 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right. \\ \left. \exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{152}{15} - z_0\right)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left(50 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (152 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\frac{1}{5} \left(\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{152}{15}}\right)}{2 \sqrt[4]{5} \sqrt{152}} + 11 \right) - 11 - 4 = \\ \left(-640 \exp\left(i\pi \left\lfloor \frac{\arg(152 - x)}{2\pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (152 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\ \left. 5^{3/4} \exp\left(i\pi \left\lfloor \frac{\arg(\phi - x)}{2\pi} \right\rfloor\right) \exp\left(\pi \exp\left(i\pi \left\lfloor \frac{\arg\left(\frac{152}{15} - x\right)}{2\pi} \right\rfloor\right) \sqrt{x}\right) \right. \\ \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{152}{15} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\ \left(50 \exp\left(i\pi \left\lfloor \frac{\arg(152 - x)}{2\pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (152 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\frac{1}{5} \left(\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{152}{15}}\right)}{2 \sqrt[4]{5} \sqrt{152}} + 11 \right) - 11 - 4 =$$

$$\left(\left(\frac{1}{z_0}\right)^{-1/2 [\arg(152-z_0)/(2\pi)]} z_0^{-1/2 [\arg(152-z_0)/(2\pi)]} \left(-640 \left(\frac{1}{z_0}\right)^{1/2 [\arg(152-z_0)/(2\pi)]} \right. \right.$$

$$z_0^{1/2 [\arg(152-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (152-z_0)^k z_0^{-k}}{k!} +$$

$$5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(\frac{152}{15}-z_0)/(2\pi)]} z_0^{1/2 (1+[\arg(\frac{152}{15}-z_0)/(2\pi)])} \right.$$

$$\left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{152}{15}-z_0\right)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 [\arg(\phi-z_0)/(2\pi)]}$$

$$z_0^{1/2 [\arg(\phi-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \left. \right) \Bigg/$$

$$\left(50 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (152-z_0)^k z_0^{-k}}{k!} \right)$$

For 9914.26836..., we obtain:

$$\sqrt{\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{250}{15}}\right)}{2 \sqrt[4]{5} \sqrt{250}} - 76 - 3 - 2 + 29 + 11}$$

where 29 and 11 are Lucas numbers

Input:

$$\sqrt{\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{250}{15}}\right)}{2 \sqrt[4]{5} \sqrt{250}} - 76 - 3 - 2 + 29 + 11}$$

ϕ is the golden ratio

Exact result:

$$\sqrt{\frac{e^{5\sqrt{2/3}\pi} \sqrt{\frac{\phi}{2}}}{10 \times 5^{3/4}} - 81 + 40}$$

Decimal approximation:

139.5704191288665481900321865698209577071282492727801662146...

139.570419...

Property:

$$40 + \sqrt{-81 + \frac{e^{5\sqrt{2/3}\pi} \sqrt{\frac{\phi}{2}}}{10 \times 5^{3/4}}} \text{ is a transcendental number}$$

Alternate forms:

$$40 + \sqrt{\frac{1}{100} \sqrt{5 + \sqrt{5}} e^{5\sqrt{2/3}\pi} - 81}$$

$$40 + \frac{1}{10} \sqrt{\sqrt{5 + \sqrt{5}} e^{5\sqrt{2/3}\pi} - 8100}$$

$$40 + \sqrt{\frac{\sqrt{1 + \sqrt{5}} e^{5\sqrt{2/3}\pi}}{20 \times 5^{3/4}} - 81}$$

Series representations:

$$\sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{250}{15}}\right)}{2 \sqrt[4]{5} \sqrt{250}} - 76 - 3 - 2 + 29 + 11 =}$$

$$40 + \sqrt{-82 + \frac{\exp\left(\pi \sqrt{\frac{50}{3}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{250}} \sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} \left(-82 + \frac{\exp\left(\pi \sqrt{\frac{50}{3}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{250}}\right)^{-k}}$$

$$\sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{250}{15}}\right)}{2 \sqrt[4]{5} \sqrt{250}} - 76 - 3 - 2 + 29 + 11 =}$$

$$40 + \sqrt{-82 + \frac{\exp\left(\pi \sqrt{\frac{50}{3}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{250}} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-82 + \frac{\exp\left(\pi \sqrt{\frac{50}{3}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{250}}\right)^{-k}}{k!}}$$

$$\sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{250}{15}}\right)}{2 \sqrt[4]{5} \sqrt{250}} - 76 - 3 - 2 + 29 + 11 =}$$

$$40 + \sqrt{z_0 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-81 + \frac{\exp\left(\pi \sqrt{\frac{50}{3}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{250}} - z_0\right)^k}{k!} z_0^{-k}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

For 1717.1255..., we obtain:

$$3 * \sqrt{\left(\left(\sqrt{\text{golden ratio}} * \exp\left(\pi * \sqrt{\frac{181}{15}}\right)\right) / \left(2 * 5^{(1/4)} * \sqrt{181}\right) - 18\right)} + 11 + 4$$

Where 11 and 4 are Lucas numbers

Input:

$$3 \sqrt{\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{181}{15}}\right)}{2 \sqrt[4]{5} \sqrt{181}} - 18 + 11 + 4}$$

ϕ is the golden ratio

Exact result:

$$3 \sqrt[3]{\frac{e^{\sqrt{181/15} \pi} \sqrt{\frac{\phi}{181}}}{2 \sqrt[4]{5}} - 18 + 15}$$

Decimal approximation:

139.3146403219552378300821545642660695061741041646012700848...

139.31464.....

Property:

$$15 + 3 \sqrt[3]{-18 + \frac{e^{\sqrt{181/15} \pi} \sqrt{\frac{\phi}{181}}}{2 \sqrt[4]{5}}} \text{ is a transcendental number}$$

Alternate forms:

$$15 + 3 \sqrt[3]{\frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{1810}} e^{\sqrt{181/15} \pi} - 18}$$

$$15 + 3 \sqrt[3]{\frac{\sqrt{\frac{1}{362} (1 + \sqrt{5})} e^{\sqrt{181/15} \pi}}{2 \sqrt[4]{5}} - 18}$$

$$\frac{3 \left(9050 + \sqrt{905 \left(5^{3/4} \sqrt{362 (1 + \sqrt{5})} e^{\sqrt{181/15} \pi} - 65160 \right)} \right)}{1810}$$

Series representations:

$$3 \sqrt[3]{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{181}{15}}\right)}{2 \sqrt[4]{5} \sqrt{181}} - 18 + 11 + 4 =}$$

$$15 + 3 \sqrt[3]{-19 + \frac{\exp\left(\pi \sqrt{\frac{181}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{181}} \sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} \left(-19 + \frac{\exp\left(\pi \sqrt{\frac{181}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{181}} \right)^{-k}}$$

$$3 \sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{181}{15}}\right)}{2 \sqrt[4]{5} \sqrt{181}} - 18 + 11 + 4 =}$$

$$15 + 3 \sqrt{-19 + \frac{\exp\left(\pi \sqrt{\frac{181}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{181}}} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-19 + \frac{\exp\left(\pi \sqrt{\frac{181}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{181}}\right)^{-k}}{k!}$$

$$3 \sqrt{\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{181}{15}}\right)}{2 \sqrt[4]{5} \sqrt{181}} - 18 + 11 + 4 =}$$

$$15 + 3 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-18 + \frac{\exp\left(\pi \sqrt{\frac{181}{15}}\right) \sqrt{\phi}}{2 \sqrt[4]{5} \sqrt{181}} - z_0\right)^k z_0^{-k}}{k!}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

We observe that all the six results 139.2761604... 139.322761... 139.156083...

139.26691.... 139.570419... 139.31464..... are practically equal to the rest mass of Pion meson 139.57 and are all transcendental numbers

But what can be further obtained from this value, and why is it so recurrent? The average of the six results is:

$$\frac{1}{6} (139.2761604 + 139.322761 + 139.156083 + 139.26691 + 139.570419 + 139.31464)$$

139.3178289

139.3178289

Multiplying this value by **12.61803398... = 11 + golden ratio** and subtracting 29 (where 11 and 29 are Lucas numbers), we obtain:

$$(11 + \text{golden ratio}) (139.3178289) - 29$$

$$(11 + \phi) \times 139.3178289 - 29$$

1728.917100...

1728.9171....

This result, 1728.9171... is practically equal to the Hardy-Ramanujan number and very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem.

Furthermore, we have that performing the 10th root of this value, we obtain:

$(139.3178289)^{1/10}$

$\sqrt[10]{139.3178289}$

1.6383273063...

1.6383273063....result $\approx \zeta(2) = \frac{\pi^2}{6} = 1.644934 \dots$

COSMOLOGICAL APPLICATIONS OF RAMANUJAN'S MATHEMATICS

From:

Spectral distortions in CMB by the bulk Comptonization due to Zeldovich pancakes - *G.S. Bisnovatyi-Kogan* - arXiv:1902.01113v1 [astro-ph.CO] 4 Feb 2019

$$f(\tilde{\nu}) = \frac{C_f}{e^{\tilde{\nu}} - 1} \left[1 + \frac{1}{12} \frac{\beta_0 \tau}{1 + \frac{\beta_0 \tau}{4}} \frac{\tilde{\nu} e^{\tilde{\nu}}}{e^{\tilde{\nu}} - 1} \right]. \quad (26)$$

For $C_f = 0.7744$ and $\beta_0 \tau = 1.2$, we obtain:

$0.7744/(e^x-1) (((1+1/12*(1.2)/(1+(1.2/4))*(x*e^x)/(e^x-1))))$

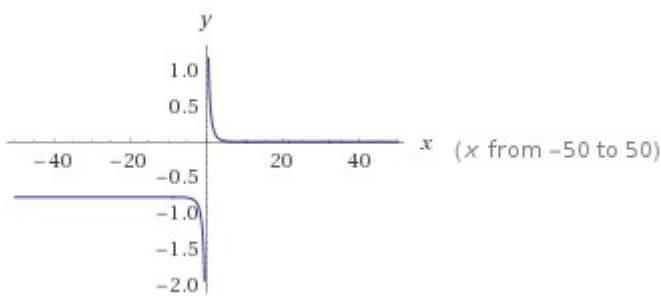
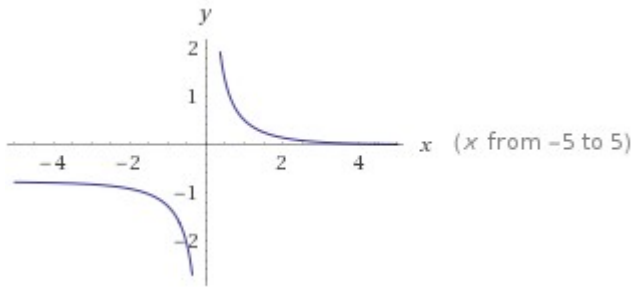
Input:

$$\frac{0.7744}{e^x - 1} \left(1 + \frac{1}{12} \times \frac{1.2}{1 + \frac{1.2}{4}} \times \frac{x e^x}{e^x - 1} \right)$$

Result:

$$\frac{0.7744 \left(\frac{0.0769231 e^x x}{e^x - 1} + 1 \right)}{e^x - 1}$$

Plots:



Alternate forms:

$$\frac{e^x (0.0595692 x + 0.7744) - 0.7744}{(e^x - 1)^2}$$

$$\frac{0.0595692 (e^x x + 13 \cdot e^x - 13)}{(e^x - 1)^2}$$

$$\frac{0.0595692 (13 (e^x - 1) + 1 \cdot e^x x)}{(e^x - 1)^2}$$

Expanded form:

$$\frac{0.0595692 e^x x}{(e^x - 1)^2} + \frac{0.7744}{e^x - 1}$$

Roots:

$$x \approx W_n(5.75137 \times 10^6) - 13, \quad 2.71828^{W_n(5.75137 \times 10^6)} - 442413. \neq 0$$

$W_k(z)$ is the analytic continuation of the product log function

Properties as a real function:

Domain

$$\{x \in \mathbb{R} : x \neq 0\}$$

Range

$$\{y \in \mathbb{R} : y < -\frac{484}{625} \text{ or } y > 0\}$$

\mathbb{R} is the set of real numbers

Series expansion at $x = 0$:

$$\frac{0.833969}{x} - 0.3872 + 0.0595692x - 0.00082735x^3 + O(x^4)$$

(Laurent series)

Derivative:

$$\frac{d}{dx} \left(\frac{0.7744 \left(1 + \frac{1.2(xe^x)}{12(1+\frac{1.2}{4})(e^x-1)} \right)}{e^x - 1} \right) = \frac{e^x (e^x (-0.0595692x - 0.714831) - 0.0595692x + 0.714831)}{(e^x - 1)^3}$$

Indefinite integral:

$$\int \frac{0.7744 \left(1 + \frac{0.0769231e^x x}{-1+e^x} \right)}{-1+e^x} dx = \left(-\frac{0.0595692}{2.71828^x - 1} - 0.833969 \right) x + 0.833969 \log(1 - 2.71828^x) + \text{constant}$$

(assuming a complex-valued logarithm)

$\log(x)$ is the natural logarithm

Limit:

$$\lim_{x \rightarrow -\infty} \frac{0.7744 \left(1 + \frac{0.0769231e^x x}{-1+e^x} \right)}{-1+e^x} = -0.7744$$

$$\lim_{x \rightarrow \infty} \frac{0.7744 \left(1 + \frac{0.0769231 e^x x}{-1+e^x}\right)}{-1 + e^x} = 0 \approx 0$$

Alternative representations:

$$\frac{\left(1 + \frac{1.2(x e^x)}{12\left(1+\frac{1.2}{4}\right)(e^x-1)}\right) 0.7744}{e^x - 1} = \frac{\left(1 + \frac{1.2(x z^x)}{12\left(1+\frac{1.2}{4}\right)(z^x-1)}\right) 0.7744}{z^x - 1} \quad \text{for } z = e$$

$$\frac{\left(1 + \frac{1.2(x e^x)}{12\left(1+\frac{1.2}{4}\right)(e^x-1)}\right) 0.7744}{e^x - 1} = \frac{\left(1 + \frac{1.2(x w^a)}{12\left(1+\frac{1.2}{4}\right)(w^a-1)}\right) 0.7744}{w^a - 1} \quad \text{for } a = \frac{x}{\log(w)}$$

$$\frac{\left(1 + \frac{1.2(x e^x)}{12\left(1+\frac{1.2}{4}\right)(e^x-1)}\right) 0.7744}{e^x - 1} = \frac{0.7744 \left(1 + \frac{1.2 x \left(1 + \frac{2}{-1 + \coth\left(\frac{x}{2}\right)}\right)}{12\left(1+\frac{1.2}{4}\right) 2 \frac{-1 + \coth\left(\frac{x}{2}\right)}{2}}\right)}{\frac{2}{-1 + \coth\left(\frac{x}{2}\right)}}$$

Definite integral after subtraction of diverging parts:

$$\int_0^\infty \left(\frac{0.7744 \left(1 + \frac{0.0769231 e^x x}{-1+e^x}\right)}{-1 + e^x} - \left(\frac{0.7744}{-1 + e^x} + \frac{0.0595692 e^x x}{(-1 + e^x)^2} \right) \right) dx = 0$$

From:

$$x \approx W_{-n}(5.75137 \times 10^6) - 13$$

Input interpretation:

$$-13 + W_n(5.75137 \times 10^6)$$

$W_k(z)$ is the analytic continuation of the product log function

Values:

n	1	2	3	4	5
$W_n\left(5.75137 \times 10^6\right) - 13$	-0.086848 + 5.85735 i	-0.288973 + 11.8174 i	-0.517543 + 17.888 i	-0.730323 + 24.034 i	-0.917853 + 30.2254 i

Global maximum:

$$\max\{W_n(5\,751\,370) - 13\} = W(5\,751\,370) - 13 \text{ at } n = 0$$

$W(z)$ is the product log function

Global minimum:

$$\min\{W_n(5\,751\,370) - 13\} = W(5\,751\,370) - 13 \text{ at } n = 0$$

Now, we have that:

$$\left(\frac{0.7744}{e^{-0.086848+5.85735i}-1}\right) * \left(\frac{1+1/12*(1.2/(1+(1.2/4)))}{1+\frac{1.2}{4}}\right) * \left(\frac{(-0.086848+5.85735i)*e^{-0.086848+5.85735i}}{e^{-0.086848+5.85735i}-1}\right)$$

