

Do the Planck length, time and mass follow the Lorentz contraction?

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ABSTRACT

The Planck length, time and mass follow the Lorentz contraction. The speed of light is different in higher dimensions. The Gravitational Constant not Really Constant.

Keywords

Special Relativity, Lorentz contraction, higher dimensions, Planck length

Introduction

Fitzgerald-Lorentz contraction

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}} \quad (1)$$

$$dX_2 = \gamma [dX_1 - v dT_1 \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}}] \quad (2)$$

$$dT_2 = \gamma \left(dT_1 - \frac{v \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}}}{c^2} dX_1 \right) \quad (3)$$

$$dM_2 = \gamma dM_1 \quad (4)$$

A in frame S_1 and at rest, B in frame S_2 and at moves so Measurements B:

From equation (3) let $dT_2 = 0$

$$dT_2 = \gamma \left(dT_1 - \frac{v \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}}}{c^2} dX_1 \right) \text{-----} (3)$$

$$0 = \gamma \left(dT_1 - \frac{v \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}}}{c^2} dX_1 \right)$$

$$dT_1 = \frac{v}{c^2} \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}} dX_1 \text{-----} (5)$$

From equation (2), (5)

$$dX_2 = \gamma \left[dX_1 - v dT_1 \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}} \right] \text{-----} (2)$$

$$dT_1 = \frac{v}{c^2} \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}} dX_1 \text{-----} (5)$$

$$dX_2 = \gamma \left[dX_1 - v \frac{v}{c^2} \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}} dX_1 \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}} \right]$$

$$dX_2 = \gamma \left[1 - \frac{v^2}{c^2} \left(1 - \frac{dX_{PL}^2}{dX_1^2} \right) \right] dX_1 \text{-----} (6)$$

From equation (1)

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \frac{dX_{PL}^2}{dX_1^2} \right)}} \text{-----} (1)$$

$$dX_2 = \sqrt{1 - \frac{v^2}{c^2} \left(1 - \frac{dX_{PL}^2}{dX_1^2} \right)} dX_1 \text{-----} (7)$$

$$dX = \sqrt{1 - \frac{v^2}{c^2} \left(1 - \frac{dX_{PL}^2}{dX_1^2} \right)} dX_o \text{-----} (8)$$

Proper time

We have equation

$$dX_1^2 + dY_1^2 + dZ_1^2 - C_1^2 dT_1^2 - \frac{G_1^2}{C_{M1}^4} dM_1^2 = dX_2^2 + dY_2^2 + dZ_2^2 - C_2^2 dT_2^2 - \frac{G_2^2}{C_{M2}^4} dM_2^2$$

----- (9)

$$dS_1^2 = dS_2^2$$

----- (10)

C_1 Speed of light and C_{M1} Speed of light at mass dimension at frame S_1

C_2 Speed of light and C_{M2} Speed of light at mass dimension at frame S_2

And $C_1 = C_2$

$$So \ dX_1^2 + dY_1^2 + dZ_1^2 - C^2 dT_1^2 - \frac{G_1^2}{C_{M1}^4} dM_1^2 = dX_2^2 + dY_2^2 + dZ_2^2 - C^2 dT_2^2 - \frac{G_2^2}{C_{M2}^4} dM_2^2$$

----- (11)

$$When \left(\frac{dX_2}{dT_2}\right)^2 + \left(\frac{dY_2}{dT_2}\right)^2 + \left(\frac{dZ_2}{dT_2}\right)^2 = 0$$

from Redefinition of the point as a circle the length of it the radius Equal the length of the Planck cT_{pl}



$$dX_1 = v \sqrt{dT_1^2 - \frac{c^2}{v^2} (dT_{pl}^2)}$$

$$dX_1 = v dT_1 \sqrt{1 - \frac{c^2}{v^2} \left(\frac{dT_{pl}^2}{dT_1^2}\right)}$$

$$\frac{dX_1}{dT_1} = v \sqrt{1 - \frac{dX_{pl}^2}{dX_1^2}}$$

In three dimensions

$$\sqrt{\left(\frac{dX_1}{dT_1}\right)^2 + \left(\frac{dY_1}{dT_1}\right)^2 + \left(\frac{dZ_1}{dT_1}\right)^2} = v \sqrt{1 - \frac{dX_{pl}^2}{dX_1^2}}$$

so

$$\left(\frac{dX_1}{dT_1}\right)^2 + \left(\frac{dY_1}{dT_1}\right)^2 + \left(\frac{dZ_1}{dT_1}\right)^2 = v^2 \left(1 - \frac{dX_{PL}^2}{dX_1^2}\right)$$

