

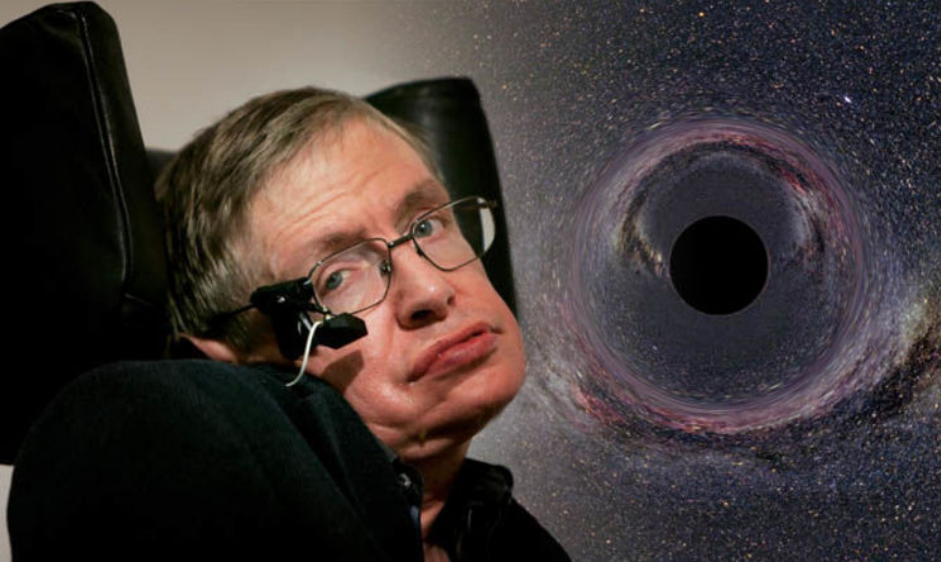
On the possible mathematical connections between some equations of the ‘Black Hole Entropy and Soft Hair’, Black Hole physics, Ramanujan’s Class Invariants and Mock Theta Functions

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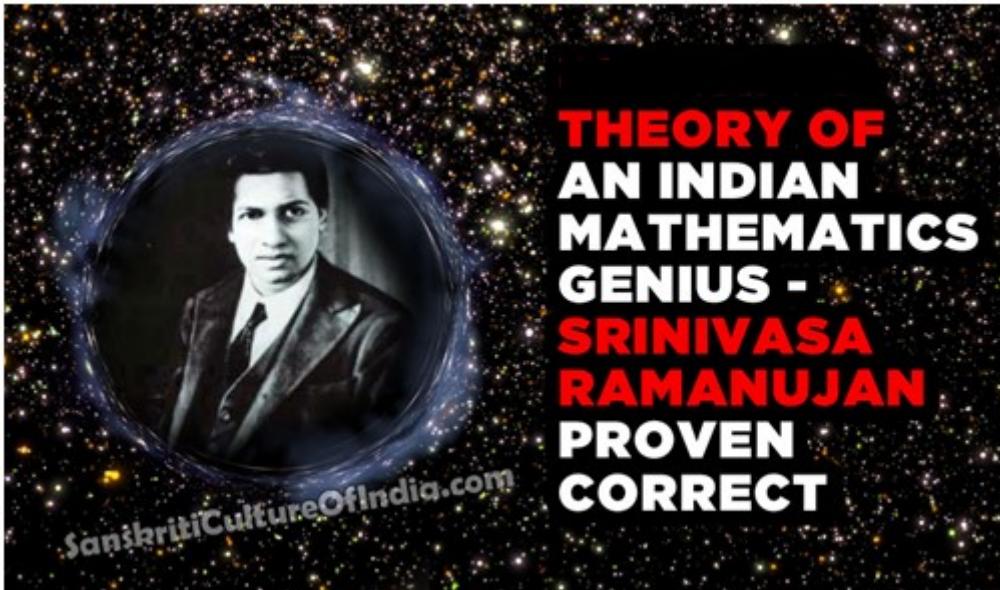
Abstract

In the present research thesis, we have obtained various and interesting mathematical connections between some equations of the ‘Black Hole Entropy and Soft Hair’, the fundamental last paper of S.W. Hawking, mathematics and physics of Black Hole, Ramanujan’s Class Invariants and Mock Theta Functions

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<https://www.express.co.uk/news/science/1030107/Stephen-Hawking-final-theory-black-holes-science-paper>



<https://www.sanskritimagazine.com/india/deathbed-theory-of-an-indian-mathematical-genius-proven-correct/>

From:

Black Hole Entropy and Soft Hair

Sasha Haco[†], Stephen W. Hawking, Malcolm J. Perry[†] and Andrew Strominger[†]

<https://arxiv.org/abs/1810.01847v4>

Throughout this paper we use units such that $c = \hbar = k = G = 1$.

2 Hidden conformal symmetry

Kerr black holes with generic mass M and spin $J \leq M^2$ exhibit a hidden conformal symmetry which acts on low-lying soft modes [52]. The symmetry emerges, not in a near-horizon region of *spacetime*, but in the near-horizon region of *phase space* defined by

$$\omega(r - r_+) \ll 1, \quad (2.1)$$

where ω is the energy of the soft mode, r is the Boyer-Lindquist radial coordinate and $r_+ = M + \sqrt{M^2 - a^2}$, with $a = \frac{J}{M}$, is the location of the outer horizon. This simply states that the soft mode wavelength is large compared to the black hole. One way to see the

Here the left and right temperatures are defined by

$$T_L = \frac{r_+ + r_-}{4\pi a}, \quad T_R = \frac{r_+ - r_-}{4\pi a}, \quad (2.4)$$

with $r_- = M - \sqrt{M^2 - a^2}$ and the left and right soft mode energies are

$$\omega_L = \frac{2M^2}{a}\omega, \quad \omega_R = \frac{2M^2}{a}\omega - m, \quad (2.5)$$

7 The area law

Using $c_L = c_R = 12J$ as given above, the temperature formulae (2.4) and the Cardy formula

$$S_{Cardy} = \frac{\pi^2}{3}(c_L T_L + c_R T_R), \quad (7.1)$$

yields the Hawking-Bekenstein area-entropy law for generic Kerr

$$S_{BH} = S_{Cardy} = 2\pi M r_+ = \frac{Area}{4}. \quad (7.2)$$

We have developed the eq (7.1) with the data of SMBH87, concerning the mass and the spin.

We have obtained the following expression:

For $a = J / M$, where $J = 0,9$ and $M = 13,12806 * 10^{39}$ that are J and M of SMBH87, we obtain:

$$(0.9 / 13.12806 * 10^{39})$$

Input interpretation:

$$\frac{0.9}{13.12806 \times 10^{39}}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

$$6.8555445359024867345213230286881687012399394883935631... \times 10^{-41}$$

[Open code](#)

Now, we have:

$$\begin{aligned} & \text{a) } (\pi^2)/3 * \\ & \left(\frac{(((((12 * 0.9^2 * 13.12806 * 10^{39}) / (4\pi * ((0.9 / 13.12806 * 10^{39})))))) + \right. \\ & \left. (((12 * 0.9^2 * \sqrt{((13.12806 * 10^{39})^2 - \right. \\ & \left. \left. ((0.9 / 13.12806 * 10^{39})^2)))))) / (4\pi * ((0.9 / 13.12806 * 10^{39})))))) \right) \end{aligned}$$

Input interpretation:

$$\frac{\pi^2}{3} \left(\frac{12 \times 0.9 \times 2 \times 13.12806 \times 10^{39}}{4 \pi \times \frac{0.9}{13.12806 \times 10^{39}}} + \frac{12 \times 0.9 \times 2 \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2}}{4 \pi \times \frac{0.9}{13.12806 \times 10^{39}}} \right)$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

Fewer digits

More digits

2.1657631992502831885592351242853104951226174156593896... × 10⁸¹

Input interpretation:

Or:

$$\text{b) } (\pi^2/3) * (((((((((6*0.9*13.12806*10^39)/((\pi*((0.9/13.12806*10^39)))))))))) + (((((6*0.9*\text{sqrt}(((13.12806*10^39)^2 - ((0.9/13.12806*10^39)^2)))))))/((\pi*((0.9/13.12806*10^39))))))))))$$

Input interpretation:

$$\frac{\pi^2}{3} \left(\frac{6 \times 0.9 \times 13.12806 \times 10^{39}}{\pi \times \frac{0.9}{13.12806 \times 10^{39}}} + \frac{6 \times 0.9 \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2}}{\pi \times \frac{0.9}{13.12806 \times 10^{39}}} \right)$$

[Open code](#)

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Result:

Fewer digits

More digits

2.1657631992502831885592351242853104951226174156593896... × 10⁸¹

Or:

$$\text{c) } 2(\pi) * (((((((((0.9*13.12806*10^39)/((0.9/13.12806*10^39)))))))) + (((((0.9*\text{sqrt}(((13.12806*10^39)^2 - ((0.9/13.12806*10^39)^2)))))))/((0.9/13.12806*10^39))))))))$$

Input interpretation:

$1.665318234631826747203812088027278191502787901128 \times 10^3$

Result:

1665.318234631826747203812088027278191502787901128

[Open code](#)

Now, we have that, calculating the integral of the above expression a), we obtain:

integrate (Pi^2)/3 *
 (((((((((12*0.9*2*13.12806*10^39)/((4Pi*((0.9/13.12806*10^39)))))))))) +
 (((((12*0.9*2*sqrt(((13.12806*10^39)^2-
 ((0.9/13.12806*10^39)^2)))))))/((4Pi*((0.9/13.12806*10^39)))))))))x

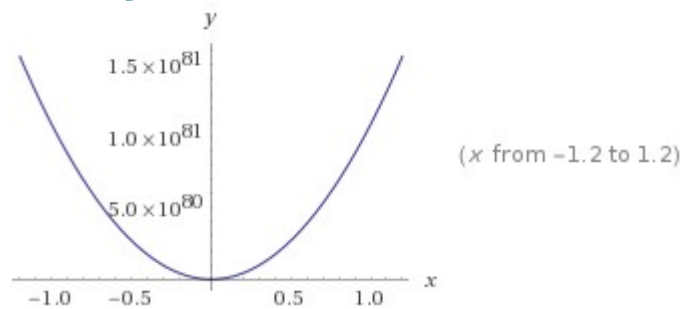
Indefinite integral:

$$\int \frac{1}{3} \pi^2 \left(\left(\frac{12 \times 0.9 \times 2 \times 13.12806 \times 10^{39}}{\frac{4 \pi 0.9}{13.12806 \times 10^{39}}} + \frac{12 \times 0.9 \times 2 \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2}}{\frac{4 \pi 0.9}{13.12806 \times 10^{39}}} \right) x \right) dx = 1.08288 \times 10^{81} x^2 + \text{constant}$$

[Open code](#)

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Plot of the integral:



[Open code](#)

Alternate form assuming x is real:

$$1.08288 \times 10^{81} x^2 + 0 + \text{constant}$$

[Open code](#)

Or, from c):

integrate 2(Pi) * ((((((((((0.9*13.12806*10^39)/((0.9/13.12806*10^39)))))))))) +
 (((((0.9*sqrt(((13.12806*10^39)^2-
 ((0.9/13.12806*10^39)^2)))))))/((0.9/13.12806*10^39))))))x

Indefinite integral:

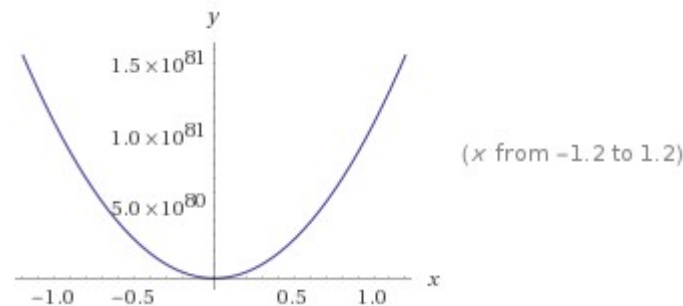
$$\int 2\pi \left[\frac{0.9 \cdot 13.12806 \times 10^{39}}{13.12806 \times 10^{39}} + \frac{0.9 \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2}}{13.12806 \times 10^{39}} \right] x dx =$$

$$1.08288 \times 10^{81} x^2 + \text{constant}$$

[Open code](#)

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Plot of the integral:



[Open code](#)

Alternate form assuming x is real:

$$1.08288 \times 10^{81} x^2 + 0 + \text{constant}$$

[Open code](#)

This result, for $x = 1$, is equal to:

Scientific notation:

$$1.08288 \times 10^{81}$$

[Open](#)

Continuing the integrations, we have:

integrate (1.08288×10^81)x

Indefinite integral:

$$\int 1.08288 \times 10^{81} x dx = 5.4144 \times 10^{80} x^2 + \text{constant}$$

[Open code](#)

integrate (5.4144×10^80)x

Indefinite integral:

$$\int 5.4144 \times 10^{80} x dx = 2.7072 \times 10^{80} x^2 + \text{constant}$$

[Open code](#)

integrate (2.7072×10^80) x

Indefinite integral:

$$\int 2.7072 \times 10^{80} x dx = 1.3536 \times 10^{80} x^2 + \text{constant}$$

[Open code](#)

integrate (1.3536×10^80) x

Indefinite integral:

$$\int 1.3536 \times 10^{80} x dx = 6.768 \times 10^{79} x^2 + \text{constant}$$

and so on.....

(Note that, for example, $0.06768 * 16 = 1,08288$; $0.13536 * 8 = 1,08288$;

$0.27072 * 4 = 1,08288$; $0.54144 * 2 = 1,08288$)

Continuing to carry out successive integrals of the values gradually obtained, the results will always be numbers with very high exponents, which decrease very slowly and are all sub-multiples of the initial result and of 1.08288 All this is strictly connected to that physical emission process of particles with a black hole called Hawking Radiation. Moreover, when the black hole emits Hawking radiation, the entropy must decrease! But, as you can already see from the results of the calculations, it will do it in extremely long times (it is calculated that the time that a black hole of a solar mass takes to evaporate is equal to 10^{67} years).

An identical result, we can to obtain, also as follows:

from eqs. (2.4) and (7.1), after some calculation, we obtain:

$$\frac{2\pi}{a} \left(MJ + \sqrt{M^2 - a^2} \right),$$

where $(MJ + \sqrt{M^2 - a^2})$, is:

$$(13.12806 * 10^{39} * 0.9) + \text{sqrt}((((13.12806 * 10^{39})^2 - (0.9 / 13.12806 * 10^{39})^2)))$$

Input interpretation:

$$13.12806 \times 10^{39} \times 0.9 + \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2}$$

[Open code](#)

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Result:

More digits

• $2.49433... \times 10^{40}$

Multiplying for $\frac{2\pi}{a}$, we obtain the final result of

$$\frac{2\pi}{a} \left(MJ + \sqrt{M^2 - a^2} \right),$$

$$2\text{Pi}/(6.8555445359024867345213230286881687012399394883935631 \times 10^{-41}) * (13.12806 * 10^{39} * 0.9) + \text{sqrt}(\left((13.12806 * 10^{39})^2 - (0.9 / 13.12806 * 10^{39})^2 \right))$$

Input interpretation:

$$2 \times \frac{\pi}{6.8555445359024867345213230286881687012399394883935631 \times 10^{-41}} \left((13.12806 \times 10^{39} \times 0.9) + \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}} \right)^2} \right)$$

[Open code](#)

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Result:

More digits

• $1.08288... \times 10^{81}$

Result:

Fewer digits

More digits

• $1.0828815996251415942796175621426552475613218358896948... \times 10^{81}$

• $1.08288159962514159427961756214265524756132183588 \times 10^{81}$

This result is identical to that obtained previously calculating the integral.

Now, we have:

$$\left((1.08288159962514159427961756214265524756132183588 \times 10^{81}) \right)^6$$

Input interpretation:

$$\left(1.08288159962514159427961756214265524756132183588 \times 10^{81} \right)^6$$

[Open code](#)

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Result:

• $1.61244847308029939489786323492279358431379319686 \times 10^{486}$

• $1.61244847308029939489786323492279358431379319686 \times 10^{486}$

Note that we have from the result of Cardy formula without exponent, the following expressions:

$$(1.0828815996251415942796175621426552475613218358896948)^6$$

Input interpretation:

$$1.08288159962514159427961756214265524756132183588^6$$

[Open code](#)

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Result:

More digits

$$1.612448473080299394897863234922793584313793196864917397696\dots$$

$$1.612448473080299394897863234922793584313793196864917397696$$

Continued fraction:

Linear form

$$\begin{aligned}
 &1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{2 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{2 + \cfrac{1}{2 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{3 + \cfrac{1}{4 + \cfrac{1}{1 + \cfrac{1}{4 + \cfrac{1}{9 + \cfrac{1}{\dots}}
 \end{aligned}$$

[Open code](#)

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Possible closed forms:

More

$$\frac{\log\left(\frac{13137257}{10779}\right)}{\log(82)} \approx 1.61244847308029943816$$

$$e^{3-31/e-35e+25/\pi+11\pi} \pi^{14+18e} \sin^9(e\pi) \cos^{18}(e\pi) \approx 1.61244847308029940447$$

$$\frac{1169706941\pi}{2278983046} \approx 1.61244847308029939498927$$

That is:

$1.612448473080299394897863234922793584313793196864917397696 \times 10^{81}$

Note that, from the following mean of 7th and 5th exponentiations, we obtain:

$$1/2 * (((((1.082881599625)^7 + (1.082881599625)^5))))$$

Input interpretation:

$$\frac{1}{2} (1.082881599625^7 + 1.082881599625^5)$$

[Open code](#)

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Result:

More digits

1.617562831071441789804763989413458288414723274020485801164...

This result is a very good approximation to the value of golden ratio

Then, we have that:

$$(1.612448473080299394897863234922793584313793196864917397696)^{1/6}$$

Input interpretation:

$$\sqrt[6]{1.612448473080299394897863234922793584313793196864917397696}$$

[Open code](#)

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Result:

More digits

1.082881599625141594279617562142655247561321835879999999999...

All 6th roots of 1.612448473080299394897863234922793584313793196864917397696:

More roots

More digits

Show trigonometric form

$$1.082881599625141594279617562142655247561321835879999999999 e^0$$

$$\approx 1.0829 \text{ (real, principal root)}$$

[Open code](#)

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$$1.082881599625141594279617562142655247561321835879999999999 e^{(i \pi)/3}$$

$$\approx 0.54144 + 0.93780 i$$

[Open code](#)

$$1.082881599625141594279617562142655247561321835879999999999 e^{(2 i \pi)/3}$$

$$\approx -0.54144 + 0.93780 i$$

[Open code](#)

$1.0828815996251415942796175621426552475613218358799999999999999 e^{i\pi}$
 ≈ -1.0829 (real root)
[Open code](#)

$1.0828815996251415942796175621426552475613218358799999999999999 e^{-(2i\pi)/3}$
 $\approx -0.54144 - 0.93780i$

We note that:

1.0828815996251415942796175621426552475613218358799999999999999

Input interpretation:

1.0828815996251415942796175621426552475613218358799999999999999
[Open code](#)

Continued fraction:

Linear form

$$\begin{aligned}
 & 1 + \cfrac{1}{12 + \cfrac{1}{15 + \cfrac{1}{3 + \cfrac{1}{2 + \cfrac{1}{4 + \cfrac{1}{1 + \cfrac{1}{9 + \cfrac{1}{1 + \cfrac{1}{5 + \cfrac{1}{1 + \cfrac{1}{3 + \cfrac{1}{7 + \cfrac{1}{5 + \cfrac{1}{3 + \cfrac{1}{1 + \cfrac{1}{3 + \cfrac{1}{1 + \cfrac{1}{2 + \cfrac{1}{1 + \cfrac{1}{6 + \cfrac{1}{1 + \cfrac{1}{\dots}} \\
 & \dots
 \end{aligned}$$

[Open code](#)

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Possible closed forms:

More

- $\frac{82\,649\,431\pi}{239\,777\,687} \approx 1.08288159962514159445780$
 $\frac{16\,935\,061\pi^2}{154\,349\,610} \approx 1.08288159962514161623$
 $\frac{174\,580\pi^2 - 921\,313}{235\,664\pi} \approx 1.0828815996251415939826$

From:

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Possible closed forms:

More

$$\pi^4 \approx 97.4090910340$$

$$36 \zeta(2)^2 \approx 97.4090910340$$

$$98 - 5 \mathcal{P}_c(5D \text{ bond}) \approx 97.4089999$$

We observe that, from this last result, we obtain:

$$97.4090910340 * 1.08288159962514159427961756214265524756132183588^{\pi}$$

Input interpretation:

$$97.4090910340 \times 1.08288159962514159427961756214265524756132183588^{\pi}$$

[Open code](#)

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Result:

More digits

$$125.094675636\dots$$

Series representations:

More

$$97.40909103400000 \times$$

$$1.082881599625141594279617562142655247561321835880000^{\pi} =$$

$$97.40909103400000 \times$$

$$1.082881599625141594279617562142655247561321835880000^{4 \sum_{k=0}^{\infty} (-1)^k / (1+2k)}$$

[Open code](#)

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$$97.40909103400000 \times$$

$$1.082881599625141594279617562142655247561321835880000^{\pi} =$$

$$83.06872455692809$$

$$0.159251271499448259511322372193820976747202644975596 \times \sum_{k=1}^{\infty} 2^k / \binom{2k}{k}$$

e

[Open code](#)

$$97.40909103400000 \times$$

$$1.082881599625141594279617562142655247561321835880000^{\pi} =$$

$$97.40909103400000 \times$$

$$1.082881599625141594279617562142655247561321835880000^{\cdot}$$

$$\sum_{k=0}^{\infty} (2^{-k} (-6+50k)) / \binom{3k}{k}$$

$\binom{n}{m}$ is the binomial coefficient

Integral representations:

More

$$97.40909103400000 \times 1.082881599625141594279617562142655247561321835880000^\pi = 97.40909103400000 e^{0.159251271499448259511322372193820976747202644975596 \int_0^\infty 1/(1+t^2) dt}$$

Open code

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$$97.40909103400000 \times 1.082881599625141594279617562142655247561321835880000^\pi = 97.40909103400000 e^{0.318502542998896519022644744387641953494405289951193 \int_0^1 \sqrt{1-t^2} dt}$$

Open code

$$97.40909103400000 \times 1.082881599625141594279617562142655247561321835880000^\pi = 97.40909103400000 e^{0.159251271499448259511322372193820976747202644975596 \int_0^\infty \sin(t)/t dt}$$

Open code

Or:

$$\pi^4 * 1.0829^\pi$$

Input interpretation:

$$\pi^4 \times 1.0829^\pi$$

Open code

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Result:

Fewer digits

More digits

$$125.1013535729926354455786502597054782033835729788897557110... \\ 125.10135357299263544557865025970547820338357297888975$$

Series representations:

More

$$\pi^4 1.0829^\pi = 256 \times 1.0829^{4 \sum_{k=0}^\infty (-1)^k / (1+2k)} \left(\sum_{k=0}^\infty \frac{(-1)^k}{1+2k} \right)^4$$

Open code

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$$\pi^4 1.0829^\pi = 1.0829^{x+2 \sum_{k=1}^\infty \sin(kx)/k} \left(x + 2 \sum_{k=1}^\infty \frac{\sin(kx)}{k} \right)^4 \text{ for } (x \in \mathbb{R} \text{ and } x > 0)$$

Open code

$$\pi^4 1.0829^\pi = 1.0829^{\sum_{k=0}^{\infty} (2^{-k} (-6+50k)) / \binom{3k}{k}} \left(\sum_{k=0}^{\infty} \frac{2^{-k} (-6+50k)}{\binom{3k}{k}} \right)^4$$

Integral representations:

More

$$\pi^4 1.0829^\pi = 16 e^{0.159285} \int_0^{\infty} \frac{1}{(1+t^2)} dt \left(\int_0^{\infty} \frac{1}{1+t^2} dt \right)^4$$

[Open code](#)

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$$\pi^4 1.0829^\pi = 16 e^{0.159285} \int_0^{\infty} \frac{\sin(t)}{t} dt \left(\int_0^{\infty} \frac{\sin(t)}{t} dt \right)^4$$

[Open code](#)

$$\pi^4 1.0829^\pi = 256 e^{0.318571} \int_0^1 \sqrt{1-t^2} dt \left(\int_0^1 \sqrt{1-t^2} dt \right)^4$$

Continued fraction:

Linear form

$$125 + \cfrac{1}{9 + \cfrac{1}{1 + \cfrac{1}{6 + \cfrac{1}{2 + \cfrac{1}{20 + \cfrac{1}{11 + \cfrac{1}{1 + \cfrac{1}{449 + \cfrac{1}{1 + \cfrac{1}{11 + \cfrac{1}{9 + \cfrac{1}{3 + \cfrac{1}{2 + \cfrac{1}{2 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{2 + \cfrac{1}{5 + \cfrac{1}{8 + \cfrac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

[Open code](#)

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Possible closed forms:

More

$$-e^{50-18/e-6e-53/\pi-11\pi} \pi^{20-e} \tan^{15}(e\pi) \sec^{14}(e\pi) \approx 125.101353572992635492346$$

$$\sqrt{-10679 - 7229e + 13453\pi + 5361 \log(2)} \approx 125.1013535729926354436935$$

$$\frac{1}{55} (-99 C - 335 + 138 \pi + 689 \pi^2 + 46 \pi \log(2) - 8 \pi \log(3)) \approx 125.101353572992635445562990$$

- $\sec(x)$ is the secant function
- $\log(x)$ is the natural logarithm
- C is Catalan's constant

This results 125,0946 and 125,1013 are practically equals to the Higgs boson mass, that is $125.18 \pm 0.16 \text{ GeV}/c^2$ that in energy is equal to $11,2662 * 10^{18}$

We obtain from 11.2662 without exponent, the following interesting result:

$$(11.2662)^{1/5}$$

Input interpretation:

$$\sqrt[5]{11.2662}$$

[Open code](#)

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Result:

Fewer digits

More digits

1.623138171930418428297253030579660681738707040868261370199...

1.6231381719304184282972530305796606817387070408682613

Continued fraction:

Linear form

$$1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{7 + \cfrac{1}{1 + \cfrac{1}{3 + \cfrac{1}{3 + \cfrac{1}{2 + \cfrac{1}{1 + \cfrac{1}{2 + \cfrac{1}{1 + \cfrac{1}{5 + \cfrac{1}{1 + \cfrac{1}{2 + \cfrac{1}{88 + \cfrac{1}{2 + \cfrac{1}{3 + \cfrac{1}{1 + \cfrac{1}{5 + \cfrac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

[Open code](#)

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Possible closed forms:

More

$$\frac{449 e e! - 8544 - 1996 e + 1228 e^2}{69 e} \approx 1.623138171930418430342$$

$$\frac{-2457 \pi \pi! - 1337 + 3210 \pi + 4785 \pi^2}{96 \pi} \approx 1.62313817193041842897710$$

$$\frac{5202007529 \pi}{10068513525} \approx 1.623138171930418428278961$$

Or, with the our results:

$$125,0946 * 9 * 10^{16} \text{ and } 125,1013 * 9 * 10^{16}$$

11,258514

11,259117

$$(11.258514)^{1/5}$$

Input interpretation:
 $\sqrt[5]{11.258514}$
[Open code](#)

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Result:

Fewer digits
 More digits

1.622916644782496914075814568204967079975605753418804467974...

1.6229166447824969140758145682049670799756057534188044

$$(11.259117)^{1/5}$$

Input interpretation:
 $\sqrt[5]{11.259117}$
[Open code](#)

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Result:

Fewer digits
 More digits

1.622934028919901880787518687142137712847096507259306533880...

1.6229340289199018807875186871421377128470965072593065

Now, we note that:

1.612448473080299394897863234922793584313793196864917397696

1.6229166447824969140758145682049670799756057534188044

1.6229340289199018807875186871421377128470965072593065

This result is a very good approximation to the value of the golden ratio
1,618033988749...

