

## **Fermat's theorem: The second case (A is multiple of n)**

In Memory of my MOTHER

All calculations are done with numbers in base n, a prime number greater than 2.

### The notations:

$A' / A_{(t)}$  – the first / the t-th digit from the end of the number A;

$A_{[t]}$  – is the k-digit ending of the number A (i.e.  $A_{[t]} = A \bmod n^t$ );

Let's assume that for co-prime natural numbers  $A [=n^k A^\circ]$ , B, C and a prime  $n > 2$

1°)  $A^n + B^n - C^n = 0$  and  $C^n - B^n = (C-B)P$ , where, as it is known [see [viXra:1707.0410](https://vixra.org/1707.0410)],

1.1°)  $(C-B)_{[kn-1]} = 0$ ,  $P = P^\circ n$ ,  $A^n = n^{kn} A^{\circ n}$ ,  $U = A + B - C = n^k u$  ( $u \neq 0$ ,  $k > 1$ ).

1.2°)  $C - A = b^n$ ,  $B = bq$ ;  $A + B = c^n$ ,  $C = cr$ ;  $q^n = Q$ ,  $r^n = R$ ,  $P^\circ = Q' = R' = 1$ ; the numbers  $A^\circ$ ,  $P^\circ$ , n, b, q, c, r – are co-prime.

### Proof of the FLT

2°) Consider the number  $D = (A+B)^n - (C-B)^n - (C-A)^n$ , where  $(C-B)_{[k+2]} = 0$ , from here

2.1°)  $D_{[k+2]} = [(A+B)^n - (C-B)^n - (C-A)^n + (A^n + B^n - C^n)]_{[k+2]} = \{[(A+B)^n - C^n] - [(C-A)^n - B^n]\}_{[k+2]}$ , or

2.2°)  $D_{[k+2]} = \{[c^n(c^{n-1} - r^n)V] - [b^n(b^{n-1} - q)W]\}$ , where  $(c^{n-1} - r)_{[k]} = (b^{n-1} - q)_{[k]} = 0$ ,  $V_{(2)} = W_{(2)} = 10$ ,  $a' = b'$

3°) and therefore,  $D_{[k+2]} = 0$ .

However after removing parenthesis in Newton's binomials in 2° and grouping the summands having equal powers into pairs, we can notice that all pairs end by k+2 zeroes and only the pair in 4°)  $n^{k+1} A^\circ C^{n-1} + n^{k+1} A^\circ B^{n-1}$  ends by k+1 zeroes, because (k+2)-th digit is equal to  $(2A^\circ)'$  (since the numbers  $C^{n-1}$  and  $B^{n-1}$  end by the digit 1 – see SFT), which contradicts to 3°!

From what follows the truth of FLT.

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P.S. The Proof of the first case see [viXra:1809.0571](https://vixra.org/1809.0571).