----- (12)

So from (9), (10), (12)

$$dS_1^2 = v^2 \left(1 - \frac{dX_{PL}^2}{dX_1^2}\right) dT_1^2 - C^2 dT_1^2 - \frac{G_1^2}{C_{M1}^4} dM_1^2 = 0 - C^2 dT_2^2 - \frac{G_2^2}{C_{M2}^4} dM_2^2$$

----- (13)

$$dS_1^2 = \left[v^2 \left(1 - \frac{dX_{PL}^2}{dX_1^2}\right) - C^2 - \frac{G_1^2}{C_{M1}^4} \left(\frac{dM_1}{dT_1}\right)^2\right] dT_1^2 = -\left[C^2 + \frac{G_2^2}{C_{M2}^4} \left(\frac{dM_2}{dT_2}\right)^2\right] dT_2^2$$

----- (14)

But $\frac{dM_1}{dT_1} = 0$ and $\frac{dM_2}{dT_2} = 0$

So

$$dS_1^2 = \left[v^2 \left(1 - \frac{dX_{PL}^2}{dX_1^2}\right) - C^2\right] dT_1^2 = -[C^2] dT_2^2$$

----- (15)

$$dT_2^2 = \left[1 - \frac{v^2}{C^2} \left(1 - \frac{dX_{PL}^2}{dX_1^2}\right)\right] dT_1^2$$

----- (16)

$$dT_2 = \sqrt{1 - \frac{v^2}{C^2} \left(1 - \frac{dX_{PL}^2}{dX_1^2}\right)} dT_1$$

----- (17)

$$dT = \sqrt{1 - \frac{v^2}{C^2} \left(1 - \frac{dX_{PL}^2}{dX_1^2}\right)} dT_o$$

----- (18)

From (4) and (1)

$$dM_2 = \gamma dM_1$$

----- (4)

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}} \quad (1)$$

$$dM_2 = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}} dM_1 \quad (19)$$

$$dM = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}} dM_o \quad (20)$$

Contribution

$$\text{Let } \mathbf{v} = v \sqrt{1 - \frac{dX_{PL}^2}{dX_1^2}} = \frac{dX}{dT} = \frac{dX}{dX_o} \cdot \frac{dX_o}{dT_o} \cdot \frac{dT_o}{dT}$$

$$= \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}} \cdot \mathbf{v}_o \cdot \gamma$$

$$\text{SO } \mathbf{v} = \mathbf{v}_o \quad (21)$$

By using the equations

$$dX = \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)} dX_o \quad (8)$$

$$dT = \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)} dT_o \quad (18)$$

$$dM = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}} dM_o \quad (20)$$

$$\mathbf{v} = \mathbf{v}_o \quad (21)$$

Then

$$\mathbf{h} = \frac{dM \cdot v \cdot d\lambda}{2\pi} = \frac{dM \cdot v \cdot 2\pi \cdot dX}{2\pi} = dM \cdot v \cdot dX = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}} dM_o \cdot \mathbf{v} \cdot \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)} dX_o$$

$$\mathbf{h} = dM_o \cdot \mathbf{v} \cdot dX_o = \mathbf{h}_o$$

Then

$$\mathbf{h} = \mathbf{h}_o \text{-----} (22)$$

$$\mathbf{v}_f = \mathbf{v}_i + \mathbf{a}dT = \mathbf{v}_i + \mathbf{a} \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)} dT_o$$

$$\mathbf{v}_f = \mathbf{v}_i + \mathbf{a}_o dT_o$$

So

$$\mathbf{a} \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)} dT_o = \mathbf{a}_o dT_o$$

$$\mathbf{a} \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)} = \mathbf{a}_o$$

$$\mathbf{a} = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}} \mathbf{a}_o \text{-----} (23)$$

Is the Gravitational Constant Really Constant?

$$\mathbf{a} = \frac{G \cdot dM}{dX^2} = \frac{G \cdot \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}} dM_o}{\left(\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)} dX_o\right)^2} = \frac{G_o \cdot dM_o}{dX_o^2} \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}}$$

$$\frac{G}{\left(\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)}\right)^2} = G_o$$

$$G = G_o \left[\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)\right)} \right]^2 \text{-----} (24)$$