Now, we have from the initial result:

$$(((90 * 1.0828815996251415942796175621426552475613218358896948))) * 18 - 27$$

Input interpretation:

$$(90 \times 1.0828815996251415942796175621426552475613218358896948) \times 18 - 27$$

[Open code](#)

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Result:

$$1727.268191392729382732980450671101501049341374141305576$$

[Open code](#)

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$(((((((90 * 1.0828815996251415942796175621426552475613218358896948))) * 18 - 27))))))^{1/3}$$

Input interpretation:

$$\sqrt[3]{(90 \times 1.0828815996251415942796175621426552475613218358896948) \times 18 - 27}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

$$11.998305759401271268515373020771298000350981408462118...$$

This result is very near to the value of black hole entropy 12,1904

$$2 * (((((((90 * 1.0828815996251415942796175621426552475613218358896948))) * 18 - 27))))))^{1/3}$$

Input interpretation:

Using $c_L = c_R = 12J$ as given above, the temperature formulae (2.4) and the Cardy formula

$$S_{Cardy} = \frac{\pi^2}{3}(c_L T_L + c_R T_R),$$

yields the Hawking-Bekenstein area-entropy law for generic Kerr

$$S_{BH} = S_{Cardy} = 2\pi M r_+ = \frac{Area}{4}.$$

We observe that from the Cardy formula, we have obtained: **a)** 1.612448473080299, a golden number; **b)** 125,0946 and 125,1013 values practically equals to the Higgs boson mass; **c)** $125,0946 * 9 * 10^{16} = 11.258514$ and $125,1013 * 9 * 10^{16} = 11,259117$ that are the values of Higgs boson energy; **d)** from the mean of the following results: 1.6124484730802; 1.6229166447824; 1.6229340289199 we have obtained 1.61768690496, a very good approximation to the golden ratio; **e)** the value 1727,26819 result that is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729. **f)** from this last result, we have obtained 11,9983 that is very near to the black hole entropy 12,1904 (that is the ln of 196884) and 23,9966 value that is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string; **g)** 1.6437054117109, which is a recurring number in Ramanujan's equations.

Now, from the result of Cardy formula, we obtain:

$$1.0828815996251415942796175621426552475613218358896948 * 10^{81} * 33021.10 * \left(\frac{5(\sqrt{34} + \sqrt{21})}{3} \right)$$

Where 33021,10 is a result of Mock Theta Function

Input interpretation:

$$1.0828815996251415942796175621426552475613218358896948 \times 10^{81} \times 33021.10 \left(5 \left(\frac{1}{3} \left(\sqrt{34} + \sqrt{21} \right) \right) \right)$$

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Result:

More digits

$$6.206105... \times 10^{86}$$

$$1.0828815996251415942796175621426552475613218358896948 * 10^{81} * 1/3 * 33021.10 * (((5(\sqrt{34}+\sqrt{21}))/3)))$$

Input interpretation:

$$1.0828815996251415942796175621426552475613218358896948 \times 10^{81} \times \frac{1}{3} \times 33\,021.10 \left(5 \left(\frac{1}{3} \left(\sqrt{34} + \sqrt{21} \right) \right) \right)$$

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Result:

More digits

$$2.068702... \times 10^{86}$$

The results $6,206105 * 10^{86}$ and $2,068702 * 10^{86}$ are the values of Dark Matter and Relic Gravitons entropies contained within the cosmic event horizon.

From the:

$$r_+ = M + \sqrt{M^2 - a^2}$$

We obtain:

$$(((((((13.12806 * 10^{39} + (((\sqrt{(13.12806 * 10^{39})^2 - ((0.9 / (13.12806 * 10^{39}))^2))))))))))$$

Input interpretation:

$$13.12806 \times 10^{39} + \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}} \right)^2}$$

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Result:

More digits

$$2.62561... \times 10^{40}$$

For r.

$$r_- = M - \sqrt{M^2 - a^2}$$

We obtain:

$$\text{(((((((13.12806*10^39 - (((sqrt((13.12806*10^39)^2 - ((0.9/(13.12806*10^39)))^2))))))))))$$

Input interpretation:

$$13.12806 \times 10^{39} - \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2}$$

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Result:

0

[Open code](#)

$$\text{sqrt(((((((((((13.12806*10^39 + (((sqrt((13.12806*10^39)^2 - ((0.9/(13.12806*10^39)))^2))))))))))))))$$

Input interpretation:

$$\sqrt{13.12806 \times 10^{39} + \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- Fewer digits
- More digits

$$1.6203740308953362141944391269810617183098199027403399... \times 10^{20}$$

$$1.62037403089533621419443912698106171830981990274 \times 10^{20}$$

From:

$$\omega(r - r_+) \ll 1,$$

We obtain the value of r for $\omega = 6.62606957 * 10^{-34}$:

$$1/(6.62606957*10^{-34}) * \text{(((((((((((13.12806*10^39 + (((sqrt((13.12806*10^39)^2 - ((0.9/(13.12806*10^39)))^2)))))))))))))) * 6.62606957*10^{-34} + 0.08333))$$

Input interpretation:

$$\frac{1}{6.62606957 \times 10^{-34}} \left(\left(13.12806 \times 10^{39} + \sqrt{(13.12806 \times 10^{39})^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2} \right) \times 6.62606957 \times 10^{-34} + 0.08333 \right)$$

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Result:

• More digits

$$2.62561... \times 10^{40}$$

This result is identical to the previous expression concerning r_+

For:

$$w^+ = \sqrt{\frac{r - r_+}{r - r_-}} e^{2\pi T_R \phi},$$

We obtain:

$$\text{sqrt}(\left(\left(\left(2.62561 \times 10^{40} + 2.62561 \times 10^{40}\right) / \left(2.62561 \times 10^{40}\right)\right)\right)) * \exp(2\pi * (2.62561 \times 10^{40}) / \left(\left(4\pi * (0.9 / 13.12806 \times 10^{39})\right)\right))$$

Input interpretation:

$$\sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}} \exp\left(2\pi \times \frac{2.62561 \times 10^{40}}{4\pi \times \frac{0.9}{13.12806 \times 10^{39}}}\right)$$

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Power of 10 representation:

$$10^{79.91994257691320}$$

We have that $T_R = (2.62561 \times 10^{40}) / \left(\left(4\pi * (0.9 / 13.12806 \times 10^{39})\right)\right)$

For:

$$\phi = \frac{1}{4\pi T_R} \ln \frac{w^+ (w^+ w^- + y^2)}{w^-}$$

From the above expression with positive sign, we obtain:

$$\ln \left(\left(\left(\left(\left(\sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}} \right) \exp \left(2\pi \times \frac{2.62561 \times 10^{40}}{4\pi \times \frac{0.9}{13.12806 \times 10^{39}}} \right) \right) \right) \right) \right)^2 \right)^2$$

Input interpretation:

$$\log \left(\left(\sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}} \exp \left(2\pi \times \frac{2.62561 \times 10^{40}}{4\pi \times \frac{0.9}{13.12806 \times 10^{39}}} \right) \right) \right)^2$$

- $\log(x)$ is the natural logarithm

Decimal approximation:

More digits

$$3.82991... \times 10^{80}$$

From this result we obtain:

$$(3.829907290733333333 \times 10^{80})^{\pi/34^2}$$

Input interpretation:

$$(3.829907290733333333 \times 10^{80})^{\pi/34^2}$$

Result:

More digits

$$1.65575529459346779927...$$

$$1.65575529459346779927$$

Continued fraction:

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{9 + \frac{1}{1 + \frac{1}{1 + \frac{1}{14 + \frac{1}{1 + \frac{1}{3 + \frac{1}{15 + \frac{1}{2 + \frac{1}{13 + \frac{1}{1 + \frac{1}{5 + \frac{1}{3 + \frac{1}{1 + \frac{1}{4 + \frac{1}{3 + \frac{1}{2 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}$$

Possible closed forms:

More

$$\pi \sqrt{\text{root of } 867x^3 - 52302x^2 + 15595x + 6182 \text{ near } x = 0.527043} \approx 1.655755294593467799257124$$

$$\text{root of } 9188x^3 - 60222x^2 + 32189x + 70096 \text{ near } x = 1.65576 \approx$$

$$\frac{1.655755294593467799263669 \cdot 327494505\pi}{621380668} \approx 1.65575529459346779948852$$

We note that, the result 1,65575529... is practically equal to the 14th root of the following Ramanujan's class invariant $Q = (G_{505}/G_{101/5})^3 = 1164,2696$ i.e. 1,65578...

Indeed:

$$\begin{aligned} & \sqrt[14]{\left(\sqrt{\frac{113+5\sqrt{505}}{8}} + \sqrt{\frac{105+5\sqrt{505}}{8}}\right)^3} = 1,65578 \dots \Rightarrow \\ & \Rightarrow \log\left(\left(\sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}} \exp\left(2\pi \times \frac{2.62561 \times 10^{40}}{4\pi \times \frac{0.9}{13.12806 \times 10^{39}}}\right)\right)^2\right) \Rightarrow \\ & \Rightarrow (3.829907290733333333 \times 10^{80})^{\pi/34^2} \\ & = 1.65575529459346779927\dots \\ & \quad 1.65575529459346779927 \end{aligned}$$

From:

$$T_R = \frac{r_+ - r_-}{4\pi a},$$

$$w^+ = \sqrt{\frac{r_- - r_+}{r_- - r_-}} e^{2\pi T_R \phi},$$

$$\phi = \frac{1}{4\pi T_R} \ln \frac{w^+(w^+ w^- + y^2)}{w^-},$$

We obtain the following inverse formula:

$$\exp \frac{2\pi T_R}{\ln(\omega^+)^2}$$

That yield:

$$\exp\left(\frac{2\pi \times 2.62561 \times 10^{40}}{\left(4\pi \times \frac{0.9}{13.12806 \times 10^{39}}\right) \log\left(\left(\sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}}\right) \exp\left(2\pi \times \frac{2.62561 \times 10^{40}}{4\pi \times \frac{0.9}{13.12806 \times 10^{39}}}\right)\right)^2}\right)$$

Input interpretation:

$$\exp\left(\frac{2\pi \times 2.62561 \times 10^{40}}{\left(4\pi \times \frac{0.9}{13.12806 \times 10^{39}}\right) \log\left(\left(\sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}}\right) \exp\left(2\pi \times \frac{2.62561 \times 10^{40}}{4\pi \times \frac{0.9}{13.12806 \times 10^{39}}}\right)\right)^2}\right)$$

Open code

- $\log(x)$ is the natural logarithm

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Result:

- Fewer digits
- More digits

1.648721270700128146848650787814163571653776100710148011575...

Or:

$$\exp\left(\frac{2\pi \times 2.62561 \times 10^{40}}{\left(4\pi \times \frac{0.9}{13.12806 \times 10^{39}}\right) \log\left(\left(\sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}}\right) \exp\left(2\pi \times \frac{2.62561 \times 10^{40}}{4\pi \times \frac{0.9}{13.12806 \times 10^{39}}}\right)\right)^2}\right)$$

Input interpretation:

$$\exp\left(\frac{2\pi \times 2.62561 \times 10^{40}}{\left(4\pi \times \frac{0.9}{13.12806 \times 10^{39}}\right) \log\left(\left(\sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}}\right) \exp\left(2\pi \times \frac{2.62561 \times 10^{40}}{4\pi \times \frac{0.9}{13.12806 \times 10^{39}}}\right)\right)^2}\right)$$

Open code

- $\log(x)$ is the natural logarithm

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Result:

- Fewer digits
- More digits

1.648721270700128146848650787814163571653776100710148011575...

1.6487212707001281468486507878141635716537761007101480

Continued fraction:

Linear form

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{5 + \frac{1}{1 + \frac{1}{1 + \frac{1}{9 + \frac{1}{1 + \frac{1}{13 + \frac{1}{1 + \frac{1}{17 + \frac{1}{1 + \frac{1}{21 + \frac{1}{1 + \frac{1}{25 + \frac{1}{1 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

Open code

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Possible closed forms:

More

$$\sqrt{e} \approx 1.648721270700128146848650787814163571653776100710148011575$$

$$e^{(5\sqrt{W_{Wad}})^3} \approx 1.648721270700128146848650787814163571653776100710148011575$$

$$\frac{3(-26 - 217\pi + 87\pi^2)}{-717 - 564\pi + 280\pi^2} \approx 1.6487212707001281451501$$

From:

$$w^+ = \sqrt{\frac{r - r_+}{r - r_-}} e^{2\pi T_R \phi},$$

where $\phi = 1.64872127 \dots$

we obtain:

$$\sqrt{\left(\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}\right)} \exp^{(\left(\left(\left(\left(1.64872127\right)2\pi\left(2.62561 \times 10^{40}\right)\right)\right)\left(\left(\left(4\pi\left(0.9/13.12806 \times 10^{39}\right)\right)\right)\right)\right))}$$

Input interpretation:

$$\sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}} \exp^{1.64872127 \times 2 \left(\frac{\pi \times \frac{2.62561 \times 10^{40}}{0.9}}{4\pi \times \frac{13.12806 \times 10^{39}}{13.12806 \times 10^{39}}} \right) (x)}$$

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Result:

$$1.41421 (e^x)^{3.15722 \times 10^{80}}$$

Series expansion at $x = 0$:

$$1.41421 + 4.46499 \times 10^{80} x + 7.04849 \times 10^{160} x^2 + 7.41789 \times 10^{240} x^3 + 5.854984930671623 \times 10^{320} x^4 + O(x^5)$$

(Taylor series)

[Open code](#)

Derivative:

Step-by-step solution

$$\frac{d}{dx} \left(1.41421 e^{315722480618006001565027434922798913353137634282076546079289821671035852078186496x} \right) = 446499014036060737765539835224486169654060965317631814922928 \cdot 252925291033599672320 e^{315722480618006001565027434922798913353137634282076546079289821671035852078186496x}$$

The result of $w^+ = ((((((1.41421 (e^1)^{(3.15722 \times 10^{80}})))))))))$

Indefinite integral:

$$\int \sqrt{\frac{2.62561 \times 10^{40} + 2.62561 \times 10^{40}}{2.62561 \times 10^{40}}} \exp \left(\frac{1.64872127 \times 2 (\pi 2.62561 \times 10^{40})}{4 \pi 0.9} \right) \frac{1}{13.12806 \times 10^{39}} (x) dx = 4.47929 \times 10^{-81} (2.71828^x)^{3.15722 \times 10^{80}} + \text{constant}$$

Then:

$$1 + 1 / \left(\frac{1.5236 + 1.4649}{2.01} \right) \left(((((((1.41421 (e^1)^{(3.15722 \times 10^{80}})))))))))^{(1/10^{240})} \right)$$

Where 1,5236 and 1,4649 are Hausdorff dimensions

Input interpretation:

$$1 + \frac{1}{\frac{1.5236 + 1.4649}{2.01}} 10^{240} \sqrt{1.41421 (e^1)^{3.15722 \times 10^{80}}}$$

[Open code](#)

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Decimal approximation:

Fewer digits

More digits

1.672578216496570185711895599799230383135352183369583403045...

$$\frac{21\,030 W_{\text{Wad}}}{3809} \approx 1.656340246783932790758729325282226306117091100026253609871$$

$$\frac{6309}{3809} \approx 1.656340246783932790758729325282226306117091100026253609871$$

$$\frac{240(5 \mathcal{L}_{\text{Li}} - 3)}{1200 \mathcal{L}_{\text{Li}} - 487} \approx 1.656340246783932790758731543$$

- W_{Wad} is the Wadsworth constant
- \mathcal{L}_{Li} is Liouville's constant

We note that, the result 1,656340... is practically equal to the 14th root of the following Ramanujan's class invariant $Q = (G_{505}/G_{101/5})^3 = 1164,2696$ i.e. 1,65578...

Indeed:

$$\sqrt[14]{\left(\sqrt{\frac{113 + \sqrt{505}}{8}} + \sqrt{\frac{105 + 5\sqrt{505}}{8}}\right)^3} = 1,65578 \dots \Rightarrow$$

$$\Rightarrow 1 + \frac{1}{1.5236 \cdot 10^{240} \sqrt[10]{1.41421 (e^1)^{3.15722 \times 10^{80}}}}$$

$$= 1,656340\dots$$

$$1 + 1 / \left(\left(\frac{21}{13} + \frac{34}{21} \right) / 2 \left(\left(\left(\left(1.41421 (e^1)^{(3.15722 \times 10^{80})} \right) \right) \right) \right) \right)^{(1/10^{240})}$$

Input interpretation:

$$1 + \frac{1}{\left(\frac{1}{2} \left(\frac{21}{13} + \frac{34}{21}\right)\right) 10^{240} \sqrt[10]{1.41421 (e^1)^{3.15722 \times 10^{80}}}}$$

[Open code](#)

In this concluding section we give a formal argument that, whenever black hole microstates are in representations of large-diffeomorphism-generated Virasoro algebras, as conjectured for Kerr in this paper, the black hole Hilbert space must be contained within the Hilbert space of states outside the black hole. The observations apply equally to the case discussed here and to the stringy black holes with near-AdS₃ regions. Our argument is a refined and sharpened version of those made elsewhere from different perspectives and is perhaps in the general spirit, if not the letter, of black hole complementarity.¹⁰

If the Hilbert space is represented from a Clifford torus, it is possible that the Kerr black hole is a toroidal structure

From Wikipedia

Any unit sphere S^{2n-1} in an even-dimensional euclidean space $\mathbf{R}^{2n} = \mathbf{C}^n$ may be expressed in terms of the complex coordinates as follows:

$$S^{2n-1} = \{(z_1, \dots, z_n) \in \mathbf{C}^n : |z_1|^2 + \dots + |z_n|^2 = 1\}.$$

Then, for any non-negative numbers r_1, \dots, r_n such that $r_1^2 + \dots + r_n^2 = 1$, we may define a generalized Clifford torus as follows:

$$T_{r_1, \dots, r_n} = \{(z_1, \dots, z_n) \in \mathbf{C}^n : |z_k| = r_k, 1 \leq k \leq n\}.$$

These generalized Clifford tori are all disjoint from one another. We may once again conclude that the union of each one of these tori T_{r_1, \dots, r_n} is the unit $(2n - 1)$ -sphere S^{2n-1} (where we must again include the degenerate cases where at least one of the radii $r_k = 0$).

Now, we have the following formulas:

Here the left and right temperatures are defined by

$$T_L = \frac{r_+ + r_-}{4\pi a}, \quad T_R = \frac{r_+ - r_-}{4\pi a}, \quad (2.4)$$

with $r_- = M - \sqrt{M^2 - a^2}$ and the left and right soft mode energies are

$$\omega_L = \frac{2M^2}{a}\omega, \quad \omega_R = \frac{2M^2}{a}\omega - m, \quad (2.5)$$

with (ω, m) the soft mode energy and axial component of angular momentum. The left/right temperatures and entropies are thermodynamically conjugate, as follows from

$$\delta S_{BH} = \frac{\omega_L}{T_L} + \frac{\omega_R}{T_R}, \quad (2.6)$$

2.18623279149823328802502730784317690450075718539435294... × 10⁸

$$\frac{(((6.66308160275862291784488672 \times 10^{87})))}{((((((2 * ((13.12806 * 10^{39})))))) / (((4\pi * ((0.9 / 13.12806 * 10^{39})))))))))}$$

Input interpretation:

$$\frac{6.66308160275862291784488672 \times 10^{87}}{4\pi \times \frac{\frac{2 \times 13.12806 \times 10^{39}}{0.9}}{13.12806 \times 10^{39}}}$$

[Open code](#)

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Result:

• Fewer digits

• More digits

2.18623279149823328802502730784320971563713277920008334... × 10⁸

and obtain:

$$(2.18623279149823328802502730784317690450075718539 \times 10^8 + 2.18623279149823328802502730784320971563713277920 \times 10^8)$$

Input interpretation:

$$2.18623279149823328802502730784317690450075718539 \times 10^8 + 2.18623279149823328802502730784320971563713277920 \times 10^8$$

[Open code](#)

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Result:

4.37246558299646657605005461568638662013788996459 × 10⁸

4.37246558299646657605005461568638662013788996459 × 10⁸

$$\frac{1}{2} \left(\left(\left(\left(\left(4.37246558299646657605005461568638662013788996459 \times 10^8 \right)^{1/41} + \left(4.37246558299646657605005461568638662013788996459 \times 10^8 \right)^{1/42} \right) \right) \right) \right)$$

Input interpretation:

$$\frac{1}{2} \left(\sqrt[41]{4.37246558299646657605005461568638662013788996459 \times 10^8} + \sqrt[42]{4.37246558299646657605005461568638662013788996459 \times 10^8} \right)$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

• More digits

1.6152797540523920836243585751513024578986036910416...

$$12 * ((4.37246558299646657605 \times 10^8)^{1/4})$$

Input interpretation:

$$12 \sqrt[4]{4.37246558299646657605 \times 10^8}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

1735.253168076459103202...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson.

$$((((12 * ((4.37246558299646657605 \times 10^8)^{1/4}))))^{1/3}}$$

Input interpretation:

$$\sqrt[3]{12 \sqrt[4]{4.37246558299646657605 \times 10^8}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

12.01676630426109271740...

This result is very near to the value of black hole entropy 12,1904

$$2 * (((((12 * ((4.37246558299646657605 \times 10^8)^{1/4}))))^{1/3}}$$

Input interpretation:

$$2 \sqrt[3]{12 \sqrt[4]{4.37246558299646657605 \times 10^8}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

24.03353260852218543480...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

$$\left(\left(\left(\left(12 * \left(4.37246558299646657605 \times 10^8\right)^{1/4}\right)\right)\right)\right)^{1/15}$$

Input interpretation:

$$\sqrt[15]{12 \sqrt[4]{4.37246558299646657605 \times 10^8}}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

- Fewer digits
- More digits

1.644210900413182503922735646388027360304860958763404231333...

1.6442109004131825039227356463880273603048609587634042

Continued fraction:

Linear form

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{4 + \frac{1}{3 + \frac{1}{1 + \frac{1}{1 + \frac{1}{4 + \frac{1}{11 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{3 + \frac{1}{1 + \frac{1}{42 + \frac{1}{2 + \frac{1}{3 + \frac{1}{3 + \frac{1}{4 + \frac{1}{1 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Possible closed forms:

- More

$$\frac{1}{660} (170 e^\pi - 364 \pi - 897 \log(\pi) - 692 \log(2 \pi) + 470 \tan^{-1}(\pi)) \approx$$

1.64421090041318250388142

$$\frac{3}{5} \pi \tan^2\left(\frac{13334359}{17749237}\right) \approx 1.644210900413182503900533$$

$$\pi \sqrt{\text{root of } 33415 x^3 + 8775 x^2 - 5581 x - 4273 \text{ near } x = 0.523369} \approx$$

1.644210900413182503941173

$$1/2 \left(\left(\left(\left(\left(12 * \left(4.37246558299646657605 \times 10^8\right)^{1/4}\right)\right)\right)\right)\right)^{1/16} + \left(\left(\left(\left(12 * \left(4.37246558299646657605 \times 10^8\right)^{1/4}\right)\right)\right)\right)^{1/15}$$

Input interpretation:

$$\frac{1}{2} \left(\sqrt[16]{12 \sqrt[4]{4.37246558299646657605 \times 10^8}} + \sqrt[15]{12 \sqrt[4]{4.37246558299646657605 \times 10^8}} \right)$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) Interactive

Result:

Fewer digits
More digits

1.619053811960483098583146711349798651221394845815955077635...
1.6190538119604830985831467113497986512213948458159550

Continued fraction:

Linear form

$$1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{2 + \cfrac{1}{365 + \cfrac{1}{1 + \cfrac{1}{3 + \cfrac{1}{2 + \cfrac{1}{4 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{15 + \cfrac{1}{2 + \cfrac{1}{6 + \cfrac{1}{1 + \cfrac{1}{6 + \cfrac{1}{5 + \cfrac{1}{190 + \cfrac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) Interactive

Possible closed forms:

More

$$\frac{3(13 - 315\pi + 235\pi^2)}{-460 + 841\pi + 31\pi^2} \approx 1.61905381196048309872111$$

$$\log\left(\frac{1}{150} \left(51 + 24\sqrt{2} + 97e + 4e^2 - 715\pi + 266\pi^2\right)\right) \approx 1.61905381196048309865059$$

$$\frac{2456808703\pi}{4767162225} \approx 1.619053811960483098564067$$

This value 1,6190538 is very near to the golden ratio.

Now, we have that:

$$(4.37246558299646657605005461568638662013788996459 \times 10^8)^{10}$$

Input interpretation:

$$(4.37246558299646657605005461568638662013788996459 \times 10^8)^{10}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

$$2.5542534991399080701476916237746879515477991253843438... \times 10^{86}$$

$$\frac{1}{2}(2.4739 + 2.3347) * (4.37246558299646657605005461568638662013788996459 \times 10^8)^{10}$$

Where 2.4739 and 2.3347 are Hausdorff dimensions

Input interpretation:

$$\frac{1}{2} (2.4739 + 2.3347) (4.37246558299646657605005461568638662013788996459 \times 10^8)^{10}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

$$6.1411916879820809730560949710414822419063734371615778... \times 10^{86}$$

$$\left(\left(\frac{2.01 + 2.05}{2} \right) * 1.2108 \right) * (4.37246558299646657605005461568638662013788996459 \times 10^8)^{10}$$

Where 1.2108, 2.01 and 2.05 are Hausdorff dimensions

Input interpretation:

$$\left(\left(\frac{1}{2} (2.01 + 2.05) \right) * 1.2108 \right) (4.37246558299646657605005461568638662013788996459 \times 10^8)^{10}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

$$6.2781609776199594034096947866747761086201726174611878... \times 10^{86}$$

This results $6,141191 * 10^{86}$ and $6,27816 * 10^{86}$ are practically equals to the value of Dark Matter entropy contained within the cosmic event horizon

$$(4.37246558299646657605005461568638662013788996459 \times 10^8)^{10} * (8^2 + 8*3)$$

Input interpretation:

$$(4.37246558299646657605005461568638662013788996459 \times 10^8)^{10} (8^2 + 8 \times 3)$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

$$2.2477430792431191017299686289217253973620632303382225... \times 10^{88}$$

This result is practically equal to the value of Photons entropy contained within the cosmic event horizon

$$1/4 (4.37246558299646657605005461568638662013788996459 \times 10^8)^{12}$$

Input interpretation:

$$\frac{1}{4} (4.37246558299646657605005461568638662013788996459 \times 10^8)^{12}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

$$1.2208345320753103915688189029689024076435144197627255... \times 10^{103}$$

This result is practically equal to the value of SMBHs entropy contained within the cosmic event horizon

$$1/2 (4.37246558299646657605005461568638662013788996459 \times 10^8)^{14} * (24+32)$$

Input interpretation:

$$\frac{1}{2} (4.37246558299646657605005461568638662013788996459 \times 10^8)^{14} (24 + 32)$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

$$2.6141326846917046142667393429828819360142207485603881... \times 10^{122}$$

$$\sqrt[3]{-8^2 + 27 \sqrt{\frac{(2 \times 13.12806 \times 10^{39})^2}{13.12806 \times 10^{39}} \times 6.62606957 \times 10^{-34}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

11.99418...

This result is very near to the value of black hole entropy 12,1904

$$2 * (((((((((-8^2 + ((((((((((((((2 * 13.12806 * 10^39)^2)))) / (((0.9 / 13.12806 * 10^39)))) * 6.62606957 * 10^-34)))))))))^1/27)))))))))^1/3$$

Input interpretation:

$$2 \sqrt[3]{-8^2 + 27 \sqrt{\frac{(2 \times 13.12806 \times 10^{39})^2}{13.12806 \times 10^{39}} \times 6.62606957 \times 10^{-34}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

23.98836...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

$$((((((((((-8^2 + ((((((((((((((2 * 13.12806 * 10^39)^2)))) / (((0.9 / 13.12806 * 10^39)))) * 6.62606957 * 10^-34)))))))))^1/27)))))))))^1/15$$

Input interpretation:

$$\sqrt[15]{-8^2 + 27 \sqrt{\frac{(2 \times 13.12806 \times 10^{39})^2}{13.12806 \times 10^{39}} \times 6.62606957 \times 10^{-34}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

Fewer digits

More digits

1.643592398058609314579936787349290163577539809136934135253...

