

1. POWER OF THE SET OF PRIME NUMBERS:

As a proof of the claim I have made (postulate), I intend to present to you a way to calculate the power of a set of prime numbers, i.e. an algorithm that allows us to determine the number of primes proper within a given numerical range $(0, x)$. This is the so-called "theorem on prime numbers".

Of course, I will base my proof on the equations derived in my innovative scientific work „Distribution of prime numbers”.

									-1	m	1								
	8	7	6	5	4	3	2	1	d	1	2	3	4	5	6	7	8		
	+48k	+42k	+36k	+30k	+24k	+18k	+12k	+6k	1	+6k	+12k	+18k	+24k	+30k	+36k	+42k	+48k	+54k	
	-343	-301	-259	-217	-175	-133	-91	-49	-7	35	77	119	161	203	245	287	329	371	
	49	43	37	31	25	19	13	7	w	5	11	17	23	29	35	41	47	53	

Fig. 4. Generation of multiples– numbers u_r fo the number $p_r = 7$.
(w – nth multiples, d i m – coefficients from equation (11)).

The "prime number theorem" defining the power of the set $\pi(n)$ is a serious problem to this day. The value of the result of this equation is burdened with an error, and its size decreases asymptotically when $n \rightarrow +\infty$.

$$\pi(n) \approx \frac{n}{\log(n)} \tag{13}$$

To this day, it has not been possible to design a formula that would unambiguously and without error calculate the number of prime numbers in the set of whole numbers. Therefore, my observations can become an innovative way to deal with this issue.

ASSUMPTIONS:

- 1) It is obvious that prime numbers are searched for odd numbers, the sum of which is not divisible by 3, which is unequivocally looking for them among the numbers that are part of the set Z_r .
- 2) The number x is the right edge of the set being examined $(0, x >)$, which we will consider in terms of the number of prime numbers proper.

POSTULATE 2:

If the number x is divided by 5 (the first first proper number of the set Z_r) we get the right boundary of the set $(0, \frac{x}{5} >$, which will contain numbers z_r affecting the generation of all numbers u_r in the entire collection space $(0, x >$.

EXAMPLE 1:

- 1) Let x be 77.
- 2) If we divide 77 into 5 we get 15,4.
- 3) We quickly notice that in a set of integers $(0,15 >$ there are four numbers $z_r : \{ 5,7,11,13 \} \in (0,15 >$.
- 4) According to the above postulate, these numbers suffice to determine all numbers u_r located in the whole space of the set $(0, x >$.
- 5) Below I present a list of all combinations of numbers u_r resulting from numbers $\{ 5,7,11,13 \}$ (products of pairs of numbers z_r):

$$\begin{aligned} \mathbf{5 \times 5} &= \mathbf{25} \\ \mathbf{5 \times 7} &= \mathbf{35} \\ \mathbf{5 \times 11} &= \mathbf{55} \\ \mathbf{5 \times 13} &= \mathbf{65} \\ \mathbf{7 \times 7} &= \mathbf{49} \\ \mathbf{7 \times 11} &= \mathbf{77} \\ \mathbf{7 \times 13} &= \mathbf{91} \\ \mathbf{11 \times 11} &= \mathbf{121} \\ \mathbf{11 \times 13} &= \mathbf{143} \\ \mathbf{13 \times 13} &= \mathbf{169} \end{aligned} \tag{14}$$

It is worth noting that all (**in bold**) above the results are exactly a two-element combination with repetitions from the $n -$ element set, in this case a four-element set. It is important to reject mirror combinations, i.e. ab and ba are treated as twin combinations. The formula for the number of two-element combinations from a four-element set is shown below:

$$C_n^k = \binom{k+n-1}{k} = \frac{(k+n-1)!}{k!(n-1)!} = \frac{(2+4-1)}{2!(4-1)!} = 10 \tag{15}$$

Let's look ...

In the above-mentioned example, we have affect with the number z_r small sizes. Questions arise as to how subsections 3 and 7 will be solved in case of much larger numbers z_r .

In this case, I will present you two ways to solve these doubts, and their order will not be accidental, because the below presented mathematical calculator will be a good reference and visualization of theoretical mathematical calculations:

- mathematical calculator (based on the EXCEL program from the MS Office package) using the above-mentioned formulas and theoretical relations;
- theoretical (using mathematical calculations);

MATHEMATICAL CALCULATOR:

In order to solve the problem related to the power of prime numbers, I used the EXCEL program from the MS Office suite, which according to my person is a great and extremely versatile tool useful not only in the world of mathematics.

In the further part of my research I intend to introduce to you step by step the algorithm used to determine the power of the set of natural numbers:

STEP 1.

Let us assume that for the experiment $x = 1411$.

STEP 2.