Input interpretation:

$$\frac{0.7744}{e^{-0.086848+5.85735i}-1} \left(1 + \frac{1}{12} \times \frac{1.2}{1+\frac{1.2}{4}} \times \frac{(-0.086848+5.85735i)e^{-0.086848+5.85735i}}{e^{-0.086848+5.85735i}-1}\right)$$

i is the imaginary unit

Result:

$$0.0000174964... - 0.0000129317... i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 0.0000217567 \text{ (radius), } \theta = -36.4684^\circ \text{ (angle)}$$

0.0000217567

Alternative representation:

$$\frac{\left(1 + \frac{1.2(-0.086848+5.85735 i)e^{-0.086848+5.85735 i}}{12\left(1+\frac{1.2}{4}\right)\left(e^{-0.086848+5.85735 i_{-1}}\right)}\right)0.7744}{e^{-0.086848+5.85735 i} - 1} = \frac{\left(1 + \frac{1.2(-0.086848+5.85735 i)\exp^{-0.086848+5.85735 i(z)}}{12\left(1+\frac{1.2}{4}\right)\left(\exp^{-0.086848+5.85735 i(z)-1}\right)}\right)0.7744}{\exp^{-0.086848+5.85735 i(z)} - 1} \text{ for } z = 1$$

Series representations:

$$\frac{\left(1 + \frac{1.2(-0.086848+5.85735 i)e^{-0.086848+5.85735 i}}{12\left(1+\frac{1.2}{4}\right)\left(e^{-0.086848+5.85735 i_{-1}}\right)}\right)0.7744}{e^{-0.086848+5.85735 i} - 1} = -\left(\left(0.7744\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.173696} - 0.993319\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.086848+5.85735 i} - 0.450565 i\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.086848+5.85735 i}\right) / \left(\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.086848} - \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{5.85735 i^2}\right)\right)$$

$$\frac{\left(1 + \frac{1.2(-0.086848+5.85735 i)e^{-0.086848+5.85735 i}}{12\left(1+\frac{1.2}{4}\right)\left(e^{-0.086848+5.85735 i_{-1}}\right)}\right)0.7744}{e^{-0.086848+5.85735 i} - 1} = -\left(\left(0.7744\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.173696} - 0.993319\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.086848+5.85735 i} - 0.450565 i\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.086848+5.85735 i}\right) / \left(\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.086848} - \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{5.85735 i^2}\right)\right)$$

$$\frac{\left(1 + \frac{1.2(-0.086848+5.85735 i)e^{-0.086848+5.85735 i}}{12\left(1+\frac{1.2}{4}\right)\left(e^{-0.086848+5.85735 i_{-1}}\right)}\right)0.7744}{e^{-0.086848+5.85735 i} - 1} = \left(0.348918\left(-2.21943\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.173696} + 2.20461\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.086848+5.85735 i} + i\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.086848+5.85735 i}\right) / \left(-\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.086848} + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{5.85735 i^2}\right)\right)$$

$$[\left(\frac{0.7744}{e^{-0.086848+5.85735i}-1}\right) * \left(\frac{(1+\frac{1}{12} * (\frac{1.2}{1+(\frac{1.2}{4}))}) * ((-0.086848+5.85735i) * e^{-0.086848+5.85735i})}{(e^{-0.086848+5.85735i}-1)}\right) \right]^{1/(64^2 * 8)}$$

Input interpretation:

$$\left(\frac{0.7744}{e^{-0.086848+5.85735i}-1} \left(1 + \frac{1}{12} \times \frac{1.2}{1+\frac{1.2}{4}} \times \frac{(-0.086848+5.85735i)e^{-0.086848+5.85735i}}{e^{-0.086848+5.85735i}-1} \right) \right)^{\frac{1}{64^2 \times 8}}$$

i is the imaginary unit

Result:

0.999672... -
0.0000194179... *i*

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

r = 0.999672 (radius), *θ* = -0.00111293° (angle)

0.999672 result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

From the inversion, we obtain:

$$1/[\left(\frac{0.7744}{e^{-0.086848+5.85735i}-1}\right) * \left(\frac{(1+\frac{1}{12} * (\frac{1.2}{1+(\frac{1.2}{4}))}) * ((-0.086848+5.85735i) * e^{-0.086848+5.85735i})}{(e^{-0.086848+5.85735i}-1)}\right) \right]$$

Input interpretation:

$$\frac{1}{\frac{0.7744}{e^{-0.086848+5.85735i}-1} \left(1 + \frac{1}{12} \times \frac{1.2}{1+\frac{1.2}{4}} \times \frac{(-0.086848+5.85735i)e^{-0.086848+5.85735i}}{e^{-0.086848+5.85735i}-1} \right)}$$

i is the imaginary unit

Result:

36962.7044800993722034825744870185106833352857721026166116... +
 27319.3785617287432693543536971720283618893708915266875571... i

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$r = 45962.9$ (radius), $\theta = 36.4684^\circ$ (angle)

45962.9

Alternative representation:

$$\frac{1}{\left(1 + \frac{1.2 \left((-0.086848 + 5.85735 i) e^{-0.086848 + 5.85735 i} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(e^{-0.086848 + 5.85735 i} \right)} \right)^{0.7744}} e^{-0.086848 + 5.85735 i} =$$

$$\frac{1}{\left(1 + \frac{1.2 \left((-0.086848 + 5.85735 i) \exp^{-0.086848 + 5.85735 i(z)} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(\exp^{-0.086848 + 5.85735 i(z-1)} \right)} \right)^{0.7744}} \exp^{-0.086848 + 5.85735 i(z-1)} \quad \text{for } z = 1$$

Series representations:

$$\frac{1}{\left(1 + \frac{1.2 \left((-0.086848 + 5.85735 i) e^{-0.086848 + 5.85735 i} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(e^{-0.086848 + 5.85735 i} \right)} \right)^{0.7744}} e^{-0.086848 + 5.85735 i} =$$

$$\left(2.866 \left(- \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{0.086848} + \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{5.85735 i} \right)^2 \right) / \left(\left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{0.086848} \right)$$

$$\left(-2.21943 \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{0.086848} + 2.20461 \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{5.85735 i} + i \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{5.85735 i} \right)$$

$$\begin{aligned}
& \frac{1}{\left(1 + \frac{1.2(-0.086848 + 5.85735i)e^{-0.086848 + 5.85735i}}{12\left(1 + \frac{1.2}{4}\right)(e^{-0.086848 + 5.85735i})}\right)^{0.7744}} = \\
& \frac{1}{e^{-0.086848 + 5.85735i}} \left(2.866 \left(-\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.086848} + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{5.85735i} \right)^2 \right) / \\
& \left(\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.086848} \left(-2.21943 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.086848} + \right. \right. \\
& \left. \left. 2.20461 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{5.85735i} + i \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{5.85735i} \right) \right) \\
& \frac{1}{\left(1 + \frac{1.2(-0.086848 + 5.85735i)e^{-0.086848 + 5.85735i}}{12\left(1 + \frac{1.2}{4}\right)(e^{-0.086848 + 5.85735i})}\right)^{0.7744}} = \\
& \frac{1}{e^{-0.086848 + 5.85735i}} \left(-\left(1.29132 \times 2^{-5.85735i} \left(2^{5.85735i} \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{0.086848} - 1.06205 \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{5.85735i} \right)^2 \right) / \right. \\
& \left(\left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{0.086848} \left(2^{5.85735i} \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{0.086848} - \right. \right. \\
& \left. \left. 1.05495 \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{5.85735i} - 0.478522i \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{5.85735i} \right) \right) \right)
\end{aligned}$$

Note that, from the formula concerning the Coefficients of the '5th order' mock theta function $\psi_1(q)$, for $n = 318$, and performing calculations with the Fibonacci numbers 8, 5 and 21, we obtain:

$$\sqrt{\phi} \times \exp(\pi \sqrt{\frac{318}{15}}) / (2 \cdot 5^{1/4} \cdot \sqrt{318}) + 8^2 \cdot 5 - 21$$

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{318}{15}}\right)}{2 \sqrt[4]{5} \sqrt{318}} + 8^2 \times 5 - 21$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{\sqrt{106/5} \pi} \sqrt{\frac{\phi}{318}}}{2 \sqrt[4]{5}} + 299$$

Decimal approximation:

45962.40172081978946797289972227124481441370285990011194842...

45962.4017208...

Property:

$299 + \frac{e^{\sqrt{106/5} \pi} \sqrt{\frac{\phi}{318}}}{2 \sqrt[4]{5}}$ is a transcendental number

Alternate forms:

$$299 + \frac{1}{4} \sqrt{\frac{1}{795} (5 + \sqrt{5})} e^{\sqrt{106/5} \pi}$$

$$299 + \frac{\sqrt{\frac{1}{159} (1 + \sqrt{5})} e^{\sqrt{106/5} \pi}}{4 \sqrt[4]{5}}$$

$$\frac{950820 + 5^{3/4} \sqrt{159 (1 + \sqrt{5})} e^{\sqrt{106/5} \pi}}{3180}$$

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{318}{15}}\right)}{2 \sqrt[4]{5} \sqrt{318}} + 8^2 \times 5 - 21 = \left(2990 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (318 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right. \\ \left. \exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{106}{5} - z_0\right)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (318 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{318}{15}}\right)}{2 \sqrt[4]{5} \sqrt{318}} + 8^2 \times 5 - 21 = \\
& \left(2990 \exp\left(i \pi \left\lfloor \frac{\arg(318-x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (318-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\
& \quad 5^{3/4} \exp\left(i \pi \left\lfloor \frac{\arg(\phi-x)}{2 \pi} \right\rfloor\right) \exp\left(\pi \exp\left(i \pi \left\lfloor \frac{\arg\left(\frac{106}{5}-x\right)}{2 \pi} \right\rfloor\right) \sqrt{x}\right) \\
& \quad \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{106}{5}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \sum_{k=0}^{\infty} \frac{(-1)^k (\phi-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\
& \left(10 \exp\left(i \pi \left\lfloor \frac{\arg(318-x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (318-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)
\end{aligned}$$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{318}{15}}\right)}{2 \sqrt[4]{5} \sqrt{318}} + 8^2 \times 5 - 21 = \\
& \left(\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(318-z_0)/(2\pi) \rfloor} z_0^{-1/2 \lfloor \arg(318-z_0)/(2\pi) \rfloor} \left(2990 \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(318-z_0)/(2\pi) \rfloor} \right. \right. \\
& \quad \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (318-z_0)^k z_0^{-k}}{k!} + \right. \\
& \quad 5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg\left(\frac{106}{5}-z_0\right)/(2\pi) \rfloor} z_0^{1/2 \lfloor 1+\arg\left(\frac{106}{5}-z_0\right)/(2\pi) \rfloor} \right. \\
& \quad \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{106}{5}-z_0\right)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(\phi-z_0)/(2\pi) \rfloor} \\
& \quad \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \right) / \\
& \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (318-z_0)^k z_0^{-k}}{k!} \right)
\end{aligned}$$

or:

$$\left(\frac{0.7744}{e^{(-0.917853+30.2254i)}-1} \right) \left(\frac{1+1/12 \cdot (1.2/(1+(1.2/4)))}{e^{(-0.917853+30.2254i)}} \right) \left(\frac{e^{(-0.917853+30.2254i)}}{e^{(-0.917853+30.2254i)}-1} \right)$$

Input interpretation:

$$\frac{0.7744}{e^{-0.917853+30.2254 i} - 1} \left(1 + \frac{1}{12} \times \frac{1.2}{1 + \frac{1.2}{4}} \times \frac{(-0.917853 + 30.2254 i) e^{-0.917853+30.2254 i}}{e^{-0.917853+30.2254 i} - 1} \right)$$

i is the imaginary unit

Result:

$$-5.95448... \times 10^{-6} - 4.17010... \times 10^{-6} i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 7.2695 \times 10^{-6} \text{ (radius), } \theta = -144.995^\circ \text{ (angle)}$$

$$7.2695 * 10^{-6}$$

Alternative representation:

$$\frac{\left(1 + \frac{1.2(-0.917853+30.2254 i) e^{-0.917853+30.2254 i}}{12 \left(1 + \frac{1.2}{4} \right) (e^{-0.917853+30.2254 i} - 1)} \right) 0.7744}{e^{-0.917853+30.2254 i} - 1} = \frac{\left(1 + \frac{1.2(-0.917853+30.2254 i) \exp^{-0.917853+30.2254 i(z)}}{12 \left(1 + \frac{1.2}{4} \right) (\exp^{-0.917853+30.2254 i(z)} - 1)} \right) 0.7744}{\exp^{-0.917853+30.2254 i(z)} - 1} \text{ for } z = 1$$

Series representations:

$$\frac{\left(1 + \frac{1.2(-0.917853+30.2254 i) e^{-0.917853+30.2254 i}}{12 \left(1 + \frac{1.2}{4} \right) (e^{-0.917853+30.2254 i} - 1)} \right) 0.7744}{e^{-0.917853+30.2254 i} - 1} = - \left(\left(0.7744 \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{1.83571} - 0.929396 \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{0.917853+30.2254 i} - 2.32503 i \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{0.917853+30.2254 i} \right) \right) / \left(\left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{0.917853} - \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{30.2254 i} \right)^2$$

$$\frac{\left(1 + \frac{1.2 \left((-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(e^{-0.917853 + 30.2254 i} - 1 \right)} \right) 0.7744}{e^{-0.917853 + 30.2254 i} - 1} =$$

$$- \left(\left(0.7744 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{1.83571} - 0.929396 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853 + 30.2254 i} - \right. \right.$$

$$\left. \left. 2.32503 i \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853 + 30.2254 i} \right) \right) /$$

$$\left(\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853} - \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{30.2254 i} \right)^2$$

$$\frac{\left(1 + \frac{1.2 \left((-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(e^{-0.917853 + 30.2254 i} - 1 \right)} \right) 0.7744}{e^{-0.917853 + 30.2254 i} - 1} =$$

$$\left(1.8005 \left(-0.430102 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{1.83571} + 0.399735 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853 + 30.2254 i} + \right. \right.$$

$$\left. \left. i \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853 + 30.2254 i} \right) \right) /$$

$$\left(- \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853} + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{30.2254 i} \right)^2$$

From the formula

$$\delta_{Bulk} = \frac{f_1(\tilde{\nu})}{f_0(\tilde{\nu})} = \frac{1}{12} \frac{\beta_0 \tau}{1 + \frac{\beta_0 \tau}{4}} \frac{\tilde{\nu} e^{\tilde{\nu}}}{e^{\tilde{\nu}} - 1}. \quad (33)$$

we obtain:

$$1/12 * (1.2 / (1 + (1.2/4))) * (((-0.917853 + 30.2254i) * e^{(-0.917853 + 30.2254i)})) / (((e^{(-0.917853 + 30.2254i)} - 1)))$$

Input interpretation:

$$\frac{1}{12} \times \frac{1.2}{1 + \frac{1.2}{4}} \times \frac{(-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i}}{e^{-0.917853 + 30.2254 i} - 1}$$

i is the imaginary unit

Result:

$$-0.999995... + 7.43819... \times 10^{-6} i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 0.999995 \text{ (radius), } \theta = 180.^\circ \text{ (angle)}$$

0.999995

Alternative representation:

$$\frac{1.2 (-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i}}{\left(1 + \frac{1.2}{4}\right) (e^{-0.917853 + 30.2254 i} - 1)} 12 = \frac{1.2 (-0.917853 + 30.2254 i) \exp^{-0.917853 + 30.2254 i(z)}}{\left(1 + \frac{1.2}{4}\right) (\exp^{-0.917853 + 30.2254 i(z)} - 1)} 12 \text{ for } z = 1$$

Series representations:

$$\frac{1.2 (-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i}}{\left(1 + \frac{1.2}{4}\right) (e^{-0.917853 + 30.2254 i} - 1)} 12 = \frac{2.32503 (-0.0303669 + i) \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{30.2254 i}}{-\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.917853} + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{30.2254 i}}$$

$$\frac{1.2 (-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i}}{\left(1 + \frac{1.2}{4}\right) (e^{-0.917853 + 30.2254 i} - 1)} 12 = \frac{2.32503 (-0.0303669 + i) \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{30.2254 i}}{-\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.917853} + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{30.2254 i}}$$

$$\frac{1.2 (-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i}}{\left(1 + \frac{1.2}{4}\right) (e^{-0.917853 + 30.2254 i} - 1)} 12 = \frac{2.32503 (-0.0303669 + i) \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{30.2254 i}}{-0.529296 e^{20.9507 i} \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{0.917853} + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{30.2254 i}}$$

$$[1/12*(1.2/(1+(1.2/4)))*((-0.917853+30.2254i)*e^{(-0.917853+30.2254i)})/(((e^{(-0.917853+30.2254i)}-1)))]^{64}$$