1.6435923980586093145799367873492901635775398091369341

Continued fraction:

Linear form

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Possible closed forms:

More

$$\frac{4054396171\pi}{7749647200} \approx 1.643592398058609314589783$$

$$\pi \left[\text{root of } 187x^5 + 58x^4 + 590x^3 - 346x^2 + 45x - 25 \text{ near } x = 0.523172 \right] \approx 1.643592398058609314582232$$

$$\left[\text{root of } 4633x^3 - 44723x^2 - 3151x + 105423 \text{ near } x = 1.64359 \right] \approx 1.6435923980586093145714356$$

Now, from the above expression without -8^2 , we obtain:

$$(1.2108+1.5236+1.2) * ((((((((((((((2 * 13.12806 * 10^{39})^2)))))) / (((0.9 / 13.12806 * 10^{39})))))) * 6.62606957 * 10^{-34}))))))^{1/27}))))^{1/16}$$

Input interpretation:

$$(1.2108 + 1.5236 + 1.2) \sqrt[16]{ \sqrt[27]{ \frac{(2 \times 13.12806 \times 10^{39})^2}{13.12806 \times 10^{39}} \times 6.62606957 \times 10^{-34} } } }$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

Fewer digits

More digits

6.283101212449482033903660253656488074073290259365730848044...

$$1715 + \frac{1}{1 + \frac{1}{7 + \frac{1}{8 + \frac{1}{1 + \frac{1}{10 + \frac{1}{2 + \frac{1}{4 + \frac{1}{2 + \frac{1}{11 + \frac{1}{3 + \frac{1}{248 + \frac{1}{21 + \frac{1}{255 + \frac{1}{17 + \frac{1}{1 + \frac{1}{2 + \frac{1}{2 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Possible closed forms:

More

$$1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468 \sqrt{\pi} - 238 \pi \approx 1715.876728876313701431438$$

$$\pi \left[\text{root of } 4x^5 - 2186x^4 + 699x^3 - 569x^2 + 916x + 3358 \text{ near } x = 546.181 \right] \approx$$

$$\frac{1715.876728876313701436315 - 5525 \pi \pi! + 7066 - 10479 \pi + 33285 \pi^2}{33 \pi} \approx 1715.8767288763137014639644$$

From the first closed form

$$1114 + (4632/\pi) + ((1249/(\sqrt{\pi}))) - (468(\sqrt{\pi})) - 238\pi$$

We obtain:

$$((((1114 + (4632/\pi) + ((1249/(\sqrt{\pi}))) - (468(\sqrt{\pi})) - 238\pi))))^{1/3}$$

Input:

$$\sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468 \sqrt{\pi} - 238 \pi}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Decimal approximation:

More digits

$$11.97187098713895577822350275022837233145095977531650277817...$$

[Open code](#)

This result is very near to the value of black hole entropy 12,1904

Property:

$$\sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468\sqrt{\pi} - 238\pi} \text{ is a transcendental number}$$

[Open code](#)

Series representations:

More

$$\sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468\sqrt{\pi} - 238\pi} = \left(1114 + \frac{4632}{\pi} - 238\pi + \frac{1249}{\sqrt{-1+\pi} \sum_{k=0}^{\infty} (-1+\pi)^{-k} \binom{\frac{1}{2}}{k}} - 468\sqrt{-1+\pi} \sum_{k=0}^{\infty} (-1+\pi)^{-k} \binom{\frac{1}{2}}{k} \right)^{1/3}$$

[Open code](#)

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$$\sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468\sqrt{\pi} - 238\pi} = \left(1114 + \frac{4632}{\pi} - 238\pi + \frac{1249}{\sqrt{-1+\pi} \sum_{k=0}^{\infty} \frac{(-1)^k (-1+\pi)^{-k} \binom{-\frac{1}{2}}{k}}{k!}} - 468\sqrt{-1+\pi} \sum_{k=0}^{\infty} \frac{(-1)^k (-1+\pi)^{-k} \binom{-\frac{1}{2}}{k}}{k!} \right)^{1/3}$$

[Open code](#)

$$\sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468\sqrt{\pi} - 238\pi} = \left(1114 + \frac{4632}{\pi} - 238\pi + \frac{2498\sqrt{\pi}}{\sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} (-1+\pi)^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)} - \frac{234 \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} (-1+\pi)^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}} \right)^{1/3}$$

Integral representation:

$$(1+z)^\alpha = \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s)\Gamma(-\alpha-s)}{z^s} ds}{(2\pi i)\Gamma(-\alpha)} \quad \text{for } (0 < \gamma < -\text{Re}(\alpha) \text{ and } |\arg(z)| < \pi)$$

$$2 * (((1114 + (4632/\pi) + ((1249/(\sqrt{\pi}))) - (468(\sqrt{\pi})) - 238\pi)))^{1/3}$$

Input:

$$2 \sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468 \sqrt{\pi} - 238 \pi}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Decimal approximation:

More digits

23.94374197427791155644700550045674466290191955063300555635...

[Open code](#)

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

Property:

$$2 \sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468 \sqrt{\pi} - 238 \pi} \text{ is a transcendental number}$$

Series representations:

More

$$2 \sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468 \sqrt{\pi} - 238 \pi} =$$

$$2 \left(1114 + \frac{4632}{\pi} - 238 \pi + \frac{1249}{\sqrt{-1+\pi} \sum_{k=0}^{\infty} (-1+\pi)^{-k} \binom{\frac{1}{2}}{k}} - 468 \sqrt{-1+\pi} \sum_{k=0}^{\infty} (-1+\pi)^{-k} \binom{\frac{1}{2}}{k} \right)^{1/3}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

$$2 \sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468 \sqrt{\pi} - 238 \pi} = 2 \left(1114 + \frac{4632}{\pi} - 238 \pi + \frac{1249}{\sqrt{-1 + \pi} \sum_{k=0}^{\infty} \frac{(-1)^k (-1 + \pi)^{-k} \left(-\frac{1}{2}\right)_k}{k!}} - 468 \sqrt{-1 + \pi} \sum_{k=0}^{\infty} \frac{(-1)^k (-1 + \pi)^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)^{1/3}$$

[Open code](#)

$$2 \sqrt[3]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468 \sqrt{\pi} - 238 \pi} = 2 \left(1114 + \frac{4632}{\pi} - 238 \pi + \frac{2498 \sqrt{\pi}}{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} (-1 + \pi)^{-s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)} - \frac{234 \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} (-1 + \pi)^{-s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)}{\sqrt{\pi}} \right)^{1/3}$$

$$\left(\left(\left(1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} \right) - (468 \sqrt{\pi} + 238 \pi) \right) \right)^{1/15}$$

Input:

$$15 \sqrt[15]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468 \sqrt{\pi} - 238 \pi}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Decimal approximation:

More digits

1.642980487335409637370662738329715383236461624513985577150...

[Open code](#)

1.6429804873354...

Property:

$$15 \sqrt[15]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468 \sqrt{\pi} - 238 \pi} \text{ is a transcendental number}$$

Continued fraction:

Linear form

$$\begin{array}{r}
1 + \frac{1}{\dots} \\
1 + \frac{1}{1 + \frac{1}{\dots}} \\
1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}} \\
4 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}} \\
41 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
6 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
19 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
2 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
3 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
8 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
3 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
2 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
2 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}} \\
\dots
\end{array}$$

Series representations:

More

$$\sqrt[15]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468\sqrt{\pi} - 238\pi} = \left(1114 + \frac{4632}{\pi} - 238\pi + \frac{1249}{\sqrt{-1+\pi} \sum_{k=0}^{\infty} (-1+\pi)^{-k} \binom{\frac{1}{2}}{k}} - 468\sqrt{-1+\pi} \sum_{k=0}^{\infty} (-1+\pi)^{-k} \binom{\frac{1}{2}}{k} \right)^{1/15}$$

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$$\sqrt[15]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468\sqrt{\pi} - 238\pi} = \left(1114 + \frac{4632}{\pi} - 238\pi + \frac{1249}{\sqrt{-1+\pi} \sum_{k=0}^{\infty} \frac{(-1)^k (-1+\pi)^{-k} \left(-\frac{1}{2}\right)_k}{k!}} - 468\sqrt{-1+\pi} \sum_{k=0}^{\infty} \frac{(-1)^k (-1+\pi)^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)^{1/15}$$

[Open code](#)

$$\sqrt[15]{1114 + \frac{4632}{\pi} + \frac{1249}{\sqrt{\pi}} - 468\sqrt{\pi} - 238\pi = \left(\frac{1114 + \frac{4632}{\pi} - 238\pi + \frac{2498\sqrt{\pi}}{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} (-1+\pi)^{-s} \Gamma(-\frac{1}{2}-s) \Gamma(s)} - \frac{234 \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} (-1+\pi)^{-s} \Gamma(-\frac{1}{2}-s) \Gamma(s)}{\sqrt{\pi}} \right)^{1/15}}$$

Integral representation:

$$(1+z)^a = \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s)\Gamma(-a-s)}{z^s} ds}{(2\pi i)\Gamma(-a)} \text{ for } (0 < \gamma < -\text{Re}(a) \text{ and } |\arg(z)| < \pi)$$

[Open code](#)

Now, we analyze two formulas concerning the Hawking radiation.

From Wikipedia

Hawking radiation is black-body radiation that is predicted to be released by black holes, due to quantum effects near the event horizon. It is named after the theoretical physicist Stephen Hawking, who provided a theoretical argument for its existence in 1974.

The radiation from a Schwarzschild black hole is blackbody radiation with temperature

$$T = \frac{\hbar c^3}{8\pi G k_B M} \approx 1.227 \times 10^{+23} \text{K} \cdot \text{kg} \times \frac{1}{M} = 6.169 \times 10^{-8} \text{K} \times \frac{M_{\odot}}{M}$$

For simplicity, assume a black hole is a perfect blackbody ($\epsilon = 1$).

Stefan–Boltzmann–Schwarzschild–Hawking black hole radiation power law derivation:

$$P = A_s \epsilon \sigma T_H^4 = \left(\frac{16\pi G^2 M^2}{c^4} \right) \left(\frac{\pi^2 k_B^4}{60\hbar^3 c^2} \right) \left(\frac{\hbar c^3}{8\pi G M k_B} \right)^4 = \frac{\hbar c^6}{15360\pi G^2 M^2}$$

Now, from the our usual values used in this research paper, we obtain the following interesting expressions:

For T, we have:

$$\frac{(((1.054571726 \times 10^{-34}) * (3 \times 10^8)^3))}{(((8\pi * 6.67408 \times 10^{-11} * 13.12806 \times 10^{39} * 1.380649 \times 10^{-23}))})}$$

Input interpretation:

$$\frac{1.054571726 \times 10^{-34} (3 \times 10^8)^3}{8 \pi \times 6.67408 \times 10^{-11} \times 13.12806 \times 10^{39} \times 1.380649 \times 10^{-23}}$$

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Result:

More digits

• $9.36537... \times 10^{-18}$

For P, where M (mass of BH) is express in energy, we have:

$$\frac{((((((6.582 \times 10^{-16}) * (3 \times 10^8)^6))))))}{((((((15360\pi * (6.67 \times 10^{-11})^2 * (13.12806 \times 10^{39} * 9 \times 10^{16})^2))))))})}$$

Input interpretation:

$$\frac{6.582 \times 10^{-16} (3 \times 10^8)^6}{15360 \pi (6.67 \times 10^{-11})^2 (13.12806 \times 10^{39} \times 9 \times 10^{16})^2}$$

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Result:

More digits

• $1.60106... \times 10^{-63}$

This result is practically equal to the 15th root of the following Ramanujan's class invariant $Q = (G_{505}/G_{101/5})^3 = 1164,2696$ i.e. 1,6010451...

Indeed, from 1,6010451 it is possible to obtain, simply multiplying by 10^{-63} , the following mathematical connection:

$$1.60104512 * 10^{-63}$$

Input interpretation:

$$\frac{1.60104512}{10^{63}}$$

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Result:

$$1.60104512 \times 10^{-63}$$

Indeed:

$$\begin{aligned} & \sqrt[15]{\left(\sqrt{\frac{113+5\sqrt{505}}{8}} + \sqrt{\frac{105+5\sqrt{505}}{8}}\right)^3} \times 10^{-63} = 1,6010451 \dots \times 10^{-63} \Rightarrow \\ & \Rightarrow \frac{6.582 \times 10^{-16} (3 \times 10^8)^6}{15360 \pi (6.67 \times 10^{-11})^2 (13.12806 \times 10^{39} \times 9 \times 10^{16})^2} \\ & = 1.60106\dots \times 10^{-63} \end{aligned}$$

Note that, this result concerning P, i.e. the energy dispersion, is an infinitesimal golden number, that is in the range of golden ratio (1.61803398...). Moreover, there is a practically perfect correspondence with the above Ramanujan class invariant, multiplied by 10^{-63}

For P, we have also this alternate formula:

$$\frac{((((((1.054571 \times 10^{-34}) * (3 \times 10^8)^6))))))}{((((((15360\pi * (6.67 \times 10^{-11})^2 * (13.12806 \times 10^{39} * 9 \times 10^{16})^2))))))}}$$

Input interpretation:

$$\frac{1.054571 \times 10^{-34} (3 \times 10^8)^6}{15360 \pi (6.67 \times 10^{-11})^2 (13.12806 \times 10^{39} \times 9 \times 10^{16})^2}$$

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Result:

More digits

$$2.56522\dots \times 10^{-82}$$

We have calculated the square root of P:

$$\sqrt{\frac{((((((1.054571 \times 10^{-34}) * (3 \times 10^8)^6))))))}{((((((15360\pi * (6.67 \times 10^{-11})^2 * (13.12806 \times 10^{39} * 9 \times 10^{16})^2))))))}}}$$

Input interpretation:

$$\sqrt{\frac{1.054571 \times 10^{-34} (3 \times 10^8)^6}{15360 \pi (6.67 \times 10^{-11})^2 (13.12806 \times 10^{39} \times 9 \times 10^{16})^2}}$$

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Result:

More digits

- $1.60163... \times 10^{-41}$

Also this result, is an infinitesimal golden number, that is in the range of golden ratio (1.61803398...)

For T, we have developed the following computations:

$$\frac{(((((((1.054571726 \times 10^{-34}) * (3 \times 10^8)^3))))))}{(((8\pi * 6.67408 \times 10^{-11} * 13.12806 \times 10^{39} * 1.380649 \times 10^{-23}))))))} * ((\pi^{5/2}))$$

Input interpretation:

$$\frac{1.054571726 \times 10^{-34} (3 \times 10^8)^3}{8 \pi \times 6.67408 \times 10^{-11} \times 13.12806 \times 10^{39} \times 1.380649 \times 10^{-23}} \pi^{5/2}$$

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Result:

More digits

- $1.63832... \times 10^{-16}$

This result is a golden number, that is in the range of golden ratio (1.61803398...)

$$\frac{(((((((1.054571726 \times 10^{-34}) * (3 \times 10^8)^3))))))}{(((8\pi * 6.67408 \times 10^{-11} * 13.12806 \times 10^{39} * 1.380649 \times 10^{-23}))))))} * ((\pi(\pi + \ln(12))))$$

Input interpretation:

$$\frac{1.054571726 \times 10^{-34} (3 \times 10^8)^3}{8 \pi \times 6.67408 \times 10^{-11} \times 13.12806 \times 10^{39} \times 1.380649 \times 10^{-23}} (\pi (\pi + \log(12)))$$

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- $\log(x)$ is the natural logarithm

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Result:

More digits

- $1.65544... \times 10^{-16}$

This result is practically equal to the 14th root of the following Ramanujan's class invariant $Q = (G_{505}/G_{101/5})^3 = 1164,2696$ i.e. 1,65578...

Indeed, from 1,65578 it is possible to obtain, simply multiplying by 10^{-16} :

$$1.65578455 \times 10^{-16}$$

Input interpretation:

$$\frac{1.65578455}{10^{16}}$$

[Open code](#)

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Result:

$$1.65578455 \times 10^{-16}$$

Thence:

$$\begin{aligned} & \sqrt[14]{\left(\sqrt{\frac{113+5\sqrt{505}}{8}} + \sqrt{\frac{105+5\sqrt{505}}{8}}\right)^3} \times 10^{-16} = 1,65578 \dots \times 10^{-16} \Rightarrow \\ & \Rightarrow \frac{1.054571726 \times 10^{-34} (3 \times 10^8)^3}{8 \pi \times 6.67408 \times 10^{-11} \times 13.12806 \times 10^{39} \times 1.380649 \times 10^{-23} (\pi (\pi + \log(12)))} \\ & = 1.65544 \dots \times 10^{-16} \end{aligned}$$

From the formula of P, we obtain:

$$2 \times 8^2 + \frac{(((((6.582 \times 10^{-16}) \times (3 \times 10^8)^6))))}{(((((15360\pi \times (6.67 \times 10^{-11})^2 \times (13.12806 \times 10^{39} \times 9 \times 10^{16})^2))))))} \times 10^{66}$$

Input interpretation:

$$2 \times 8^2 + \frac{6.582 \times 10^{-16} (3 \times 10^8)^6}{15360 \pi (6.67 \times 10^{-11})^2 (13.12806 \times 10^{39} \times 9 \times 10^{16})^2} \times 10^{66}$$

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Result:

• Fewer digits
• More digits

1729.056010479749693139142267348025670972966858326142299973...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$\left(\frac{\left(\left(\left(\left(2 \times 8^2 + \left(\left(\left(6.582 \times 10^{-16}\right) \times \left(3 \times 10^8\right)^6\right)\right)\right)\right)\right)}{\left(\left(\left(\left(15360\pi \times \left(6.67 \times 10^{-11}\right)^2 \times \left(13.12806 \times 10^{39} \times 9 \times 10^{16}\right)^2\right)\right)\right)\right)\right) \times 10^{66}}\right)^{1/3}$$

Input interpretation:

$$\sqrt[3]{2 \times 8^2 + \frac{6.582 \times 10^{-16} (3 \times 10^8)^6}{15360 \pi (6.67 \times 10^{-11})^2 (13.12806 \times 10^{39} \times 9 \times 10^{16})^2} \times 10^{66}}$$

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Result:

More digits

12.0024...

This result is very near to the value of black hole entropy 12,1904

$$2 \times \left(\frac{\left(\left(\left(\left(2 \times 8^2 + \left(\left(\left(6.582 \times 10^{-16}\right) \times \left(3 \times 10^8\right)^6\right)\right)\right)\right)\right)}{\left(\left(\left(\left(15360\pi \times \left(6.67 \times 10^{-11}\right)^2 \times \left(13.12806 \times 10^{39} \times 9 \times 10^{16}\right)^2\right)\right)\right)\right)\right) \times 10^{66}}\right)^{1/3}$$

Input interpretation:

$$2 \sqrt[3]{2 \times 8^2 + \frac{6.582 \times 10^{-16} (3 \times 10^8)^6}{15360 \pi (6.67 \times 10^{-11})^2 (13.12806 \times 10^{39} \times 9 \times 10^{16})^2} \times 10^{66}}$$

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Result:

More digits

24.0049...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

$$\left(\frac{\left(\left(\left(\left(2 \times 8^2 + \left(\left(\left(6.582 \times 10^{-16}\right) \times \left(3 \times 10^8\right)^6\right)\right)\right)\right)\right)}{\left(\left(\left(\left(15360\pi \times \left(6.67 \times 10^{-11}\right)^2 \times \left(13.12806 \times 10^{39} \times 9 \times 10^{16}\right)^2\right)\right)\right)\right)\right) \times 10^{66}}\right)^{1/15}$$

- $\log(x)$ is the natural logarithm

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Result:

- More digits
23.9974...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

$$\left(\frac{24 \times 3 + \frac{1.054571726 \times 10^{-34} (3 \times 10^8)^3}{8 \pi \times 6.67408 \times 10^{-11} \times 13.12806 \times 10^{39} \times 1.380649 \times 10^{-23}}}{(\pi (\pi + \log(12))) \times 10^{19}} \right)^{1/15}$$

Input interpretation:

$$\left(24 \times 3 + \frac{1.054571726 \times 10^{-34} (3 \times 10^8)^3}{8 \pi \times 6.67408 \times 10^{-11} \times 13.12806 \times 10^{39} \times 1.380649 \times 10^{-23}} \right)^{1/15}$$

[Open code](#)

- $\log(x)$ is the natural logarithm

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Result:

- Fewer digits
- More digits
1.643716185610309160791099966247523548170651778381071336977...

1.6437161856103091607910999662475235481706517783810713

Continued fraction:

- Linear form

Abstract. In the classical theory black holes can only absorb and not emit particles. However it is shown that quantum mechanical effects cause black holes to create and emit particles as if they were hot bodies with temperature $\frac{\hbar\kappa}{2\pi k} \approx 10^{-6} \left(\frac{M_{\odot}}{M}\right) \text{ }^{\circ}\text{K}$ where κ is the surface gravity of the black hole. This thermal emission leads to a slow decrease in the mass of the black hole and to its eventual disappearance: any primordial black hole of mass less than about 10^{15} g would have evaporated by now. Although these quantum effects violate the classical law that the area of the event horizon of a black hole cannot decrease, there remains a Generalized Second Law: $S + \frac{1}{4}A$ never decreases where S is the entropy of matter outside black holes and A is the sum of the surface areas of the event horizons. This shows that gravitational collapse converts the baryons and leptons in the collapsing body into entropy. It is tempting to speculate that this might be the reason why the Universe contains so much entropy per baryon.

For a given frequency ω , i.e. a given value of j , the absorption fraction Γ_{jn} goes to zero as the angular quantum number l increases because of the centrifugal barrier. Thus at first sight it might seem that each wave-packet mode of high l value would contain

$$\{\exp(2\pi\omega\kappa^{-1}) - 1\}^{-1}$$

particles and that the total rate of particles and energy crossing the event horizon would be infinite. This calculation would, of course, be inconsistent with the result obtained above that an observer crossing the event horizon would see only a finite small energy density of order M^{-4} . The reason for this discrepancy seems to be that the wave-packets $\{p_{jn}\}$ and $\{q_{jn}\}$ provide a complete basis for solutions

We have:

$$\text{temperature } \frac{\hbar\kappa}{2\pi k} \approx 10^{-6} \left(\frac{M_{\odot}}{M}\right) \text{ }^{\circ}\text{K}$$

and the particles contained in each wave-packet mode of high value of quantum number l , are:

$$\{\exp(2\pi\omega\kappa^{-1}) - 1\}^{-1}$$

With the our values, where $\mathbf{a} = J/M$ and

$$\text{For a Schwarzschild black hole } \kappa = \frac{1}{4M}$$

$$\text{and } \omega = \Omega = \frac{a}{\alpha} = \frac{J}{M} \cdot \frac{1}{\alpha}$$

thence:

$$1 / \exp(2\pi * (J/M * 1/\alpha) * 1/(1/4M) - 1)$$

remember that:

$$\begin{cases} \Theta = \frac{r_+ - r_-}{4\alpha} & \text{“gravità di superficie”} \\ \phi = \frac{r_+ Q}{\alpha} & \text{“potenziale elettrico”} \\ \Omega = \frac{a}{\alpha} & \text{“frequenza angolare”}. \end{cases}$$

We obtain:

$$1 / (((\exp(((((((2\pi * (0.9/13.12806 * 10^{39}) * 1/(6.8938278721 * 10^{80}) * 4 * (13.12806 * 10^{39})))))))))) - 1))))$$

Input interpretation:

$$\frac{1}{\exp\left(2\pi \times \frac{0.9}{13.12806 \times 10^{39}} \times \frac{1}{6.8938278721 \times 10^{80}} \times 4 \times 13.12806 \times 10^{39}\right) - 1}$$

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Result:

∞

• ∞ is complex infinity

Decimal approximation:

More digits

• $3.04774... \times 10^{79}$

$3.047741062970548 \times 10^{79}$

$((3.04774106297054838149866381067383501125196657352 \times 10^{79}))^{(\pi/1140)}$

Input interpretation:

$$(3.04774106297054838149866381067383501125196657352 \times 10^{79})^{\pi/1140}$$

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Result:

More digits

• $1.6559247521630664083848387291410505307142963602050...$

Or:

$((((3.04774106297054838149866381067383501125196657352 \times 10^{79})))^{\pi/(34^2-16)})$

Input interpretation:

$(3.04774106297054838149866381067383501125196657352 \times 10^{79})^{\pi/(34^2-16)}$

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Result:

More digits

1.6559247521630664083848387291410505307142963602050...

1.655924752163...

We note that, the result 1,655924... is practically equal to the 14th root of the following Ramanujan's class invariant $Q = (G_{505}/G_{101/5})^3 = 1164,2696$ i.e. 1,65578...

Indeed:

$$\sqrt[14]{\left(\sqrt{\frac{113+5\sqrt{505}}{8}} + \sqrt{\frac{105\sqrt{505}}{8}}\right)^3} = 1,65578 \dots \Rightarrow$$

$$\Rightarrow (3.04774106297054838149866381067383501125196657352 \times 10^{79})^{\pi/(34^2-16)}$$

$$= 1,655924$$

And:

$((((3.04774106297054838149866381067383501125196657352 \times 10^{79})))^{\pi/(34^2+21+13+5)})$

Input interpretation:

$(3.04774106297054838149866381067383501125196657352 \times 10^{79})^{\pi/(34^2+21+13+5)}$

[Open code](#)

• [Units »](#)

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Result:

More digits

1.6179281506203672598152036020629183817177756921349...

1.6179281506203672598152036020629183817177756921349

This result is a very good approximation to the value of the golden ratio 1,618033988749...