Let's build a numerical table whose elements u_r are multiples of all numbers z_r determined in postulate No. 2. This table will therefore have sizes (Figure 5):

a. height:93

- ✓ the number of rows in the numeric table should be consistent with the number of numbers z_r falling within the range $(0, \frac{x}{5} >$, it means $(0; 282,6 >$,

a. width: 12

- ✓ the number of columns in the numeric table should be consistent with the number of numbers z_r falling within the range $(0, \sqrt{x} >$, it means $(0; 37,6 >$,

- with red in the tabular summary of numbers u_r (Figure 5.), check the repeated numbers being the results of a two-element combination with the repetitions from the numbers z_r in the range $(0, \frac{x}{5} >$ and affecting the generation of numbers u_r in the range $(0, x >$;
- for this purpose, let us use conditional formatting (one of the interesting functions of the EXCEL program) to capture duplicate values of the number u_r ;
- please note that in the first row of the table there are only numbers z_r raised to the square. Because in the tabular summary we do not capture the results of the two-element combinations being their mirror reflection in the record (reminder: the $ab = ba$ combination);
- the idea of tabular summary of numbers u_r (Figure 6a, 6b) presents schemes:

	a	b	c	d	e	f	g	h	i	j
a	aa	ab	ac	ad	ae	af	ag	ah	ai	aj
b	ba	bb	bc	bd	be	bf	bg	bh	bi	bj
c	ca	cb	cc	cd	ce	cf	cg	ch	ci	cj
d	da	db	dc	dd	de	df	dg	dh	di	dj
e	ea	eb	ec	ed	ee	ef	eg	eh	ei	ej
f	fa	fb	fc	fd	fe	ff	fg	fh	fi	fj
g	ga	gb	gc	gd	ge	gf	gg	gh	gi	gj
h	ha	hb	hc	hd	he	hf	hg	hh	hi	hj
i	ia	ib	ic	id	ie	if	ig	ih	ii	ij
j	ja	jb	jc	jd	je	jf	jg	jh	ji	jj

Fig. 6a. The idea tabular summary of number u_r - postulate No. 2.

(tabular sets of numbers u_r represent only the above-mentioned black boxes)

	a	b	c	d	e	f	g	h	i	j
a	aa	bb	cc	dd	ee	ff	gg	hh	ii	jj
b	ba	cb	dc	ed	fe	gf	hg	ih	ji	0
c	ca	db	dc	fd	ge	hf	ig	jh	0	0
d	da	eb	fc	gd	he	if	jg	0	0	0
e	ea	fb	gc	hd	ie	jf	0	0	0	0
f	fa	gb	hc	id	je	0	0	0	0	0
g	ga	hb	ic	jd	0	0	0	0	0	0
h	ha	ib	jc	0	0	0	0	0	0	0
i	ia	jb	0	0	0	0	0	0	0	0
j	ja	0	0	0	0	0	0	0	0	0

Fig. 6b. The idea tabular summary of number u_r - postulate No. 2.

(after changing cell values - field conversion)

STEP 3.

Marking (underlining) only those values of numbers u_r , which are within the tested range $(0, x >$.

- the numbers 0 seen at the bottom of the table are caused by the offsets of the rows of subsequent columns in accordance with the illustration of the idea of tabular summary of number u_r (Fig. 6.);
- comparing two figures 5 and 7, we come to the conclusion that among the generated numbers u_r in the range $(0, x >$ there are still repeating values.

STEP 4.

Determination of the multiplicity of repetitions of the numbers u_r in the interval $(0, x >$;

- using very useful formulas of the EXCEL program we are able to count the duplication times (repetitions) of individual values of the number u_r (see. Fig. 9.);
- result:

ILOŚĆ	WKR	Zr
206	1	206
48	2	24
54	3	18
4	4	1
0	5	0
0	6	0
0	7	0
0	8	0
0	9	0
312	Ur	249

Fig.8. The multiplicity of the repetitions of generated u_r numbers (results).

- according to the table in Fig. 8. and the postulate No 2 from the numbers z_r falling within the range $(0, \frac{x}{5} >$ we are able to generate in the numerical range $(0, x >$ up to 312 numbers u_r , with the proviso that:
 - 48 numbers u_r are repeated twice;
 - 54 numbers u_r are repeated three times;
 - 4 numbers u_r are repeated four times;
- if the number of repeated numbers of each group divide by their multiplicity, we will get an interesting set of numbers u_r ;
- finally we receive information that the number of generated and different numbers u_r (i.e. without repetitions) in the range $(0, x >$ is exactly 249;

STEP 5.