Input interpretation:

$$\left(\frac{1}{12} \times \frac{1.2}{1 + \frac{1.2}{4}} \times \frac{(-0.917853 + 30.2254i) e^{-0.917853+30.2254i}}{e^{-0.917853+30.2254i} - 1} \right)^{64}$$

i is the imaginary unit

Result:

$$0.999709... - 0.000475908... i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 0.999709 \text{ (radius), } \theta = -0.0272755^\circ \text{ (angle)}$$

0.999709 result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}}}{1 + \sqrt[5]{\sqrt{\varphi^5 4 \sqrt{5^3} - 1}} - \varphi + 1} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

From the formula

$$f_{ETH}(\tilde{\nu}) = \frac{\tilde{\nu}^3}{e^{\tilde{\nu}} - 1} \left\{ 1 + y\tilde{\nu} \frac{e^{\tilde{\nu}}}{e^{\tilde{\nu}} - 1} \left[\frac{\tilde{\nu}}{\tanh(\tilde{\nu}/2)} - 4 \right] \right\}. \tag{32}$$

we obtain:

$$((-0.917853+30.2254i)^3/(e^{(-0.917853+30.2254i)}-1))*((((1+1/60*(-0.917853+30.2254i)*(e^{(-0.917853+30.2254i)})/(e^{(-0.917853+30.2254i)}-1))*((-0.917853+30.2254i)/(tanh((-0.917853+30.2254i)/2))-4))))))$$

Input interpretation:

$$\frac{(-0.917853 + 30.2254 i)^3}{e^{-0.917853+30.2254 i} - 1} \left(\left(1 + \frac{1}{60} \times (-0.917853 + 30.2254 i) \times \frac{e^{-0.917853+30.2254 i}}{e^{-0.917853+30.2254 i} - 1} \right) \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} \times (-0.917853 + 30.2254 i)\right)} - 4 \right) \right)$$

$\tanh(x)$ is the hyperbolic tangent function

i is the imaginary unit

Result:

$$4.56033... \times 10^5 - 8.65133... \times 10^5 i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 977968. \text{ (radius), } \theta = -62.2052^\circ \text{ (angle)}$$

977968

Alternative representations:

$$\left(\left(\left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853+30.2254 i}}{60 (e^{-0.917853+30.2254 i} - 1)} \right) \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} (-0.917853 + 30.2254 i)\right)} - 4 \right) \right) (-0.917853 + 30.2254 i)^3 \right) / (e^{-0.917853+30.2254 i} - 1) =$$

$$\left((-0.917853 + 30.2254 i)^3 \left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853+30.2254 i}}{60 (-1 + e^{-0.917853+30.2254 i})} \right) \left(-4 + \frac{-0.917853 + 30.2254 i}{-1 + \frac{2}{1+e^{0.917853-30.2254 i}}} \right) \right) / (-1 + e^{-0.917853+30.2254 i})$$

$$\left(\left(\left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853+30.2254 i}}{60 (e^{-0.917853+30.2254 i} - 1)} \right) \right. \right. \\ \left. \left. \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} (-0.917853 + 30.2254 i)\right)} - 4 \right) \right) \right) \\ (-0.917853 + 30.2254 i)^3 \Big/ (e^{-0.917853+30.2254 i} - 1) = \\ \left((-0.917853 + 30.2254 i)^3 \left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853+30.2254 i}}{60 (-1 + e^{-0.917853+30.2254 i})} \right) \right) \\ \left(-4 + \frac{-0.917853 + 30.2254 i}{\frac{1}{\coth\left(\frac{1}{2} (-0.917853+30.2254 i)\right)}} \right) \Big/ (-1 + e^{-0.917853+30.2254 i})$$

$$\left(\left(\left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853+30.2254 i}}{60 (e^{-0.917853+30.2254 i} - 1)} \right) \right. \right. \\ \left. \left. \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} (-0.917853 + 30.2254 i)\right)} - 4 \right) \right) \right) \\ (-0.917853 + 30.2254 i)^3 \Big/ (e^{-0.917853+30.2254 i} - 1) = \\ \left((-0.917853 + 30.2254 i)^3 \left(-4 + \frac{-0.917853 + 30.2254 i}{\coth\left(\frac{1}{2} (-0.917853 + 30.2254 i) - \frac{i\pi}{2}\right)} \right) \right) \\ \left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853+30.2254 i}}{60 (-1 + e^{-0.917853+30.2254 i})} \right) \Big/ (-1 + e^{-0.917853+30.2254 i})$$

Series representations:

$$\left(\left(\left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853+30.2254 i}}{60 (e^{-0.917853+30.2254 i} - 1)} \right) \right. \right. \\ \left. \left. \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} (-0.917853 + 30.2254 i)\right)} - 4 \right) \right) \right) \\ (-0.917853 + 30.2254 i)^3 \Big/ (e^{-0.917853+30.2254 i} - 1) = \\ \left((-0.917853 + 30.2254 i)^3 \left(1 + \frac{e^{-0.917853+30.2254 i} (-0.917853 + 30.2254 i)}{60 (-1 + e^{-0.917853+30.2254 i})} \right) \right) \\ \left(-4 + \frac{-0.917853 + 30.2254 i}{-1 - 2 \sum_{k=1}^{\infty} (-1)^k q^{2k}} \right) \Big/ \\ (-1 + e^{-0.917853+30.2254 i}) \text{ for } q = -0.523265 + 0.354358 i$$

$$\left(\left(\left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i}}{60 (e^{-0.917853 + 30.2254 i} - 1)} \right) \right. \right. \\ \left. \left. \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} (-0.917853 + 30.2254 i)\right)} - 4 \right) \right) \right) \\ (-0.917853 + 30.2254 i)^3 \Big/ (e^{-0.917853 + 30.2254 i} - 1) = \\ \left((-0.917853 + 30.2254 i)^3 \left(1 + \frac{0.503757 e^{30.2254 i} (-0.0303669 + i)}{-e^{0.917853} + e^{30.2254 i}} \right) \right. \\ \left. \left(-4 + \frac{-0.917853 + 30.2254 i}{-1 + 2 \sum_{k=0}^{\infty} (-1)^k \mathcal{A}^{(-0.917853 + 30.2254 i)(1+k)}} \right) \right) \Big/ (-1 + e^{-0.917853 + 30.2254 i})$$

$$\left(\left(\left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i}}{60 (e^{-0.917853 + 30.2254 i} - 1)} \right) \right. \right. \\ \left. \left. \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} (-0.917853 + 30.2254 i)\right)} - 4 \right) \right) \right) \\ (-0.917853 + 30.2254 i)^3 \Big/ (e^{-0.917853 + 30.2254 i} - 1) = \\ \left((-0.917853 + 30.2254 i)^3 \left(1 + \frac{0.503757 e^{30.2254 i} (-0.0303669 + i)}{-e^{0.917853} + e^{30.2254 i}} \right) \right. \\ \left. \left(-4 + \frac{1}{4 \sum_{k=1}^{\infty} \frac{1}{(0.917853 - 30.2254 i)^2 + (1-2k)^2 \pi^2}} \right) \right) \Big/ (-1 + e^{-0.917853 + 30.2254 i})$$

Integral representation:

$$\left(\left(\left(1 + \frac{(-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i}}{60 (e^{-0.917853 + 30.2254 i} - 1)} \right) \right. \right. \\ \left. \left. \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} (-0.917853 + 30.2254 i)\right)} - 4 \right) \right) \right) \\ (-0.917853 + 30.2254 i)^3 \Big/ (e^{-0.917853 + 30.2254 i} - 1) = \\ \left((-0.917853 + 30.2254 i)^3 \left(1 + \frac{e^{-0.917853 + 30.2254 i} (-0.917853 + 30.2254 i)}{60 (-1 + e^{-0.917853 + 30.2254 i})} \right) \right. \\ \left. \left(-4 + \frac{-0.917853 + 30.2254 i}{\int_b^{\frac{1}{2} (-0.917853 + 30.2254 i)} \operatorname{sech}^2(t) dt} \right) \right) \Big/ (-1 + e^{-0.917853 + 30.2254 i})$$

From which:

$$\sqrt{977968}$$

Input:

$$\sqrt{977968}$$

Result:

$$4\sqrt{61123}$$

Decimal approximation:

988.9226461154583146165859860316604817912803577021468700549...

988.92264611...

From which:

$$1/8*\sqrt{977968}+\text{golden ratio}$$

Input:

$$\frac{1}{8}\sqrt{977968} + \phi$$

ϕ is the golden ratio

Result:

$$\phi + \frac{\sqrt{61123}}{2}$$

Decimal approximation:

125.2333647531821841752778350883231983416303538925741216190...

125.23336475... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

Alternate forms:

$$\frac{1}{2}(\sqrt{61123} + 1 + \sqrt{5})$$

$$\frac{1}{2}(2\phi + \sqrt{61123})$$

$$\frac{1}{2} \left(1 + \sqrt{2 \left(30564 + \sqrt{305615} \right)} \right)$$

Minimal polynomial:

$$16x^4 - 32x^3 - 489000x^2 + 489016x + 3735287669$$

Series representations:

$$\frac{\sqrt{977968}}{8} + \phi = \phi + \frac{1}{8} \sqrt{977967} \sum_{k=0}^{\infty} 977967^{-k} \binom{\frac{1}{2}}{k}$$

$$\frac{\sqrt{977968}}{8} + \phi = \phi + \frac{1}{8} \sqrt{977967} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{977967}\right)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$\frac{\sqrt{977968}}{8} + \phi = \phi + \frac{\sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 977967^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{16\sqrt{\pi}}$$

And:

$$1/8 * \sqrt{977968} + 13 + \pi$$

Input:

$$\frac{1}{8} \sqrt{977968} + 13 + \pi$$

Result:

$$13 + \frac{\sqrt{61123}}{2} + \pi$$

Decimal approximation:

139.7569234180220825655358916372370631081072141121434645778...

139.7569234... result practically equal to the rest mass of Pion meson 139.57 MeV

Property:

$13 + \frac{\sqrt{61123}}{2} + \pi$ is a transcendental number

Alternate forms:

$$\frac{1}{2} \left(\sqrt{61123} + 26 + 2\pi \right)$$

$$\frac{1}{2} \left(26 + \sqrt{61123} \right) + \pi$$

Series representations:

$$\frac{\sqrt{977968}}{8} + 13 + \pi = 13 + \pi + \frac{1}{8} \sqrt{977967} \sum_{k=0}^{\infty} 977967^{-k} \binom{\frac{1}{2}}{k}$$

$$\frac{\sqrt{977968}}{8} + 13 + \pi = 13 + \pi + \frac{1}{8} \sqrt{977967} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{977967}\right)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$\frac{\sqrt{977968}}{8} + 13 + \pi = 13 + \pi + \frac{\sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 977967^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{16 \sqrt{\pi}}$$

Note that, from the formula concerning the Coefficients of the '5th order' mock theta function $\psi_1(q)$, for $n = 161$, we obtain:

$$\sqrt{\phi} \times \exp(\pi \sqrt{\frac{161}{15}}) / (2 \cdot 5^{1/4} \cdot \sqrt{161})$$

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{161}{15}}\right)}{2 \sqrt[4]{5} \sqrt{161}}$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{\sqrt{161/15} \pi} \sqrt{\frac{\phi}{161}}}{2 \sqrt[4]{5}}$$

Decimal approximation:

989.1139226912270618582583933900009064774141355274909551997...

989.1139226...

Property:

$$\frac{e^{\sqrt{161/15} \pi} \sqrt{\frac{\phi}{161}}}{2 \sqrt[4]{5}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{1610}} e^{\sqrt{161/15} \pi}$$

$$\frac{\sqrt{\frac{1}{322} (1 + \sqrt{5})} e^{\sqrt{161/15} \pi}}{2 \sqrt[4]{5}}$$

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{161}{15}}\right)}{2 \sqrt[4]{5} \sqrt{161}} = \frac{\exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{161}{15} - z_0\right)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!}}{2 \sqrt[4]{5} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (161 - z_0)^k z_0^{-k}}{k!}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{161}{15}}\right)}{2 \sqrt[4]{5} \sqrt{161}} = \left(\exp\left(i \pi \left\lfloor \frac{\arg(\phi - x)}{2 \pi} \right\rfloor\right) \exp\left(\pi \exp\left(i \pi \left\lfloor \frac{\arg\left(\frac{161}{15} - x\right)}{2 \pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{161}{15} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \left(2 \sqrt[4]{5} \exp\left(i \pi \left\lfloor \frac{\arg(161 - x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (161 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{161}{15}}\right)}{2 \sqrt[4]{5} \sqrt{161}} = \left(\exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg\left(\frac{161}{15} - z_0\right) / (2 \pi) \rfloor} z_0^{1/2 (1 + \lfloor \arg\left(\frac{161}{15} - z_0\right) / (2 \pi) \rfloor)} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{161}{15} - z_0\right)^k z_0^{-k}}{k!}\right) \left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(161 - z_0) / (2 \pi) \rfloor + 1/2 \lfloor \arg(\phi - z_0) / (2 \pi) \rfloor} z_0^{-1/2 \lfloor \arg(161 - z_0) / (2 \pi) \rfloor + 1/2 \lfloor \arg(\phi - z_0) / (2 \pi) \rfloor} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \left(2 \sqrt[4]{5} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (161 - z_0)^k z_0^{-k}}{k!} \right)$$

Now, we have that:

$$\frac{1}{e^{\tilde{\nu}} - 1} \left\{ 1 + y\tilde{\nu} \frac{e^{\tilde{\nu}}}{e^{\tilde{\nu}} - 1} \left[\frac{\tilde{\nu}}{\tanh(\tilde{\nu}/2)} - 4 \right] \right\}. \quad (31)$$

$$(1/(e^{(-0.917853+30.2254i)}-1))*((((1+1/60*(-0.917853+30.2254i)*(e^{(-0.917853+30.2254i)})/(e^{(-0.917853+30.2254i)}-1))*((-0.917853+30.2254i)/(tanh((-0.917853+30.2254i)/2))-4))))))$$

Input interpretation:

$$\frac{1}{e^{-0.917853+30.2254i} - 1} \left(\left(1 + \frac{1}{60} \times (-0.917853 + 30.2254i) \times \frac{e^{-0.917853+30.2254i}}{e^{-0.917853+30.2254i} - 1} \right) \left(\frac{-0.917853 + 30.2254i}{\tanh\left(\frac{1}{2} \times (-0.917853 + 30.2254i)\right)} - 4 \right) \right)$$

$\tanh(x)$ is the hyperbolic tangent function

i is the imaginary unit

Result:

$$32.6574... + 13.5784... i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 35.3678 \text{ (radius)}, \quad \theta = 22.5767^\circ \text{ (angle)}$$

35.3678

Alternative representations:

$$\frac{\left(1 + \frac{(-0.917853+30.2254i)e^{-0.917853+30.2254i}}{60(e^{-0.917853+30.2254i}-1)} \right) \left(\frac{-0.917853+30.2254i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254i)\right)} - 4 \right)}{e^{-0.917853+30.2254i} - 1} = \frac{\left(1 + \frac{(-0.917853+30.2254i)e^{-0.917853+30.2254i}}{60(-1+e^{-0.917853+30.2254i})} \right) \left(-4 + \frac{-0.917853+30.2254i}{-1+\frac{2}{1+e^{0.917853-30.2254i}}} \right)}{-1 + e^{-0.917853+30.2254i}}$$

$$\begin{aligned}
& \frac{\left(1 + \frac{(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{60(e^{-0.917853+30.2254 i}-1)}\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right)}{e^{-0.917853+30.2254 i} - 1} = \\
& \frac{\left(1 + \frac{(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{60(-1+e^{-0.917853+30.2254 i})}\right) \left(-4 + \frac{-0.917853+30.2254 i}{\coth\left(\frac{1}{2}(-0.917853+30.2254 i)\right)}\right)}{-1 + e^{-0.917853+30.2254 i}} \\
& \frac{\left(1 + \frac{(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{60(e^{-0.917853+30.2254 i}-1)}\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right)}{e^{-0.917853+30.2254 i} - 1} = \\
& \frac{\left(-4 + \frac{-0.917853+30.2254 i}{\coth\left(\frac{1}{2}(-0.917853+30.2254 i)-\frac{i\pi}{2}\right)}\right) \left(1 + \frac{(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{60(-1+e^{-0.917853+30.2254 i})}\right)}{-1 + e^{-0.917853+30.2254 i}}
\end{aligned}$$

