

# **PMBH theory of representation of gravity field equation and solutions, Hawking Radiation in Data General Relativity theory**

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## **ABSTRACT**

In the general relativity theory, we find the representation of the gravity field equation and solutions. We treat the representation of Schwarzschild solution, Reissner-Nodstrom solution, Kerr-Newman solution, Robertson -Walker solution. We found new general relativity theory (we call it Data General Relativity Theory;DGRT). We treat the data of Hawking radiation by Data general relativity theory. This theory has to apply black hole (specially, Primordial Massive Black Hole; PMBH) because black hole(PMBH) is an idealistic structure.

**PACS Number:04,04.90.+e**

**Key words:General relativity theory,**

**The other solution,**

**Schwarzschild solution,**

**Reissner- Nodstrom solution,**

**Kerr-Newman solution,**

**Robertson-Walker solution**

**Data General relativity theory,**

**Hawking radiation**

**Primordial Massive Black Hole**

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## 1. Introduction

In the general relativity theory, our article's aim is that we find the representation of the gravity field equation and solutions. We found new general relativity theory (we can call it Data General relativity theory). We more obtain data of Hawking radiation by Data general relativity theory.

First, the gravity potential  $g_{\mu\nu}$  is

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu \quad (1)$$

In gravity potential  $g_{\mu\nu}$ , we introduce tensor  $f_{\mu\nu}$  and scalar  $K$ .

In this time, the condition is

$$\frac{\partial K}{\partial x^\lambda} = 0$$

$$\text{i) If } g_{00} = -1, f_{\mu\nu} = g_{\mu\nu}, K = 1 \quad (1\text{-i})$$

$$\text{ii) If } g_{00} \neq -1, f_{\mu\nu} = Kg_{\mu\nu} \quad (1\text{-ii})$$

Hence,

$$\begin{aligned} ds^{12} &= f_{\mu\nu} dx^\mu dx^\nu = \bar{g}_{\mu\nu} d\bar{x}^\mu d\bar{x}^\nu = \bar{g}_{\mu\nu} \frac{\partial \bar{x}^\mu}{\partial \bar{x}^{\prime\alpha}} \frac{\partial \bar{x}^\nu}{\partial \bar{x}^{\prime\beta}} d\bar{x}^{\prime\alpha} d\bar{x}^{\prime\beta} \\ &= \bar{g}'_{\alpha\beta} d\bar{x}^{\prime\alpha} d\bar{x}^{\prime\beta} = f'_{\alpha\beta} dx^{\prime\alpha} dx^{\prime\beta} \end{aligned} \quad (2)$$

$$\begin{aligned} \bar{g}'_{\alpha\beta} &= \bar{g}_{\mu\nu} \frac{\partial \bar{x}^\mu}{\partial \bar{x}^{\prime\alpha}} \frac{\partial \bar{x}^\nu}{\partial \bar{x}^{\prime\beta}}, \quad g_{\mu\nu} = \bar{g}_{\mu\nu}, \quad g'_{\alpha\beta} = \bar{g}'_{\alpha\beta} \\ d\bar{x}^\mu &= \sqrt{K} dx^\mu, \quad d\bar{x}^\nu = \sqrt{K} dx^\nu, \\ d\bar{x}^{\prime\alpha} &= \sqrt{K} dx^{\prime\alpha}, \quad d\bar{x}^{\prime\beta} = \sqrt{K} dx^{\prime\beta} \end{aligned} \quad (3)$$

In Christoffel symbol  $\Gamma^\rho_{\mu\nu}$ ,

$$\bar{\Gamma}^\rho_{\mu\nu} = \frac{1}{2} \bar{g}^{\rho\lambda} \left( \frac{\partial \bar{g}_{\mu\lambda}}{\partial \bar{x}^\nu} + \frac{\partial \bar{g}_{\nu\lambda}}{\partial \bar{x}^\mu} - \frac{\partial \bar{g}_{\mu\nu}}{\partial \bar{x}^\lambda} \right) = \frac{1}{\sqrt{K}} \Gamma^\rho_{\mu\nu} \quad (4)$$