UNEARTHING THE VISIONS OF A MASTER: HARMONIC MAASS FORMS AND NUMBER THEORY

KEN ONO

The function $T_1(n)$ alone gives the Hardy-Ramanujan asymptotic formula

$$(2.2) \quad p(n) \sim \frac{1}{4n\sqrt{3}} \cdot e^{\pi\sqrt{2n/3}}.$$

Partition number $p(n)$ for $n = 5046$; $p(5046)$ from OEIS is:

3,8685436234477791770474674590313143573886331896398541703329035537709
5128484

From Ramanujan formula for $p(5046)$, we obtain:

$$\left(\frac{1}{4 \cdot 5046 \cdot \sqrt{3}} \right) \cdot \exp\left(\pi \cdot \sqrt{\frac{2 \cdot 5046}{3}} \right)$$

Input:

$$\frac{1}{4 \times 5046 \sqrt{3}} \exp\left(\pi \sqrt{\frac{2 \times 5046}{3}} \right)$$

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Exact result:

$$\frac{e^{58\pi}}{20184\sqrt{3}}$$

Decimal approximation:

More digits

$$3.8927871496803691534559901688545454305815654571794088... \times 10^{74}$$

[Open code](#)

Property:

$$\frac{e^{58\pi}}{20184\sqrt{3}} \text{ is a transcendental number}$$

Series representations:

More

$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 5046}{3}}\right)}{4 \times 5046 \sqrt{3}} = \frac{\exp\left(\pi \sqrt{3363} \sum_{k=0}^{\infty} 3363^{-k} \binom{\frac{1}{2}}{k}\right)}{20184 \sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \binom{\frac{1}{2}}{k}}$$

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$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 5046}{3}}\right)}{4 \times 5046 \sqrt{3}} = \frac{\exp\left(\pi \sqrt{3363} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{3363}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)}{20\,184 \sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!}}$$

Open code

$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 5046}{3}}\right)}{4 \times 5046 \sqrt{3}} = \frac{\exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3364 - z_0)^k z_0^{-k}}{k!}\right)}{20\,184 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3 - z_0)^k z_0^{-k}}{k!}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

Now, from the previous result of p(5046)

3.8927871496803691534559901688545454305815654571794088966578688910⁷⁴
83582474627675878586533542069601779911930696... × 10⁷⁴

3.8927871496803691534559901688545454305815654571794088966578688910835
8247462 × 10⁷⁴

after some calculations, we obtain:

((((196884*1/(ln(4)/ln(3)*2)))))[(((1/(4*5046*sqrt(3))))*
exp((((Pi*(((sqrt(((2*5046)/3)))))))]

Thence, multiplying

Input:

$$\left(196\,884 \times \frac{1}{\frac{\log(4)}{\log(3)} \times 2}\right) \left(\frac{1}{4 \times 5046 \sqrt{3}} \exp\left(\pi \sqrt{\frac{2 \times 5046}{3}}\right)\right)$$

Open code

- $\log(x)$ is the natural logarithm

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Exact result:

$$\frac{5469 \sqrt{3} e^{58\pi} \log(3)}{3364 \log(4)}$$

Decimal approximation:

More digits

3.0368971380696910100645999497040251010799179715079078... × 10⁷⁹

Open code

3.0368971380696910100645999497040251010799179715079078 × 10⁷⁹

Series representations:

More

$$\frac{\exp\left(\pi\sqrt{\frac{2 \times 5046}{3}}\right) 196\,884}{\frac{(4 \times 5046\sqrt{3})(\log(4)2)}{\log(3)}} = \frac{5469\sqrt{3} e^{58\pi} \left(\log(2) - \sum_{k=1}^{\infty} \frac{\left(\frac{-1}{2}\right)^k}{k}\right)}{3364 \left(\log(3) - \sum_{k=1}^{\infty} \frac{\left(\frac{-1}{3}\right)^k}{k}\right)}$$

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$$\frac{\exp\left(\pi\sqrt{\frac{2 \times 5046}{3}}\right) 196\,884}{\frac{(4 \times 5046\sqrt{3})(\log(4)2)}{\log(3)}} = \frac{5469\sqrt{3} e^{58\pi} \left(2\pi \left[\frac{\arg(3-x)}{2\pi}\right] - i \log(x) + i \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k}\right)}{3364 \left(2\pi \left[\frac{\arg(4-x)}{2\pi}\right] - i \log(x) + i \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k}\right)} \text{ for } x < 0$$

[Open code](#)

$$\frac{\exp\left(\pi\sqrt{\frac{2 \times 5046}{3}}\right) 196\,884}{\frac{(4 \times 5046\sqrt{3})(\log(4)2)}{\log(3)}} = \frac{5469\sqrt{3} e^{58\pi} \left(2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi}\right] - i \log(z_0) + i \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k}\right)}{3364 \left(2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi}\right] - i \log(z_0) + i \sum_{k=1}^{\infty} \frac{(-1)^k (4-z_0)^k z_0^{-k}}{k}\right)}$$

Integral representations:

$$\frac{\exp\left(\pi\sqrt{\frac{2 \times 5046}{3}}\right) 196\,884}{\frac{(4 \times 5046\sqrt{3})(\log(4)2)}{\log(3)}} = \frac{5469\sqrt{3} e^{58\pi} \int_1^3 \frac{1}{t} dt}{3364 \int_1^4 \frac{1}{t} dt}$$

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$$\frac{\exp\left(\pi\sqrt{\frac{2 \times 5046}{3}}\right) 196\,884}{\frac{(4 \times 5046\sqrt{3})(\log(4)2)}{\log(3)}} = \frac{5469\sqrt{3} e^{58\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{2^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds}{3364 \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{3^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds} \text{ for } -1 < \gamma < 0$$

This result $3.036897138... \times 10^{79}$ is a good approximation to the value of the particles' number contained in each wave-packet mode.

For $n = 5697$ from OEIS

$$p(5697) = 3.0538723337391660587957188453906776444982487452257640926684434740142157911918583 \times 10^{79}$$

From the Ramanujan formula, we obtain:

$$\left(\frac{1}{4 \times 5697 \sqrt{3}} \right) \times \exp\left(\pi \sqrt{\frac{2 \times 5697}{3}} \right)$$

Input:

$$\frac{1}{4 \times 5697 \sqrt{3}} \exp\left(\pi \sqrt{\frac{2 \times 5697}{3}} \right)$$

[Open code](#)

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Exact result:

$$\frac{e^{3 \sqrt{422} \pi}}{22788 \sqrt{3}}$$

Decimal approximation:

More digits

$$3.0718793263020345822883525238695115274200010311387072... \times 10^{79}$$

[Open code](#)

Property:

$$\frac{e^{3 \sqrt{422} \pi}}{22788 \sqrt{3}} \text{ is a transcendental number}$$

Series representations:

More

$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 5697}{3}} \right)}{4 \times 5697 \sqrt{3}} = \frac{\exp\left(\pi \sqrt{3797} \sum_{k=0}^{\infty} 3797^{-k} \binom{\frac{1}{2}}{k} \right)}{22788 \sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \binom{\frac{1}{2}}{k}}$$

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$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 5697}{3}}\right)}{4 \times 5697 \sqrt{3}} = \frac{\exp\left(\pi \sqrt{3797} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{3797}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)}{22\,788 \sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!}}$$

Open code

$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 5697}{3}}\right)}{4 \times 5697 \sqrt{3}} = \frac{\exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3798 - z_0)^k z_0^{-k}}{k!}\right)}{22\,788 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3 - z_0)^k z_0^{-k}}{k!}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

3.0718793263020345822883525238695115274200010311387072960591001602:
73810658480156514428247369468992012899508346... × 10⁷⁹

3.0718793263020345822883525238695115274200010311387072960591001602738
106584801565 * 10⁷⁹

This value is a good approximation to the particles' number contained in each wave-packet mode of high value of quantum number l

From the following coefficient formula, that is linked to the partition formula

The problem of estimating the coefficients $\alpha(n)$ has a long history, one which even precedes Dyson's definition of partition ranks. Indeed, Ramanujan's last letter to Hardy already includes the claim that

$$\alpha(n) = (-1)^{n-1} \frac{\exp\left(\pi \sqrt{\frac{n}{6} - \frac{1}{144}}\right)}{2\sqrt{n - \frac{1}{24}}} + O\left(\frac{\exp\left(\frac{1}{2}\pi \sqrt{\frac{n}{6} - \frac{1}{144}}\right)}{\sqrt{n - \frac{1}{24}}}\right).$$

for $n = 5697$, we obtain:

$$\left(\frac{\exp(\pi \sqrt{5697/6 - 1/144})}{2\sqrt{5697 - 1/24}}\right) + \left(\frac{\exp(\pi/2 \sqrt{5697/6 - 1/144})}{\sqrt{5697 - 1/24}}\right)$$

Input:

$$\frac{\exp\left(\pi\sqrt{\frac{5697}{6}-\frac{1}{144}}\right)}{2\sqrt{5697-\frac{1}{24}}} + \frac{\exp\left(\frac{\pi}{2}\sqrt{\frac{5697}{6}-\frac{1}{144}}\right)}{\sqrt{5697-\frac{1}{24}}}$$

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Exact result:

$$2\sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/12}$$

Decimal approximation:

More digits

$$7.2917242148745695868420092647065351666410224157037936... \times 10^{39}$$

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Property:

$$2\sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/12}$$

is a transcendental number

Series representations:

More

$$\frac{\exp\left(\pi\sqrt{\frac{5697}{6}-\frac{1}{144}}\right)}{2\sqrt{5697-\frac{1}{24}}} + \frac{\exp\left(\frac{1}{2}\sqrt{\frac{5697}{6}-\frac{1}{144}}\pi\right)}{\sqrt{5697-\frac{1}{24}}} =$$

$$\frac{2\exp\left(\frac{1}{2}\pi\sqrt{\frac{136583}{144}}\sum_{k=0}^{\infty}\left(\frac{136583}{144}\right)^{-k}\binom{\frac{1}{2}}{k}\right) + \exp\left(\pi\sqrt{\frac{136583}{144}}\sum_{k=0}^{\infty}\left(\frac{136583}{144}\right)^{-k}\binom{\frac{1}{2}}{k}\right)}{2\sqrt{\frac{136703}{24}}\sum_{k=0}^{\infty}\left(\frac{136703}{24}\right)^{-k}\binom{\frac{1}{2}}{k}}$$

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$$\frac{\exp\left(\pi\sqrt{\frac{5697}{6}-\frac{1}{144}}\right)}{2\sqrt{5697-\frac{1}{24}}} + \frac{\exp\left(\frac{1}{2}\sqrt{\frac{5697}{6}-\frac{1}{144}}\pi\right)}{\sqrt{5697-\frac{1}{24}}} =$$

$$\frac{2\exp\left(\frac{1}{2}\pi\sqrt{\frac{136583}{144}}\sum_{k=0}^{\infty}\frac{\left(-\frac{144}{136583}\right)^k\binom{-\frac{1}{2}}{k}}{k!}\right) + \exp\left(\pi\sqrt{\frac{136583}{144}}\sum_{k=0}^{\infty}\frac{\left(-\frac{144}{136583}\right)^k\binom{-\frac{1}{2}}{k}}{k!}\right)}{2\sqrt{\frac{136703}{24}}\sum_{k=0}^{\infty}\frac{\left(-\frac{24}{136703}\right)^k\binom{-\frac{1}{2}}{k}}{k!}}$$

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$$\frac{\exp\left(\pi\sqrt{\frac{5697}{6}-\frac{1}{144}}\right)}{2\sqrt{5697-\frac{1}{24}}} + \frac{\exp\left(\frac{1}{2}\sqrt{\frac{5697}{6}-\frac{1}{144}}\pi\right)}{\sqrt{5697-\frac{1}{24}}} =$$

$$\left(2\exp\left(\frac{1}{2}\pi\sqrt{z_0}\sum_{k=0}^{\infty}\frac{(-1)^k\left(-\frac{1}{2}\right)_k\left(\frac{136727}{144}-z_0\right)^k z_0^{-k}}{k!}\right) + \right.$$

$$\left.\exp\left(\pi\sqrt{z_0}\sum_{k=0}^{\infty}\frac{(-1)^k\left(-\frac{1}{2}\right)_k\left(\frac{136727}{144}-z_0\right)^k z_0^{-k}}{k!}\right)\right) /$$

$$\left(2\sqrt{z_0}\sum_{k=0}^{\infty}\frac{(-1)^k\left(-\frac{1}{2}\right)_k\left(\frac{136727}{24}-z_0\right)^k z_0^{-k}}{k!}\right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

From the formula of property

$$2\sqrt{\frac{6}{136727}}e^{(\sqrt{136727}\pi)/24} + \sqrt{\frac{6}{136727}}e^{(\sqrt{136727}\pi)/12}$$

is a transcendental number

after some calculations, we obtain:

$$\left(\left(\left(\left(\left(2\sqrt{\frac{6}{136727}}e^{(\sqrt{136727}\pi)/24} + \sqrt{\frac{6}{136727}}e^{(\sqrt{136727}\pi)/12}\right)\right)\right)\right)\right)^{\left(\left(\pi^{3/5}\right)\right)}$$

Input:

$$\left(2\sqrt{\frac{6}{136727}}e^{1/24(\sqrt{136727}\pi)} + \sqrt{\frac{6}{136727}}e^{1/12(\sqrt{136727}\pi)}\right)^{\pi^{3/5}}$$

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Exact result:

$$\left(2\sqrt{\frac{6}{136727}}e^{(\sqrt{136727}\pi)/24} + \sqrt{\frac{6}{136727}}e^{(\sqrt{136727}\pi)/12}\right)^{\pi^{3/5}}$$

Decimal approximation:

More digits

$$1.6758490374095693734231955464410496996302060768869779... \times 10^{79}$$

[Open code](#)

This value $1,675849 \times 10^{79}$ is a multiple that is in the range of the golden ratio value. It can be defined a golden number.

Series representations:

$$\left(2 \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/12} \right)^{\pi^{3/5}} =$$

$$\left(\exp \left(\frac{1}{24} \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \right) \right.$$

$$\left. \left(2 + \exp \left(\frac{1}{24} \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \right) \right) \sqrt{z_0} \right.$$

$$\left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!} \right)^{\pi^{3/5}} \quad \text{for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

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$$\left(2 \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/12} \right)^{\pi^{3/5}} =$$

$$\left(2 \exp \left(\frac{1}{24} \pi \exp \left(i \pi \left[\frac{\arg(136727 - x)}{2 \pi} \right] \right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (136727 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \right.$$

$$\exp \left(i \pi \left[\frac{\arg\left(\frac{6}{136727} - x\right)}{2 \pi} \right] \right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{6}{136727} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} +$$

$$\exp \left(\frac{1}{12} \pi \exp \left(i \pi \left[\frac{\arg(136727 - x)}{2 \pi} \right] \right) \sqrt{x} \right.$$

$$\left. \sum_{k=0}^{\infty} \frac{(-1)^k (136727 - x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \exp \left(i \pi \left[\frac{\arg\left(\frac{6}{136727} - x\right)}{2 \pi} \right] \right)$$

$$\sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{6}{136727} - x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right)^{\pi^{3/5}} \quad \text{for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\left(2 \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/12} \right)^{\pi^{3/5}} =$$

$$\left(2 \exp\left(\frac{1}{24} \pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(136727-z_0)/(2\pi)]} z_0^{1/2+1/2 [\arg(136727-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727-z_0)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 [\arg(\frac{6}{136727}-z_0)/(2\pi)]} z_0^{1/2+1/2 [\arg(\frac{6}{136727}-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727}-z_0\right)^k z_0^{-k}}{k!} + \exp\left(\frac{1}{12} \pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(136727-z_0)/(2\pi)]} z_0^{1/2+1/2 [\arg(136727-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727-z_0)^k z_0^{-k}}{k!} \right) \left(\frac{1}{z_0}\right)^{1/2 [\arg(\frac{6}{136727}-z_0)/(2\pi)]} z_0^{1/2+1/2 [\arg(\frac{6}{136727}-z_0)/(2\pi)]} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727}-z_0\right)^k z_0^{-k}}{k!} \right)^{\pi^{3/5}}$$

Integral representation:

$$(1+z)^a = \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s)\Gamma(-a-s)}{z^s} ds}{(2\pi i)\Gamma(-a)} \text{ for } (0 < \gamma < -\text{Re}(a) \text{ and } |\arg(z)| < \pi)$$

And:

$$1.2108/2.05 \left(\left(\left(\left(\left(\left(\left(2 \sqrt{6/136727} e^{(\sqrt{136727} \pi)/24} + \sqrt{6/136727} e^{(\sqrt{136727} \pi)/12} \right) \right) \right) \right) \right) \right) \right)^2$$

Where 1,2108 and 2,05 are Hausdorff dimensions

Input interpretation:

$$\frac{1.2108}{2.05} \left(2 \sqrt{\frac{6}{136727}} e^{1/24 (\sqrt{136727} \pi)} + \sqrt{\frac{6}{136727}} e^{1/12 (\sqrt{136727} \pi)} \right)^2$$

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Result:

More digits

• $3.14036... \times 10^{79}$

This result is a good approximation to the particles' number contained in each wave-packet mode of high value of quantum number l and to the value of π (multiple)

Series representations:

$$\frac{\left(2 \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/12}\right)^2 1.2108}{2.05} =$$

$$0.590634 \exp\left(\frac{1}{12} \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!}\right)$$

$$\left(4 \sqrt{z_0}^{-2} \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!}\right)^2 +\right.$$

$$4 \exp\left(\frac{1}{24} \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!}\right)$$

$$\left.\sqrt{z_0}^{-2} \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!}\right)^2 +\right.$$

$$\exp\left(\frac{1}{12} \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!}\right) \sqrt{z_0}^{-2}$$

$$\left.\left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!}\right)^2\right) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$$

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$$\frac{\left(2\sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/12}\right)^2 1.2108}{2.05} = 0.590634$$

$$\begin{aligned} & \exp\left(\frac{1}{12}\pi \exp\left(i\pi \left[\frac{\arg(136727-x)}{2\pi}\right]\right)\sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (136727-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \\ & \left(4 \exp^2\left(i\pi \left[\frac{\arg\left(\frac{6}{136727}-x\right)}{2\pi}\right]\right)\sqrt{x}^2 \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{6}{136727}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right)^2 + 4 \exp\left(\frac{1}{24}\pi \exp\left(i\pi \left[\frac{\arg(136727-x)}{2\pi}\right]\right)\sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (136727-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \right. \\ & \left. \exp^2\left(i\pi \left[\frac{\arg\left(\frac{6}{136727}-x\right)}{2\pi}\right]\right)\sqrt{x}^2 \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{6}{136727}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right)^2 + \right. \\ & \left. \exp\left(\frac{1}{12}\pi \exp\left(i\pi \left[\frac{\arg(136727-x)}{2\pi}\right]\right)\sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (136727-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \right. \\ & \left. \exp^2\left(i\pi \left[\frac{\arg\left(\frac{6}{136727}-x\right)}{2\pi}\right]\right)\sqrt{x}^2 \right. \\ & \left. \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{6}{136727}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right)^2\right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0) \end{aligned}$$

$$\begin{aligned}
& \frac{\left(2 \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/12}\right)^2}{2.05} = \\
& 0.590634 \exp\left(\frac{1}{12} \pi \left(\frac{1}{z_0}\right)^{1/2} \pi \left(\frac{1}{z_0}\right)^{1/2} \left[\arg(136727 - z_0)/(2\pi)\right] z_0^{1/2+1/2} \left[\arg(136727 - z_0)/(2\pi)\right]\right) \\
& \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \left(4 \left(\frac{1}{z_0}\right)^{\left[\arg\left(\frac{6}{136727} - z_0\right)/(2\pi)\right]}\right. \\
& \left. z_0^{1+\left[\arg\left(\frac{6}{136727} - z_0\right)/(2\pi)\right]} \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!}\right)^2\right) + \\
& 4 \exp\left(\frac{1}{24} \pi \left(\frac{1}{z_0}\right)^{1/2} \pi \left(\frac{1}{z_0}\right)^{1/2} \left[\arg(136727 - z_0)/(2\pi)\right] z_0^{1/2+1/2} \left[\arg(136727 - z_0)/(2\pi)\right]\right) \\
& \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \left(\frac{1}{z_0}\right)^{\left[\arg\left(\frac{6}{136727} - z_0\right)/(2\pi)\right]} \\
& z_0^{1+\left[\arg\left(\frac{6}{136727} - z_0\right)/(2\pi)\right]} \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!}\right)^2 + \\
& \exp\left(\frac{1}{12} \pi \left(\frac{1}{z_0}\right)^{1/2} \pi \left(\frac{1}{z_0}\right)^{1/2} \left[\arg(136727 - z_0)/(2\pi)\right] z_0^{1/2+1/2} \left[\arg(136727 - z_0)/(2\pi)\right]\right) \\
& \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \left(\frac{1}{z_0}\right)^{\left[\arg\left(\frac{6}{136727} - z_0\right)/(2\pi)\right]} \\
& z_0^{1+\left[\arg\left(\frac{6}{136727} - z_0\right)/(2\pi)\right]} \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!}\right)^2
\end{aligned}$$

Note that, multiplying by 2 this expression, we obtain:

$$2 * 1.2108 / 2.05 \left(\left(\left(\left(\left(\left(2 \sqrt{6/136727} \right) e^{((\sqrt{136727} \pi)/24)} + \sqrt{6/136727} \right) e^{((\sqrt{136727} \pi)/12)} \right) \right) \right) \right)^2$$

Input interpretation:

$$2 \times \frac{1.2108}{2.05} \left(2 \sqrt{\frac{6}{136727}} e^{1/24 (\sqrt{136727} \pi)} + \sqrt{\frac{6}{136727}} e^{1/12 (\sqrt{136727} \pi)} \right)^2$$

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Result:

More digits

• 6.28071... × 10⁷⁹

This result is very near to the value of length of a circle with radius equal to 1: 2π (multiple)

Series representations:

$$\begin{aligned}
 & \left(2 \left(2 \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727} \pi)/12} \right)^2 \right) 1.2108 \\
 & \hline
 & \quad 2.05 \\
 & 1.18127 \exp \left(\frac{1}{12} \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \right) \\
 & \left(4 \sqrt{z_0}^2 \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!} \right)^2 \right) + \\
 & 4 \exp \left(\frac{1}{24} \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \right) \\
 & \sqrt{z_0}^2 \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!} \right)^2 + \\
 & \exp \left(\frac{1}{12} \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \right) \sqrt{z_0}^2 \\
 & \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(\frac{6}{136727} - z_0\right)^k z_0^{-k}}{k!} \right)^2 \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))
 \end{aligned}$$

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$$\frac{\left(2\left(2\sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/12}\right)^2\right) 1.2108}{2.05} = 1.18127$$

$$\begin{aligned} & \exp\left(\frac{1}{12}\pi \exp\left(i\pi \left[\frac{\arg(136727-x)}{2\pi}\right]\right)\sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (136727-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \\ & \left(4 \exp^2\left(i\pi \left[\frac{\arg\left(\frac{6}{136727}-x\right)}{2\pi}\right]\right)\sqrt{x^2} \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{6}{136727}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right)^2 + 4 \exp\left(\frac{1}{24}\pi \exp\left(i\pi \left[\frac{\arg(136727-x)}{2\pi}\right]\right)\sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (136727-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \right. \\ & \left. \exp^2\left(i\pi \left[\frac{\arg\left(\frac{6}{136727}-x\right)}{2\pi}\right]\right)\sqrt{x^2} \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{6}{136727}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right)^2 + \right. \\ & \left. \exp\left(\frac{1}{12}\pi \exp\left(i\pi \left[\frac{\arg(136727-x)}{2\pi}\right]\right)\sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (136727-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \right. \\ & \left. \exp^2\left(i\pi \left[\frac{\arg\left(\frac{6}{136727}-x\right)}{2\pi}\right]\right)\sqrt{x^2} \right. \\ & \left. \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{6}{136727}-x\right)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right)^2\right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0) \end{aligned}$$

$$\frac{\left(2\left(2\sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/24} + \sqrt{\frac{6}{136727}} e^{(\sqrt{136727}\pi)/12}\right)^2\right)}{2.05} =$$

$$1.18127 \exp\left(\frac{1}{12} \pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(136727-z_0)/(2\pi)]} z_0^{1/2+1/2 [\arg(136727-z_0)/(2\pi)]}\right)$$

$$\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \left(4 \left(\frac{1}{z_0}\right)^{[\arg(\frac{6}{136727-z_0})/(2\pi)]} z_0^{1+[\arg(\frac{6}{136727-z_0})/(2\pi)]}\right) +$$

$$4 \exp\left(\frac{1}{24} \pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(136727-z_0)/(2\pi)]} z_0^{1/2+1/2 [\arg(136727-z_0)/(2\pi)]}\right)$$

$$\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \left(\frac{1}{z_0}\right)^{[\arg(\frac{6}{136727-z_0})/(2\pi)]} z_0^{1+[\arg(\frac{6}{136727-z_0})/(2\pi)]} +$$

$$\exp\left(\frac{1}{12} \pi \left(\frac{1}{z_0}\right)^{1/2 [\arg(136727-z_0)/(2\pi)]} z_0^{1/2+1/2 [\arg(136727-z_0)/(2\pi)]}\right)$$

$$\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (136727 - z_0)^k z_0^{-k}}{k!} \left(\frac{1}{z_0}\right)^{[\arg(\frac{6}{136727-z_0})/(2\pi)]} z_0^{1+[\arg(\frac{6}{136727-z_0})/(2\pi)]} +$$

- $n!$ is the factorial function
- $(a)_n$ is the Pochhammer symbol (rising factorial)
- \mathbb{R} is the set of real numbers
- $\arg(z)$ is the complex argument
 - $[x]$ is the floor function
 - i is the imaginary unit
 - [More information](#)

We have

$$\left\{ \begin{array}{ll} \Theta = \frac{r_+ - r_-}{4\alpha} & \text{“gravità di superficie”} \\ \phi = \frac{r_+ Q}{\alpha} & \text{“potenziale elettrico”} \\ \Omega = \frac{a}{\alpha} & \text{“frequenza angolare”} \end{array} \right.$$

Where $\mathbf{a} = J/M$

Result:

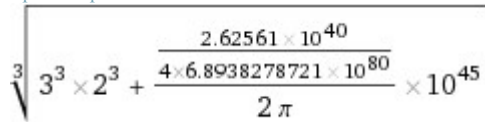
More digits

1731.41...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$\left(\left(\left(\left(\left(3^3 \times 2^3\right) + \left(\frac{2.62561 \times 10^{40}}{4 \times 6.8938278721 \times 10^{80}}\right)\right)\right) / (2\pi) \times 10^{45}\right)\right)\right)^{1/3}$$

Input interpretation:



Open code

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Result:

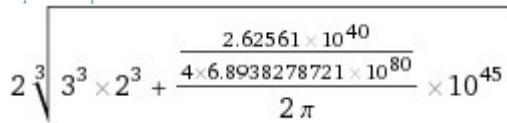
More digits

12.0079...

This result is very near to the value of black hole entropy 12,1904

$$2 \times \left(\left(\left(\left(\left(3^3 \times 2^3\right) + \left(\frac{2.62561 \times 10^{40}}{4 \times 6.8938278721 \times 10^{80}}\right)\right)\right) / (2\pi) \times 10^{45}\right)\right)\right)^{1/3}$$

Input interpretation:



Open code

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Result:

More digits

24.0158...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

$$\left(\left(\left(\left(\left(\left(3^3 \cdot 2^3\right) + \left(\left(\left(2.62561 \cdot 10^{40}\right) / \left(4 \cdot 6.8938278721 \cdot 10^{80}\right)\right)\right) / \left(2\pi\right) \cdot 10^{45}\right)\right)\right)\right)\right)^{1/15}$$

Input interpretation:

$$\sqrt[15]{3^3 \times 2^3 + \frac{2.62561 \times 10^{40}}{4 \times 6.8938278721 \times 10^{80}} \times 10^{45}}$$

Open code

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Result:

- Fewer digits

- More digits

1.643967830409512506779509641312779849901524429356232307605...