Series representations:

$$\begin{aligned}
& \frac{\left(1 + \frac{(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{60(e^{-0.917853+30.2254 i}-1)}\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right)}{e^{-0.917853+30.2254 i} - 1} = \\
& \frac{\left(1 + \frac{e^{-0.917853+30.2254 i}(-0.917853+30.2254 i)}{60(-1+e^{-0.917853+30.2254 i})}\right) \left(-4 + \frac{-0.917853+30.2254 i}{-1-2\sum_{k=1}^{\infty}(-1)^k q^{2k}}\right)}{-1 + e^{-0.917853+30.2254 i}}
\end{aligned}$$

for $q = -0.523265 + 0.354358 i$

$$\begin{aligned}
& \frac{\left(1 + \frac{(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{60(e^{-0.917853+30.2254 i}-1)}\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right)}{e^{-0.917853+30.2254 i} - 1} = \\
& \frac{\left(1 + \frac{0.503757 e^{30.2254 i}(-0.0303669+i)}{-e^{-0.917853+30.2254 i}}\right) \left(-4 + \frac{-0.917853+30.2254 i}{-1+2\sum_{k=0}^{\infty}(-1)^k \mathcal{A}^{(-0.917853+30.2254 i)(1+k)}}\right)}{-1 + e^{-0.917853+30.2254 i}}
\end{aligned}$$

$$\begin{aligned}
& \frac{\left(1 + \frac{(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{60(e^{-0.917853+30.2254 i}-1)}\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right)}{e^{-0.917853+30.2254 i} - 1} = \\
& \frac{\left(1 + \frac{0.503757 e^{30.2254 i}(-0.0303669+i)}{-e^{-0.917853+30.2254 i}}\right) \left(-4 + \frac{1}{4\sum_{k=1}^{\infty} \frac{1}{(0.917853-30.2254 i)^2+(1-2k)^2 \pi^2}}\right)}{-1 + e^{-0.917853+30.2254 i}}
\end{aligned}$$

Integral representation:

$$\frac{\left(1 + \frac{(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{60(e^{-0.917853+30.2254 i}-1)}\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right)}{e^{-0.917853+30.2254 i} - 1} = \frac{\left(1 + \frac{e^{-0.917853+30.2254 i}(-0.917853+30.2254 i)}{60(-1+e^{-0.917853+30.2254 i})}\right) \left(-4 + \frac{-0.917853+30.2254 i}{\int_0^2 \frac{1}{(-0.917853+30.2254 i) \operatorname{sech}^2(t) dt}\right)}{-1 + e^{-0.917853+30.2254 i}}$$

From the ratio of two previous results, we obtain:

$$(977968/35.3678)*1/16$$

Input interpretation:

$$\frac{977968}{35.3678} \times \frac{1}{16}$$

Result:

1728.210406075582874818337583904003076244493578905105774178...

1728.2104...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$(((977968/35.3678)^{1/2} - (29 + 11 + 1/\text{golden ratio}))$$

Input interpretation:

$$\sqrt{\frac{977968}{35.3678}} - \left(29 + 11 + \frac{1}{\phi}\right)$$

ϕ is the golden ratio

Result:

125.669...

125.669... result very near to the dilaton mass calculated as a type of Higgs boson:

125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

And:

$(977968/35.3678)^{1/2} - 21 - 5 - 1/\text{golden ratio}$

Input interpretation:

$$\sqrt{\frac{977968}{35.3678} - 21 - 5 - \frac{1}{\phi}}$$

ϕ is the golden ratio

Result:

139.669...

139.669... result practically equal to the rest mass of Pion meson 139.57 MeV

$$f_{Eb}(\tilde{\nu}) = \frac{C_f \tilde{\nu}^3}{e^{\tilde{\nu}} - 1} \left[1 + \frac{1}{12} \frac{\beta_0 \tau}{1 + \frac{\beta_0 \tau}{4}} \frac{\tilde{\nu} e^{\tilde{\nu}}}{e^{\tilde{\nu}} - 1} \right], \quad f_{E0}(\tilde{\nu}) = \frac{\tilde{\nu}^3}{e^{\tilde{\nu}} - 1}. \quad (27)$$

$$\begin{aligned} & (((0.7744 * (-0.086848 + 5.85735i)^3)) / (e^{(-0.086848 + 5.85735i)} - 1)) * \\ & (((1 + 1/12 * (1.2 / (1 + (1.2/4))) * ((-0.086848 + 5.85735i) * e^{(-0.086848 + 5.85735i)})) / ((e^{(-0.086848 + 5.85735i)} - 1)))))) \end{aligned}$$

Input interpretation:

$$\frac{0.7744 (-0.086848 + 5.85735 i)^3}{e^{-0.086848 + 5.85735 i} - 1}$$

$$\left(1 + \frac{1}{12} \times \frac{1.2}{1 + \frac{1.2}{4}} \times \frac{(-0.086848 + 5.85735 i) e^{-0.086848 + 5.85735 i}}{e^{-0.086848 + 5.85735 i} - 1} \right)$$

i is the imaginary unit

Result:

$$-0.00244062... - 0.00362929... i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 0.0043736 \text{ (radius), } \theta = -123.92^\circ \text{ (angle)}$$

$$0.0043736$$

Alternative representation:

$$\frac{\left(1 + \frac{1.2(-0.086848 + 5.85735 i)e^{-0.086848 + 5.85735 i}}{12\left(1 + \frac{1.2}{4}\right)(e^{-0.086848 + 5.85735 i} - 1)}\right)(0.7744(-0.086848 + 5.85735 i)^3)}{\left(1 + \frac{1.2(-0.086848 + 5.85735 i)\exp^{-0.086848 + 5.85735 i(z)}}{12\left(1 + \frac{1.2}{4}\right)(\exp^{-0.086848 + 5.85735 i(z)} - 1)}\right)(0.7744(-0.086848 + 5.85735 i)^3)} \Bigg/ (\exp^{-0.086848 + 5.85735 i(z)} - 1) \text{ for } z = 1$$

Series representations:

$$\frac{\left(1 + \frac{1.2(-0.086848 + 5.85735 i)e^{-0.086848 + 5.85735 i}}{12\left(1 + \frac{1.2}{4}\right)(e^{-0.086848 + 5.85735 i} - 1)}\right)(0.7744(-0.086848 + 5.85735 i)^3)}{\left(1 + \frac{1.2(-0.086848 + 5.85735 i)\exp^{-0.086848 + 5.85735 i(z)}}{12\left(1 + \frac{1.2}{4}\right)(\exp^{-0.086848 + 5.85735 i(z)} - 1)}\right)(0.7744(-0.086848 + 5.85735 i)^3)} \Bigg/ (\exp^{-0.086848 + 5.85735 i(z)} - 1) \text{ for } z = 1$$

$$\left(70.1175 \left(7.23466 \times 10^{-6} \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.173696} - 0.0014638 i \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.173696} + 0.0987238 i^2 \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.173696} - 2.21943 i^3 \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.173696} + 7.18633 \times 10^{-6} \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.086848 + 5.85735 i} + 0.00145076 i \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.086848 + 5.85735 i} - 0.0974048 i^2 \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.086848 + 5.85735 i} + 2.16012 i^3 \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.086848 + 5.85735 i} + i^4 \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.086848 + 5.85735 i}\right) \Bigg/ \left(\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.086848} - \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{5.85735 i}\right)^2$$

$$\begin{aligned}
& \left(1 + \frac{1.2 \left((-0.086848 + 5.85735 i) e^{-0.086848 + 5.85735 i} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(e^{-0.086848 + 5.85735 i} \right)} \right) (0.7744 (-0.086848 + 5.85735 i)^3) \\
& \quad = \\
& \left(70.1175 \left(7.23466 \times 10^{-6} \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.173696} - 0.0014638 i \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.173696} + \right. \right. \\
& \quad 0.0987238 i^2 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.173696} - 2.21943 i^3 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.173696} - \\
& \quad 7.18633 \times 10^{-6} \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} + \\
& \quad 0.00145076 i \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} - \\
& \quad 0.0974048 i^2 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} + 2.16012 i^3 \\
& \quad \left. \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} + i^4 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} \right) \Bigg/ \\
& \left(- \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848} + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{5.85735 i^2} \right)
\end{aligned}$$

$$\begin{aligned}
& \left(1 + \frac{1.2 \left((-0.086848 + 5.85735 i) e^{-0.086848 + 5.85735 i} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(e^{-0.086848 + 5.85735 i} \right)} \right) (0.7744 (-0.086848 + 5.85735 i)^3) \\
& \quad = \\
& \left(70.1175 \left(7.23466 \times 10^{-6} \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.173696} - 0.0014638 i \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.173696} + \right. \right. \\
& \quad 0.0987238 i^2 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.173696} - 2.21943 i^3 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.173696} - \\
& \quad 7.18633 \times 10^{-6} \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} + \\
& \quad 0.00145076 i \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} - \\
& \quad 0.0974048 i^2 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} + 2.16012 i^3 \\
& \quad \left. \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} + i^4 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848 + 5.85735 i} \right) \Bigg/ \\
& \left(\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.086848} - \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{5.85735 i^2} \right)
\end{aligned}$$

or:

$$\left(\frac{(0.7744 \cdot (-0.917853 + 30.2254i)^3)}{e^{(-0.917853 + 30.2254i) - 1}} \right) \cdot \left(1 + \frac{1}{12} \cdot \left(\frac{1.2}{1 + \frac{1.2}{4}} \right) \right) \cdot \left(\frac{(-0.917853 + 30.2254i) \cdot e^{(-0.917853 + 30.2254i)}}{e^{(-0.917853 + 30.2254i) - 1}} \right)$$

Input interpretation:

$$\frac{0.7744 (-0.917853 + 30.2254 i)^3}{e^{-0.917853 + 30.2254 i} - 1} \left(1 + \frac{1}{12} \times \frac{1.2}{1 + \frac{1.2}{4}} \times \frac{(-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i}}{e^{-0.917853 + 30.2254 i} - 1} \right)$$

i is the imaginary unit

Result:

$$-0.129806... + 0.153480... i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 0.201012 \text{ (radius), } \theta = 130.223^\circ \text{ (angle)}$$

0.201012

Alternative representation:

$$\frac{\left(1 + \frac{1.2 \left((-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(e^{-0.917853 + 30.2254 i} - 1 \right)} \right) (0.7744 (-0.917853 + 30.2254 i)^3)}{e^{-0.917853 + 30.2254 i} - 1} = \left(\left(1 + \frac{1.2 \left((-0.917853 + 30.2254 i) \exp^{-0.917853 + 30.2254 i(z)} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(\exp^{-0.917853 + 30.2254 i(z)} - 1 \right)} \right) (0.7744 (-0.917853 + 30.2254 i)^3) \right) / \left(\exp^{-0.917853 + 30.2254 i(z)} - 1 \right) \text{ for } z = 1$$

Series representations:

$$\frac{\left(1 + \frac{1.2(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{12\left(1+\frac{1.2}{4}\right)\left(e^{-0.917853+30.2254 i-1}\right)}\right)(0.7744(-0.917853+30.2254 i)^3)}{e^{-0.917853+30.2254 i}-1} =$$

$$\left(49717.6\left(0.0000120441\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{1.83571}-0.00118986 i\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{1.83571}+\right.\right.$$

$$0.0391826 i^2\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{1.83571}-0.430102 i^3\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{1.83571}-$$

$$0.0000111937\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{0.917853+30.2254 i}+0.00107785 i$$

$$\left.\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{0.917853+30.2254 i}-0.0336497 i^2\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{0.917853+30.2254 i}+\right.$$

$$0.308634 i^3\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{0.917853+30.2254 i}+i^4\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{0.917853+30.2254 i}\left.\right)/$$

$$\left(\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{0.917853}-\left(\sum_{k=0}^{\infty}\frac{1}{k!}\right)^{30.2254 i}\right)^2$$

$$\frac{\left(1 + \frac{1.2(-0.917853+30.2254 i)e^{-0.917853+30.2254 i}}{12\left(1+\frac{1.2}{4}\right)\left(e^{-0.917853+30.2254 i-1}\right)}\right)(0.7744(-0.917853+30.2254 i)^3)}{e^{-0.917853+30.2254 i}-1} =$$

$$\left(49717.6\left(0.0000120441\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{1.83571}-0.00118986 i\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{1.83571}+\right.\right.$$

$$0.0391826 i^2\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{1.83571}-0.430102 i^3\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{1.83571}-$$

$$0.0000111937\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{0.917853+30.2254 i}+0.00107785 i$$

$$\left.\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{0.917853+30.2254 i}-0.0336497 i^2\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{0.917853+30.2254 i}+\right.$$

$$0.308634 i^3\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{0.917853+30.2254 i}+i^4\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{0.917853+30.2254 i}\left.\right)/$$

$$\left(-\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{0.917853}+\left(\sum_{k=0}^{\infty}\frac{(-1+k)^2}{k!}\right)^{30.2254 i}\right)^2$$

$$\frac{\left(1 + \frac{1.2 \left((-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i} \right)}{12 \left(1 + \frac{1.2}{4} \right) \left(e^{-0.917853 + 30.2254 i} - 1 \right)} \right) (0.7744 (-0.917853 + 30.2254 i)^3)}{e^{-0.917853 + 30.2254 i} - 1} =$$

$$\left(49717.6 \left(0.0000120441 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{1.83571} - 0.00118986 i \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{1.83571} + \right. \right.$$

$$0.0391826 i^2 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{1.83571} - 0.430102 i^3 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{1.83571} -$$

$$0.0000111937 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853 + 30.2254 i} +$$

$$0.00107785 i \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853 + 30.2254 i} -$$

$$0.0336497 i^2 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853 + 30.2254 i} + 0.308634 i^3$$

$$\left. \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853 + 30.2254 i} + i^4 \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853 + 30.2254 i} \right) /$$

$$\left(\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{0.917853} - \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{30.2254 i} \right)^2$$

$$(-0.086848 + 5.85735i)^3 / (e^{(-0.086848 + 5.85735i)} - 1)$$

Input interpretation:

$$\frac{(-0.086848 + 5.85735 i)^3}{e^{-0.086848 + 5.85735 i} - 1}$$

i is the imaginary unit

Result:

$$436.979... + 214.054... i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 486.59 \text{ (radius)}, \quad \theta = 26.0978^\circ \text{ (angle)}$$

$$486.59$$

Alternative representation:

$$\frac{(-0.086848 + 5.85735 i)^3}{e^{-0.086848 + 5.85735 i} - 1} = \frac{(-0.086848 + 5.85735 i)^3}{\exp^{-0.086848 + 5.85735 i}(z) - 1} \text{ for } z = 1$$

Series representations:

$$\frac{(-0.086848 + 5.85735 i)^3}{e^{-0.086848 + 5.85735 i} - 1} = \frac{(-0.086848 + 5.85735 i)^3}{-1 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{-0.086848 + 5.85735 i}}$$

$$\frac{(-0.086848 + 5.85735 i)^3}{e^{-0.086848 + 5.85735 i} - 1} = \frac{(-0.086848 + 5.85735 i)^3}{-1 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{-0.086848 + 5.85735 i}}$$

$$\frac{(-0.086848 + 5.85735 i)^3}{e^{-0.086848 + 5.85735 i} - 1} = \frac{(-0.086848 + 5.85735 i)^3}{-1 + \left(\sum_{k=0}^{\infty} \frac{1+2k}{(2k)!}\right)^{-0.086848 + 5.85735 i}}$$

or:

$$\frac{((-0.917853 + 30.2254i)^3)}{(e^{(-0.917853 + 30.2254i)} - 1)}$$

Input interpretation:

$$\frac{(-0.917853 + 30.2254 i)^3}{e^{-0.917853 + 30.2254 i} - 1}$$

i is the imaginary unit

Result:

$$9350.66... + 28258.0... i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 29764.9 \text{ (radius), } \theta = 71.6904^\circ \text{ (angle)}$$

29764.9

Alternative representation:

$$\frac{(-0.917853 + 30.2254 i)^3}{e^{-0.917853+30.2254 i} - 1} = \frac{(-0.917853 + 30.2254 i)^3}{\exp^{-0.917853+30.2254 i}(z) - 1} \text{ for } z = 1$$