Therefore, in the curvature tensor  $R^\rho_{\mu\nu\lambda}$ ,

$$\begin{aligned} \bar{R}^\rho_{\mu\nu\lambda} &= \frac{\partial \bar{\Gamma}^\rho_{\mu\nu}}{\partial \bar{x}^\lambda} - \frac{\partial \bar{\Gamma}^\rho_{\mu\lambda}}{\partial \bar{x}^\nu} + \bar{\Gamma}^\sigma_{\mu\nu} \bar{\Gamma}^\rho_{\sigma\lambda} - \bar{\Gamma}^\sigma_{\mu\lambda} \bar{\Gamma}^\rho_{\sigma\nu} \\ &= \frac{1}{K} \left( \frac{\partial \Gamma^\rho_{\mu\nu}}{\partial x^\lambda} - \frac{\partial \Gamma^\rho_{\mu\lambda}}{\partial x^\nu} + \Gamma^\sigma_{\mu\nu} \Gamma^\rho_{\sigma\lambda} - \Gamma^\sigma_{\mu\lambda} \Gamma^\rho_{\sigma\nu} \right) = \frac{1}{K} R^\rho_{\mu\nu\lambda} \end{aligned} \quad (5)$$

In Ricci tensor  $R_{\mu\nu}$ ,

$$\bar{R}_{\mu\nu} = \bar{R}^{\rho}{}_{\mu\rho\nu} = \frac{1}{K} R^{\rho}{}_{\mu\rho\nu} = \frac{1}{K} R_{\mu\nu} \quad (6)$$

In curvature scalar  $R$

$$\bar{R} = \bar{g}^{\mu\nu} \bar{R}_{\mu\nu} = \frac{1}{K} g^{\mu\nu} R_{\mu\nu} = \frac{1}{K} R \quad (7)$$

Hence, in the gravity field equation of Einstein,

$$\begin{aligned} \bar{R}_{\mu\nu} - \frac{1}{2} \bar{g}_{\mu\nu} \bar{R} &= \frac{1}{K} (R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R) \\ &= -\frac{8\pi G}{c^4} \frac{1}{K} T_{\mu\nu} \end{aligned} \quad (8)$$

In Newtonian approximation, Energy-momentum tensor  $T_{\mu\nu}$  is

$$\nabla^2 \bar{g}_{00} = \frac{1}{K} \nabla^2 g_{00} \approx -\frac{8\pi G}{c^4} \frac{1}{K} T_{00} = -\frac{8\pi G}{c^4} \bar{T}_{00} \quad (9)$$

$$\rho c^2 = T_{00}, \quad \frac{1}{K} \rho c^2 = \bar{T}_{00} \quad (10)$$

Hence,

$$\frac{1}{K} T_{\mu\nu} = \bar{T}_{\mu\nu} \quad (11)$$

Therefore, revised Einstein's gravity field equation is

$$\bar{R}_{\mu\nu} - \frac{1}{2} \bar{g}_{\mu\nu} \bar{R} = \frac{1}{K} (R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R) = -\frac{1}{K} \frac{8\pi G}{c^4} T_{\mu\nu} = -\frac{8\pi G}{c^4} \bar{T}_{\mu\nu} \quad (12)$$

Therefore, revised gravity field equation of tensor  $\bar{g}_{\mu\nu}$  is able to reduce Einstein's gravity field equation.

Therefore,

$$\begin{aligned} \bar{g}^{\mu\nu} [\bar{R}_{\mu\nu} - \frac{1}{2} \bar{g}_{\mu\nu} \bar{R}] &= \frac{1}{K} g^{\mu\nu} [R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R] = -\frac{8\pi G}{c^4} \frac{1}{K} g^{\mu\nu} T_{\mu\nu} = -\frac{8\pi G}{c^4} \frac{1}{K} T^{\lambda}{}_{\lambda} \\ &= -\frac{8\pi G}{c^4} \bar{g}^{\mu\nu} \bar{T}_{\mu\nu} = -\frac{8\pi G}{c^4} \bar{T}^{\lambda}{}_{\lambda} \\ \rightarrow -\bar{R} &= -\frac{1}{K} R = -\frac{8\pi G}{c^4} \frac{1}{K} T^{\lambda}{}_{\lambda} = -\frac{8\pi G}{c^4} \bar{T}^{\lambda}{}_{\lambda} \end{aligned} \quad (13)$$

Hence,

$$\frac{1}{K} T^{\lambda}_{\lambda} = \bar{T}^{\lambda}_{\lambda} \quad (14)$$

Ricci tensor is

$$\bar{R}_{\mu\nu} = \frac{1}{K} R_{\mu\nu} = -\frac{8\pi G}{c^4} \frac{1}{K} (T_{\mu\nu} - \frac{1}{2} g_{\mu\nu} T^{\lambda}_{\lambda}) = -\frac{8\pi G}{c^4} (\bar{T}_{\mu\nu} - \frac{1}{2} \bar{g}_{\mu\nu} \bar{T}^{\lambda}_{\lambda}) \quad (15)$$