But we have from the

$$X_1^2 - C^2 T_1^2 - \frac{G_1^2}{C^4} M_1^2 = X_2^2 - C^2 T_2^2 - \frac{G_2^2}{C^4} M_2^2$$

$$G = G_o \left[\sqrt{1 - \frac{v^2}{C^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)}\right)} \right] \text{----- (25) [1]}$$

But the correct

$$X_1^2 - C_1^2 T_1^2 - \frac{G_1^2}{C_{M1}^4} M_1^2 = X_2^2 - C_2^2 T_2^2 - \frac{G_2^2}{C_{M2}^4} M_2^2 [2]$$

$$C_M \neq C$$

And we have

$$\frac{G_o^2}{C_{M1}^4} = \frac{G^2}{C_{M2}^4} \left[\frac{1}{\sqrt{1 - \frac{v^2}{C^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)}\right)}} \right]^2$$

$$\frac{G_o^2}{C_{M1}^4} = \frac{G_o^2 \left[\sqrt{1 - \frac{v^2}{C^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)}\right)} \right]^4}{C_{M2}^4} \left[\frac{1}{\sqrt{1 - \frac{v^2}{C^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)}\right)}} \right]^2$$

$$\frac{1}{C_{M1}^4} = \frac{1 \left[\sqrt{1 - \frac{v^2}{C^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)}\right)} \right]^4}{C_{M2}^4} \left[\frac{1}{\sqrt{1 - \frac{v^2}{C^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)}\right)}} \right]^2$$

$$C_{M2}^4 = C_{M1}^4 \left[\sqrt{1 - \frac{v^2}{C^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)}\right)} \right]^2$$

$$C_{M2} = C_{M1} \sqrt[4]{1 - \frac{v^2}{C^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2}\right)}\right)} \text{----- (26)}$$

PLANCK

$$l_{pl} = \sqrt{\frac{G\hbar}{C^3}}$$

$$l_{pl} = \sqrt{\frac{G_o \left[\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{pl}^2}{dX_1^2}\right)}\right)^2} \right] \hbar}{C^3}}$$

$$l_{pl}rest = \sqrt{\frac{G_o \hbar}{C^3}}$$

$$l_{pl} = l_{pl}rest \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{pl}^2}{dX_1^2}\right)}\right)} \text{----- (27)}$$

$$t_{pl} = \sqrt{\frac{G\hbar}{C^5}}$$

$$t_{pl} = \sqrt{\frac{G_o \left[\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{pl}^2}{dX_1^2}\right)}\right)^2} \right] \hbar}{C^5}}$$

$$t_{pl}rest = \sqrt{\frac{G_o \hbar}{C^5}}$$

$$t_{pl} = t_{pl}rest \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{pl}^2}{dX_1^2}\right)}\right)} \text{----- (28)}$$

$$m_{pl} = \sqrt{\frac{C\hbar}{G}}$$

$$m_{pl} = \frac{\text{Ch}}{\sqrt{G_o \left[\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2} \right)^2} \right)^2} \right]}}$$

$$m_{plrest} = \sqrt{\frac{\text{Ch}}{G}}$$

$$m_{pl} = l_{plrest} \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2} \right)^2 \right)}} \text{----- (29)}$$

Conclusion

$$dX = \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2} \right)^2 \right)} dX_o \text{----- (8)}$$

$$dT = \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2} \right)^2 \right)} dT_o \text{----- (18)}$$

$$dM = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}^2}{dX_1^2} \right)^2 \right)}} dM_o \text{----- (20)}$$

$$\mathbf{v} = \mathbf{v}_o \text{----- (21)}$$

$$\hbar = \hbar_o \text{----- (22)}$$

$$\mathbf{a} = \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}}{dX_1}\right)^2\right)}} \mathbf{a}_o \text{----- (23)}$$

$$G = G_o \left[\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}}{dX_1}\right)^2\right)} \right]^2 \text{----- (24)}$$

$$C_{M2} = C_{M1} \sqrt[4]{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}}{dX_1}\right)^2\right)} \text{----- (26)}$$

$$l_{pl} = l_{plrest} \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}}{dX_1}\right)^2\right)} \text{----- (27)}$$

$$t_{pl} = t_{plrest} \sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}}{dX_1}\right)^2\right)} \text{----- (28)}$$

$$m_{pl} = l_{plrest} \frac{1}{\sqrt{1 - \frac{v^2}{c^2} \left(1 - \left(\frac{dX_{PL}}{dX_1}\right)^2\right)}} \text{----- (29)}$$

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