1.6439678304095125067795096413127798499015244293562323

Continued fraction:

- Linear form

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{4 + \frac{1}{4 + \frac{1}{2 + \frac{1}{1 + \frac{1}{1 + \frac{1}{3 + \frac{1}{144 + \frac{1}{9 + \frac{1}{1 + \frac{1}{115 + \frac{1}{1 + \frac{1}{13 + \frac{1}{2 + \frac{1}{8 + \frac{1}{1 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

Open code

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Possible closed forms:

- More

$$\frac{2778445344\pi}{5309558569} \approx 1.643967830409512506750391$$

$$\pi \sqrt{\text{root of } 7500x^3 - 58341x^2 - 44415x + 38143 \text{ near } x = 0.523291} \approx 1.6439678304095125067782314$$

$$\frac{2}{11} \pi \tanh^{-1}\left(\frac{47507592}{50811905}\right) \approx 1.64396783040951250686271$$

$$\frac{2(390\pi\pi! - 5068 - 535\pi + 71\pi^2)}{1085\pi} \approx 1.61882182401120175187004$$

$$\frac{2183652937\pi}{4237741253} \approx 1.618821824011201751961162$$

Now, for:

For $j \gg \varepsilon, n \gg \varepsilon$

$$|\alpha_{jn\omega'}| = \left| (2\pi)^{-1} P_{\omega}^{-} \omega^{-\frac{1}{2}} \Gamma\left(1 - \frac{i\omega}{\kappa}\right) \varepsilon^{-\frac{1}{2}} (\omega')^{-\frac{1}{2}} \cdot \int_{j\varepsilon}^{(j+1)\varepsilon} \exp i\omega'' (-2\pi n\varepsilon^{-1} + \kappa^{-1} \log \omega') d\omega'' \right|$$

$$= \left| \pi^{-1} P_{\omega}^{-} \omega^{-\frac{1}{2}} \Gamma\left(1 - \frac{i\omega}{\kappa}\right) \varepsilon^{-\frac{1}{2}} (\omega')^{-\frac{1}{2}} z^{-1} \sin \frac{1}{2} \varepsilon z \right| \quad (2.25)$$

where $\omega = j\varepsilon$ and $z = \kappa^{-1} \log \omega' - 2\pi n\varepsilon^{-1}$. For wave-packets which reach \mathcal{I}^+ at

And

Thus the total number of particles created in the mode p_{jn} is

$$\Gamma_{jn} (\exp(2\pi\omega\kappa^{-1}) - 1)^{-1}. \quad (2.29)$$

We obtain, from (2.29):

$$\Gamma\left(\frac{1}{12}\right) \frac{1}{\left(\exp\left(\frac{2\pi \cdot 0.9}{13.12806 \cdot 10^{39}}\right) - 1\right) \cdot \left(\frac{1}{6.8938278721 \cdot 10^{80}}\right) \cdot 4 \cdot 13.12806 \cdot 10^{39}}$$

Input interpretation:

$$\Gamma\left(\frac{1}{12}\right) \times \frac{1}{\exp\left(2\pi \times \frac{0.9}{13.12806 \times 10^{39}} \times \frac{1}{6.8938278721 \times 10^{80}} \times 4 \times 13.12806 \times 10^{39}\right) - 1}$$

[Open code](#)

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Result:

∞

Decimal approximation:

More digits

$3.50473... \times 10^{80}$

- $\Gamma(x)$ is the gamma function

- ∞ is complex infinity

Now, from the extended result, we obtain:

$$11 \times 33021.10 \times (3.50472794833786293306830406830717699438350879312 \times 10^{80})^{1.2108}$$

Where 33021,10 is a result of a Ramanujan Mock Theta Function, and 1,2108 is the following Hausdorff dimension:

$$2 \log_2 \left(\frac{\sqrt[3]{27 - 3\sqrt{78}} + \sqrt[3]{27 + 3\sqrt{78}}}{3} \right),$$

or root of $2^x - 1 = 2^{(2-x)/2}$

Input interpretation:

11 × 33 021.10

$$(3.50472794833786293306830406830717699438350879312 \times 10^{80})^{1.2108}$$

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Result:

More digits

$$1.21242... \times 10^{103}$$

This result is practically equal to the value of SMBHs entropy contained within the cosmic event horizon $1,2 \times 10^{103}$

Now, we have also:

$$\left((33021.10 \times (54 + \frac{3}{10})) \times \text{gamma} \left(\frac{1}{12} \right) \frac{1}{\left(\exp \left(\frac{2\pi \times (0.9/13.12806 \times 10^{39})}{6.8938278721 \times 10^{80}} \times 4 \times (13.12806 \times 10^{39}) \right) - 1 \right)} \right)$$

Where 33021,10 is a result of a Ramanujan Mock Theta Function (see next pages)

Input interpretation:

$$\left(33021.10 \left(54 + \frac{3}{10} \right) \right) \Gamma \left(\frac{1}{12} \right) \times \frac{1}{\exp \left(2\pi \times \frac{0.9}{13.12806 \times 10^{39}} \times \frac{1}{6.8938278721 \times 10^{80}} \times 4 \times 13.12806 \times 10^{39} \right) - 1}$$

[Open code](#)

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Result:

∞

Decimal approximation:

More digits

$$6.28414... \times 10^{86}$$

• $\Gamma(x)$ is the gamma function

• ∞ is complex infinity

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Possible closed forms:

More

$$\frac{8}{3} \pi \sinh^{-1} \left(\frac{1991044}{4351179} \right)^2 \approx 1.6437859005782310686275$$

$$\pi \left[\text{root of } 22765x^3 + 8208x^2 + 5718x - 8500 \text{ near } x = 0.523233 \right] \approx 1.6437859005782310620130399$$

$$-\frac{3337e!}{24} - \frac{649}{8} + \frac{171}{e} + \frac{901e}{4} \approx 1.6437859005782310605182$$

Now:

For $j \gg \varepsilon, n \gg \varepsilon$

$$|\alpha_{jn\omega'}| = \left| (2\pi)^{-1} P_{\omega}^{-} \omega^{-\frac{1}{2}} \Gamma \left(1 - \frac{i\omega}{\kappa} \right) \varepsilon^{-\frac{1}{2}} (\omega')^{-\frac{1}{2}} \cdot \int_{j\varepsilon}^{(j+1)\varepsilon} \exp i\omega'' (-2\pi n\varepsilon^{-1} + \kappa^{-1} \log \omega') d\omega'' \right|$$

$$= \left| \pi^{-1} P_{\omega}^{-} \omega^{-\frac{1}{2}} \Gamma \left(1 - \frac{i\omega}{\kappa} \right) \varepsilon^{-\frac{1}{2}} (\omega')^{-\frac{1}{2}} z^{-1} \sin \frac{1}{2} \varepsilon z \right| \quad (2.25)$$

where $\omega = j\varepsilon$ and $z = \kappa^{-1} \log \omega' - 2\pi n\varepsilon^{-1}$. For wave-packets which reach \mathcal{I}^+ at

For a Schwarzschild black hole $\kappa = \frac{1}{4M}$

where $P_{\omega}^{-} \equiv P_{\omega}(2M)$ is the value of the radial function for P_{ω} on the past event horizon in the analytically continued Schwarzschild solution. The expression $\omega' = \omega$

where j and n are integers, $j \geq 0, \varepsilon > 0$. For ε small these wave packets will have frequency $j\varepsilon$ and will be peaked around retarded time $u = 2\pi n\varepsilon^{-1}$ with width ε^{-1} .

We obtain the following interesting expressions:

$$\left(\frac{1}{\pi} \times 2 \times 13.12806 \times 10^{39} \left(\frac{1}{12} \right)^{-0.5} \gamma \times (-1) \left(1 - \frac{1}{3} \times 13.12806 \times 10^{39} \right) \times \frac{1}{\left(\frac{1}{4} \right)^{0.5} \left(\frac{1}{12} \right)^{0.5}} \right)$$

Input interpretation:

$$\frac{1}{\pi} \times 2 \times 13.12806 \times 10^{39} \left(\frac{1}{12} \right)^{-0.5} \gamma \times (-1) \left(1 - \frac{1}{3} \times 13.12806 \times 10^{39} \right) \times \frac{1}{\left(\frac{1}{4} \right)^{0.5} \left(\frac{1}{12} \right)^{0.5}}$$

• γ is the Euler-Mascheroni constant

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Result:

Fewer digits

More digits

$$\sin\left(\frac{4 \times 13.1281 \left(\log\left(\frac{1}{12}\right) - \frac{8\pi}{5}\right)}{\left(4 \times 13.1281 \left(\log\left(\frac{1}{12}\right) - \frac{8\pi}{5}\right)\right) 8}\right) = \sum_{k=0}^{\infty} \frac{(-1)^k \left(0.125 - \frac{\pi}{2}\right)^{2k}}{(2k)!}$$

Integral representations:

$$\sin\left(\frac{4 \times 13.1281 \left(\log\left(\frac{1}{12}\right) - \frac{8\pi}{5}\right)}{\left(4 \times 13.1281 \left(\log\left(\frac{1}{12}\right) - \frac{8\pi}{5}\right)\right) 8}\right) = 0.125 \int_0^1 \cos(0.125 t) dt$$

[Open code](#)

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$$\sin\left(\frac{4 \times 13.1281 \left(\log\left(\frac{1}{12}\right) - \frac{8\pi}{5}\right)}{\left(4 \times 13.1281 \left(\log\left(\frac{1}{12}\right) - \frac{8\pi}{5}\right)\right) 8}\right) = \frac{0.03125 \sqrt{\pi}}{i \pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{e^{-0.00390625/s+s}}{s^{3/2}} ds \text{ for } \gamma > 0$$

[Open code](#)

$$\sin\left(\frac{4 \times 13.1281 \left(\log\left(\frac{1}{12}\right) - \frac{8\pi}{5}\right)}{\left(4 \times 13.1281 \left(\log\left(\frac{1}{12}\right) - \frac{8\pi}{5}\right)\right) 8}\right) = \frac{0.03125 \sqrt{\pi}}{i \pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{e^{5.54518 s} \Gamma(s)}{\Gamma\left(\frac{3}{2} - s\right)} ds$$

for $0 < \gamma < 1$

$$0.1246747333852276899574427 * (((((((1/\pi * 2 * 13.12806 * 10^{39} * (1/12)^{-0.5}) * \text{gamma} * -(((1-(1/3 * 13.12806 * 10^{39})))) * [((((1/4)^{-0.5}) * (1/12)^{-0.5})])])$$

Input interpretation:

0.1246747333852276899574427

$$\left(\frac{1}{\pi} \times 2 \times 13.12806 \times 10^{39} \left(\frac{1}{12}\right)^{-0.5} \gamma \times (-1) \left(1 - \frac{1}{3} \times 13.12806 \times 10^{39}\right) \times \frac{1}{\left(\frac{1}{4}\right)^{0.5} \left(\frac{1}{12}\right)^{0.5}}\right)$$

- γ is the Euler-Mascheroni constant

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Result:

• Fewer digits

• More digits

$$6.3166639495304794318006693900235503061152113166610197... \times 10^{79}$$

$$6.31666394953047943180066939002355030611521131666 \times 10^{79}$$

$$(6.3166639495304794318 \times 10^{79})^1 / ((32^2 + 24 * 5) / \pi)$$

Input interpretation:

$$\frac{32^2 + 24 * 5}{\pi} \sqrt{6.3166639495304794318 \times 10^{79}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

1.656318695628409142159...

1.656318695628409142159

We note that, the result 1,656318... is practically equal to the 14th root of the following Ramanujan's class invariant $Q = (G_{505}/G_{101/5})^3 = 1164,2696$ i.e. 1,65578...

Indeed:

$$\begin{aligned} & \sqrt[14]{\left(\sqrt{\frac{113+5\sqrt{505}}{8}} + \sqrt{\frac{105+\sqrt{505}}{8}}\right)^3} = 1,65578 \dots \Rightarrow \\ & \Rightarrow \frac{32^2+24 \times 5}{\pi} \sqrt{6.3166639495304794318 \times 10^{79}} \\ & = 1.656318 \end{aligned}$$

$$24 \times 3 + 10^3 * (6.3166639495304794318 \times 10^{79})^{1/((32^2+24 \times 5)/\pi)}$$

Input interpretation:

$$24 \times 3 + 10^3 \frac{32^2+24 \times 5}{\pi} \sqrt{6.3166639495304794318 \times 10^{79}}$$

[Open code](#)

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Result:

More digits

1728.318695628409142159...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$\left(\left(\left(\left(24 \times 3 + 10^3 \times (6.3166639495304794318 \times 10^{79})^{1/\left(\frac{32^2+24 \times 5}{\pi}\right)}\right)\right)\right)\right)^{1/3}$$

Input interpretation:

$$\sqrt[3]{24 \times 3 + 10^3 \times \frac{32^2+24 \times 5}{\pi} \sqrt{6.3166639495304794318 \times 10^{79}}}$$

[Open code](#)

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Result:

More digits

12.000737676013970525180...

This result is very near to the value of black hole entropy 12,1904

$$2 * \left(\left(\left(\left(24 \times 3 + 10^3 \times (6.3166639495304794318 \times 10^{79})^{1/\left(\frac{32^2+24 \times 5}{\pi}\right)}\right)\right)\right)\right)^{1/3}$$

Input interpretation:

$$2 \sqrt[3]{24 \times 3 + 10^3 \times \frac{32^2+24 \times 5}{\pi} \sqrt{6.3166639495304794318 \times 10^{79}}}$$

[Open code](#)

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Result:

More digits

24.001475352027941050359...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

$$\left(\left(\left(\left(24 \times 3 + 10^3 \times (6.3166639495304794318 \times 10^{79})^{1/\left(\frac{32^2+24 \times 5}{\pi}\right)}\right)\right)\right)\right)^{1/15}$$

Input interpretation:

$$\sqrt[15]{24 \times 3 + 10^3 \times \frac{32^2+24 \times 5}{\pi} \sqrt{6.3166639495304794318 \times 10^{79}}}$$

[Open code](#)

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Result:

More digits

1.6437720382919401759948...

1.6437720382919401759948

Continued fraction:

Linear form

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{4 + \frac{1}{5 + \frac{1}{2 + \frac{1}{1 + \frac{1}{3 + \frac{1}{6 + \frac{1}{6 + \frac{1}{11 + \frac{1}{1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{2 + \frac{1}{1 + \frac{1}{8 + \frac{1}{1 + \frac{1}{97 + \frac{1}{3 + \frac{1}{\dots}}$$

[Open code](#)

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Possible closed forms:

More

- $\frac{641\ 357\ 815\ \pi}{1225\ 769\ 117} \approx 1.643772038291940175975387$
 $\frac{7}{11} \pi \sinh^2\left(\frac{1591\ 936}{1955\ 973}\right) \approx 1.6437720382919401731983$
 $\frac{20\sqrt{\frac{11429\ 426}{17370\ 077}}}{\pi^2} \approx 1.643772038291940182770$

(6.3166639495304794318 × 10⁷⁹)^{1/(1200/π)}

Input interpretation:

$$\frac{1200}{\pi} \sqrt[1200]{6.3166639495304794318 \times 10^{79}}$$

[Open code](#)

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Result:

- More digits
- 1.617771530518557825041...
- 1.617771530518557825041

This result is a very good approximation to the value of golden ratio

Continued fraction:

- Linear form

The Schwarzschild metric (1916) is a solution to the vacuum Einstein equations $R_{\mu\nu} = 0$. It is given by

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu = - \left(1 - \frac{2M}{r}\right) dt^2 + \left(1 - \frac{2M}{r}\right)^{-1} dr^2 + r^2 d\Omega_2^2, \quad (1.1)$$

where $0 < r < \infty$ is a radial coordinate and $d\Omega_2^2 = d\theta^2 + \sin^2\theta d\phi^2$ is the round metric on the two-sphere.

We now make a coordinate transformation from (t, r, θ, ϕ) to (v, r, θ, ϕ) , i.e. we replace t by the coordinate v that labels ingoing radial null lines. The coordinates (v, r, θ, ϕ) are called *ingoing Eddington-Finkelstein (IEF) coordinates* and the line-element in *IEF* coordinates reads (exercise)

$$ds^2 = - \left(1 - \frac{2M}{r}\right) dv^2 + 2dvdr + r^2 d\Omega_2^2. \quad (1.22)$$

This metric is perfectly regular at $r = 2M$ (i.e. it is non-degenerate: $\det g_{\mu\nu} \neq 0$). In fact, it is fine *everywhere* except at $r = 0$. We may therefore extend the range of

and:

[21, 22].) The operators \mathbf{a}_i and \mathbf{a}_i^\dagger have the natural interpretation as the annihilation and creation operators for ingoing particles i.e. for particles at past null infinity \mathcal{I}^- . Because massless fields are completely determined by their data on

To calculate the coefficients $\alpha_{\omega\omega'}$ and $\beta_{\omega\omega'}$, consider a solution p_ω propagating backwards from \mathcal{I}^+ with zero Cauchy data on the event horizon. A part $p_\omega^{(1)}$ of the solution p_ω will be scattered by the static Schwarzschild field outside the collapsing body and will end up on \mathcal{I}^- with the same frequency ω . This will give a $\delta(\omega' - \omega)$ term in $\alpha_{\omega\omega'}$. The remainder $p_\omega^{(2)}$ of p_ω will enter the collapsing body where it will be partly scattered and partly reflected through the centre, eventually emerging to \mathcal{I}^- . It is this part $p_\omega^{(2)}$ which produces the interesting effects. Because the retarded time coordinate u goes to infinity on the event horizon, the surfaces of constant phase of the solution p_ω will pile up near the event horizon (Fig. 4). To an observer on the collapsing body the wave would seem to have a very large blue-shift. Because its effective frequency was very high, the wave would propagate by geometric optics through the centre of the body and out on \mathcal{I}^- . On \mathcal{I}^- $p_\omega^{(2)}$ would have an infinite number of cycles just before the advanced time $v = v_0$ where v_0 is the latest time that a null geodesic could leave \mathcal{I}^- , pass through the centre of the body and escape to \mathcal{I}^- before being trapped by the event horizon. One can estimate the form of $p_\omega^{(2)}$ on \mathcal{I}^- near $v = v_0$ in the following way. Let x be a point on the event horizon outside the matter and let l^a be a null vector tangent to the horizon. Let n^a be the future-directed null vector at x which is directed radially inwards and normalized so that $l^a n_a = -1$. The vector $-\epsilon n^a$ (ϵ small and positive) will connect the point x on the event horizon with a nearby null surface of constant retarded time u and therefore with a surface of constant phase of the solution $p_\omega^{(2)}$. If the vectors l^a and n^a are parallelly transported along the null geodesic γ through x which generates the horizon, the vector $-\epsilon n^a$ will always connect the event horizon with the same surface of constant phase of $p_\omega^{(2)}$.

$$p_\omega^{(2)} \sim (2\pi)^{-\frac{1}{2}} \omega^{-\frac{1}{2}} r^{-1} P_\omega^- \exp\left(-i \frac{\omega}{\kappa} \left(\log\left(\frac{v_0 - v}{CD}\right)\right)\right) \quad (2.18)$$

where $P_\omega^- \equiv P_\omega(2M)$ is the value of the radial function for P_ω on the past event horizon in the analytically continued Schwarzschild solution. The expression (2.18) for $p_\omega^{(2)}$ is valid only for $v_0 - v$ small and positive. At earlier advanced times the amplitude will be different and the frequency measured with respect to v , will approach the original frequency ω .

We have that for: $r = 2.62561 \times 10^{40}$; $\omega = 6.62606957 * 10^{-34}$; $\kappa = 1 / 4M$;
 $P_\omega^- = P_\omega(2M) = 2M$ (as a radial coordinate r); $CD = 1$ and $v_0 - v = v$; we obtain,
from (2.18):

$$(2\pi)^{-0.5} * (6.62606957 * 10^{-34})^{-0.5} * 1/(2.62561 * 10^{40}) * \\
(2 * 13.12806 * 10^{39}) * \exp(((((((((-6.62606957 * 10^{-34}i) * ((4 * 13.12806 * 10^{39}))) * \\
\ln(2.188745451993 * 10^6))))))))))$$

Input interpretation:

$$\frac{1}{(2\pi)^{0.5} \left(\frac{6.62606957}{10^{34}}\right)^{0.5}} \frac{1}{2.62561 \times 10^{40}} (2 \times 13.12806 \times 10^{39}) \exp\left(-\frac{6.62606957 i}{10^{34}} (4 \times 13.12806 \times 10^{39})\right) \log(2.188745451993 \times 10^6)$$

Open code

- $\log(x)$ is the natural logarithm
- i is the imaginary unit

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Result:

More digits

$$-1.49514... \times 10^{16} - 4.08053... \times 10^{15} i$$

Polar coordinates:

$$r = 1.54982 \times 10^{16} \text{ (radius), } \theta = -164.735^\circ \text{ (angle)}$$

Open code

$$\left(\left(\left(\left(\left(2\pi\right)^{-0.5} * \left(6.62606957 * 10^{-34}\right)^{-0.5} * 1/\left(2.62561 * 10^{40}\right) * \left(2 * 13.12806 * 10^{39}\right) * \exp\left(\left(\left(\left(\left(-6.62606957 * 10^{-34}i\right) * \left(4 * 13.12806 * 10^{39}\right)\right)\right)\right) * \ln\left(2.188745451993 * 10^6\right)\right)\right)\right)\right)\right)^{1/5}$$

Input interpretation:

$$\left(\left(\frac{1}{2.62561 \times 10^{40}} (2 \times 13.12806 \times 10^{39}) \exp\left(-\frac{6.62606957 i}{10^{34}} (4 \times 13.12806 \times 10^{39})\right) \log(2.188745451993 \times 10^6)\right)\right) / \left((2\pi)^{0.5} \left(\frac{6.62606957}{10^{34}}\right)^{0.5}\right)^{(1/5)}$$

Open code

- $\log(x)$ is the natural logarithm
- i is the imaginary unit

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Result:

More digits

$$1451.81... - 940.904... i$$

Polar coordinates:

$$r = 1730.04 \text{ (radius), } \theta = -32.9469^\circ \text{ (angle)}$$

1730.04

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Result:

More digits

3.1386072523864963972495593637536878229078622628502229540... -
0.13082655987048263266335707960510786645214239534570242667... i

[Open code](#)

Polar coordinates:

$r = 3.14133$ (radius), $\theta = -2.38688^\circ$ (angle)

Continued fraction:

Linear form

$$\begin{aligned}
& 3 + \frac{1}{7 + \frac{1}{13 + \frac{1}{4 + \frac{1}{1 + \frac{1}{1 + \frac{1}{7 + \frac{1}{1 + \frac{1}{\dots}}}}}}}}}
\end{aligned}$$

[Open code](#)

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Possible closed forms:

More

$\pi \approx 3.14159265$

$$\sqrt[3]{31} \approx 3.141380652$$

$$\frac{289}{92} \approx 3.141304347$$

This result 3.14133... is a very good approximation to π .

Now, from:

Charged and rotating AdS black holes and their CFT duals

S.W. Hawking and H.S. Reall† - <https://arxiv.org/abs/hep-th/9908109v2>

We have:

The AdS/CFT correspondence relates the worldvolume theory of N M2-branes in the large N limit to eleven dimensional supergravity on S^7 . Four dimensional Kerr-AdS black holes are expected to be dual to the worldvolume CFT in a rotating three dimensional Einstein universe. For completeness we present the free CFT results for this case. The CFT is a free supersingleton field theory [31]. There are eight real scalar fields and eight Majorana spin-1/2 fields. The energy levels of these fields are $\omega = j + 1/2$ where $j = 0, 1, \dots$ for the scalars and $j = 1/2, 3/2, \dots$ for the fermions [32]. The partition functions can be evaluated

Thus the partition function for the free CFT of an M2-brane is

$$\log Z = 8 \sum_{n \text{ odd}} \frac{\cosh(\beta n/2)}{n \sinh(\beta n(1 - \Omega)/2) \sinh(\beta n(1 + \Omega)/2)} \quad (2.34)$$

We have also:

$$\log Z \approx \frac{16}{\beta(1 - \Omega^2)} \sum_{n \text{ odd}} \frac{1}{n^2 \sinh(\beta n/2)} \quad (2.38)$$

The divergence is of the same form as that obtained from the bulk supergravity action in the limit $|a| \rightarrow 1$ [11].

From (2.38) we obtain, for $\beta = 0.58$; $\Omega = 0.637^{1/6}$:

((((16* 1/(((0.58*(1-(((0.637)^1/6))^2)))))) sum 1 / (k^2 sinh(0.58/2k)), k = 1 to infinity

Input interpretation:

$$\left(16 \times \frac{1}{0.58 \left(1 - \sqrt[6]{0.637^2} \right)} \right) \sum_{k=1}^{\infty} \frac{1}{k^2 \sinh\left(\frac{0.58}{2} k\right)}$$

- $\sinh(x)$ is the hyperbolic sine function

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Result:

792.136

792.136

From (2.34), we obtain:

sum 1/((k sinh(0.58k((1-0.637^(1/6))/2)) sinh(0.58k((1+0.637^(1/6))/2)))), k = 1 to infinity

Infinite sum:

$$\sum_{k=1}^{\infty} \frac{1}{k \sinh\left(\frac{1}{2} \times 0.58 \left(1 - \sqrt[6]{0.637} \right) k\right) \sinh\left(\frac{1}{2} \times 0.58 \left(1 + \sqrt[6]{0.637} \right) k\right)} = 92.7062$$

[Open code](#)

- $\sinh(x)$ is the hyperbolic sine function

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Convergence tests:

By the comparison test, the series converges.

sum (cosh(0.58/2k), k = 1 to infinity

Input interpretation:

$$\sum_{k=1}^{\infty} \cosh\left(\frac{0.58 k}{2}\right)$$

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Result:

$$\sum_{k=1}^{\infty} \cosh\left(\frac{0.58 k}{2}\right) \text{ (sum diverges)}$$

Convergence tests:

By the limit test, the series diverges.

Partial sum formula:

$$\sum_{k=1}^n \cosh\left(\frac{0.58 k}{2}\right) \approx 0.5 (6.87244 \sinh(0.29 (n + 0.5)) - 1)$$

$$0.5(6.87244 \sinh(0.29(n+0.5))-1)$$

Input interpretation:

$$0.5 (6.87244 \sinh(0.29 (n + 0.5)) - 1)$$

Values:

More

n	1	2	3	4	5
0.5 (6.87244 $\sinh(0.29 (n + 0.5)) - 1$)	1.04234	2.21531	3.61824	5.36995	7.61879

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Alternate forms:

More

$$3.43622 \sinh(0.29 n + 0.145) - 0.5$$

[Open code](#)

$$3.43622 (\sinh(0.29 (n + 0.5)) - 0.145509)$$

[Open code](#)

$$3.43622 \sinh(0.29 (n + 0.5)) - 0.5$$

[Open code](#)

Real root:

Step-by-step solution

$$n \approx 3.03817 \times 10^{-7}$$

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Roots:

Approximate forms

Step-by-step solution

$$n = \frac{1}{58} i \left(400 \pi m + 29 i - 200 i \sinh^{-1}\left(\frac{25000}{171811}\right) \right), \quad m \in \mathbb{Z}$$

- $\cosh(x)$ is the hyperbolic cosine function

- $\cosh(x)$ is the hyperbolic cosine function

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[Open code](#)

$$n = \frac{1}{58} i \left(400 \pi m + 200 \pi + 29 i + 200 i \sinh^{-1} \left(\frac{25000}{171811} \right) \right), \quad m \in \mathbb{Z}$$

Periodicity:

Approximate form

periodic in n with period $\frac{200 i \pi}{29}$

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Series expansion at $n = 0$:

$$-3.05943 \times 10^{-7} + 1.007 n + 0.021025 n^2 + 0.0141148 n^3 + 0.00014735 n^4 + O(n^5)$$

(Taylor series)

[Open code](#)

Series expansion at $n = \infty$:

$$3.43622 \sinh(0.29 n + 0.145) - 0.5$$

[Open code](#)

Derivative:

Step-by-step solution

$$\frac{d}{dn} (0.5 (6.87244 \sinh(0.29 (n + 0.5)) - 1)) = 0.996504 \cosh(0.29 n + 0.145)$$

[Open code](#)

- $\cosh(x)$ is the hyperbolic cosine function

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Indefinite integral:

$$\int 0.5 (6.87244 \sinh(0.29 (n + 0.5)) - 1) dn = -0.5 n + 1.72414 \sinh(0.29 n) + 11.9738 \cosh(0.29 n) + \text{constant}$$

For $n = 4$, we obtain:

$$8 * 5.36995 * \sum_{k=1}^{\infty} \frac{1}{(k \sinh(0.58k((1-0.637^{(1/6)})/2)) \sinh(0.58k((1+0.637^{(1/6)})/2))))}, \quad k = 1 \text{ to infinity}$$

Input interpretation:

$$8 \times 5.36995 \sum_{k=1}^{\infty} \frac{1}{k \sinh\left(0.58 k \left(\frac{1}{2} \left(1 - \sqrt[6]{0.637}\right)\right)\right) \sinh\left(0.58 k \left(\frac{1}{2} \left(1 + \sqrt[6]{0.637}\right)\right)\right)}$$

- $\sinh(x)$ is the hyperbolic sine function

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Result:

3982.62

$$5.36995 * \sum_{k=1}^{\infty} \frac{1}{(k \sinh(0.58k((1-0.637^{(1/6)})/2)) \sinh(0.58k((1+0.637^{(1/6)})/2))))}, \quad k = 1 \text{ to infinity}$$

Input interpretation:

$$5.36995 \sum_{k=1}^{\infty} \frac{1}{k \sinh\left(0.58 k \left(\frac{1}{2} \left(1 - \sqrt[6]{0.637}\right)\right)\right) \sinh\left(0.58 k \left(\frac{1}{2} \left(1 + \sqrt[6]{0.637}\right)\right)\right)}$$

- $\sinh(x)$ is the hyperbolic sine function

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Result:

497.828
497.828

From Ramanujan formula for $p(20.56) \approx 21$, we obtain:

$$\left(\left(\frac{1}{4 \times 20.56 \times \sqrt{3}}\right) * \exp\left(\left(\left(\pi * \left(\sqrt{\frac{2 \times 20.56}{3}}\right)\right)\right)\right)\right)$$

Input:

$$\frac{1}{4 \times 20.56 \sqrt{3}} \exp\left(\pi \sqrt{\frac{2 \times 20.56}{3}}\right)$$

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Result:

More digits
789.988...