Calculation of the power of a set of prime numbers, which at this moment becomes the proverbial "bread roll", because it is enough to determine which number according to the formula (9) is the number x and subtract from it the number 249 received above (see formula 12);

	1	2	3	4	5	6	7	8	9	10	11	12
5	1	1	1	1	1	1	1	2	1	1	4	1
7	2	1	1	1	1	1	2	2	1	3	3	
11	3	1	1	1	1	2	1	2	3	1		
13	4	1	1	1	1	2	1	3	1	1		
17	5	1	1	1	2	1	1	3	2	1	1	
19	6	1	1	2	1	1	3	1	2	1		
23	7	1	2	1	1	3	1	1	2	1		
25	8	1	1	1	3	1	1	1	2			
29	9	1	1	3	1	1	1	1	4			
31	10	1	2	1	1	1	1	2	2			
35	11	2	1	1	1	1	2	1	3			
37	12	1	1	1	1	2	1	3				
41	13	1	1	1	2	1	3	1				
43	14	1	1	2	1	3	1	1				
47	15	1	1	1	3	1	1					
49	16	2	1	2	1	1	3					
53	17	1	3	1	1	3	1					
55	18	2	1	1	2	1	1					
59	19	1	1	3	1	1	1					
61	20	1	3	1	1	1						
65	21	2	1	1	1	3						
67	22	1	1	1	3	1						
71	23	1	1	2	1	1						
73	24	1	2	1	1							
77	25	3	1	1	3							
79	26	1	1	3	1							
83	27	1	3	1	2							
85	28	2	1	3	3							
89	29	1	2	3	1							
91	30	3	3	1	1							
95	31	2	1	1	1							
97	32	1	1	1	1							
101	33	1	1	1								
103	34	1	1	1								
107	35	1	1	1								
109	36	1	1	3								
113	37	1	3	3								
115	38	2	2	1								
119	39	3	2	3								
121	40	2	3	1								
125	41	2	1									
127	42	1	1									
131	43	1	2									
133	44	3	1									
137	45	1	1									
139	46	1	3									
143	47	3	3									
145	48	2	1									
149	49	1	1									
151	50	1	3									
155	51	2	1									
157	52	1	2									
161	53	3	1									
163	54	1	1									
167	55	1	2									
169	56	2	1									
173	57	1	4									
175	58	3	1									
179	59	1	1									
181	60	1	3									
185	61	2	3									
187	62	3	1									
191	63	1	1									
193	64	1	1									
197	65	1	1									
199	66	1										
203	67	3										
205	68	2										
209	69	3										
211	70	1										
215	71	2										
217	72	3										
221	73	3										
223	74	1										
227	75	1										
229	76	1										
233	77	1										
235	78	2										
239	79	1										
241	80	1										
245	81	4										
247	82	3										
251	83	1										
253	84	3										
257	85	1										
259	86	3										
263	87	1										
265	88	2										
269	89	1										
271	90	1										
275	91	3										
277	92	1										
281	93	1										
283	94											

Fig.9. Multiplicity of duplicate values of numbers u_r less than x .

$$z_{r_k} = O_r + 6 \sum_1^k (-1)^{k+1} k \quad (9)$$

$$z_{r_k} = 1411$$

$$k = 470$$

- for those who still accept the number t_r for the proper prime numbers - add the number two to the result obtained:

$$Z_r - U_r + T_r = P_r \quad (12)$$

$$470 - 249 + T_r = 211 + T_r$$

$$\pi(1411) = 211 + T_r$$

MATHEMATICAL CALCULATIONS:

REFERENCE TO STEP 2.

In order to resolve item 3 from example No. 1, the number of numbers z_r included in the set should be determined by using the formula $(0, \frac{x}{5} > :$

$$n(Z_{r_i}) = \left[\frac{x-5}{30} \right] + \left[\frac{x+5}{30} \right] \quad (16)$$

— where:

- $n(Z_{r_i})$ — power of the set Z_{r_i} ;
- i — (auxiliary record)
index informing about the number of z_r in the set $(0, \frac{x}{5} >$
the value of the index is synonymous with the table height;
- $[]$ — means the result trait (integer part) used for next activities;

The above result of the amount z_{r_i} is at the same time the height (indicates the number of rows) of the tabular summary of the number u_r (Fig.5.).

The width (number of columns) of the tabular summary of number u_r (Fig.5.) is able to be determined using a very similar formula:

$$n(Z_{r_j}) = \left[\frac{[\sqrt{x}] - 1}{6} \right] + \left[\frac{[\sqrt{x}] + 1}{6} \right] \quad (17)$$

— where:

- $n(Z_{r_j})$ — power of the set Z_{r_j} ;
- j — (auxiliary record)
index informing about the number of z_r in the set ($0, \sqrt{x} >$,
the value of the index is synonymous with the table width;
- $[]$ — means the result trait (integer part) used for next activities;

EXAMPLE 2:

Table's height:

- 1) Let x be 1411.
- 2) If we set 1411 under the formula 16 we get **93** – number of numbers z_{r_i} = number of rows.
- 3) If the numbers from 1 to 93 are substituted by the formula (9), then we obtain the values of all numbers z_{r_i} of the set ($0, 282, 2 >$, where the largest is $z_{r_{93}} = 281$.