The proper distance is

$$ds^2 = g_{\mu\nu} dx^{\mu} dx^{\nu}, \quad ds^{12} = f_{\mu\nu} dx^{\mu} dx^{\nu} = \bar{g}_{\mu\nu} d\bar{x}^{\mu} d\bar{x}^{\nu} \quad (16)$$

## 2. Weak gravity field approximation.

Weak gravity field approximation is

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}, \quad |h_{\mu\nu}| \ll 1$$

$$R_{\mu\nu} = -\frac{8\pi G}{c^4} (T_{\mu\nu} - \frac{1}{2} g_{\mu\nu} T^{\lambda}_{\lambda}) \quad (17)$$

According to Eq(15),

$$\bar{g}_{\mu\nu} = \bar{\eta}_{\mu\nu} + \bar{h}_{\mu\nu}, \quad |\bar{h}_{\mu\nu}| \ll 1$$

$$\bar{R}_{\mu\nu} = -\frac{8\pi G}{c^4} (\bar{T}_{\mu\nu} - \frac{1}{2} \bar{g}_{\mu\nu} \bar{T}^{\lambda}_{\lambda}) \quad (18)$$

The tensor of weak gravity field is

$$\begin{aligned} R_{\mu\nu} &\approx -\frac{8\pi G}{c^4} S_{\mu\nu}, \quad \bar{R}_{\mu\nu} \approx -\frac{8\pi G}{c^4} \bar{S}_{\mu\nu} \\ S_{\mu\nu} &= T_{\mu\nu} - \frac{1}{2} \eta_{\mu\nu} T^{\lambda}_{\lambda}, \\ \bar{S}_{\mu\nu} &= \bar{T}_{\mu\nu} - \frac{1}{2} \bar{\eta}_{\mu\nu} \bar{T}^{\lambda}_{\lambda} \end{aligned} \quad (19)$$

The solution is

$$\begin{aligned} h_{\mu\nu}(t, \vec{x}) &= \frac{4G}{c^2} \int d^4 x' \frac{S_{\mu\nu}(t - |\vec{x} - \vec{x}'|, \vec{x}')}{|\vec{x} - \vec{x}'|}, \\ \int d^3 x T_{00} &= M, \text{ otherwise } T_{\mu\nu} = 0 \end{aligned} \quad (20)$$

$$\bar{h}_{\mu\nu}(\bar{t}, \bar{\vec{x}}) = \frac{4G}{c^2} \int d^4 \bar{x}' \frac{\bar{S}_{\mu\nu}(\bar{t} - |\bar{\vec{x}} - \bar{\vec{x}}'|, \bar{\vec{x}}')}{|\bar{\vec{x}} - \bar{\vec{x}}'|},$$

$$\int d^3\bar{x}\bar{T}_{00} = \int K\sqrt{K}d^3x\frac{1}{K}T_{00} = \sqrt{KM} = \bar{M} \quad , \quad T_{00} = K\bar{T}_{00}$$

$$\text{otherwise} \quad \frac{1}{K}T_{\mu\nu} = \bar{T}_{\mu\nu} = 0$$
(21)

As

$$\bar{h}_{00}(\bar{x}) \approx \frac{4G}{\bar{r}c^2} \int d^3\bar{x}' [\bar{T}_{00} - \frac{1}{2}\bar{T}_{00}] = \frac{2\sqrt{KGM}}{\bar{r}c^2},$$

$$\bar{h}_{ij}(\bar{x}) \approx \frac{4G}{\bar{r}c^2} \int d^3\bar{x}' [\frac{1}{2}\delta_{ij}\bar{T}_{00}] = \frac{2\sqrt{KGM}}{\bar{r}c^2} \delta_{ij},$$
(22)

The proper distance is

$$-ds^2 = c^2d\tau^2 = -g_{\mu\nu}dx^\mu dx^\nu \approx (1 - \frac{2GM}{rc^2})c^2dt^2 - (1 + \frac{2GM}{rc^2})\delta_{ij}dx^i dx^j$$
(23)