Series representations:

More

$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 20.56}{3}}\right)}{4 \times 20.56 \sqrt{3}} = \frac{0.0121595 \exp\left(\pi \sqrt{12.7067} \sum_{k=0}^{\infty} e^{-2.54213 k} \left(\frac{1}{2}\right)_k\right)}{\sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \left(\frac{1}{2}\right)_k}$$

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$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 20.56}{3}}\right)}{4 \times 20.56 \sqrt{3}} = \frac{0.0121595 \exp\left(\pi \sqrt{12.7067} \sum_{k=0}^{\infty} \frac{(-0.0786988)^k \left(-\frac{1}{2}\right)_k}{k!}\right)}{\sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)_k \left(-\frac{1}{2}\right)_k}{k!}}$$

[Open code](#)

$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 20.56}{3}}\right)}{4 \times 20.56 \sqrt{3}} = \frac{0.0121595 \exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (13.7067 - z_0)^k z_0^{-k}}{k!}\right)}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3 - z_0)^k z_0^{-k}}{k!}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

From Ramanujan formula for $p(18.56) \approx 19$, we obtain:

$$\left(\frac{1}{4 \times 18.56 \sqrt{3}} \right) * \exp\left(\pi \sqrt{\frac{2 \times 18.56}{3}} \right)$$

Input:

$$\frac{1}{4 \times 18.56 \sqrt{3}} \exp\left(\pi \sqrt{\frac{2 \times 18.56}{3}} \right)$$

[Open code](#)

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Result:

More digits

489.889...

Series representations:

More

$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 18.56}{3}} \right)}{4 \times 18.56 \sqrt{3}} = \frac{0.0134698 \exp\left(\pi \sqrt{11.3733} \sum_{k=0}^{\infty} e^{-2.43127k} \binom{\frac{1}{2}}{k} \right)}{\sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \binom{\frac{1}{2}}{k}}$$

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$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 18.56}{3}} \right)}{4 \times 18.56 \sqrt{3}} = \frac{0.0134698 \exp\left(\pi \sqrt{11.3733} \sum_{k=0}^{\infty} \frac{(-0.087925)^k \binom{-\frac{1}{2}}{k}}{k!} \right)}{\sqrt{2} \sum_{k=0}^{\infty} \frac{\binom{-\frac{1}{2}}{k} \binom{-\frac{1}{2}}{k}}{k!}}$$

[Open code](#)

$$\frac{\exp\left(\pi \sqrt{\frac{2 \times 18.56}{3}} \right)}{4 \times 18.56 \sqrt{3}} = \frac{0.0134698 \exp\left(\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \binom{-\frac{1}{2}}{k} (12.3733 - z_0)^k z_0^{-k}}{k!} \right)}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \binom{-\frac{1}{2}}{k} (3 - z_0)^k z_0^{-k}}{k!}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

We note that the two results, concerning the partition functions (eqs. 2.34 and 2.38)

792,136 and 497,828 are very closed to the two results regarding the Hardy-Ramanujan partition formula for $p(19)$ and $p(21)$, i.e., 789,988 and 489,889. We note that for to obtain the above results, n is equal to 18,56 and 20,56, that are good approximations to the numbers 19 and 21.

Now, we observe that, for $c = 24$ and $c = 48$, the (holomorphic) partition functions read

$$Z_{24}(\tau) = j(\tau) - 744 \\ = q^{-1} + 196884q + 21493760q^2 + 864299970q^3 + 20245856256q^4 + \dots, \quad (1.5)$$

where $j(\tau)$ is the modular j-function and $q = e^{2\pi i\tau}$. The partition function in (1.5) defines a very special theory among the 71 holomorphic CFTs believed to exist at $c = 24$. Note that:

$\ln(864299970) = 20,577430454012695912396758411399$, a value very near to 20.56, utilized for the calculation of $p(21)$.

While, for 18.56, we note that:

$$(((\ln(302198519 \div 2) + \ln(86645620)))) / 2 = 18,555392263251482338584975642891,$$

where 302198519 and 86645620 are values concerning some coefficients of $Z(\tau)$ modular j-invariant (or modular j-function).

Note that, 497,828 and 792,136 are very near to the rest mass of the Kaon meson, that is equal to 497.614 ± 0.024 , and to the rest mass of the Omega meson, that is equal to 782.65 ± 0.12 and to the scalar meson $K^*_0(700)$ Breit-Wigner Mass, that is 824 ± 30 (lower value 794) OUR AVERAGE, or 797 ± 19 (i.e. 797)

Now, we have:

we introduce the stringy parameters. The five dimensional Newton constant is related to the ten dimensional one by $1/G_5 = \pi^3/G_{10}$, where the numerator is simply the volume of the internal S^5 . We are still using units for which the AdS length scale is unity, which means that $\lambda^{1/4}l_s = 1$ when we appeal to the AdS/CFT correspondence. The ten-dimensional Newton constant is related to the CFT parameters by $G_{10} = \pi^4/(2N^2)$ so $G_5 = \pi/(2N^2)$. The supergravity action can then be written

Notable examples are $d = 4$, $N = 4$ supersymmetric Yang–Mills theory, which is dual to Type IIB string theory on $AdS_5 \times S^5$. In our case we take $N = 4$.

For $N = 4$, $G_5 = \pi / 32$; $\Phi = 1$ and $r_+ = 2.62561 * 10^{40}$

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Result:

More digits

• $1.62435... \times 10^{61}$

This result is an evident multiple of a golden number in the range of golden ratio value.

Note that, from this formula, we can to obtain also the size of the Monster Group. Indeed:

$$1/(2*10^7) * (((((-Pi/(8*Pi / 32) * 0.58 * (((((2.62561*10^40)^2*((1-(2.62561*10^40))))^2-(2.62561*10^40)^4)))))))*Pi))))))^{1/2}$$

Input interpretation:

$$\frac{1}{2 \times 10^7} \sqrt{\left(-\frac{\pi}{8 \times \frac{\pi}{32}} \times 0.58 ((2.62561 \times 10^{40})^2 (1 - 2.62561 \times 10^{40})^2 - (2.62561 \times 10^{40})^4)\right) \pi}$$

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Result:

More digits

• $8.12174... \times 10^{53}$

Comparisons:

≈ the size of the Monster group (≈ 8.1 × 10⁵³)

And:

$$((((((((((((((-Pi/(8*Pi / 32) * 0.58 * (((((2.62561*10^40)^2*((1-(2.62561*10^40))))^2-(2.62561*10^40)^4)))))))*Pi))))))^{1/2}))))))^{1/12} * ((12^2+12)/(10^2)) + 89$$

Input interpretation:

$$12 \sqrt{\sqrt{\left(-\frac{\pi}{8 \times \frac{\pi}{32}} \times 0.58 ((2.62561 \times 10^{40})^2 (1 - 2.62561 \times 10^{40})^2 - (2.62561 \times 10^{40})^4)\right) \pi} \times \frac{12^2 + 12}{10^2} + 89}$$

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Result:

More digits

• $1.96884... \times 10^5$

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Possible closed forms:

More

$$\pi \approx 3.141592653589793238462643383279502884$$

$$\log(G_{Ge}) \approx 3.141592653589793238462643383279502884$$

$$\sqrt{6 \zeta(2)} \approx 3.141592653589793238462643383279502884$$

Furthermore, we have also:

$$2 * -(8.398633577258719 \times 10^{121} * 0.785398163397448) / (((((((0.58 * ((((((2.62561 \times 10^{40})^2 * (((1 - (2.62561 \times 10^{40}))))^2 - (2.62561 \times 10^{40})^4))))))))))))$$

Input interpretation:

$$2 \left(- \frac{(8.398633577258719 \times 10^{121}) \times 0.785398163397448}{0.58 ((2.62561 \times 10^{40})^2 (1 - 2.62561 \times 10^{40})^2 - (2.62561 \times 10^{40})^4)} \right)$$

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Result:

∞

∞ is complex infinity

Decimal approximation:

More digits

6.283185307179583862345929741300617850685210095286003752250...

[Open code](#)

6.283185307179583862345929741300617850685210095286003752250

Continued fraction:

Linear form

$$\begin{aligned}
&6 + \cfrac{1}{3 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{7 + \cfrac{1}{2 + \cfrac{1}{146 + \cfrac{1}{3 + \cfrac{1}{6 + \cfrac{1}{1 + \cfrac{1}{1 + \cfrac{1}{2 + \cfrac{1}{6 + \cfrac{1}{1 + \cfrac{1}{3 + \cfrac{1}{2 + \cfrac{1}{1 + \cfrac{1}{4 + \cfrac{1}{2 + \cfrac{1}{1 + \cfrac{1}{5 + \cfrac{1}{1 + \cfrac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}
\end{aligned}$$

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Possible closed forms:

More

$$\sqrt[3]{\frac{1}{5} (391 - 1763 e + 806 \pi + 4486 \log(2))} \approx 6.2831853071795838616353$$

$$\frac{\text{root of } 453 x^3 - 2665 x^2 - 11504 x + 65\,125 \text{ near } x = 6.28319}{6.2831853071795838655663} \approx 1$$

$$\frac{\text{root of } 65\,125 x^3 - 11504 x^2 - 2665 x + 453 \text{ near } x = 0.159155}{6.2831853071795838655663} \approx 1$$

Or:

Input interpretation:

6.283185307179583

[Open code](#)

6.283185307179583

Possible closed forms:

More

$$2\pi \approx 6.2831853071795864769$$

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$$\frac{1}{\mathcal{P}_A} \approx 6.2831853071795864769$$

$$2\sqrt{6\zeta(2)} \approx 6.2831853071795864769$$

This result is equal to the length of a circle with radius equal to 1: 2π

This last result, which concerns the action of a Reissner-Nordstrom-AdS black hole in G_5 , reinforces the vision that the imprint of very different, perhaps all, the structures of the cosmos (black holes, stars, galaxies, planets. ...) is the circumference. Furthermore, from the equations that we have developed, we always find solutions with values equal to golden numbers or, just, to the golden ratio. This allows us to predict in an ever more convincing way, that the universe is the product of the infinite ways in which π and ϕ are manifested and concretized in the marvelous varieties of which the multiverse is studded.

Now, from (3.12):

$$\beta = \frac{2\pi r_+}{1 - \Phi(r_+)^2 + 2r_+^2}$$

We obtain:

$$(2\pi \times 2.62561 \times 10^{40}) / (((1 - (2.62561 \times 10^{40})^2 + 2 \times (2.62561 \times 10^{40})^2)))$$

Input interpretation:

$$\frac{2\pi \times 2.62561 \times 10^{40}}{1 - (2.62561 \times 10^{40})^2 + 2(2.62561 \times 10^{40})^2}$$

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Result:

More digits

$$2.39304... \times 10^{-40}$$

$$((((1 / (((2\pi \times 2.62561 \times 10^{40}) / (((1 - (2.62561 \times 10^{40})^2 + 2 \times (2.62561 \times 10^{40})^2))))))))))^{1/3}$$

Input interpretation:

$$\sqrt[3]{\frac{1}{\frac{2\pi \times 2.62561 \times 10^{40}}{1 - (2.62561 \times 10^{40})^2 + 2(2.62561 \times 10^{40})^2}}}$$

[Open code](#)

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Result:

Fewer digits

More digits

$$1.6107078791561146741886837093545784297119265995199574... \times 10^{13}$$

$$1.61070787915611467418868370935457842971192659951 \times 10^{13}$$

$$((((1 / (((2\pi \times 2.62561 \times 10^{40}) / (((1 - (2.62561 \times 10^{40})^2 + 2 \times (2.62561 \times 10^{40})^2))))))))))^{1/3} * 1/10^{10} + 27 \times 4 + 8$$

Input interpretation:

$$\sqrt[3]{\frac{1}{\frac{2\pi \times 2.62561 \times 10^{40}}{1 - (2.62561 \times 10^{40})^2 + 2(2.62561 \times 10^{40})^2}}} \times \frac{1}{10^{10}} + 27 \times 4 + 8$$

[Open code](#)

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Result:

More digits

$$1726.71...$$

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–

$$\sqrt[15]{\sqrt[3]{\frac{1}{\frac{2\pi \times 2.62561 \times 10^{40}}{1-(2.62561 \times 10^{40})^2 + 2(2.62561 \times 10^{40})^2}}}} \times \frac{1}{10^{10}} + 27 \times 4 + 8$$

[Open code](#)

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Result:

- Fewer digits
- More digits

1.643669859320177518437090594238055353777057356692880322562...

1.6436698593201775184370905942380553537770573566928803

Continued fraction:

Linear form

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{4 + \frac{1}{6 + \frac{1}{15 + \frac{1}{1 + \frac{1}{3 + \frac{1}{16 + \frac{1}{12 + \frac{1}{4 + \frac{1}{30 + \frac{1}{1 + \frac{1}{27 + \frac{1}{1 + \frac{1}{1 + \frac{1}{3 + \frac{1}{1 + \frac{1}{29 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

[Open code](#)

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Possible closed forms:

More

- $\frac{778\,095\,317\pi}{1487\,195\,569} \approx 1.64366985932017751852651$
- $\pi \sqrt{\text{root of } 2580x^4 - 6500x^3 - 4680x^2 + 2098x + 921 \text{ near } x = 0.523196} \approx 1.643669859320177518428253$
- $\frac{2(-350 + 124\pi + 69\pi^2)}{337 - 290\pi + 147\pi^2} \approx 1.64366985932017751874142$

Now:

The action I of the black hole relative to AdS is [12]

$$I = \frac{\pi}{8G_5} \beta (r_+^2 (1 - \Phi(r_+)^2) - r_+^4) \quad (3.11)$$

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Possible closed forms:

More

$$\log\left(\frac{1}{3}\left(251 - 331\sqrt{2} - 46e + 90e^2 - 35\pi - 20\pi^2\right)\right) \approx 1.6436180426361211085006$$

$$\text{root of } 3325x^3 - 2824x^2 - 30196x + 42496 \text{ near } x = 1.64362 \approx$$

$$1.643618042636121106891300$$

$$\frac{5239249949\pi}{10014242192} \approx 1.6436180426361211068596801$$

From:

Entropia e Termodinamica dei Buchi Neri

Candidato: **FRANCESCO BATTISTEL** Relatore: **Prof. STEFANO ANSOLDI**

Anno Accademico 2014/2015 - UNIVERSITÀ DEGLI STUDI DI TRIESTE CORSO DI STUDI IN FISICA

Important and useful note in Italian

“.....”

Definiamo ora le seguenti funzioni:

$$\begin{cases} \Theta = \frac{r_+ - r_-}{4\alpha} & \text{“gravità di superficie”} \\ \phi = \frac{r_+ Q}{\alpha} & \text{“potenziale elettrico”} \\ \Omega = \frac{a}{\alpha} & \text{“frequenza angolare”}. \end{cases} \quad (3.11)$$

Otteniamo quindi una formula che ricorda molto quella che esprime il primo principio della termodinamica, che riporto sotto:

$$dM = \Theta d\alpha + \phi dQ + \Omega \cdot dL \quad (3.12)$$

$$dE = T dS - p dV. \quad (3.13)$$

Dai risultati di Hawking [6] sappiamo che l'area (razionalizzata o meno) dell'orizzonte degli eventi non può diminuire, ovvero che $d\alpha \geq 0$, così come in termodinamica $dS \geq 0$. La gravità di superficie dunque svolgerebbe il ruolo della temperatura (in particolare si nota facilmente da (3.9) che è una quantità sempre positiva), mentre $\phi dQ + \Omega \cdot dL$ rappresenterebbe il lavoro fatto sul buco nero dall'esterno. Si noti come definire un'entropia comporti anche inevitabilmente la definizione di una “temperatura”.

L'interpretazione fisica di Θ come una temperatura termodinamica non è comunque immediata, soprattutto poiché resta da capire se gli si possa assegnare lo stesso significato fisico della temperatura in processi in cui quest'ultima compare. La teoria della radiazione di Hawking suggerisce una risposta positiva: un buco nero infatti emetterebbe radiazione di corpo nero con temperatura $T \propto \Theta$, anche se sperimentalmente questo non è stato ancora verificato [10].

.....”

We have:

$$r_{\pm} = M \pm \sqrt{M^2 - Q^2 - a^2}.$$

we can to obtain Q and Q²

We have also:

$$\begin{aligned} \alpha &= \left(M + \sqrt{M^2 - Q^2 - a^2} \right)^2 + a^2 \\ &= M^2 + M^2 - Q^2 - a^2 + 2M\sqrt{M^2 - Q^2 - a^2} + a^2 \\ &= 2M \left(M + \sqrt{M^2 - Q^2 - a^2} \right) - Q^2 \\ &= 2Mr_+ - Q^2 \end{aligned}$$

and:

$$\phi = \frac{r_+ Q}{\alpha}$$

$$\Theta = \frac{r_+ - r_-}{4\alpha}$$

From the above formulas, we obtain, after some calculations, various interesting results.

For Q, we obtain:

$$\text{sqrt}(\left(\left(\left(13.12806 \times 10^{39}\right)^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2 - \left(2.62561 \times 10^{40} - 13.12806 \times 10^{39}\right)^2\right)\right))$$

Input interpretation:

$$\sqrt{\left(13.12806 \times 10^{39}\right)^2 - \left(\frac{0.9}{13.12806 \times 10^{39}}\right)^2 - \left(2.62561 \times 10^{40} - 13.12806 \times 10^{39}\right)^2}$$

[Open code](#)

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Result:

More digits

$$2.29155... \times 10^{37}$$

For Q², we obtain:

Input interpretation:

0.604634319297810930445826988746530721982611151127023401400...

And:

$$1/((((((((2.29155 \times 10^{37} * 2.62561 \times 10^{40})) / ((6.8938278721 \times 10^{80}))))))))))^{1/14}$$

Input interpretation:

$$\frac{1}{\sqrt[14]{\frac{2.29155 \times 10^{37} \times 2.62561 \times 10^{40}}{6.8938278721 \times 10^{80}}}}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

- Fewer digits
- More digits

1.653892225570895550580899170745003769310106711597702021006...

1.6538922255708955505808991707450037693101067115977020

We note that, the result 1,653892... is practically equal to the 14th root of the following Ramanujan's class invariant $Q = (G_{505}/G_{101/5})^3 = 1164,2696$ i.e. 1,65578...

Indeed:

$$\sqrt[14]{\left(\sqrt{\frac{113+5\sqrt{505}}{8}} + \sqrt{\frac{105+5\sqrt{505}}{8}}\right)^3} = 1,65578 \dots \Rightarrow$$

$$\Rightarrow \frac{1}{\sqrt[14]{\frac{2.29155 \times 10^{37} \times 2.62561 \times 10^{40}}{6.8938278721 \times 10^{80}}}}$$

$$= 1,653892\dots$$

Continued fraction:

Linear form

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{8 + \frac{1}{31 + \frac{1}{1 + \frac{1}{142 + \frac{1}{2 + \frac{1}{2 + \frac{1}{1 + \frac{1}{22 + \frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{10 + \frac{1}{3 + \frac{1}{44 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

Open code

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Possible closed forms:

- More $\frac{4854 136 156 \pi}{9 220 503 157} \approx 1.653892225570895550574111$
- $\frac{1}{77} (-7 C - 2 - 621 \pi + 99 \pi^2 + 294 \pi \log(2) + 136 \pi \log(3)) \approx$
 $1.653892225570895550599129$
- $e^{19/2-3/e+16 e-19/(2 \pi)+7 \pi} \pi^{-5/2-19 e} \cos^{17}(e \pi) \cot^3(e \pi) \approx 1.65389222557089555088074$

$$1 + ((((((((((2.29155 * 10^{37} * 2.62561 * 10^{40}))) / (((6.8938278721 * 10^{80}))))))))))^{1/16}$$

Input interpretation:

$$1 + \sqrt[16]{\frac{2.29155 \times 10^{37} \times 2.62561 \times 10^{40}}{6.8938278721 \times 10^{80}}}$$

Open code

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Result:

- Fewer digits
- More digits
- $1.643881867488984117775060251756886610116821865101659670144...$
- $1.6438818674889841177750602517568866101168218651016596$

Now, from the square root of Q and some calculations, we obtain:

$$(((((((sqrt((((((13.12806 * 10^{39})^2 - (0.9/13.12806 * 10^{39})^2 - (2.62561 * 10^{40} - 13.12806 * 10^{39})^2))))))))))))^{1/(27*4+24*3)}$$

Input interpretation:

Input interpretation:

$$\frac{2.62561 \times 10^{40}}{4 \times 6.8938278721 \times 10^{80}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- More digits

$$9.5215968860569543839336382783429374507257361146552610... \times 10^{-42}$$

[Open code](#)

And, after some calculations, the following interesting result:

$$1/2 * (((((2.62561*10^40)/(4*6.8938278721*10^80))))^-0.5$$

Input interpretation:

$$\frac{\frac{1}{2}}{\left(\frac{2.62561 \times 10^{40}}{4 \times 6.8938278721 \times 10^{80}}\right)^{0.5}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- Fewer digits
- More digits

$$1.6203734137537557117495892679784638305318710060786596... \times 10^{20}$$

$$1.62037341375375571174958926797846383053187100607 \times 10^{20}$$

And:

$$(((((((1/((((((2.62561*10^40)/(4*6.8938278721*10^80))))))))))))))^{1/(24*8)}$$

Input interpretation:

$$\sqrt[24 \times 8]{\frac{1}{\frac{2.62561 \times 10^{40}}{4 \times 6.8938278721 \times 10^{80}}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- Fewer digits
- More digits

$$1.635507549516017707975691842575833324846746655353471172542...$$

$$1.6355075495160177079756918425758333248467466553534711$$

Continued fraction:

- Linear form

We require here only the metric in the Einstein frame; the other fields in the solution may be found in [12]. The extremal limit is $r_0 \rightarrow 0$, $\sigma_i \rightarrow \infty$ with r_i fixed; we shall be interested in the sections of the moduli space where the BPS state is the extreme Reissner-Nordstrom solution, where the limiting values of r_i are equal to r_e , the Schwarzschild radius.

We require here only the metric in the Einstein frame; the other fields in the solution may be found in [12]. The extremal limit is $r_0 \rightarrow 0$, $\sigma_i \rightarrow \infty$ with r_i fixed; we shall be interested in the sections of the moduli space where the BPS state is the extreme Reissner-Nordstrom solution, where the limiting values of r_i are equal to r_e , the Schwarzschild radius.

We may regard the black hole as the compactification of a six-dimensional black string carrying momentum about the circle direction; we will be using this six-dimensional solution in the following sections, and the metric (in the Einstein frame) is given by:

$$ds^2 = \left(1 + \frac{r_1^2}{r^2}\right)^{-1/2} \left(1 + \frac{r_5^2}{r^2}\right)^{-1/2} [-dt^2 + dx_5^2 + \frac{r_0^2}{r^2} (\cosh \sigma_K dt + \sinh \sigma_K dx_5)^2] \\ + \left(1 + \frac{r_1^2}{r^2}\right)^{1/2} \left(1 + \frac{r_5^2}{r^2}\right)^{1/2} \left[\left(1 - \frac{r_0^2}{r^2}\right)^{-1} dr^2 + r^2 d\Omega_3^2 \right]. \quad (7)$$

We assume that we are in the very near extremal region where $r_0 \ll r_e$, and moreover will consider all three hyperbolic angles to be finite. It is here that our analysis differs from previous work; with this choice of parameters, we move away from the dilute gas region and a straightforward D-brane analysis of emission rates is not possible.

The entropy is:

$$S = \frac{A_h}{4G_5} = \frac{2\pi^2 r_0^3 \prod_i \cosh \sigma_i}{4G_5} \quad (8)$$

where we have taken $l = 0$ since we will be interested in very low energy scalars. We assume the low energy condition:

$$\omega r_e \ll 1, \quad (18)$$

Since the Hawking temperature T_H is much smaller than $1/r_e$ in the near extremal limit, $a \gg b$ and the low energy condition (18) implies that $b \ll 1$. From (29) we find:

$$\sigma_{abs}^S = \frac{1}{2} \pi \omega^3 r_1 r_3 r_K = \frac{1}{4\pi} A_h \omega^3. \quad (33)$$

where $\phi_K = \tanh \sigma_K$ is the Kaluza-Klein electrostatic potential on the horizon. Let us take the low energy limit, assuming that the emitted particles are non-relativistic, with kinetic energy δ ; the near extremality condition implies that $\phi_K = 1 - \mu_K$ with $\mu_K \ll 1$. Under these conditions,

$$r'_K = r_K \frac{|\delta - m\mu_K|}{\sqrt{2m\delta}}. \quad (41)$$

The other region of interest is when the kinetic energy is very small, that is, $\delta \leq m\mu_K^2$; we then find that r'_K is of the same order or greater than the Schwarzschild radius. Since the thermal factor in the emission rate is large at small kinetic energies, it is important to consider carefully the behaviour of the absorption probability in this limit. Note that in this region the enforcement of the low energy condition requires that

$$mr_e \ll \frac{1}{\mu_K}. \quad (42)$$

This is the general expression for the absorption probability, and applies even when the mass is of the order of $1/r_e$, provided that the kinetic energy is greater than $m\mu_K^2$. It is interesting to consider the limiting expression when the kinetic energy is much smaller than the temperature. Now, the Hawking temperature is

$$T_H = \frac{\mu}{\pi r_e}, \quad (48)$$

Since the charged particles are emitted non-relativistically, emission of light charged particles dominates the emission of neutral scalars at very small energy. Since the density of states factor in (55) peaks for small kinetic energy, this indicates that the total rate of emission of light charged particles dominates that of neutrals. When we integrate the differential emission rate for neutrals, we find that the total rate of emission is

$$\Gamma_{neut}^{tot} = \frac{\pi^2}{120} A_h T_H^4. \quad (60)$$

The total emission rate of light charged particles is approximated by

$$carefully \Gamma_{char}^{tot} = \frac{\zeta(3)}{2\pi^2} A_h m T_H^3, \quad (61)$$

and we find that most of the particles are emitted with kinetic energies of the order of $m\mu_K$. So comparing the total neutral and charged emission rates we find that

$$\frac{\Gamma_{char}^{tot}}{\Gamma_{neut}^{tot}} = \frac{60\zeta(3)}{\pi^4} \left(\frac{m}{T_H} \right). \quad (62)$$

We remember that:

$$G_5 = \pi / (2N^2).$$

From Wikipedia:

The **Schwarzschild radius** (sometimes historically referred to as the **gravitational radius**) is a physical parameter that shows up in the Schwarzschild solution to [Einstein's field equations](#), corresponding to the [radius](#) defining the [event horizon](#) of a Schwarzschild [black hole](#). It is a characteristic radius associated with every quantity of mass. The *Schwarzschild radius* was named after the [German](#) astronomer [Karl Schwarzschild](#), who calculated this exact solution for the theory of [general relativity](#) in 1916.

The Schwarzschild radius is given as

$$r_s = \frac{2GM}{c^2}$$

where G is the [gravitational constant](#), M is the object mass, and c is the [speed of light](#).

Object	Mass: M	Schwarzschild radius:	Schwarzschild density:
SMBH in Messier 87 ^[9]	1.3×10^{40} kg	1.9×10^{13} m	0.44 kg/m ³

1.6147350085943156705592910519697862580037293692275889 *10

This result is a multiple that is a good approximation to the value of the golden ratio
1,618033988749

That is:

Result:

16.147350085943156705592910519697862580037293692275889

From the following formula of the Schwarzschild radius, we obtain a very good approximation to π :

$$\frac{1}{3} * ((((((((((2*6.67*10^{-11}*13.12806*10^{39})/(9*10^{16}))))))^{1/24} + ((((((((((2*6.67*10^{-11}*13.12806*10^{39})/(9*10^{16}))))))^{1/26} + ((((((((((2*6.67*10^{-11}*13.12806*10^{39})/(9*10^{16}))))))^{1/32}))))))$$

Input interpretation:

$$\frac{1}{3} \left(\sqrt[24]{\frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} + \sqrt[26]{\frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} + \sqrt[32]{\frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} \right)$$

[Open code](#)

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Result:

- Fewer digits
- More digits

3.141585120422757363404336968339718350902753479335502585667...