Series representations:

$$\frac{(-0.917853 + 30.2254 i)^3}{e^{-0.917853+30.2254 i} - 1} = \frac{(-0.917853 + 30.2254 i)^3}{-1 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{-0.917853+30.2254 i}}$$

$$\frac{(-0.917853 + 30.2254 i)^3}{e^{-0.917853+30.2254 i} - 1} = \frac{(-0.917853 + 30.2254 i)^3}{-1 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{-0.917853+30.2254 i}}$$

$$\frac{(-0.917853 + 30.2254 i)^3}{e^{-0.917853+30.2254 i} - 1} = \frac{(-0.917853 + 30.2254 i)^3}{-1 + \left(\sum_{k=0}^{\infty} \frac{1+2k}{(2k)!}\right)^{-0.917853+30.2254 i}}$$

From the formula

$$\delta_{Th} = y\tilde{\nu} \frac{e^{\tilde{\nu}}}{e^{\tilde{\nu}} - 1} \left[\frac{\tilde{\nu}}{\tanh(\tilde{\nu}/2)} - 4 \right]. \tag{28}$$

we obtain:

$$1/60*(-0.086848+5.85735i)*((e^{(-0.086848+5.85735i)}))/((e^{(-0.086848+5.85735i)}-1))*(((((-0.086848+5.85735i))/(\tanh(((0.086848-5.85735i)/2)))))-4$$

Input interpretation:

$$\frac{1}{60} \times (-0.086848 + 5.85735 i) \times \frac{e^{-0.086848+5.85735 i}}{e^{-0.086848+5.85735 i} - 1} \left(\frac{-0.086848 + 5.85735 i}{\tanh\left(\frac{1}{2} \times (-0.086848 + 5.85735 i)\right)} - 4 \right)$$

$\tanh(x)$ is the hyperbolic tangent function

i is the imaginary unit

Result:

$$6.48130\dots + 1.26918\dots i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 6.60439 \text{ (radius), } \theta = 11.0795^\circ \text{ (angle)}$$

$$6.60439$$

Alternative representations:

$$\frac{\left((-0.086848 + 5.85735 i) \left(\frac{-0.086848 + 5.85735 i}{\tanh\left(\frac{1}{2}(-0.086848 + 5.85735 i)\right)} - 4 \right) \right) e^{-0.086848 + 5.85735 i}}{60 (e^{-0.086848 + 5.85735 i} - 1)} = \frac{(-0.086848 + 5.85735 i) e^{-0.086848 + 5.85735 i} \left(-4 + \frac{-0.086848 + 5.85735 i}{-1 + \frac{2}{1 + e^{0.086848 - 5.85735 i}}} \right)}{60 (-1 + e^{-0.086848 + 5.85735 i})}$$

$$\frac{\left((-0.086848 + 5.85735 i) \left(\frac{-0.086848 + 5.85735 i}{\tanh\left(\frac{1}{2}(-0.086848 + 5.85735 i)\right)} - 4 \right) \right) e^{-0.086848 + 5.85735 i}}{60 (e^{-0.086848 + 5.85735 i} - 1)} = \frac{(-0.086848 + 5.85735 i) e^{-0.086848 + 5.85735 i} \left(-4 + \frac{-0.086848 + 5.85735 i}{\frac{1}{\coth\left(\frac{1}{2}(-0.086848 + 5.85735 i)\right)}} \right)}{60 (-1 + e^{-0.086848 + 5.85735 i})}$$

$$\frac{\left((-0.086848 + 5.85735 i) \left(\frac{-0.086848 + 5.85735 i}{\tanh\left(\frac{1}{2}(-0.086848 + 5.85735 i)\right)} - 4 \right) \right) e^{-0.086848 + 5.85735 i}}{60 (e^{-0.086848 + 5.85735 i} - 1)} = \frac{(-0.086848 + 5.85735 i) e^{-0.086848 + 5.85735 i} \left(-4 + \frac{-0.086848 + 5.85735 i}{\coth\left(\frac{1}{2}(-0.086848 + 5.85735 i) - \frac{i\pi}{2}\right)} \right)}{60 (-1 + e^{-0.086848 + 5.85735 i})}$$

Series representations:

$$\frac{\left((-0.086848 + 5.85735 i) \left(\frac{-0.086848 + 5.85735 i}{\tanh\left(\frac{1}{2}(-0.086848 + 5.85735 i)\right)} - 4 \right) \right) e^{-0.086848 + 5.85735 i}}{60 (e^{-0.086848 + 5.85735 i} - 1)} = \frac{e^{-0.086848 + 5.85735 i} (-0.086848 + 5.85735 i) \left(-4 + \frac{-0.086848 + 5.85735 i}{-1 - 2 \sum_{k=1}^{\infty} (-1)^k q^{-2k}} \right)}{60 (-1 + e^{-0.086848 + 5.85735 i})}$$

$$\text{for } q = -0.935883 + 0.202333 i$$

$$\frac{\left(-0.086848 + 5.85735 i\right) \left(\frac{-0.086848+5.85735 i}{\tanh\left(\frac{1}{2}(-0.086848+5.85735 i)\right)} - 4\right) e^{-0.086848+5.85735 i}}{60 \left(e^{-0.086848+5.85735 i} - 1\right)} =$$

$$\frac{\left(e^{-0.086848+5.85735 i} (-0.086848 + 5.85735 i) \left(-4 + \frac{-0.086848 + 5.85735 i}{-1 + 2 \sum_{k=0}^{\infty} (-1)^k \mathcal{A}^{(-0.086848+5.85735 i)(1+k)}}\right)\right)}{\left(60 \left(-1 + e^{-0.086848+5.85735 i}\right)\right)}$$

$$\frac{\left(-0.086848 + 5.85735 i\right) \left(\frac{-0.086848+5.85735 i}{\tanh\left(\frac{1}{2}(-0.086848+5.85735 i)\right)} - 4\right) e^{-0.086848+5.85735 i}}{60 \left(e^{-0.086848+5.85735 i} - 1\right)} =$$

$$\frac{e^{-0.086848+5.85735 i} (-0.086848 + 5.85735 i) \left(-4 + \frac{1}{4 \sum_{k=1}^{\infty} \frac{1}{(0.086848 - 5.85735 i)^2 + (1-2k)^2 \pi^2}}\right)}{60 \left(-1 + e^{-0.086848+5.85735 i}\right)}$$

Integral representation:

$$\frac{\left(-0.086848 + 5.85735 i\right) \left(\frac{-0.086848+5.85735 i}{\tanh\left(\frac{1}{2}(-0.086848+5.85735 i)\right)} - 4\right) e^{-0.086848+5.85735 i}}{60 \left(e^{-0.086848+5.85735 i} - 1\right)} =$$

$$\frac{e^{-0.086848+5.85735 i} (-0.086848 + 5.85735 i) \left(-4 + \frac{-0.086848+5.85735 i}{\int_0^{-0.043424+2.92868 i} \operatorname{sech}^2(t) dt}\right)}{60 \left(-1 + e^{-0.086848+5.85735 i}\right)}$$

or:

$$\frac{1}{60} \times (-0.917853 + 30.2254 i) \times \left(\frac{e^{-0.917853+30.2254 i}}{e^{-0.917853+30.2254 i} - 1} \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} \times (-0.917853 + 30.2254 i)\right)} - 4 \right) \right)$$

Input interpretation:

$$\frac{1}{60} \times (-0.917853 + 30.2254 i) \times \frac{e^{-0.917853+30.2254 i}}{e^{-0.917853+30.2254 i} - 1} \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2} \times (-0.917853 + 30.2254 i)\right)} - 4 \right)$$

$\tanh(x)$ is the hyperbolic tangent function

i is the imaginary unit

Result:

$$6.30113... + 6.54872... i$$

(using the principal branch of the logarithm for complex exponentiation)

Polar coordinates:

$$r = 9.0879 \text{ (radius), } \theta = 46.1038^\circ \text{ (angle)}$$

9.0879

Alternative representations:

$$\frac{\left((-0.917853 + 30.2254 i) \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853 + 30.2254 i)\right)} - 4 \right) \right) e^{-0.917853 + 30.2254 i}}{60 (e^{-0.917853 + 30.2254 i} - 1)} = \frac{(-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i} \left(-4 + \frac{-0.917853 + 30.2254 i}{-1 + \frac{2}{1 + e^{0.917853 - 30.2254 i}}} \right)}{60 (-1 + e^{-0.917853 + 30.2254 i})}$$

$$\frac{\left((-0.917853 + 30.2254 i) \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853 + 30.2254 i)\right)} - 4 \right) \right) e^{-0.917853 + 30.2254 i}}{60 (e^{-0.917853 + 30.2254 i} - 1)} = \frac{(-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i} \left(-4 + \frac{-0.917853 + 30.2254 i}{\coth\left(\frac{1}{2}(-0.917853 + 30.2254 i)\right)} \right)}{60 (-1 + e^{-0.917853 + 30.2254 i})}$$

$$\frac{\left((-0.917853 + 30.2254 i) \left(\frac{-0.917853 + 30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853 + 30.2254 i)\right)} - 4 \right) \right) e^{-0.917853 + 30.2254 i}}{60 (e^{-0.917853 + 30.2254 i} - 1)} = \frac{(-0.917853 + 30.2254 i) e^{-0.917853 + 30.2254 i} \left(-4 + \frac{-0.917853 + 30.2254 i}{\coth\left(\frac{1}{2}(-0.917853 + 30.2254 i) - \frac{i\pi}{2}\right)} \right)}{60 (-1 + e^{-0.917853 + 30.2254 i})}$$

Series representations:

$$\frac{\left(-0.917853 + 30.2254 i\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right) e^{-0.917853+30.2254 i}}{60 \left(e^{-0.917853+30.2254 i} - 1\right)} =$$

$$\frac{e^{-0.917853+30.2254 i} (-0.917853 + 30.2254 i) \left(-4 + \frac{-0.917853+30.2254 i}{-1-2 \sum_{k=1}^{\infty} (-1)^k q^{2k}}\right)}{60 \left(-1 + e^{-0.917853+30.2254 i}\right)}$$

for $q = -0.523265 + 0.354358 i$

$$\frac{\left(-0.917853 + 30.2254 i\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right) e^{-0.917853+30.2254 i}}{60 \left(e^{-0.917853+30.2254 i} - 1\right)} =$$

$$\left(e^{-0.917853+30.2254 i} (-0.917853 + 30.2254 i) \right.$$

$$\left. \left(-4 + \frac{-0.917853 + 30.2254 i}{-1 + 2 \sum_{k=0}^{\infty} (-1)^k \mathcal{A}^{(-0.917853+30.2254 i)(1+k)}} \right) \right) /$$

$$\left(60 \left(-1 + e^{-0.917853+30.2254 i}\right) \right)$$

$$\frac{\left(-0.917853 + 30.2254 i\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right) e^{-0.917853+30.2254 i}}{60 \left(e^{-0.917853+30.2254 i} - 1\right)} =$$

$$\frac{e^{-0.917853+30.2254 i} (-0.917853 + 30.2254 i) \left(-4 + \frac{1}{4 \sum_{k=1}^{\infty} \frac{1}{(0.917853-30.2254 i)^2 + (1-2k)^2 \pi^2}}\right)}{60 \left(-1 + e^{-0.917853+30.2254 i}\right)}$$

Integral representation:

$$\frac{\left(-0.917853 + 30.2254 i\right) \left(\frac{-0.917853+30.2254 i}{\tanh\left(\frac{1}{2}(-0.917853+30.2254 i)\right)} - 4\right) e^{-0.917853+30.2254 i}}{60 \left(e^{-0.917853+30.2254 i} - 1\right)} =$$

$$\frac{e^{-0.917853+30.2254 i} (-0.917853 + 30.2254 i) \left(-4 + \frac{-0.917853+30.2254 i}{\int_0^{-0.458927+15.1127 i} \operatorname{sech}^2(t) dt}\right)}{60 \left(-1 + e^{-0.917853+30.2254 i}\right)}$$

From the results of eqs. (26), (27), (31) and (32), we obtain:

a)

$$34((977968/(29764.9+0.201012)))-1/\text{golden ratio}-89-8$$

Input interpretation:

$$34 \times \frac{977968}{29764.9 + 0.201012} - \frac{1}{\phi} - 89 - 8$$

ϕ is the golden ratio

Result:

1019.49...

1019.49... result practically equal to the rest mass of Phi meson 1019.445

Alternative representations:

$$\frac{34 \times 977968}{29764.9 + 0.201012} - \frac{1}{\phi} - 89 - 8 = -97 + \frac{33\,250\,912}{29\,765.1} - \frac{1}{2 \sin(54^\circ)}$$

$$\frac{34 \times 977968}{29764.9 + 0.201012} - \frac{1}{\phi} - 89 - 8 = -97 + \frac{33\,250\,912}{29\,765.1} - \frac{1}{2 \cos(216^\circ)}$$

$$\frac{34 \times 977968}{29764.9 + 0.201012} - \frac{1}{\phi} - 89 - 8 = -97 + \frac{33\,250\,912}{29\,765.1} - \frac{1}{2 \sin(66^\circ)}$$

b)

$$(((977968/(29764.9+0.201012+35.3678))))+7.2695e-6$$

Input interpretation:

$$\frac{977968}{29764.9 + 0.201012 + 35.3678} + 7.2695 \times 10^{-6}$$

Result:

32.81720911184798272340682799322667246366540147972488212142...

32.817209...

And also:

$$1/((((977968*1/(29764.9+0.201012+35.3678)))))+1/(((7.2695e-6)))$$

Input interpretation:

$$\frac{1}{977968 \times \frac{1}{29764.9+0.201012+35.3678}} + \frac{1}{7.2695 \times 10^{-6}}$$

Result:

137561.0731845278015268857136755871865958852765119812887634...

137561.0731845...

From which:

$$1/10^3 * [1/((((977968*1/(29764.9+0.201012+35.3678)))))+1/(((7.2695e-6)))] + \pi/2 + 1/\text{golden ratio}$$

Input interpretation:

$$\frac{1}{10^3} \left(\frac{1}{977968 \times \frac{1}{29764.9+0.201012+35.3678}} + \frac{1}{7.2695 \times 10^{-6}} \right) + \frac{\pi}{2} + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

139.750...

139.75... result practically equal to the rest mass of Pion meson 139.57 MeV

$$1/10^3 * [1/((((977968*1/(29764.9+0.201012+35.3678)))))+1/(((7.2695e-6)))] - 13 + 1/\text{golden ratio}$$

Input interpretation:

$$\frac{1}{10^3} \left(\frac{1}{977968 \times \frac{1}{29764.9+0.201012+35.3678}} + \frac{1}{7.2695 \times 10^{-6}} \right) - 13 + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

125.179...

125.179... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

$$1/10^{52}(((1/29(((977968/(29764.9+0.201012+35.3678)))+7.2695e-6))-Pi/10^2+(47+7)/10^4))$$

Input interpretation:

$$\frac{1}{10^{52}} \left(\frac{1}{29} \left(\frac{977968}{29764.9 + 0.201012 + 35.3678} + 7.2695 \times 10^{-6} \right) - \frac{\pi}{10^2} + \frac{47+7}{10^4} \right)$$

Result:

$$1.10561... \times 10^{-52}$$

1.10561... * 10⁻⁵² result practically equal to the value of Cosmological Constant

$$1.1056 \times 10^{-52} \text{ m}^{-2}$$

Note that, from the formula concerning the Coefficients of the '5th order' mock theta function $\psi_1(q)$, for $n = 372$ and adding 144, 13, that are Fibonacci numbers, and π , we obtain:

$$\text{sqrt(golden ratio)} * \exp(\text{Pi} * \text{sqrt}(372/15)) / (2 * 5^{(1/4)} * \text{sqrt}(372)) + 144 + 13 + \text{Pi}$$

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{372}{15}}\right)}{2 \sqrt[4]{5} \sqrt{372}} + 144 + 13 + \pi$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{2\sqrt{31/5} \pi} \sqrt{\frac{\phi}{93}}}{4 \sqrt[4]{5}} + 157 + \pi$$

Decimal approximation:

137560.9541708438968779934653662573441257102139759735825035...

137560.9541708...