Table's width:

- 1) If we set 1411 under the formula 17 we get **12** – number of numbers z_{r_j} = number of columns.
- 2) If the numbers from 1 to 12 are substituted by the formula (9), then we obtain the values of all numbers z_{r_j} of the set ($0; 37, 56 >$, where the largest is $z_{r_{12}} = 37$.

REFERENCE TO STEP 3.

The formula for calculating the total number of numbers u_r being a numerical combination (Fig. 7.) smaller than the numer x is a combination of three formulas: 9, 16 i 17:

$$n(U_{r_k}) = \sum_{j=1}^{n(Z_{r_j})} \left[\frac{x - |z_{r_j}|}{6 |z_{r_j}|} \right] + \left[\frac{x + |z_{r_j}|}{6 |z_{r_j}|} \right] - (j - 1) \quad (18)$$

— gdzie:

- $n(U_{r_k})$ — power of the set U_{r_k} ;
- $n(Z_{r_j})$ — power of the set Z_{r_j} according to formula 17.
- $[]$ — means the result trait (integer part) used for next activities;

- z_{r_j} — individual numbers z_r with the index above interval j ;
- j — ordinal number of the number z_{r_j} ($j \in C$);

REFERENCE TO STEP 4.

Dispose of the multiplicity of repetitions of the numbers u_r constituting the numerical combination (Fig. 7.). For this purpose, we can use the following general formula of the set U_r consisting of the value of the function $f(z_{r_j}z_{r_i})$:

$$U_r \leftrightarrow f(z_{r_j}z_{r_i}) \quad (19)$$

$$\bigwedge_{z_{r_j}} j \in \langle 1; n(Z_{r_j}) \rangle \bigwedge_{z_{r_i}} i \in \langle j; \left[\frac{x - |z_{r_j}|}{6|z_{r_j}|} \right] + \left[\frac{x + |z_{r_j}|}{6|z_{r_j}|} \right] + (j - 1) \rangle \rightarrow f(z_{r_j}z_{r_i}) \quad (20)$$

$$\text{where } f(z_{r_j}z_{r_i}) = z_{r_j}z_{r_i} \quad (21)$$

— gdzie:

- U_r — a set consisting of unique values of the number u_r ;
- i — ordinal number of the number z_{r_i} ,
where $i \in \langle j; \left[\frac{x - |z_{r_j}|}{6|z_{r_j}|} \right] + \left[\frac{x + |z_{r_j}|}{6|z_{r_j}|} \right] + (j - 1) \rangle \wedge i \in C$;
- j — ordinal number of the number z_{r_j} ,
where $j \in \langle 1; n(Z_{r_j}) \rangle \wedge j \in C$;

In this way, we get all the data (values) necessary to calculate the power of prime numbers using the formula 12 - which has its confirmation in the work of the mathematical calculator (EXCEL).

2. VERIFICATION OF THE "PRIME" NUMBER z_r

The proverbial "icing on the cake" would be the solution to the problem of verifying the number z_r in terms of its primacy, i.e. whether it is the prime number or the imaginary prime number.

I believe that it is logically possible if we follow the algorithm below - if we compare the cell values of the highest rows of all the columns of the table summary of numbers u_r with the number x being the right boundary of the whole set of integers numbers:

$$\bigwedge_{z_{r_j}} j \in \langle 1; n(z_{r_j}) \rangle > \bigvee_{z_{r_i}} i = \left\lfloor \frac{x - |z_{r_j}|}{6|z_{r_j}|} \right\rfloor + \left\lfloor \frac{x + |z_{r_j}|}{6|z_{r_j}|} \right\rfloor + (j - 1) \rightarrow f(z_{r_j}z_{r_i}) \quad (22)$$

$$f(z_{r_j}z_{r_i}) = z_{r_j}z_{r_i} \quad (23)$$

— where:

- i — ordinal number of the number z_{r_i} ;
- j — ordinal number of the number z_{r_j} ($j \in C$);

— if:

- $f(z_{r_j}z_{r_i}) < x$ — number z_r is the proper prime number p_r ;
- $f(z_{r_j}z_{r_i}) = x$ — number z_r is the improper prime number u_r ;

The number of comparisons made in accordance with the above algorithm equals only the harvesting power $n(z_{r_j})$, and its display shows blue ellipses on the table summary of numbers u_r (Fig. 5.)

PREPARED

kpt. mgr. inż. Dariusz GOŁOFIT