And to the value of a circle length with radius equal to 1:

$$\frac{2}{3} * ((((((((((2*6.67*10^{-11}*13.12806*10^{39})/(9*10^{16}))))))^{1/24} + ((((((((((2*6.67*10^{-11}*13.12806*10^{39})/(9*10^{16}))))))^{1/26} + ((((((((((2*6.67*10^{-11}*13.12806*10^{39})/(9*10^{16}))))))^{1/32}))))))$$

Input interpretation:

$$\frac{2}{3} \left(\sqrt[24]{\frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} + \sqrt[26]{\frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} + \sqrt[32]{\frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} \right)$$

[Open code](#)

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Result:

More digits

1.65730098498572735175727093310907637885...
1.65730098498572735175727093310907637885

And:

$$\left(\frac{4.758144315808687592468787929539135845 \times 10^{27}}{4 \times \frac{\pi}{32}}\right)^{0.0072973525693}$$

Where 0,007297... is the fine-structure constant

Input interpretation:

$$\left(\frac{4.758144315808687592468787929539135845 \times 10^{27}}{4 \times \frac{\pi}{32}}\right)^{0.0072973525693}$$

[Open code](#)

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Result:

Fewer digits

More digits

1.603002902042071380264289790644565624702203240615903355676...

In conclusion, from $1/134,3775$ as exponent, where the denominator is a very good approximation to the rest mass of the π^0 : $134.9766(6) \text{ MeV}/c^2$

$$\left(\frac{4.758144315808687592468787929539135845 \times 10^{27}}{4 \times \frac{\pi}{32}}\right)^{1/134.3775}$$

Input interpretation:

$$134.3775 \sqrt[134.3775]{\frac{4.758144315808687592468787929539135845 \times 10^{27}}{4 \times \frac{\pi}{32}}}$$

[Open code](#)

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Result:

Fewer digits

More digits

1.618037900709754242930845681631117438589626606961615449665...
1.6180379007097542429308456816311174385896266069616154

Continued fraction:

Linear form

$$\frac{1}{2} \left(134.977 \sqrt{\frac{4.7581443158086875920000 \times 10^{27}}{\frac{4\pi}{32}}} + 139.57 \sqrt{\frac{4.7581443158086875920000 \times 10^{27}}{\frac{4\pi}{32}}} \right) = 0.793289 \left(\left(\frac{1}{\int_0^1 \sqrt{1-t^2} dt} \right)^{0.00716485} + 1.01583 \left(\frac{1}{\int_0^1 \sqrt{1-t^2} dt} \right)^{0.00740869} \right)$$

This result 1,601956 is very near to the value of electric charge of positron.

From eq. (61), we obtain total emission rate of light charged particles:

Note that:

the low energy condition implies that $m \ll 1/r_e \mu_K$.

Thence $m = 0.0416666.../ r_e \mu_K$ where $0.0416666... = 1/24$

$$\zeta(3) / (2\pi^2) 4\pi (1.945870226666 \times 10^{13})^2 * (((0.041666/(((1.945870226666 \times 10^{13}*(1/12)))))) * (((((1.36319 \times 10^{-15})^3))))]$$

Input interpretation:

$$\frac{\zeta(3)}{2\pi^2} \times 4\pi (1.945870226666 \times 10^{13})^2 \left(\frac{0.041666}{1.945870226666 \times 10^{13} \times \frac{1}{12}} (1.36319 \times 10^{-15})^3 \right)$$

[Open code](#)

- $\zeta(s)$ is the Riemann zeta function

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Result:

More digits

$$1.88604... \times 10^{-32}$$

And we obtain a golden number, after some calculations. Indeed:

$$\sqrt{55+21} * \zeta(3) / (2\pi^2) 4\pi (1.945870226666 \times 10^{13})^2 * (((0.041666/(((1.945870226666 \times 10^{13}*(1/12)))))) * (((((1.36319 \times 10^{-15})^3))))]$$

Input interpretation:

Where 2.02 is a Hausdorff dimension

Input interpretation:

$$2.02 \sqrt{55 + 13} \times \frac{\zeta(3)}{2\pi^2} \left(4\pi (1.945870226666 \times 10^{13})^2 \left(\frac{0.041666}{1.945870226666 \times 10^{13} \times \frac{1}{12}} (1.36319 \times 10^{-15})^3 \right) \right)$$

[Open code](#)

- $\zeta(s)$ is the Riemann zeta function

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Result:

- Fewer digits
- More digits

$$3.1416447826127819571929552797586422793218400287631010... \times 10^{-31}$$

$$3.1416447826127819571929552797586422793218400287 \times 10^{-31}$$

Or:

$$\tan(\pi^3/27) * \text{sqrt}(24+32) * \text{zeta}(3) / (2*\text{Pi}^2) 4\text{Pi}*(1.945870226666 \times 10^{13})^2 * (((0.041666/(((1.945870226666 \times 10^{13}*(1/12)))))) * [(((1.36319 \times 10^{-15})^3))])$$

Input interpretation:

$$\tan\left(\frac{\pi^3}{27}\right) \sqrt{24 + 32} \times \frac{\zeta(3)}{2\pi^2} \left(4\pi (1.945870226666 \times 10^{13})^2 \left(\frac{0.041666}{1.945870226666 \times 10^{13} \times \frac{1}{12}} (1.36319 \times 10^{-15})^3 \right) \right)$$

[Open code](#)

- $\zeta(s)$ is the Riemann zeta function

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Result:

- Fewer digits
- More digits

$$3.1400858023149057147399878920763356266065256769221713... \times 10^{-31}$$

$$3.1400858023149057147399878920763356266065256769 \times 10^{-31}$$

$$2 * \tan(\pi^3/27) * \text{sqrt}(24+32) * \text{zeta}(3) / (2*\text{Pi}^2) 4\text{Pi}*(1.945870226666 \times 10^{13})^2 * (((0.041666/(((1.945870226666 \times 10^{13}*(1/12)))))) * [(((1.36319 \times 10^{-15})^3))])$$

Input interpretation:

$$2 \tan\left(\frac{\pi^3}{27}\right) \sqrt{24 + 32} \times \frac{\zeta(3)}{2\pi^2} \left(4\pi (1.945870226666 \times 10^{13})^2 \left(\frac{0.041666}{1.945870226666 \times 10^{13} \times \frac{1}{12}} (1.36319 \times 10^{-15})^3 \right) \right)$$

[Open code](#)

- $\zeta(s)$ is the Riemann zeta function

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Result:

- Fewer digits
- More digits

$$6.2801716046298114294799757841526712532130513538443426... \times 10^{-31}$$

$$6.2801716046298114294799757841526712532130513538 \times 10^{-31}$$

Results that are very good approximations to the sub-multiple of π and of the length of a circle with radius equal to 1: 2π

From the ratio of (61) and (60), we obtain:

$$\frac{(((1.8860415371116967863093997773516420550064110429 \times 10^{-32})))}{((((((\pi^2/120) * 4\pi * (1.94587022666666 \times 10^{13})^2 * (1.36319 * 10^{-15})^4))))))}$$

Input interpretation:

$$\frac{1.8860415371116967863093997773516420550064110429 \times 10^{-32}}{\frac{\pi^2}{120} \times 4 (\pi (1.94587022666666 \times 10^{13})^2 (1.36319 \times 10^{-15})^4)}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

- More digits

13.9563...

Note that:

$$\frac{10 * (((1.8860415371116967863093997773516420550064110429 \times 10^{-32})))}{((((((\pi^2/120) * 4\pi * (1.94587022666666 \times 10^{13})^2 * (1.36319 * 10^{-15})^4))))))}$$

Input interpretation:

$$10 \times \frac{1.8860415371116967863093997773516420550064110429 \times 10^{-32}}{\frac{\pi^2}{120} \times 4 (\pi (1.94587022666666 \times 10^{13})^2 (1.36319 \times 10^{-15})^4)}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

- More digits

139.563...

139.563...

This result is practically equal to the rest mass of Pion meson 139.57018 ± 0.00035

Moreover, we obtain:

$$\frac{1/2 * (((((((((39/(8\pi)) + (((((((((1.8860415371116967863093997773516420550064110429 \times 10^{-32})))))))))$$

Input interpretation:

$$\frac{3}{5} \left(\sqrt{\frac{27}{4}}^2 \sqrt[6]{\frac{1.8860415371116967863093997773516420550064110429 \times 10^{-32}}{\frac{\pi^2}{120} \times 4 (\pi (1.94587022666666 \times 10^{13})^2 (1.36319 \times 10^{-15})^4)}} \right)$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

Fewer digits

• More digits

6.284199340190524546780078239784160129347220426240225525258...

6.2841993401905245467800782397841601293472204262402255

Results that are very good approximations to the values of the golden ratio, of π and of the length of a circle with radius equal to 1: 2π

In conclusion, we obtain the following result:

$$(288+21*2) + 10^2 * (((1.8860415371116967863093997773516420550064110429 \times 10^{-32}))) / (((((\pi^2/120) * 4\pi * (1.94587022666666 \times 10^{13})^2 * (1.36319 * 10^{-15})^4))))))$$

Input interpretation:

$$(288 + 21 \times 2) + 10^2 \times \frac{1.8860415371116967863093997773516420550064110429 \times 10^{-32}}{\frac{\pi^2}{120} \times 4 (\pi (1.94587022666666 \times 10^{13})^2 (1.36319 \times 10^{-15})^4)}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

• More digits

1725.63...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729.

$$(((((((288+21*2) + 10^2 * (((1.8860415371116967863 \times 10^{-32}))) / (((((\pi^2/120) * 4\pi * (1.94587022666666 \times 10^{13})^2 * (1.36319 * 10^{-15})^4)))))))))))))^{1/3}$$

Input interpretation:

$$\sqrt[3]{(288 + 21 \times 2) + 10^2 \times \frac{1.8860415371116967863 \times 10^{-32}}{\frac{\pi^2}{120} \times 4 (\pi (1.94587022666666 \times 10^{13})^2 (1.36319 \times 10^{-15})^4)}}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

11.9945...

This result is very near to the value of black hole entropy 12,1904

$$2 * (((((((((288 + 21 * 2) + 10^2 * (((1.8860415371116967863 \times 10^{-32}))) / (((((\text{Pi}^2 / 120) * 4\text{Pi} * (1.94587022666666 \times 10^{13})^2 * (1.36319 * 10^{-15})^4)))))))))))))^{1/3}$$

Input interpretation:

$$2 \sqrt[3]{(288 + 21 \times 2) + 10^2 \times \frac{1.8860415371116967863 \times 10^{-32}}{\frac{\pi^2}{120} \times 4 (\pi (1.94587022666666 \times 10^{13})^2 (1.36319 \times 10^{-15})^4)}}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

23.9890...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

$$((((((((((288 + 21 * 2) + 10^2 * (((1.8860415371116967863 \times 10^{-32}))) / (((((\text{Pi}^2 / 120) * 4\text{Pi} * (1.94587022666666 \times 10^{13})^2 * (1.36319 * 10^{-15})^4)))))))))))))^{1/15}$$

Input interpretation:

$$15 \sqrt{(288 + 21 \times 2) + 10^2 \times \frac{1.8860415371116967863 \times 10^{-32}}{\frac{\pi^2}{120} \times 4 (\pi (1.94587022666666 \times 10^{13})^2 (1.36319 \times 10^{-15})^4)}}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

Fewer digits

More digits

1.643601289781022355362256847780804625738372542906323612454...

1.6436012897810223553622568477808046257383725429063236

Continued fraction:

Linear form

- More digits
1725.951671855066898473334878492988308841298971245363894821...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

And from the result 1725.95167185506689847333487849298..., we obtain:

$$(1725.9516718550668984733348784929883088412989712453638)^{1/3}$$

Input interpretation:

$$\sqrt[3]{1725.9516718550668984733348784929883088412989712453638}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

- More digits
11.995256624944309932306432942141887620743658571921392...

This result is very near to the value of black hole entropy 12,1904

$$2 * (1725.9516718550668984733348784929883088412989712453638)^{1/3}$$

Input interpretation:

$$2 \sqrt[3]{1725.9516718550668984733348784929883088412989712453638}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

- More digits
23.990513249888619864612865884283775241487317143842784...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

$$(1725.9516718550668984733348784929883088412989712453638)^{1/15}$$

Input interpretation:

$$\sqrt[15]{1725.9516718550668984733348784929883088412989712453638}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

- More digits

1.64362186010871455873490720337034033149194459420173908...

1.64362186010871455873490720337034033149194459420173908

Now:

and so we find the ratio of energy loss rates to be using (48)

$$\frac{\frac{d\Delta E}{dt} \text{ char}}{\frac{d\Delta E}{dt} \text{ neut}} \approx \frac{\pi^6}{180\zeta(5)} \frac{n}{\mu} e^{-\pi\sqrt{n}}. \tag{77}$$

It is not difficult to extend the analysis of the section above to show that, under the conditions $R^2 \gg g$ and $n_i = n$, for emission of the other two types of charges, the energy loss rates compare as

$$\frac{\frac{d\Delta E}{dt} \text{ i}}{\frac{d\Delta E}{dt} \text{ neut}} \approx \frac{\pi^6}{180\zeta(5)} \frac{n}{\mu_i} e^{-\pi\sqrt{n}}, \tag{80}$$

where we assume that the μ_i are very small, but non-zero. There are two important points

We have that $\mu = 1/12$ and $n = 576$, thence we obtain, for (77) and (80), the following result:

$$\left(\frac{\pi^6}{180 \zeta(5)}\right) * \left(\frac{576}{(1/12)}\right) * \left(\exp(-\pi * \sqrt{576})\right)$$

Input:

$$\frac{\pi^6}{180 \zeta(5)} \times \frac{576}{\frac{1}{12}} \exp\left(-\pi \sqrt{576}\right)$$

[Open code](#)

- $\zeta(s)$ is the Riemann zeta function

Enlarge Data Customize A Plaintext Interactive

Exact result:

$$\frac{192 e^{-24\pi} \pi^6}{5 \zeta(5)}$$

Decimal approximation:

- More digits

6.4039726586841887297127010770185813039177508985143948... $\times 10^{-29}$

[Open code](#)

Series representations:

- More

$$\frac{\left(576 \exp\left(-\pi \sqrt{576}\right)\right) \pi^6}{\frac{180 \zeta(5)}{12}} = \frac{192 e^{-24 \pi} \pi^6}{5 \sum_{k=1}^{\infty} \frac{1}{k^5}}$$

Open code

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

$$\frac{\left(576 \exp\left(-\pi \sqrt{576}\right)\right) \pi^6}{\frac{180 \zeta(5)}{12}} = \frac{186 e^{-24 \pi} \pi^6}{5 \sum_{k=0}^{\infty} \frac{1}{(1+2k)^5}}$$

Open code

$$\frac{\left(576 \exp\left(-\pi \sqrt{576}\right)\right) \pi^6}{\frac{180 \zeta(5)}{12}} = \frac{192}{5} e^{-24 \pi - \sum_{k=1}^{\infty} P(5k)/k} \pi^6$$

Open code

- $P(z)$ gives the prime zeta function

Integral representations:

More

$$\frac{\left(576 \exp\left(-\pi \sqrt{576}\right)\right) \pi^6}{\frac{180 \zeta(5)}{12}} = - \frac{1152 e^{-24 \pi} \pi^6}{\int_0^1 \frac{\log^5(1-t^4)}{t^5} dt}$$

Open code

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

$$\frac{\left(576 \exp\left(-\pi \sqrt{576}\right)\right) \pi^6}{\frac{180 \zeta(5)}{12}} = \frac{864 e^{-24 \pi} \pi^6}{\int_0^{\infty} \frac{t^4}{1+t^5} dt}$$

Open code

$$\frac{\left(576 \exp\left(-\pi \sqrt{576}\right)\right) \pi^6}{\frac{180 \zeta(5)}{12}} = \frac{8928 e^{-24 \pi} \pi^6}{5 \int_0^{\infty} t^4 \operatorname{csch}(t) dt}$$

Open code

- $\log(x)$ is the natural logarithm
- $\operatorname{csch}(x)$ is the hyperbolic cosecant function

Note that, we obtain:

$$(7\pi)/(87) * ((((((\pi^6) / (180 * \zeta(5)) * ((576 / (1/12)))) * ((\exp(-\pi * \sqrt{576})))))))))$$

Input:

$$\frac{7\pi}{87} \left(\frac{\pi^6}{180 \zeta(5)} \times \frac{576}{12} \exp(-\pi \sqrt{576}) \right)$$

[Open code](#)

- $\zeta(s)$ is the Riemann zeta function

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Exact result:

$$\frac{448 e^{-24\pi} \pi^7}{145 \zeta(5)}$$

Decimal approximation:

More digits

$$1.6187438414733908751431813333704766005093323784227589... \times 10^{-29}$$

[Open code](#)

Series representations:

More

$$\frac{(\pi^6 576 \exp(-\pi \sqrt{576})) (7\pi)}{\frac{1}{12} (180 \zeta(5)) 87} = \frac{448 e^{-24\pi} \pi^7}{145 \sum_{k=1}^{\infty} \frac{1}{k^5}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

$$\frac{(\pi^6 576 \exp(-\pi \sqrt{576})) (7\pi)}{\frac{1}{12} (180 \zeta(5)) 87} = \frac{434 e^{-24\pi} \pi^7}{145 \sum_{k=0}^{\infty} \frac{1}{(1+2k)^5}}$$

[Open code](#)

$$\frac{(\pi^6 576 \exp(-\pi \sqrt{576})) (7\pi)}{\frac{1}{12} (180 \zeta(5)) 87} = \frac{448}{145} e^{-24\pi - \sum_{k=1}^{\infty} P(5k)/k} \pi^7$$

[Open code](#)

- $P(z)$ gives the prime zeta function

Integral representations:

More

$$\frac{(\pi^6 576 \exp(-\pi \sqrt{576})) (7\pi)}{\frac{1}{12} (180 \zeta(5)) 87} = \frac{20832 e^{-24\pi} \pi^7}{145 \int_0^{\infty} t^4 \operatorname{csch}(t) dt}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

$$\frac{\left(\pi^6 576 \exp\left(-\pi \sqrt{576}\right)\right) (7 \pi)}{\frac{1}{12} (180 \zeta(5)) 87} = \frac{672 e^{-24 \pi} \pi^7}{29 \int_0^\infty t^5 \operatorname{csch}^2(t) dt}$$

Open code

$$\frac{\left(\pi^6 576 \exp\left(-\pi \sqrt{576}\right)\right) (7 \pi)}{\frac{1}{12} (180 \zeta(5)) 87} = \frac{630 e^{-24 \pi} \pi^7}{29 \int_0^\infty t^5 \operatorname{sech}^2(t) dt}$$

Open code

- $\operatorname{csch}(x)$ is the hyperbolic cosecant function
- $\operatorname{sech}(x)$ is the hyperbolic secant function
-

The result $1.6187438414733908751431813333704766005093323784227589 \times 10^{-29}$ is a very good approximation to the value of golden ratio 1,61803398...

From:

If $n_K \gg n_1 n_5$ we must allow for emission of particles of greater than the minimum BPS mass. For a Reissner-Nordstrom solution, the mass of Kaluza-Klein charged particles is quantised as

$$m = \frac{c}{r_e} \sqrt{\frac{n_1 n_5}{n_K}}, \quad (83)$$

where c is an integer; the mass is small on the scale of the Schwarzschild radius, and charged emission will dominate neutral emission. We calculate the rate of energy emission for a particle of general mass m , using (54) and (74) as,

$$\frac{d\Delta E}{dt}_{char} \approx \frac{\pi^3}{60} A_h T_H^4 \frac{m^2 r_e}{(e^{\pi m r_e} - 1)}, \quad (84)$$

and integrate over all masses to find that

$$\frac{d\Delta E}{dt}_{KK} \approx \frac{\zeta(3)}{30} A_h T_H^4 \frac{1}{r_e} \sqrt{\frac{n_K}{n_1 n_5}}. \quad (85)$$

For $n_1 n_5 = 8$, $c = 3$ and $n_K = 128$, from the eq. (83), we obtain:

$$\left(\left(\left(3 / (1.945870226666 \times 10^{13})\right)\right)\right) * (\operatorname{sqrt}(8/128))$$

Input interpretation:

$$\frac{3}{1.945870226666 \times 10^{13}} \sqrt{\frac{8}{128}}$$

$$\frac{2}{\sqrt[27]{\frac{3}{1.945870226666 \times 10^{13}} \sqrt{\frac{8}{128}}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- Fewer digits
- More digits

6.278367872158852846912881740638213242856032886328749075213...

6.2783678721588528469128817406382132428560328863287490

Results that are very near to the values of π and of the length of a circle of radius equal to 1: 2π

From eq. (84), we obtain:

$$\left(\frac{\pi^3}{60}\right) * (4.7581443158086875924 * 10^{27}) * \left(\frac{1}{12} * \frac{1}{\left(\frac{\pi * (2 * 6.67 * 10^{-11} * 13.12806 * 10^{39})}{9 * 10^{16}}\right)}\right)^4$$

Input interpretation:

$$\frac{\pi^3}{60} (4.7581443158086875924 \times 10^{27}) \left(\frac{1}{12} \times \frac{1}{\pi \times \frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} \right)^4$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- More digits

$8.49094... \times 10^{-33}$

$$\frac{\left(\left(\left(3.854316643124907506385 \times 10^{-14}\right)^2 * (1.945870226666 \times 10^{13})\right)\right)}{\left(\left(\exp\left(\left(\pi * 3.854316643124907506385 \times 10^{-14} * 1.945870226666 \times 10^{13}\right)\right) - 1\right)\right)}$$

Input interpretation:

$$\frac{\left(3.854316643124907506385 \times 10^{-14}\right)^2 \times 1.945870226666 \times 10^{13}}{\exp\left(\pi \times 3.854316643124907506385 \times 10^{-14} \times 1.945870226666 \times 10^{13}\right) - 1}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- More digits

$3.02672075948... \times 10^{-15}$

The final result is:

$$(\pi^3/60) * (4.7581443158086875924 * 10^{27}) * (((((((((1/12 * 1/((\pi*(2*6.67*10^{-11}*13.12806*10^{39})/(9*10^{16})))))))))))))^4 * ((3.0267207594796896211468181363271747269049649317 * 10^{-15}))$$

Input interpretation:

$$\frac{\pi^3}{60} (4.7581443158086875924 \times 10^{27}) \left(\frac{1}{12} \times \frac{1}{\pi \times \frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} \right)^4 \times 3.0267207594796896211468181363271747269049649317 \times 10^{-15}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

$$2.56997... \times 10^{-47}$$

$$1/ (2.5699718484414413879084168551853846277523893240 \times 10^{-47})^{1/223}$$

Input interpretation:

$$\frac{1}{\sqrt[223]{2.5699718484414413879084168551853846277523893240 \times 10^{-47}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

$$1.617797232103301159000614387871237651834082097712... \\ 1.617797232103301159000614387871237651834082097712$$

This result is a very good approximation to the value of the golden ratio 1,618033988749...

[Continued fraction:](#)

Linear form

$$\frac{1}{1.945870226666 \times 10^{13}} \sqrt{\frac{128}{8}}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

$$2.0556355429999506700720918753252904806167461960586301... \times 10^{-13}$$

[Open code](#)

The final result is:

$$(\zeta(3)/30) * (4.7581443158086875924 * 10^{27}) * (((((((((1/12 * 1/((\pi*(2*6.67*10^{-11}*13.12806*10^{39})/(9*10^{16}))))))))))^{4} * ((2.0556355429999506700720918753252904806167461960586301 \times 10^{-13})))$$

Input interpretation:

$$\frac{\zeta(3)}{30} (4.7581443158086875924 \times 10^{27}) \left(\frac{1}{12} \times \frac{1}{\pi \times \frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} \right)^4 \times 2.0556355429999506700720918753252904806167461960586301 \times 10^{-13}$$

[Open code](#)

- $\zeta(s)$ is the Riemann zeta function

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

$$1.35334... \times 10^{-46}$$

$$1/2 (((((1/ ((1.3533419166425984230015741260045868872261962557 \times 10^{-46}))^{1/220} + 1/ ((1.3533419166425984230015741260045868872261962557 \times 10^{-46}))^{1/219}))))))$$

Input interpretation:

$$\frac{1}{2} \left(\frac{1}{\sqrt[220]{1.3533419166425984230015741260045868872261962557 \times 10^{-46}}} + \frac{1}{\sqrt[219]{1.3533419166425984230015741260045868872261962557 \times 10^{-46}}} \right)$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

$$1.617967805714668735089583962613054814469912033398...$$

$$1.617967805714668735089583962613054814469912033398$$

$$\frac{4574027289 \pi}{8742717484} \approx 1.643622884388018283194453$$

Enlarge Data Customize A Plaintext Interactive

$$\frac{100 \sqrt[3]{\frac{83077600}{20243211}}}{\pi^4} \approx 1.64362288438801831013$$

$$\frac{322217\pi^2 - 2385090}{153975\pi} \approx 1.64362288438801828309598$$

$$\frac{3(-27 - 220\pi + 252\pi^2)}{657 + 627\pi + 61\pi^2} \approx 1.6436228843880182826264$$

$$\pi \left[\text{root of } 33497x^3 + 46721x^2 - 3250x - 15885 \text{ near } x = 0.523181 \right] \approx 1.6436228843880182831813991$$

$$\left[\text{root of } 195x^5 - 32x^4 - 296x^3 - 405x^2 + 208x - 39 \text{ near } x = 1.64362 \right] \approx 1.64362288438801828323556$$

$$\pi \left[\text{root of } 234x^5 - 15x^4 + 193x^3 + 480x^2 + 342x - 346 \text{ near } x = 0.523181 \right] \approx 1.643622884388018283166376$$

$$\left[\text{root of } 167x^4 - 5482x^3 + 3926x^2 + 7151x + 763 \text{ near } x = 1.64362 \right] \approx 1.643622884388018283193680$$

$$\left[\text{root of } 20428x^3 - 38193x^2 + 36568x - 47631 \text{ near } x = 1.64362 \right] \approx 1.6436228843880182831894207$$

$$\pi \left[\text{root of } 1676x^4 + 4308x^3 + 301x^2 - 3748x + 1136 \text{ near } x = 0.523181 \right] \approx 1.64362288438801828308652$$

$$\frac{1}{\left[\text{root of } 763x^4 + 7151x^3 + 3926x^2 - 5482x + 167 \text{ near } x = 0.608412 \right]} \approx 1.643622884388018283193680$$

Now, from:

where we will assume only particles of minimum BPS mass are emitted. Now the energy loss rate by neutral emission is

$$\frac{d\Delta E}{dt}_{neut} \approx \frac{3\zeta(5)}{\pi^2} A_h T_H^5. \tag{75}$$

We obtain:

$$(3 * \text{zeta}(5) / \text{Pi}^2) * (4.7581443158086875924 * 10^{27}) * (((((((((1/12 * 1/((\text{Pi}*(2*6.67*10^{-11}*13.12806*10^{39})/(9*10^{16}))))))))))))))^{5}$$

$$\left(\frac{\zeta(3)}{30} (4.7581443158 \times 10^{27}) \left(\left(\frac{1}{12} \times \frac{1}{\pi \times \frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}} \right) \times 2.0556355429 \times 10^{-13} \times \frac{1}{7.059641699 \times 10^{-48}} \right) \right)^{1/6}$$

[Open code](#)

- $\zeta(s)$ is the Riemann zeta function

Enlarge Data Customize A Plaintext Interactive

Result:

- Fewer digits
- More digits

1.635952961520542934727971866777729026762633346355984865890...
 1.6359529615205429347279718667777290267626333463559848

Continued fraction:

- Linear form

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{19 + \frac{1}{2 + \frac{1}{1 + \frac{1}{12 + \frac{1}{52 + \frac{1}{2 + \frac{1}{3 + \frac{1}{4 + \frac{1}{2 + \frac{1}{1 + \frac{1}{1 + \frac{1}{6 + \frac{1}{2 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

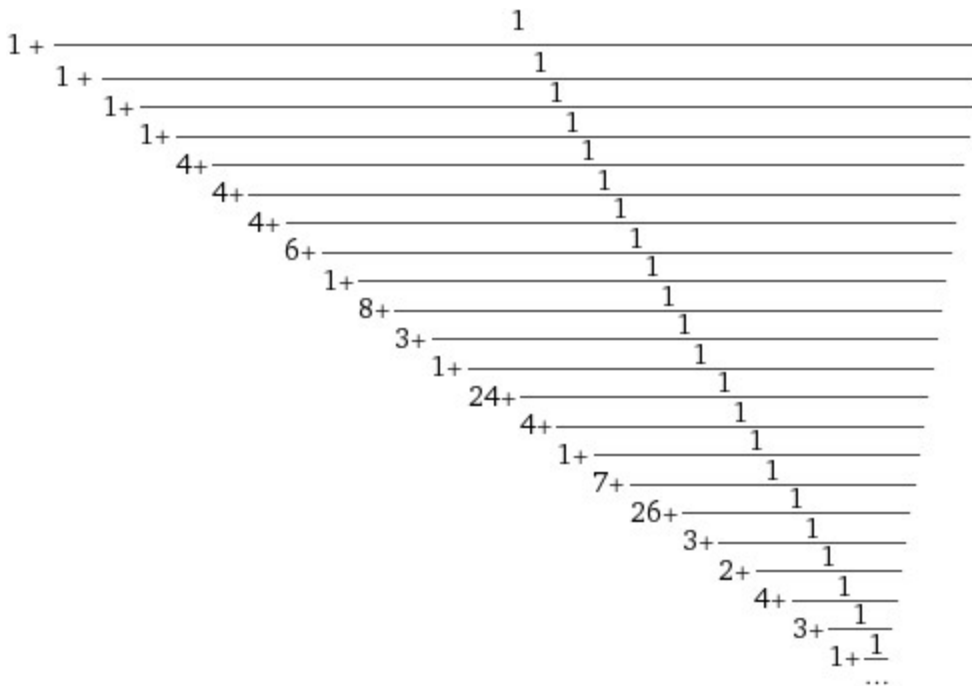
[Open code](#)

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Possible closed forms:

- More
 - $e^{5+2/e+13e+25/\pi+30\pi} \pi^{-11-44e} \tan^{13}(e\pi) \sec^9(e\pi) \approx 1.6359529615205429312162$
 - $\frac{510\,078\,227\,\pi}{979\,525\,725} \approx 1.63595296152054293456316$
 - $\frac{6}{11} \pi \sin^2\left(\frac{3\,622\,963}{2\,671\,223}\right) \approx 1.6359529615205429354459$

Moreover:



[Open code](#)

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Possible closed forms:

More

- $\cot\left(\cot\left(\frac{41994802}{13862273}\right)\right) \approx 1.644002244693740636766$
- $\frac{5\sqrt{\frac{2538955}{2379526}}}{\pi} \approx 1.64400224469374053659$
- root of $894x^3 + 8963x^2 - 75551x + 96009$ near $x = 1.644$ \approx
1.644002244693740601236981

Hawking said, (see eq.83-84-85):

...Thus we find that emission of KK charged scalars dominates neutral emission, independently of the moduli, for any near extremal state with n_K very large. Thus we find that, although the absolute rates of energy emission by the black hole are moduli dependent, the relative rates of neutral and charged emission depend only on the integral charges and horizon potentials.