Alternate forms:

$$157 + \frac{1}{4} \sqrt{\frac{1}{930} (5 + \sqrt{5})} e^{2\sqrt{31/5} \pi} + \pi$$

$$157 + \frac{\sqrt{\frac{1}{186}(1+\sqrt{5})} e^{2\sqrt{31/5}\pi}}{4\sqrt[4]{5}} + \pi$$

$$\frac{584040 + 5^{3/4} \sqrt{186(1+\sqrt{5})} e^{2\sqrt{31/5}\pi} + 3720\pi}{3720}$$

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{372}{15}}\right)}{2\sqrt[4]{5} \sqrt{372}} + 144 + 13 + \pi =$$

$$\left(1570 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (372 - z_0)^k z_0^{-k}}{k!} + 10\pi \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (372 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right.$$

$$\left. \exp\left[\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{124}{5} - z_0\right)^k z_0^{-k}}{k!}\right] \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) /$$

$$\left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (372 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{372}{15}}\right)}{2\sqrt[4]{5} \sqrt{372}} + 144 + 13 + \pi =$$

$$\left(1570 \exp\left(i\pi \left\lfloor \frac{\arg(372 - x)}{2\pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (372 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right.$$

$$10\pi \exp\left(i\pi \left\lfloor \frac{\arg(372 - x)}{2\pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (372 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} +$$

$$5^{3/4} \exp\left(i\pi \left\lfloor \frac{\arg(\phi - x)}{2\pi} \right\rfloor\right) \exp\left[\pi \exp\left(i\pi \left\lfloor \frac{\arg\left(\frac{124}{5} - x\right)}{2\pi} \right\rfloor\right) \sqrt{x}\right]$$

$$\sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{124}{5} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \Big/$$

$$\left(10 \exp\left(i\pi \left\lfloor \frac{\arg(372 - x)}{2\pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (372 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{372}{15}}\right)}{2^{\frac{4}{5}} \sqrt{372}} + 144 + 13 + \pi = \\
& \left(\left(\frac{1}{z_0}\right)^{-1/2 [\arg(372-z_0)/(2\pi)]} z_0^{-1/2 [\arg(372-z_0)/(2\pi)]} \left(1570 \left(\frac{1}{z_0}\right)^{1/2 [\arg(372-z_0)/(2\pi)]} \right. \right. \\
& \quad \left. \left. z_0^{1/2 [\arg(372-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (372-z_0)^k z_0^{-k}}{k!} + \right. \right. \\
& \quad \left. \left. 10 \pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(372-z_0)/(2\pi)]} z_0^{1/2 [\arg(372-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (372-z_0)^k z_0^{-k}}{k!} + 5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(\frac{124}{5}-z_0)/(2\pi)]}\right) \right. \right. \\
& \quad \left. \left. z_0^{1/2 (1+[\arg(\frac{124}{5}-z_0)/(2\pi)])} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{124}{5}-z_0\right)^k z_0^{-k}}{k!} \right) \right) \\
& \quad \left. \left. \left(\frac{1}{z_0}\right)^{1/2 [\arg(\phi-z_0)/(2\pi)]} z_0^{1/2 [\arg(\phi-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \right) \Bigg/ \\
& \quad \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (372-z_0)^k z_0^{-k}}{k!} \right)
\end{aligned}$$

From the value of Cosmological Constant, we obtain:

$$(1/(1.1056e-52))^{1/16}$$

Input interpretation:

$$\sqrt[16]{\frac{1}{1.1056 \times 10^{-52}}}$$

Result:

1767.16...

1767.16... result in the range of the mass of candidate “glueball” $f_0(1710)$ (“glueball” = 1760 ± 15 MeV).

We observe that, for $n = 182$, from the previous formula concerning the Coefficients of the '5th order' mock theta function $\psi_1(q)$, subtracting 16, we obtain:

$$\sqrt{\phi} \times \exp(\pi \sqrt{182/15}) / (2 \cdot 5^{1/4} \sqrt{182}) - 16$$

Input:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{182}{15}}\right)}{2 \sqrt[4]{5} \sqrt{182}} - 16$$

ϕ is the golden ratio

Exact result:

$$\frac{e^{\sqrt{182/15} \pi} \sqrt{\frac{\phi}{182}}}{2 \sqrt[4]{5}} - 16$$

Decimal approximation:

1767.236154164859098625330490739993663216984415742076667965...

1767.236154... as above

Property:

$$-16 + \frac{e^{\sqrt{182/15} \pi} \sqrt{\frac{\phi}{182}}}{2 \sqrt[4]{5}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{1}{4} \sqrt{\frac{1}{455} (5 + \sqrt{5})} e^{\sqrt{182/15} \pi} - 16$$

$$\frac{\sqrt{\frac{1}{91} (1 + \sqrt{5})} e^{\sqrt{182/15} \pi}}{4 \sqrt[4]{5}} - 16$$

$$\frac{5^{3/4} \sqrt{91 (1 + \sqrt{5})} e^{\sqrt{182/15} \pi} - 29120}{1820}$$

Series representations:

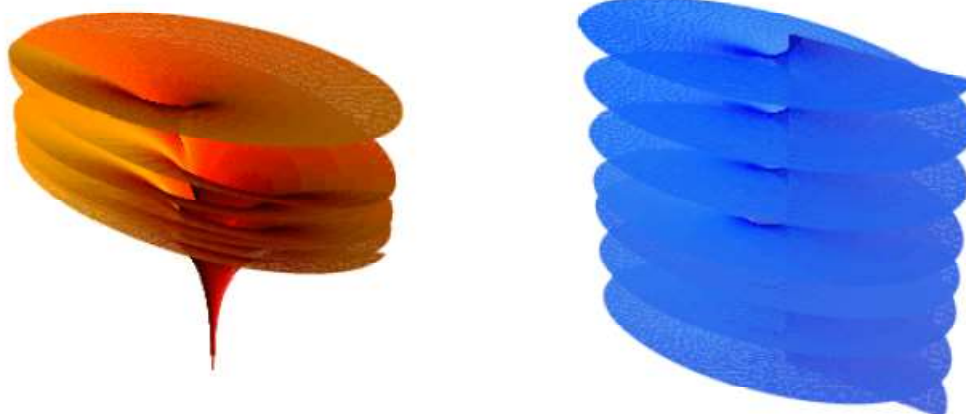
$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{182}{15}}\right)}{2 \sqrt[4]{5} \sqrt{182}} - 16 = \left(-160 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (182 - z_0)^k z_0^{-k}}{k!} + 5^{3/4} \right. \\ \left. \exp\left[\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{182}{15} - z_0\right)^k z_0^{-k}}{k!} \right] \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (182 - z_0)^k z_0^{-k}}{k!} \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{182}{15}}\right)}{2 \sqrt[4]{5} \sqrt{182}} - 16 = \left(-160 \exp\left(i \pi \left[\frac{\arg(182 - x)}{2 \pi} \right]\right) \sum_{k=0}^{\infty} \frac{(-1)^k (182 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \\ \left. 5^{3/4} \exp\left(i \pi \left[\frac{\arg(\phi - x)}{2 \pi} \right]\right) \exp\left[\pi \exp\left(i \pi \left[\frac{\arg\left(\frac{182}{15} - x\right)}{2 \pi} \right]\right) \sqrt{x} \right. \right. \\ \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{182}{15} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right] \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\ \left(10 \exp\left(i \pi \left[\frac{\arg(182 - x)}{2 \pi} \right]\right) \sum_{k=0}^{\infty} \frac{(-1)^k (182 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\begin{aligned}
& \frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{182}{15}}\right)}{2 \sqrt[4]{5} \sqrt{182}} - 16 = \\
& \left(\left(\frac{1}{z_0}\right)^{-1/2 [\arg(182-z_0)/(2\pi)]} z_0^{-1/2 [\arg(182-z_0)/(2\pi)]} \left[-160 \left(\frac{1}{z_0}\right)^{1/2 [\arg(182-z_0)/(2\pi)]} \right. \right. \\
& \quad \left. \left. z_0^{1/2 [\arg(182-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (182-z_0)^k z_0^{-k}}{k!} + \right. \right. \\
& \quad \left. \left. 5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(\frac{182}{15}-z_0)/(2\pi)]} z_0^{1/2 (1+[\arg(\frac{182}{15}-z_0)/(2\pi)])} \right. \right. \right. \\
& \quad \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{182}{15}-z_0\right)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 [\arg(\phi-z_0)/(2\pi)]} \right. \\
& \quad \left. \left. z_0^{1/2 [\arg(\phi-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi-z_0)^k z_0^{-k}}{k!} \right) \right) / \\
& \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (182-z_0)^k z_0^{-k}}{k!} \right)
\end{aligned}$$

Lambert W-Function -- from Wolfram MathWorld



The real (left) and imaginary (right) parts of the analytic continuation of $W(z)$ over the complex plane are illustrated above (M. Trott, pers. comm.).

$W(x)$ is real for $x \geq -1/e$. It has the special values

$$W\left(-\frac{1}{2}\pi\right) = \frac{1}{2}i\pi \tag{5}$$

$$W\left(-e^{-1}\right) = -1 \tag{6}$$

$$W(0) = 0 \tag{7}$$

$$W(1) = 0.567143 \dots \tag{8}$$

$W(1) = 0.567143 \dots$ (OEIS A030178) is called the **omega constant** and can be considered a sort of "golden ratio" of exponentials since

$$\exp[-W(1)] = W(1), \tag{9}$$

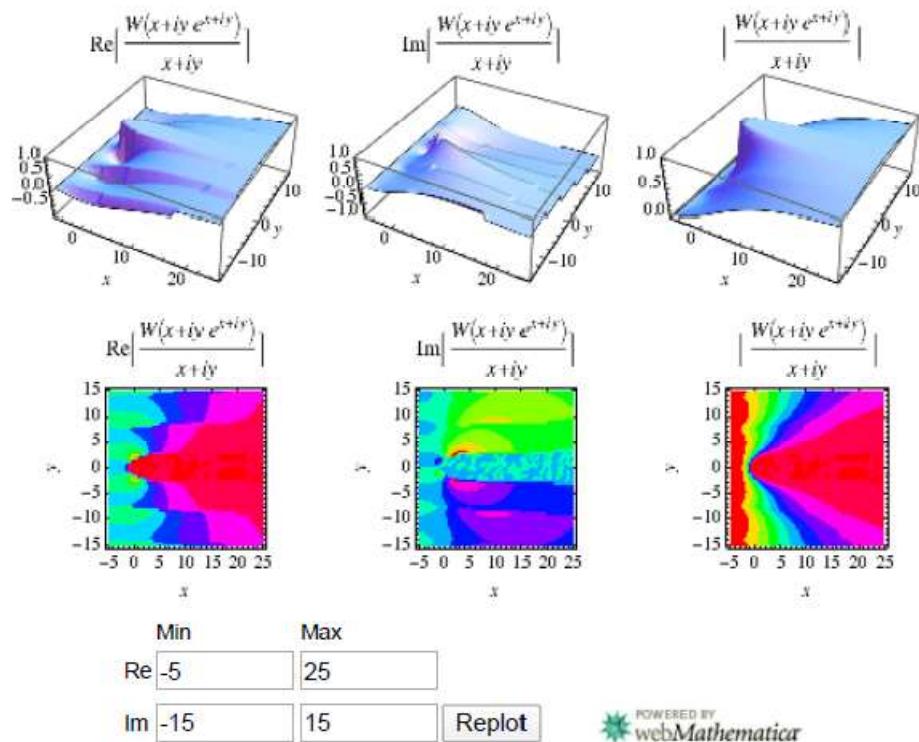
giving

$$\ln\left[\frac{1}{W(1)}\right] = W(1). \tag{10}$$

The Lambert W -function obeys the identity

$$W(x) + W(y) = W\left(xy\left(\frac{1}{W(x)} + \frac{1}{W(y)}\right)\right) \tag{11}$$

(pers. comm. from R. Corless to O. Marichev, Sep. 29, 2015).



The function $W(z e^z)/z$ has a very complicated structure in the complex plane, but is simply equal to 1 for $\Re[z] \geq 1$ and a slightly extended region above and below the real axis.

The Lambert W -function has the series expansion

$$W(x) = \sum_{n=1}^{\infty} \frac{(-1)^{n-1} n^{n-2}}{(n-1)!} x^n \quad (12)$$

$$= x - x^2 + \frac{3}{2} x^3 - \frac{8}{3} x^4 + \frac{125}{24} x^5 - \frac{54}{5} x^6 + \frac{16807}{720} x^7 + \dots \quad (13)$$

The [Lagrange inversion theorem](#) gives the equivalent series expansion

$$W(z) = \sum_{n=1}^{\infty} \frac{(-n)^{n-1}}{n!} z^n, \quad (14)$$

where $n!$ is a [factorial](#). However, this series oscillates between ever larger [positive](#) and [negative](#) values for [real](#) $z \gtrsim 0.4$, and so cannot be used for practical numerical computation.

An asymptotic [formula](#) which yields reasonably accurate results for $z \gtrsim 3$ is

$$W(z) = \ln z - \ln \ln z + \sum_{k=0}^{\infty} \sum_{m=0}^{\infty} c_{k m} (\ln \ln z)^{m+1} (\ln z)^{-k-m-1} \quad (15)$$

$$= L_1 - L_2 + \frac{L_2}{L_1} + \frac{L_2(-2+L_2)}{2L_1^2} + \frac{L_2(6-9L_2+2L_2^2)}{6L_1^3} + \frac{L_2(-12+36L_2-22L_2^2+3L_2^3)}{12L_1^4} + \dots \quad (16)$$

$$= \frac{L_2(60-300L_2+350L_2^2-125L_2^3+12L_2^4)}{60L_1^5} + O\left[\left(\frac{L_2}{L_1}\right)^6\right],$$

where

$$L_1 = \ln z \tag{17}$$

$$L_2 = \ln \ln z \tag{18}$$

(Corless *et al.* 1996), correcting a typographical error in de Bruijn (1981). Another expansion due to Gosper (pers. comm., July 22, 1996) is the [double series](#)

$$W(x) = a + \sum_{n=0}^{\infty} \left\{ \sum_{k=0}^n \frac{S_1(n, k)}{[\ln(\frac{x}{a}) - a]^{k-1} (n-k+1)!} \right\} \left[1 - \frac{\ln(\frac{x}{a})}{a} \right]^n, \tag{19}$$

where S_1 is a [nonnegative Stirling number of the first kind](#) and a is a first approximation which can be used to select between branches. The Lambert W -function is two-valued for $-1/e \leq x < 0$. For $W(x) \geq -1$, the function is denoted $W_0(x)$ or simply $W(x)$, and this is called the [principal branch](#). For $W(x) \leq -1$, the function is denoted $W_{-1}(x)$. The [derivative](#) of W is

$$W'(x) = \frac{1}{[1 + W(x)] \exp[W(x)]} \tag{20}$$

$$= \frac{W(x)}{x [1 + W(x)]} \tag{21}$$

for $x \neq 0$. For the [principal branch](#) when $z > 0$,

$$\ln[W(z)] = \ln z - W(z). \tag{22}$$

The n th derivatives of the Lambert W -function are given by

$$W^{(n)}(z) = \frac{W^{n-1}(z)}{z^n [1 + W(z)]^{2n-1}} \sum_{k=1}^n a_{kn} W^k(z), \tag{23}$$

where a_{kn} is the number triangle

$$\begin{array}{ccccccc} & & & & & & 1 \\ & & & & & -2 & -1 \\ & & & 9 & 8 & 2 & \\ & & -64 & -79 & -36 & -6 & \\ 625 & 974 & 622 & 192 & 24 & & \end{array} \tag{24}$$

(OEIS A042977). This has [exponential generating function](#)

$$f(x) = \frac{W(e^x(x+y(1+x)^2)) - x}{1+x} \tag{25}$$

$$= y - \frac{1}{2!} (x+2)y^2 + \frac{1}{3!} (2x^2 + 8x + 9)y^3 - \frac{1}{4!} (6x^3 + 36x^2 + 79x + 64)y^4 + \dots \tag{26}$$

From:

Implications of Symmetry and Pressure in Friedmann Cosmology. I. Formalism

K. S. Croker and J. L. Weiner

Department of Physics and Astronomy, University of Hawai‘i at Mānoa, 2505 Correa Road, Honolulu, HI 96822, USA; kcroker@phys.hawaii.edu

Department of Mathematics, University of Hawai‘i at Mānoa, 2565 McCarthy Mall, Honolulu, HI 96822, USA

Received 2019 February 12; revised 2019 June 8; accepted 2019 July 15; published 2019 August 28

We have that:

$$\frac{\Delta E_{\text{star}}}{E_{\text{star}}} = \left(\frac{1}{1+2} \right)^{3 \times 10^{-7}} - 1 \simeq -10^{-7}.$$

$$(1/(1+2))^{(3e-7)}-1$$

Input interpretation:

$$\left(\frac{1}{1+2} \right)^{3 \times 10^{-7}} - 1$$

Result:

$$\frac{1}{3^{3/10000000}} - 1$$

Decimal approximation:

$$-3.295836322877356377122135707665837715955737794495012... \times 10^{-7}$$

$$-3.29583632... * 10^{-7}$$

Alternate forms:

$$\frac{1}{3} \left(3^{9999997/10000000} - 3 \right)$$

$$\frac{1 - 3^{3/10000000}}{3^{3/10000000}}$$

$$\frac{\Delta E_{\text{cluster}}}{E_{\text{cluster}}} = \left(\frac{1+1}{1+1.001} \right)^{3 \times 10^{-5}} - 1 \simeq -10^{-8}. \quad (116)$$

$$(((1+1)/(1+1.001)))^{(3e-5)-1}$$

Input interpretation:

$$\left(\frac{1+1}{1+1.001} \right)^{3 \times 10^{-5}} - 1$$

Result:

$$\begin{aligned} & -1.499625113708766221445023725294060759470745149850823... \times 10^{-8} \\ & -1.49962511... * 10^{-8} \end{aligned}$$

From the sum of the two results, we obtain:

$$((((1/(1+2))^{(3e-7)-1}))) + ((((((1+1)/(1+1.001)))^{(3e-5)-1})))$$

Input interpretation:

$$\left(\left(\frac{1}{1+2} \right)^{3 \times 10^{-7}} - 1 \right) + \left(\left(\frac{1+1}{1+1.001} \right)^{3 \times 10^{-5}} - 1 \right)$$

Result:

$$\begin{aligned} & -3.44580... \times 10^{-7} \\ & -3.4458... * 10^{-7} \end{aligned}$$

$$-1/[((((1/(1+2))^{(3e-7)-1}))) + ((((((1+1)/(1+1.001)))^{(3e-5)-1})))]$$

Input interpretation:

$$-\frac{1}{\left(\left(\frac{1}{1+2} \right)^{3 \times 10^{-7}} - 1 \right) + \left(\left(\frac{1+1}{1+1.001} \right)^{3 \times 10^{-5}} - 1 \right)}$$

Result:

$$\begin{aligned} & 2.90208467790073168742587892519336198124721057203979193... \times 10^6 \\ & 2902084.6779.... \end{aligned}$$

$$\ln^2(((((-1/[((((1/(1+2))^{(3e-7)-1}))) + ((((((1+1)/(1+1.001)))^{(3e-5)-1})))))))+34+1/\text{golden ratio}$$

Input interpretation:

$$\log^2 \left(-\frac{1}{\left(\left(\frac{1}{1+2} \right)^{3 \times 10^{-7}} - 1 \right) + \left(\left(\frac{1+1}{1+1.001} \right)^{3 \times 10^{-5}} - 1 \right)} \right) + 34 + \frac{1}{\phi}$$

$\log(x)$ is the natural logarithm

ϕ is the golden ratio

Result:

256.060...

256.060...

8sqrt((((((ln^2(((((-1/[(((1/(1+2))^3e-7)-1))) + (((((1+1)/(1+1.001)))^3e-5)-1)))))))+34)))))))-Pi+1/golden ratio

Input interpretation:

$$8 \sqrt{\log^2 \left(-\frac{1}{\left(\left(\frac{1}{1+2} \right)^{3 \times 10^{-7}} - 1 \right) + \left(\left(\frac{1+1}{1+1.001} \right)^{3 \times 10^{-5}} - 1 \right)} \right) + 34 - \pi + \frac{1}{\phi}}$$

$\log(x)$ is the natural logarithm

ϕ is the golden ratio

Result:

125.337...

125.337... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

8sqrt((((((ln^2(((((-1/[(((1/(1+2))^3e-7)-1))) + (((((1+1)/(1+1.001)))^3e-5)-1)))))))+55)))))))+7-1/golden ratio

Input interpretation:

$$8 \sqrt{\log^2 \left(-\frac{1}{\left(\left(\frac{1}{1+2} \right)^{3 \times 10^{-7}} - 1 \right) + \left(\left(\frac{1+1}{1+1.001} \right)^{3 \times 10^{-5}} - 1 \right)} \right) + 55 + 7 - \frac{1}{\phi}}$$

$\log(x)$ is the natural logarithm

ϕ is the golden ratio

Result:

139.394...

139.394... result practically equal to the rest mass of Pion meson 139.57 MeV

Note that, from the formula concerning the Coefficients of the '5th order' mock theta function $\psi_1(q)$, for $n = 541.94201$, we obtain:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{541.94201}{15}}\right)}{2 \sqrt[4]{5} \sqrt{541.94201}}$$

Input interpretation:

$$\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{541.94201}{15}}\right)}{2 \sqrt[4]{5} \sqrt{541.94201}}$$

ϕ is the golden ratio

Result:

$$2.90208419088668530116743324309952146822185039972468743... \times 10^6$$

2902084.19....

Series representations:

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{541.942}{15}}\right)}{2 \sqrt[4]{5} \sqrt{541.942}} = \frac{\exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (36.1295 - z_0)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!}}{2 \sqrt[4]{5} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (541.942 - z_0)^k z_0^{-k}}{k!}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{541.942}{15}}\right)}{2 \sqrt[4]{5} \sqrt{541.942}} = \left(\exp\left(i \pi \left\lfloor \frac{\arg(\phi - x)}{2 \pi} \right\rfloor\right) \right. \\ \left. \exp\left(\pi \exp\left(i \pi \left\lfloor \frac{\arg(36.1295 - x)}{2 \pi} \right\rfloor\right)\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (36.1295 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \\ \left. \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) / \\ \left(2 \sqrt[4]{5} \exp\left(i \pi \left\lfloor \frac{\arg(541.942 - x)}{2 \pi} \right\rfloor\right) \sum_{k=0}^{\infty} \frac{(-1)^k (541.942 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{541.942}{15}}\right)}{2 \sqrt[4]{5} \sqrt{541.942}} = \left(\exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(36.1295 - z_0) / (2 \pi) \rfloor} \right. \right. \\ \left. \left. z_0^{1/2 (1 + \lfloor \arg(36.1295 - z_0) / (2 \pi) \rfloor)} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (36.1295 - z_0)^k z_0^{-k}}{k!} \right) \right. \\ \left. \left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(541.942 - z_0) / (2 \pi) \rfloor + 1/2 \lfloor \arg(\phi - z_0) / (2 \pi) \rfloor} \right. \\ \left. z_0^{-1/2 \lfloor \arg(541.942 - z_0) / (2 \pi) \rfloor + 1/2 \lfloor \arg(\phi - z_0) / (2 \pi) \rfloor} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} \right) / \\ \left(2 \sqrt[4]{5} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (541.942 - z_0)^k z_0^{-k}}{k!} \right)$$

We have also that:

$$\left(\ln\left(\left(-1/\left[\left(\left(\left(1/(1+2)\right)^{(3e-7)-1}\right)\right)\right]\right)\right) + \left(\left(\left(\left(1+1\right)/\left(1+1.001\right)\right)\right)^{(3e-5)-1}\right)\right)\right) + 4 - 1/\text{golden ratio}$$

Input interpretation:

$$\log\left(\frac{1}{\left(\left(\frac{1}{1+2}\right)^{3 \times 10^{-7}} - 1\right) + \left(\left(\frac{1+1}{1+1.001}\right)^{3 \times 10^{-5}} - 1\right)}\right) + 4 - \frac{1}{\phi}$$

$\log(x)$ is the natural logarithm

ϕ is the golden ratio

Result:

18.2629...

18.2629.... result very near to the black hole entropy 18.2773

$$E_{\text{dS}} = 3M_{\odot} \left(\frac{1 + 1.5}{1 + 0.1} \right)^3 = 35.2M_{\odot}.$$

$$(3 \times 1.9891 \times 10^{30}) \times \left(\frac{1 + 1.5}{1 + 0.1} \right)^3$$

Input interpretation:

$$(3 \times 1.9891 \times 10^{30}) \left(\frac{1 + 1.5}{1 + 0.1} \right)^3$$

Result:

$$7.0051887678437265214124718256949661908339594290007513... \times 10^{31}$$
$$7.00518876... \times 10^{31}$$

$$1/\pi \times \ln \left(\left((3 \times 1.9891 \times 10^{30}) \times \left(\frac{1 + 1.5}{1 + 0.1} \right)^3 \right) \right)$$

Input interpretation:

$$\frac{1}{\pi} \log \left((3 \times 1.9891 \times 10^{30}) \left(\frac{1 + 1.5}{1 + 0.1} \right)^3 \right)$$

$\log(x)$ is the natural logarithm

Result:

$$23.34064186394113522995025338550979309995310889226732370714...$$

23.34064.... result very near to the black hole entropy 23.3621

From:

Dark Energy

N. Straumann

Institute for Theoretical Physics, University of Zurich, Winterthurerstrasse 180,
8057 Zurich, Switzerland - norbert.straumann@freesurf.ch

$$v = \sqrt{\frac{2m^2}{\lambda}} = 2^{-1/4} G_F^{-1/2} \sim 246 \text{ GeV}, \quad (16)$$

$$V(\phi = v) = -\frac{m^4}{2\lambda} = -\frac{1}{8\sqrt{2}} M_F^2 M_H^2 = \mathcal{O}(M_F^4). \quad (17)$$

$$M_F = G_F^{-1/2} \approx 300 \text{ GeV}$$

$$M_H = 125.18 \text{ GeV}$$

$$-1/(8\sqrt{2}) * (300^2 * 125.18^2)$$

Input interpretation:

$$\frac{300^2 \times 125.18^2}{8\sqrt{2}}$$

Result:

$$-1.2465434442884523920438649459232856223040033468795615... \times 10^8$$

$$-124654344.428$$

$$\text{For } n = 792.384$$

$$-\sqrt{\phi} * \exp(\pi * \sqrt{792.384/15}) / (2 * 5^{1/4} * \sqrt{792.384}) - \sqrt{729}$$

Input interpretation:

$$-\sqrt{\phi} \times \frac{\exp\left(\pi \sqrt{\frac{792.384}{15}}\right)}{2 \sqrt[4]{5} \sqrt{792.384}} - \sqrt{729}$$

ϕ is the golden ratio

Result:

$$-1.2465439799749910042371976489866068422042603693773138... \times 10^8$$

$$-1.246543979... * 10^8$$

Series representations:

$$\begin{aligned}
 & -\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{792.384}{15}}\right)}{2 \sqrt[4]{5} \sqrt{792.384}} - \sqrt{729} = \\
 & -\left(\left(5^{3/4} \exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (52.8256 - z_0)^k z_0^{-k}}{k!}\right) \right. \right. \\
 & \quad \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} + 10 \sqrt{z_0} \right. \\
 & \quad \left. \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{(-1)^{k_1+k_2} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} (729 - z_0)^{k_1} (792.384 - z_0)^{k_2} z_0^{-k_1-k_2}}{k_1! k_2!} \right) \\
 & \quad \left. \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (792.384 - z_0)^k z_0^{-k}}{k!} \right) \right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))
 \end{aligned}$$

$$\begin{aligned}
 & -\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{792.384}{15}}\right)}{2 \sqrt[4]{5} \sqrt{792.384}} - \sqrt{729} = \\
 & -\left(\left(5^{3/4} \exp\left(i \pi \left\lfloor \frac{\arg(\phi - x)}{2 \pi} \right\rfloor\right) \exp\left(\pi \exp\left(i \pi \left\lfloor \frac{\arg(52.8256 - x)}{2 \pi} \right\rfloor\right) \sqrt{x}\right) \right. \right. \\
 & \quad \sum_{k=0}^{\infty} \frac{(-1)^k (52.8256 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \sum_{k=0}^{\infty} \frac{(-1)^k (\phi - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \\
 & \quad 10 \exp\left(i \pi \left\lfloor \frac{\arg(729 - x)}{2 \pi} \right\rfloor\right) \exp\left(i \pi \left\lfloor \frac{\arg(792.384 - x)}{2 \pi} \right\rfloor\right) \sqrt{x} \\
 & \quad \left. \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{(-1)^{k_1+k_2} (729 - x)^{k_1} (792.384 - x)^{k_2} x^{-k_1-k_2} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2}}{k_1! k_2!} \right) \\
 & \quad \left. \left(10 \exp\left(i \pi \left\lfloor \frac{\arg(792.384 - x)}{2 \pi} \right\rfloor\right) \right. \right. \\
 & \quad \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k (792.384 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)
 \end{aligned}$$

$$\begin{aligned}
& -\frac{\sqrt{\phi} \exp\left(\pi \sqrt{\frac{792.384}{15}}\right)}{2 \sqrt[4]{5} \sqrt{792.384}} - \sqrt{729} = \\
& -\left[\left(\frac{1}{z_0}\right)^{-1/2 [\arg(792.384 - z_0)/(2\pi)]} z_0^{-1/2 [\arg(792.384 - z_0)/(2\pi)]} \right. \\
& \quad \left(5^{3/4} \exp\left(\pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(52.8256 - z_0)/(2\pi)]} z_0^{1/2 (1 + [\arg(52.8256 - z_0)/(2\pi)])}\right) \right. \\
& \quad \quad \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (52.8256 - z_0)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 [\arg(\phi - z_0)/(2\pi)]} \\
& \quad z_0^{1/2 [\arg(\phi - z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (\phi - z_0)^k z_0^{-k}}{k!} + \\
& \quad 10 \left(\frac{1}{z_0}\right)^{1/2 [\arg(729 - z_0)/(2\pi)] + 1/2 [\arg(792.384 - z_0)/(2\pi)]} \\
& \quad z_0^{1/2 + 1/2 [\arg(729 - z_0)/(2\pi)] + 1/2 [\arg(792.384 - z_0)/(2\pi)]} \\
& \quad \left. \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{(-1)^{k_1+k_2} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} (729 - z_0)^{k_1} (792.384 - z_0)^{k_2} z_0^{-k_1-k_2}}{k_1! k_2!} \right) \\
& \quad \left. / \left(10 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (792.384 - z_0)^k z_0^{-k}}{k!} \right) \right)
\end{aligned}$$

$$\ln(((-((-1)/(8\sqrt{2})) * (300^2 * 125.18^2))))$$

Input interpretation:

$$\log\left(-\frac{(300^2 \times 125.18^2)}{8 \sqrt{2}}\right)$$

log(x) is the natural logarithm

Result:

18.6411...

18.6411... result very near to the black hole entropy 18.7328

Alternative representations:

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) = \log_e\left(\frac{125.18^2 \times 300^2}{8\sqrt{2}}\right)$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) = \log(a) \log_a\left(\frac{125.18^2 \times 300^2}{8\sqrt{2}}\right)$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) = -\text{Li}_1\left(1 - \frac{125.18^2 \times 300^2}{8\sqrt{2}}\right)$$

Series representations:

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) = \log\left(-1 + \frac{1.76288 \times 10^8}{\sqrt{2}}\right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1.76288 \times 10^8}{\sqrt{2}}\right)^{-k}}{k}$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) = 2i\pi \left[\frac{\arg\left(-x + \frac{1.76288 \times 10^8}{\sqrt{2}}\right)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k x^{-k} \left(-x + \frac{1.76288 \times 10^8}{\sqrt{2}}\right)^k}{k} \quad \text{for } x < 0$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) = \left[\frac{\arg\left(\frac{1.76288 \times 10^8}{\sqrt{2}} - z_0\right)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg\left(\frac{1.76288 \times 10^8}{\sqrt{2}} - z_0\right)}{2\pi} \right] \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{1.76288 \times 10^8}{\sqrt{2}} - z_0\right)^k z_0^{-k}}{k}$$

Integral representations:

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) = \int_1^{\frac{1.76288 \times 10^8}{\sqrt{2}}} \frac{1}{t} dt$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) = \frac{1}{2i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s) \left(-1 + \frac{1.76288 \times 10^8}{\sqrt{2}}\right)^{-s}}{\Gamma(1-s)} ds$$

for $-1 < \gamma < 0$

$$\ln(\frac{(((-1)/(8\sqrt{2}))*(300^2*125.18^2))}{-2})$$

Input interpretation:

$$\log\left(-\frac{(300^2 \times 125.18^2)}{8 \sqrt{2}}\right) - 2$$

log(x) is the natural logarithm

Result:

16.6411...