Mathematical connections between the Ramanujan Mock Theta Functions and the result of Cardy formula:

$$1.0828815996251415942796175621426552475613218358896948 * 10^{81}$$

We remember that:

For $q = -e^{-t}$, $t = 0.5$ $q^n = -21.79216 * -e^{-0.5}$, we obtain:

$$\begin{aligned}\phi(q) &= 1 + \frac{q}{1+q^2} + \frac{q^4}{(1+q^2)(1+q^4)} + \dots \\ \psi(q) &= \frac{q}{1-q} + \frac{q^4}{(1-q)(1-q^3)} + \frac{q^9}{(1-q)(1-q^3)(1-q^5)} + \dots \\ \chi(q) &= 1 + \frac{q}{1-q+q^2} + \frac{q^4}{(1-q+q^2)(1-q^2+q^4)} + \dots\end{aligned}$$

Where

$$\psi(q) = -1.08185 + 1.08232 - 1.08232 = -1.08185 \text{ or:}$$

$$\psi(q) = 1.08185 - 1.08232 + 1.08232 = 1.08185$$

Indeed:

$$((-e^{-(0.5)}*(-21.79216))/((1-(((-e^{-(0.5)}*(-21.79216))))))$$

Input interpretation:

$$\frac{e^{-0.5} \times (-21.79216)}{1 - \frac{-21.79216}{e^{0.5}}}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

• -1.08185...

Alternative representation:

$$-\frac{e^{-0.5}(-21.7922)}{1 - \frac{-21.7922}{e^{0.5}}} = -\frac{\exp^{-0.5}(z)(-21.7922)}{1 - \frac{-21.7922}{\exp^{0.5}(z)}} \text{ for } z = 1$$

[Open code](#)

[More information](#)

Series representations:

More

$$-\frac{e^{-0.5}(-21.7922)}{1 - \frac{-21.7922}{e^{0.5}}} = \frac{21.7922}{-21.7922 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.5}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

$$-\frac{e^{-0.5}(-21.7922)}{1 - \frac{-21.7922}{e^{0.5}}} = \frac{30.8188}{-30.8188 + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{0.5}}$$

[Open code](#)

$$-\frac{e^{-0.5}(-21.7922)}{1 - \frac{-21.7922}{e^{0.5}}} = \frac{21.7922}{-21.7922 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.5}}$$

$$\left(\left(-e^{-(0.5)}(-21.79216)\right)^4\right) / \left(\left(\left(\left(1 - \left(-e^{-(0.5)}(-21.79216)\right)\right)^1\right)\right)\left(\left(1 - \left(-e^{-(0.5)}(-21.79216)\right)\right)^3\right)\right)$$

Input interpretation:

$$\frac{\left(-e^{-0.5} \times (-21.79216)\right)^4}{\left(1 - \left(-\frac{21.79216}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{21.79216}{e^{0.5}}\right)^3\right)}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

1.08232...

Alternative representation:

$$\frac{\left(-e^{-0.5}(-1)21.7922\right)^4}{\left(1 - \left(-\frac{21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{21.7922}{e^{0.5}}\right)^3\right)} = \frac{\left(-\exp^{-0.5}(z)(-1)21.7922\right)^4}{\left(1 - \left(-\frac{21.7922}{\exp^{0.5}(z)}\right)^1\right)\left(1 - \left(-\frac{21.7922}{\exp^{0.5}(z)}\right)^3\right)} \text{ for } z = 1$$

[Open code](#)

Series representations:

More

$$\frac{(-e^{-0.5} (-1) 21.7922)^4}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)} = \frac{225\,528.}{\left(-21.7922 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.5}\right)\left(-10\,349.1 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{1.5}\right)}$$

Open code

Enlarge Data Customize A Plaintext Interactive

$$\frac{(-e^{-0.5} (-1) 21.7922)^4}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)} = \frac{902\,113.}{\left(-30.8188 + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{0.5}\right)\left(-29\,271.6 + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{1.5}\right)}$$

Open code

$$\frac{(-e^{-0.5} (-1) 21.7922)^4}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)} = \frac{225\,528.}{\left(-21.7922 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.5}\right)\left(-10\,349.1 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{1.5}\right)}$$

$$\left(\frac{((-e^{-(0.5)*(-21.79216)})^9)}{\left(\frac{(((((1-((-e^{-(0.5)*(-21.79216))}^1)))\left(\frac{((1-((-e^{-(0.5)*(-21.79216))}^3))}{((1-((-e^{-(0.5)*(-21.79216))}^5))))\right)}\right)}\right)}\right)$$

Input interpretation:

$$\frac{(-e^{-0.5} \times (-21.79216))^9}{\left(1 - \left(-\frac{-21.79216}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.79216}{e^{0.5}}\right)^3\right)\left(1 - \left(-\frac{-21.79216}{e^{0.5}}\right)^5\right)}$$

Open code

Enlarge Data Customize A Plaintext Interactive

Result:

More digits

• -1.08232...

Alternative representation:

$$\frac{(-e^{-0.5} (-1) 21.7922)^9}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^5\right)} = \frac{(-\exp^{-0.5}(z) (-1) 21.7922)^9}{\left(1 - \left(-\frac{-21.7922}{\exp^{0.5}(z)}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{\exp^{0.5}(z)}\right)^3\right)\left(1 - \left(-\frac{-21.7922}{\exp^{0.5}(z)}\right)^5\right)} \quad \text{for } z = 1$$

Series representations:

- More

$$\frac{(-e^{-0.5} (-1) 21.7922)^9}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^5\right)} = \frac{1.10842 \times 10^{12}}{\left(-21.7922 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.5}\right)\left(-10\,349.1 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{1.5}\right)\left(-4.91475 \times 10^6 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{2.5}\right)}$$

[Open code](#)

Enlarge Data Customize A Plaintext Interactive

$$\frac{(-e^{-0.5} (-1) 21.7922)^9}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^5\right)} = \frac{2.50806 \times 10^{13}}{\left(-30.8188 + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{0.5}\right)\left(-29\,271.6 + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{1.5}\right)\left(-2.7802 \times 10^7 + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{2.5}\right)}$$

[Open code](#)

$$\frac{(-e^{-0.5} (-1) 21.7922)^9}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^5\right)} = \frac{1.10842 \times 10^{12}}{\left(-21.7922 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.5}\right)\left(-10\,349.1 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{1.5}\right)\left(-4.91475 \times 10^6 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{2.5}\right)}$$

We note that, from the following Mock Theta Function (that is the result of $\psi(q)$ with minus sign):

$$\psi(q) = 1.08185 - 1.08232 + 1.08232 = 1.08185$$

the value obtained 1,08185 is a sub-multiple and is just half of the Cardy formula, i.e. $1.08288159962514159427961756214265524756132183588 \times 10^{81}$

Indeed:

$$-((((((-e^{-(0.5)}*(-21.79216))/((1-(((((-e^{-(0.5)}*(-21.79216)))))))))) * 10^{81}$$

Input interpretation:

$$-\left[\frac{e^{-0.5} \times (-21.79216)}{1 - \frac{-21.79216}{e^{0.5}}} \times 10^{81} \right]$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- More digits
 $1.08185... \times 10^{81}$

Series representations:

- More

$$-\frac{(-e^{-0.5}(-21.7922))10^{81}}{1 - \frac{-21.7922}{e^{0.5}}} = -\frac{2.17922 \times 10^{82}}{-21.7922 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.5}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

$$-\frac{(-e^{-0.5}(-21.7922))10^{81}}{1 - \frac{-21.7922}{e^{0.5}}} = -\frac{3.08188 \times 10^{82}}{-30.8188 + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{0.5}}$$

[Open code](#)

$$-\frac{(-e^{-0.5}(-21.7922))10^{81}}{1 - \frac{-21.7922}{e^{0.5}}} = -\frac{2.17922 \times 10^{82}}{-21.7922 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.5}}$$

The result 1.08185×10^{81} is very near to the above described value (Cardy formula)

Moreover we have that:

$$\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(-e^{-(0.5)} \times (-21.79216)\right) / \left(1 - \left(\left(\left(-e^{-(0.5)} \times (-21.79216)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right) \times 10^{81}\right)^6$$

Input interpretation:

$$\left(-\frac{e^{-0.5} \times (-21.79216)}{1 - \frac{-21.79216}{e^{0.5}}}\right) \times 10^{81}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- Fewer digits
- More digits
 $1.6032453978877785334468482638727968441412222708953959... \times 10^{486}$
 $1.6032453978877785334468482638727968441412222708 \times 10^{486}$

This result is a good approximation to the previous expression, i.e.:

$$\left((1.08288159962514159427961756214265524756132183588 \times 10^{81})\right)^6$$

$$\left(1.08288159962514159427961756214265524756132183588 \times 10^{81}\right)^6$$

$$1.61244847308029939489786323492279358431379319686 \times 10^{486}$$

$$1.61244847308029939489786323492279358431379319686 \times 10^{486}$$

Indeed, we have:

$$1.603245397887 * 10^{486} \approx 1.612448473080 * 10^{486}$$

This is a further confirm that the mathematics of the Ramanujan's Mock Theta Function is linked to the black holes physics and mathematics

We have also that:

$$\text{For } q = -e^{-t}, t = 0.5 \quad q^n = -21.79216 * -e^{-0.5}$$

Mock ϑ -functions (of 5th order)

$$f(q) = 1 + \frac{q}{1+q^2} + \frac{q^4}{(1+q)(1+q^2)} + \frac{q^9}{(1+q)(1+q^2)(1+q^3)} + \dots$$

$$\phi(q) = 1 + q(1+q) + q^4(1+q)(1+q^3) + q^9(1+q)(1+q^3)(1+q^5) + \dots$$

$$\psi(q) = q + q^3(1+q) + q^6(1+q)(1+q^2) + q^{10}(1+q)(1+q^2)(1+q^3) + \dots$$

$$\chi(q) = 1 + \frac{q}{1-q^2} + \frac{q^2}{(1-q^3)(1-q^4)} + \frac{q^3}{(1-q^4)(1-q^5)(1-q^6)} + \dots$$

$$= 1 + \left\{ \frac{q}{1-q} + \frac{q^3}{(1-q^2)(1-q^3)} + \frac{q^5}{(1-q^3)(1-q^4)(1-q^5)} + \dots \right\}$$

$$F(q) = 1 + \frac{q^2}{1-q} + \frac{q^8}{(1-q)(1-q^3)} + \dots$$

$$\chi(q) = 1 + (-1.08185) + (0.00575937) + (-1.41949 \times 10^{-8}) = -0.0760906441949$$

$$= 1 + (-0.0760922) + (2.47992 \times 10^{-6}) + (-3.51705 \times 10^{-14}) =$$

$$= 0.9239102799199648295$$

$$F(q) = 1 + (-14.2995) + (33034.4) = 33021.1005$$

Indeed, we have:

$$((-e^{-(0.5)} * (-21.79216))^2 / ((1 - (((-e^{-(0.5)} * (-21.79216))))))$$

Input interpretation:

$$\frac{(-e^{-0.5} \times (-21.79216))^2}{1 - \frac{-21.79216}{e^{0.5}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

-14.2995...

Series representations:

More

$$\frac{(-e^{-0.5} (-1) 21.7922)^2}{1 - \frac{-21.7922}{e^{0.5}}} = \frac{474.898}{(-21.7922 + (\sum_{k=0}^{\infty} \frac{1}{k!})^{0.5}) (\sum_{k=0}^{\infty} \frac{1}{k!})^{0.5}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

$$\frac{(-e^{-0.5} (-1) 21.7922)^2}{1 - \frac{-21.7922}{e^{0.5}}} = \frac{949.796}{(-30.8188 + (\sum_{k=0}^{\infty} \frac{1+k}{k!})^{0.5}) (\sum_{k=0}^{\infty} \frac{1+k}{k!})^{0.5}}$$

[Open code](#)

$$\frac{(-e^{-0.5} (-1) 21.7922)^2}{1 - \frac{-21.7922}{e^{0.5}}} = \frac{474.898}{(-21.7922 + (\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!})^{0.5}) (\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!})^{0.5}}$$

And:

$$(((e^{-(0.5)*(-21.79216)})^8)) / ((((((1-(((e^{-(0.5)*(-21.79216)})^1)))) ((1-(((e^{-(0.5)*(-21.79216)})^3))))))$$

Input interpretation:

$$\frac{(-e^{-0.5} \times (-21.79216))^8}{(1 - (-\frac{-21.79216}{e^{0.5}})^1)(1 - (-\frac{-21.79216}{e^{0.5}})^3)}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

More digits

33034.4...

Series representations:

More

$$\frac{(-e^{-0.5} (-1) 21.7922)^8}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)} = \frac{5.0863 \times 10^{10}}{\left(-21.7922 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{0.5}\right)\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^2 \left(-10\,349.1 + \left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{1.5}\right)}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

$$\frac{(-e^{-0.5} (-1) 21.7922)^8}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)} = \frac{8.13808 \times 10^{11}}{\left(-30.8188 + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{0.5}\right)\left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^2 \left(-29\,271.6 + \left(\sum_{k=0}^{\infty} \frac{1+k}{k!}\right)^{1.5}\right)}$$

[Open code](#)

$$\frac{(-e^{-0.5} (-1) 21.7922)^8}{\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^1\right)\left(1 - \left(-\frac{-21.7922}{e^{0.5}}\right)^3\right)} = \frac{5.0863 \times 10^{10}}{\left(-21.7922 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{0.5}\right)\left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^2 \left(-10\,349.1 + \left(\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}\right)^{1.5}\right)}$$

From the sum and some calculations of the following results previously obtained:

1.64370541171099062871185131629251928958432650892909035

1.6487212707001281468486507878141635716537761007101480

1.6442109004131825039227356463880273603048609587634042

1.6435923980586093145799367873492901635775398091369341

1.6429804873354...

1.6438187787578943564494183488914510895650008348787332

1.6437161856103091607910999662475235481706517783810713

1.6477158283216220606108224071415601414977900114636670

1.6439678304095125067795096413127798499015244293562323

1.6437859005782310620161084756021656195303526362348984

1.6437720382919401759948

1.64388

1.6438818674889841177750602517568866101168218651016596

We obtain:

21,37774889433

From:

$$(21.37774889433)^{\pi/20}$$

We obtain:

Input interpretation:
21.37774889433^{π/20}
Open code

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Result:

More digits

1.6177445222553...

Series representations:

More

$$21.377748894330000^{\pi/20} = 21.377748894330000^{1/5 \sum_{k=0}^{\infty} (-1)^k / (1+2k)}$$

Open code

Enlarge Data Customize A Plaintext Interactive

$$21.377748894330000^{\pi/20} = 0.736213544038280895 e^{0.30623506097976445 \times \sum_{k=1}^{\infty} 2^k / \binom{2k}{k}}$$

Open code

$$21.377748894330000^{\pi/20} = 21.377748894330000^{1/20 \sum_{k=0}^{\infty} (2^{-k} (-6+50k)) / \binom{3k}{k}}$$

Open code

• $\binom{n}{m}$ is the binomial coefficient •

Integral representations:

More

In conclusion, we have:

Working in the Reissner-Nordstrom sector, neutral emission will dominate until the ratio of rates in (77) is approximately one; but when this happens, the remaining excess energy is

$$\Delta E \sim \frac{n^{5/2} e^{-2\pi\sqrt{n}}}{r_e}, \quad (90)$$

which compares to an energy scale set by the uncertainty principle of

$$E_{\text{uncert}} \sim \frac{1}{n^{3/2} r_e}, \quad (91)$$

which is much larger. That is, before charged emission can become significant, the excess energy falls below the uncertainty in energy of the BPS state (and the statistical approximations implicit in our rates break down).

$$\begin{aligned} \text{for } n = 576, r_e &= \left(\frac{(2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39})}{(9 \times 10^{16})} \right) = \\ &= (1.945870226666 \times 10^{13}) \end{aligned}$$

We obtain, from (90):

$$\left(\frac{(576^{5/2} \times \exp(-2\pi \sqrt{576}))}{\left(\frac{(2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39})}{(9 \times 10^{16})} \right)} \right)$$

Input interpretation:

$$576^{5/2} \times \frac{\exp(-2\pi \sqrt{576})}{\frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}}$$

[Open code](#)

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Result:

More digits

$$1.32397... \times 10^{-72}$$

$$1.32397 \times 10^{-72}$$

And:

$$10^5 * \left(\frac{(576^{5/2} \times \exp(-2\pi \sqrt{576}))}{\left(\frac{(2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39})}{(9 \times 10^{16})} \right)} \right)^{1/15}$$

Input interpretation:

$$10^5 \sqrt[15]{576^{5/2} \times \frac{\exp(-2\pi \sqrt{576})}{\frac{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}{9 \times 10^{16}}}}$$

[Open code](#)

- More digits
23.9930273...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

$$\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(27 \times 4 + 10^3 / \left(\left(\left(\left(\left(\left(\left(576^{5/2} \times \exp(-2\pi \sqrt{576})\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)^{1/\left(\left(\left(\left(\left(18 + \frac{27}{50}\right)^2\right)\right)\right)\right)\right)^{1/\left(\left(\left(\left(\left(2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}\right)\right)\right)\right)\right)\right)\right)^{1/15}}$$

Input interpretation:

$$\sqrt[15]{27 \times 4 + \frac{10^3}{\left(18 + \frac{27}{50}\right)^2 \sqrt{576^{5/2} \times \frac{\exp(-2\pi \sqrt{576})}{2 \times 6.67 \times 10^{-11} \times 13.12806 \times 10^{39}}}}}$$

[Open code](#)

Enlarge Data Customize A [Plaintext](#) [Interactive](#)

Result:

- Fewer digits
 - More digits
- 1.643656307521192885392461806766318993567547829108894733676...
1.6436563075211928853924618067663189935675478291088947

Continued fraction:

- Linear form

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{4 + \frac{1}{6 + \frac{1}{5 + \frac{1}{1 + \frac{1}{7 + \frac{1}{1 + \frac{1}{2 + \frac{1}{13 + \frac{1}{3 + \frac{1}{6 + \frac{1}{7 + \frac{1}{1 + \frac{1}{8 + \frac{1}{19 + \frac{1}{1 + \frac{1}{5 + \frac{1}{1 + \frac{1}{\dots}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$$

[Open code](#)

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Possible closed forms:

More

$$\frac{655 \pi \pi! - 8600 - 2355 \pi + 149 \pi^2}{51 \pi} \approx 1.64365630752119288568569$$

$$\pi \left[\text{root of } 222 x^5 - 930 x^4 - 179 x^3 - 82 x^2 + 132 x + 40 \text{ near } x = 0.523192 \right] \approx 1.643656307521192885374586$$

$$\frac{5324844513 \pi}{10177609715} \approx 1.643656307521192885379993$$

Conclusions

As we can see, the results of the present thesis are particle-type solutions (glueball with the average value of its mass, mesons, baryon, etc...), values of black holes entropies, π and ϕ approximations. Many solutions of our mathematical expressions are golden numbers, numbers that are in the range that goes from 1.6 to 1,675, then an interval of the value of golden ratio: 1.61803398. These values of the solutions, which are results from the study and development of some equations inherent the black holes physics, mainly the solutions that provide golden numbers or the golden ratio itself and the π approximations, let us suppose that the multiverse is based on these two wonderful mathematical constants: π and ϕ

Appendix A

From:

TRANSACTIONS OF THE
AMERICAN MATHEMATICAL SOCIETY
Volume 349, Number 6, June 1997, Pages 2125(2173
S 0002-9947(97)01738-8

RAMANUJAN'S CLASS INVARIANTS, KRONECKER'S LIMIT FORMULA, AND MODULAR EQUATIONS
BRUCE C. BERNDT, HENG HUAT CHAN, AND LIANG{CHENG ZHANG

Theorem 4.11.

$$G_{505} = (\sqrt{5} + 2)^{1/2} \left(\frac{\sqrt{5} + 1}{2} \right)^{1/4} (\sqrt{101} + 10)^{1/4} \\ \times \left(\sqrt{\frac{113 + 5\sqrt{505}}{8}} + \sqrt{\frac{105 + 5\sqrt{505}}{8}} \right)^{1/2}.$$

Proof. We compose the following table.

d_1	d_2	χ	\mathbf{G}	C	$\chi(\mathbf{G}_0)$ $\chi(\mathbf{G}_2)$	$\chi(\mathbf{G}_1)$ $\chi(\mathbf{G}_3)$	h_1	h_2	w_2	ϵ_1
1	-2020	χ_0	\mathbf{G}_0	$[1, \Omega]$ $[5, \Omega]$	1 1	1 1				
5	-404	χ_1	\mathbf{G}_1	$[2, 1 + \Omega]$ $[10, 5 + \Omega]$	1 1	-1 -1	1	14	2	$\frac{\sqrt{5} + 1}{2}$
101	-20	χ_2	\mathbf{G}_2	$[11, 1 + \Omega]$ $[11, -1 + \Omega]$	1 -1	-1 1	1	2	2	$\sqrt{101} + 10$
505	-4	χ_3	\mathbf{G}_3	$[22, 1 + \Omega]$ $[22, -1 + \Omega]$	1 -1	1 -1				

Hence, 505 is of the second kind. Applying Theorem 3.2 with $h = 8$ and $w = 2$, we find that

$$P^{-2} := (G_{505}G_{101/5})^4 = \left(\frac{\sqrt{5} + 1}{2} \right)^{14} (\sqrt{101} + 10)^2,$$

so that

$$P^{-1} = \left(\frac{\sqrt{5} + 1}{2} \right)^7 (\sqrt{101} + 10) = (\sqrt{5} + 2) \left(\frac{\sqrt{5} + 1}{2} \right)^4 (\sqrt{101} + 10) \\ (4.35) \quad = (\sqrt{5} + 2) \left(\frac{7 + 3\sqrt{5}}{2} \right) (\sqrt{101} + 10).$$

Let $Q = (G_{505}/G_{101/5})^3$. Then, by Lemma 3.4 and (4.35),

$$Q = (P^{-1} - P) + \sqrt{(P^{-1} - P)^2 - 1} \\ (4.36) \quad = (130\sqrt{5} + 29\sqrt{101}) + \sqrt{169440 + 7540\sqrt{505}}.$$

Therefore, by (4.35) and (4.36),

$$G_{505} = P^{-1/4}Q^{1/6} = (\sqrt{5} + 2)^{1/2} \left(\frac{\sqrt{5} + 1}{2} \right)^{1/4} (\sqrt{101} + 10)^{1/4} \\ \times \left((130\sqrt{5} + 29\sqrt{101}) + \sqrt{169440 + 7540\sqrt{505}} \right)^{1/6}.$$

Thus, it remains to show that

$$(130\sqrt{5} + 29\sqrt{101}) + \sqrt{169440 + 7540\sqrt{505}} = \left(\sqrt{\frac{113 + 5\sqrt{505}}{8}} + \sqrt{\frac{105 + 5\sqrt{505}}{8}} \right)^3,$$

which is straightforward. \square

From:

Three-dimensional AdS gravity and extremal CFTs at $c = 8m$

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m	L_0	d	S	S_{BH}
3	1	196883	12.1904	12.5664
	2	21296876	16.8741	17.7715
	3	842609326	20.5520	21.7656
4	2/3	139503	11.8458	11.8477
	5/3	69193488	18.0524	18.7328
	8/3	6928824200	22.6589	23.6954
5	1/3	20619	9.9340	9.3664
	4/3	86645620	18.2773	18.7328
	7/3	24157197490	23.9078	24.7812

m	L_0	d	S	S_{BH}
6	1	42987519	17.5764	17.7715
	2	40448921875	24.4233	25.1327
	3	8463511703277	29.7668	30.7812
7	2/3	7402775	15.8174	15.6730
	5/3	33934039437	24.2477	24.7812
	8/3	16953652012291	30.4615	31.3460
8	1/3	278511	12.5372	11.8477
	4/3	13996384631	23.3621	23.6954
	7/3	19400406113385	30.5963	31.3460

Table 1: Degeneracies, microscopic entropies and semiclassical entropies for the first few values of m and L_0 .

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EVOLUTION OF NEAR-EXTREMAL BLACK HOLES

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S. Ramanujan to G.H. Hardy 12 January 1920 - University of Madras

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