16.6411... result very near to the mass of the hypothetical light particle, the boson $m_x = 16.84 \text{ MeV}$

Alternative representations:

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8 \sqrt{2}}\right) - 2 = -2 + \log_e\left(\frac{125.18^2 \times 300^2}{8 \sqrt{2}}\right)$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8 \sqrt{2}}\right) - 2 = -2 + \log(a) \log_a\left(\frac{125.18^2 \times 300^2}{8 \sqrt{2}}\right)$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8 \sqrt{2}}\right) - 2 = -2 - \text{Li}_1\left(1 - \frac{125.18^2 \times 300^2}{8 \sqrt{2}}\right)$$

Series representations:

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8 \sqrt{2}}\right) - 2 = -2 + \log\left(-1 + \frac{1.76288 \times 10^8}{\sqrt{2}}\right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1.76288 \times 10^8}{\sqrt{2}}\right)^{-k}}{k}$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8 \sqrt{2}}\right) - 2 = -2 + 2i\pi \left[\frac{\arg\left(-x + \frac{1.76288 \times 10^8}{\sqrt{2}}\right)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k x^{-k} \left(-x + \frac{1.76288 \times 10^8}{\sqrt{2}}\right)^k}{k} \text{ for } x < 0$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) - 2 = -2 + \left[\frac{\arg\left(\frac{1.76288 \times 10^8}{\sqrt{2}} - z_0\right)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) +$$

$$\log(z_0) + \left[\frac{\arg\left(\frac{1.76288 \times 10^8}{\sqrt{2}} - z_0\right)}{2\pi} \right] \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{1.76288 \times 10^8}{\sqrt{2}} - z_0\right)^k z_0^{-k}}{k}$$

Integral representations:

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) - 2 = -2 + \int_1^{\frac{1.76288 \times 10^8}{\sqrt{2}}} \frac{1}{t} dt$$

$$\log\left(-\frac{(300^2 \times 125.18^2)(-1)}{8\sqrt{2}}\right) - 2 =$$

$$-2 + \frac{1}{2i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s) \left(-1 + \frac{1.76288 \times 10^8}{\sqrt{2}}\right)^{-s}}{\Gamma(1-s)} ds \quad \text{for } -1 < \gamma < 0$$

From:

<http://www.mpia.de/~maccio/ringberg/Talks/Wetterich.pdf>

homogeneous dark energy: $\rho_h/M^4 = 6.5 \cdot 10^{-121}$

matter: $\rho_m/M^4 = 3.5 \cdot 10^{-121}$

$$6.5 * 10^{-121}$$

$$\left(\left(-\left(1/\ln(6.5e-121)\right)\right)\right)^{1/512}$$

Input:

$$\sqrt[512]{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}}$$

log(x) is the natural logarithm

Result:

0.98907750629...

0.98907750629... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

And:

$$((-1/\ln(3.5e-121)))^{1/512}$$

Input:

$$\sqrt[512]{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}}$$

$\log(x)$ is the natural logarithm

Result:

0.98907318992...

0.98907318992... as above

$$(e)^{1/-(((1 * 1/\ln(6.5e-121))))} + 8\pi + 3 * \text{golden ratio}$$

Input:

$$e^{\left(-\frac{1}{1 \times \frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}}\right)} + 8\pi + 3\phi$$

$\log(x)$ is the natural logarithm

ϕ is the golden ratio

Result:

782.24686...

782.24686... result practically equal to the rest mass of Omega meson 782.65 MeV

Alternative representations:

$$-\frac{e}{\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + 8\pi + 3\phi = 3\phi + 8\pi + -\frac{e}{\frac{1}{\log_e\left(\frac{6.5}{10^{121}}\right)}}$$

$$-\frac{e}{\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + 8\pi + 3\phi = 3\phi + 8\pi + -\frac{e}{\frac{1}{\log(a)\log_a\left(\frac{6.5}{10^{121}}\right)}}$$

$$-\frac{e}{\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + 8\pi + 3\phi = \left(3\phi + 8\pi + -\frac{e}{\frac{1}{\text{Li}_1\left(1-\frac{6.5}{10^{121}}\right)}} = 3\phi + 8\pi + e \text{Li}_1(1) \right)$$

Series representations:

$$-\frac{e}{\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + 8\pi + 3\phi = 3\phi + 8\pi - 2e i \pi \left[\frac{\arg(6.5 \times 10^{-121} - x)}{2\pi} \right] -$$

$$e \log(x) + e \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - x)^k x^{-k}}{k} \text{ for } x < 0$$

$$-\frac{e}{\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + 8\pi + 3\phi = 3\phi + 8\pi - e \left[\frac{\arg(6.5 \times 10^{-121} - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) - e \log(z_0) -$$

$$e \left[\frac{\arg(6.5 \times 10^{-121} - z_0)}{2\pi} \right] \log(z_0) + e \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k}$$

$$-\frac{e}{\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + 8\pi + 3\phi = 3\phi + 8\pi - 2e i \pi \left[-\frac{-\pi + \arg\left(\frac{6.5 \times 10^{-121}}{z_0}\right) + \arg(z_0)}{2\pi} \right] -$$

$$e \log(z_0) + e \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k}$$

Integral representation:

$$-\frac{e}{\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + 8\pi + 3\phi = 3\phi + 8\pi - e \int_1^{6.5 \times 10^{-121}} \frac{1}{t} dt$$

$$\left(\left(\left(-\frac{1}{\ln(6.5e-121)}\right)\right)^{1/512} + \left(-\frac{1}{\ln(3.5e-121)}\right)^{1/512}\right)$$

Input:

$${}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}}$$

log(x) is the natural logarithm

Result:

1.9781506962...

1.9781506962...

Alternative representations:

$${}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} = {}^{512}\sqrt{-\frac{1}{\log_e\left(\frac{3.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log_e\left(\frac{6.5}{10^{121}}\right)}}$$

$$\begin{aligned} & {}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} = \\ & {}^{512}\sqrt{-\frac{1}{\log(a) \log_a\left(\frac{3.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log(a) \log_a\left(\frac{6.5}{10^{121}}\right)}} \end{aligned}$$

$$\begin{aligned} & {}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} = \\ & \left({}^{512}\sqrt{\frac{-1}{-\text{Li}_1\left(1 - \frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{\frac{-1}{-\text{Li}_1\left(1 - \frac{3.5}{10^{121}}\right)}} \right) = 2 {}^{512}\sqrt{\frac{1}{\text{Li}_1(1)}} \end{aligned}$$

Series representations:

$$\begin{aligned}
 & {}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} = \\
 & {}^{512}\sqrt{-\frac{1}{2i\pi\left[\frac{\arg(3.5 \times 10^{-121} - x)}{2\pi}\right]} + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (3.5 \times 10^{-121} - x)^k x^{-k}}{k}} + \\
 & {}^{512}\sqrt{-\frac{1}{2i\pi\left[\frac{\arg(6.5 \times 10^{-121} - x)}{2\pi}\right]} + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - x)^k x^{-k}}{k}} \quad \text{for } x < 0
 \end{aligned}$$

$$\begin{aligned}
 & {}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} = \\
 & {}^{512}\sqrt{-\frac{1}{2i\pi\left[\frac{\pi - \arg\left(\frac{3.5 \times 10^{-121}}{z_0}\right) - \arg(z_0)}{2\pi}\right]} + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k}} + \\
 & {}^{512}\sqrt{-\frac{1}{2i\pi\left[\frac{\pi - \arg\left(\frac{6.5 \times 10^{-121}}{z_0}\right) - \arg(z_0)}{2\pi}\right]} + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k}}
 \end{aligned}$$

$$\begin{aligned}
 & {}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} = \\
 & \left(-\left[1 / \left(\left[\frac{\arg(3.5 \times 10^{-121} - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(3.5 \times 10^{-121} - z_0)}{2\pi} \right] \log(z_0) - \right. \right. \\
 & \quad \left. \left. \sum_{k=1}^{\infty} \frac{(-1)^k (3.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k} \right) \right] \right)^{(1/512)} + \\
 & \left(-\left[1 / \left(\left[\frac{\arg(6.5 \times 10^{-121} - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(6.5 \times 10^{-121} - z_0)}{2\pi} \right] \log(z_0) - \right. \right. \\
 & \quad \left. \left. \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k} \right) \right] \right)^{(1/512)}
 \end{aligned}$$

Integral representation:

$${}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} = {}^{512}\sqrt{-\frac{1}{\int_1^{3.5 \times 10^{-121}} \frac{1}{t} dt}} + {}^{512}\sqrt{-\frac{1}{\int_1^{6.5 \times 10^{-121}} \frac{1}{t} dt}}$$

$64 * [(((((-1/\ln(6.5e-121))))^{1/512} + ((-1/\ln(3.5e-121))))^{1/512})] - \pi + \text{golden ratio}$

Input:

$$64 \left({}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) - \pi + \phi$$

$\log(x)$ is the natural logarithm

ϕ is the golden ratio

Result:

125.07808589...

125.07808589... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

Alternative representations:

$$64 \left({}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) - \pi + \phi =$$

$$\phi - \pi + 64 \left({}^{512}\sqrt{-\frac{1}{\log_e\left(\frac{3.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log_e\left(\frac{6.5}{10^{121}}\right)}} \right)$$

$$64 \left({}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) - \pi + \phi =$$

$$\phi - \pi + 64 \left({}^{512}\sqrt{-\frac{1}{\log(a) \log_a\left(\frac{3.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log(a) \log_a\left(\frac{6.5}{10^{121}}\right)}} \right)$$

$$64 \left({}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) - \pi + \phi =$$

$$\left(\phi - \pi + 64 \left({}^{512}\sqrt{\frac{-1}{-\text{Li}_1\left(1 - \frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{\frac{-1}{-\text{Li}_1\left(1 - \frac{3.5}{10^{121}}\right)}} \right) \right) = \phi - \pi + 128 {}^{512}\sqrt{\frac{1}{\text{Li}_1(1)}}$$

Series representations:

$$64 \left(\sqrt[512]{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + \sqrt[512]{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) - \pi + \phi =$$

$$\phi - \pi + 64 \sqrt[512]{\frac{1}{2i\pi \left[\frac{\arg(3.5 \times 10^{-121} - x)}{2\pi} \right]} + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (3.5 \times 10^{-121} - x)^k x^{-k}}{k}} +$$

$$64 \sqrt[512]{\frac{1}{2i\pi \left[\frac{\arg(6.5 \times 10^{-121} - x)}{2\pi} \right]} + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - x)^k x^{-k}}{k}} \quad \text{for } x < 0$$

$$64 \left(\sqrt[512]{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + \sqrt[512]{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) - \pi + \phi = \phi - \pi +$$

$$64 \sqrt[512]{\frac{1}{2i\pi \left[\frac{\pi - \arg\left(\frac{3.5 \times 10^{-121}}{z_0}\right) - \arg(z_0)}{2\pi} \right]} + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k}} +$$

$$64 \sqrt[512]{\frac{1}{2i\pi \left[\frac{\pi - \arg\left(\frac{6.5 \times 10^{-121}}{z_0}\right) - \arg(z_0)}{2\pi} \right]} + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k}}$$

$$64 \left(\sqrt[512]{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + \sqrt[512]{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) - \pi + \phi =$$

$$\phi - \pi + 64 \left(- \left(1 / \left(\left[\frac{\arg(3.5 \times 10^{-121} - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(3.5 \times 10^{-121} - z_0)}{2\pi} \right] \right. \right. \right.$$

$$\left. \left. \left. \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k} \right) \right) \right)^{\wedge (1/512)} +$$

$$64 \left(- \left(1 / \left(\left[\frac{\arg(6.5 \times 10^{-121} - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(6.5 \times 10^{-121} - z_0)}{2\pi} \right] \right. \right. \right.$$

$$\left. \left. \left. \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k} \right) \right) \right)^{\wedge (1/512)}$$

Integral representation:

$$64 \left(\sqrt[512]{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + \sqrt[512]{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) - \pi + \phi =$$

$$\phi - \pi + 64 \sqrt[512]{-\frac{1}{\int_1^{3.5 \times 10^{-121}} \frac{1}{t} dt}} + 64 \sqrt[512]{-\frac{1}{\int_1^{6.5 \times 10^{-121}} \frac{1}{t} dt}}$$

$$64 * [(((((-1/\ln(6.5e-121))))^{1/512} + ((-1/\ln(3.5e-121))))^{1/512})] + 13$$

Input:

$$64 \left({}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) + 13$$

$\log(x)$ is the natural logarithm

Result:

139.60164456...

139.60164456... result practically equal to the rest mass of Pion meson 139.57 MeV

Alternative representations:

$$64 \left({}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) + 13 =$$

$$13 + 64 \left({}^{512}\sqrt{-\frac{1}{\log_e\left(\frac{3.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log_e\left(\frac{6.5}{10^{121}}\right)}} \right)$$

$$64 \left({}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) + 13 =$$

$$13 + 64 \left({}^{512}\sqrt{-\frac{1}{\log(a) \log_a\left(\frac{3.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log(a) \log_a\left(\frac{6.5}{10^{121}}\right)}} \right)$$

$$64 \left({}^{512}\sqrt{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) + 13 =$$

$$\left(13 + 64 \left({}^{512}\sqrt{\frac{-1}{-\text{Li}_1\left(1 - \frac{6.5}{10^{121}}\right)}} + {}^{512}\sqrt{\frac{-1}{-\text{Li}_1\left(1 - \frac{3.5}{10^{121}}\right)}} \right) \right) = 13 + 128 {}^{512}\sqrt{\frac{1}{\text{Li}_1(1)}}$$

Series representations:

$$\begin{aligned}
 & 64 \left(\sqrt[512]{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + \sqrt[512]{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) + 13 = \\
 & 13 + 64 \sqrt[512]{-\frac{1}{2i\pi \left[\frac{\arg(3.5 \times 10^{-121} - x)}{2\pi} \right]} + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (3.5 \times 10^{-121} - x)^k x^{-k}}{k}} + \\
 & 64 \sqrt[512]{-\frac{1}{2i\pi \left[\frac{\arg(6.5 \times 10^{-121} - x)}{2\pi} \right]} + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - x)^k x^{-k}}{k}} \quad \text{for } x < 0
 \end{aligned}$$

$$\begin{aligned}
 & 64 \left(\sqrt[512]{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + \sqrt[512]{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) + 13 = \\
 & 13 + 64 \sqrt[512]{-\frac{1}{2i\pi \left[\frac{\pi - \arg\left(\frac{3.5 \times 10^{-121}}{z_0}\right) - \arg(z_0)}{2\pi} \right]} + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k}} + \\
 & 64 \sqrt[512]{-\frac{1}{2i\pi \left[\frac{\pi - \arg\left(\frac{6.5 \times 10^{-121}}{z_0}\right) - \arg(z_0)}{2\pi} \right]} + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k}}
 \end{aligned}$$

$$\begin{aligned}
 & 64 \left(\sqrt[512]{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + \sqrt[512]{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) + 13 = \\
 & 13 + 64 \left(- \left(1 / \left(\left[\frac{\arg(3.5 \times 10^{-121} - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(3.5 \times 10^{-121} - z_0)}{2\pi} \right] \right. \right. \right. \\
 & \quad \left. \left. \left. \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k} \right) \right) \right)^{(1/512)} + \\
 & 64 \left(- \left(1 / \left(\left[\frac{\arg(6.5 \times 10^{-121} - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(6.5 \times 10^{-121} - z_0)}{2\pi} \right] \right. \right. \right. \\
 & \quad \left. \left. \left. \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (6.5 \times 10^{-121} - z_0)^k z_0^{-k}}{k} \right) \right) \right)^{(1/512)}
 \end{aligned}$$

Integral representation:

$$\begin{aligned}
 & 64 \left(\sqrt[512]{-\frac{1}{\log\left(\frac{6.5}{10^{121}}\right)}} + \sqrt[512]{-\frac{1}{\log\left(\frac{3.5}{10^{121}}\right)}} \right) + 13 = \\
 & 13 + 64 \sqrt[512]{-\frac{1}{\int_1^{3.5 \times 10^{-121}} \frac{1}{t} dt}} + 64 \sqrt[512]{-\frac{1}{\int_1^{6.5 \times 10^{-121}} \frac{1}{t} dt}}
 \end{aligned}$$

Acknowledgments

We would like to thank Prof. **George E. Andrews** Evan Pugh Professor of Mathematics at Pennsylvania State University for his great availability and kindness towards me

References

Andrews, George E. (1986), "**The fifth and seventh order mock theta functions**", *Transactions of the American Mathematical Society*, **293** (1): 113–134, doi:10.2307/2000275, ISSN 0002-9947, JSTOR 2000275, MR 0814916

Andrews, George E. (1988), "**Ramanujan's fifth order mock theta functions as constant terms**", *Ramanujan revisited (Urbana-Champaign, Ill., 1987)*, Boston, MA: Academic Press, pp. 47–56, MR 0938959