The proper distance is in this theory

$$-ds'^2 = -Kds^2 = Kc^2d\tau^2 = -Kg_{\mu\nu}dx^\mu dx^\nu$$

$$\approx K(1 - \frac{2GM}{rc^2})c^2dt^2 - K(1 + \frac{2GM}{rc^2})\delta_{ij}dx^i dx^j$$

$$= (1 - \frac{2\sqrt{KGM}}{\bar{r}c^2})c^2d\bar{t}^2 - (1 + \frac{2\sqrt{KGM}}{\bar{r}c^2})\delta_{ij}d\bar{x}^i d\bar{x}^j$$

$$= (1 - \frac{2G\bar{M}}{\bar{r}c^2})c^2d\bar{t}^2 - (1 + \frac{2G\bar{M}}{\bar{r}c^2})\delta_{ij}d\bar{x}^i d\bar{x}^j$$

$$\approx \bar{g}_{\mu\nu}d\bar{x}^\mu d\bar{x}^\nu$$

$$\sqrt{K}t = \bar{t}, \sqrt{K}x^i = \bar{x}^i, \sqrt{K}x^j = \bar{x}^j, \sqrt{K}r = \bar{r}, \sqrt{KM} = \bar{M}$$
(24)

### 3. The other representation in Schwarzschild solution, Reissner-Nodstrom solution, Kerr-Newman solution and Robertson-Walker solution

Schwarzschild solution (vacuum solution) is

$$R_{\mu\nu} = 0$$

$$ds^2 = -c^2(1 - \frac{2GM}{rc^2})dt^2 + \frac{dr^2}{1 - \frac{2GM}{rc^2}} + r^2d\theta^2 + r^2\sin^2\theta d\phi^2$$
(25)

The other representation of Schwarzschild solution is

$$\begin{aligned}
ds'^2 &= f_{\mu\nu} dx^\mu dx^\nu = Kg_{\mu\nu} dx^\mu dx^\nu = K \cdot ds^2 \\
&= -c^2 K \left(1 - \frac{2GM}{rc^2}\right) dt^2 + \frac{Kdr^2}{1 - \frac{2GM}{rc^2}} + Kr^2 d\theta^2 + Kr^2 \sin^2 \theta d\phi^2 \\
&= -c^2 \left(1 - \frac{2\sqrt{KGM}}{\bar{r}c^2}\right) d\bar{t}^2 + \frac{d\bar{r}^2}{1 - \frac{2\sqrt{KGM}}{\bar{r}c^2}} + \bar{r}^2 d\bar{\theta}^2 + \bar{r}^2 \sin^2 \bar{\theta} d\bar{\phi}^2 \\
&= -c^2 \left(1 - \frac{2G\bar{M}}{\bar{r}c^2}\right) d\bar{t}^2 + \frac{d\bar{r}^2}{1 - \frac{2G\bar{M}}{\bar{r}c^2}} + \bar{r}^2 d\bar{\theta}^2 + \bar{r}^2 \sin^2 \bar{\theta} d\bar{\phi}^2 = \bar{g}_{\mu\nu} d\bar{x}^\mu d\bar{x}^\nu \\
\sqrt{K}t &= \bar{t}, \quad \sqrt{K}r = \bar{r}, \quad \theta = \bar{\theta}, \quad \phi = \bar{\phi}, \quad \sqrt{KM} = \bar{M}
\end{aligned} \tag{26}$$

Reissner-Nodstrom solution is

$$\begin{aligned}
ds^2 &= g_{\mu\nu} dx^\mu dx^\nu \\
&= -c^2 \left(1 - \frac{2GM}{rc^2} + \frac{kGQ^2}{r^2 c^4}\right) dt^2 + \frac{dr^2}{1 - \frac{2GM}{rc^2} + \frac{kGQ^2}{r^2 c^4}} + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2 \quad (27)
\end{aligned}$$

The other representation of Reissner-Nodstrom solution is

$$\begin{aligned}
ds'^2 &= f_{\mu\nu} dx^\mu dx^\nu = Kg_{\mu\nu} dx^\mu dx^\nu = K \cdot ds^2 \\
&= -Kc^2 \left(1 - \frac{2GM}{rc^2} + \frac{kGQ^2}{r^2 c^4}\right) dt^2 + \frac{Kdr^2}{1 - \frac{2GM}{rc^2} + \frac{kGQ^2}{r^2 c^4}} + Kr^2 d\theta^2 + Kr^2 \sin^2 \theta d\phi^2 \\
&= -c^2 \left(1 - \frac{2\sqrt{KGM}}{\bar{r}c^2} + \frac{KkGQ^2}{\bar{r}^2 c^4}\right) d\bar{t}^2 + \frac{d\bar{r}^2}{1 - \frac{2\sqrt{KGM}}{\bar{r}c^2} + \frac{KkGQ^2}{\bar{r}^2 c^4}} + \bar{r}^2 d\bar{\theta}^2 + \bar{r}^2 \sin^2 \bar{\theta} d\bar{\phi}^2 \\
&= -c^2 \left(1 - \frac{2G\bar{M}}{\bar{r}c^2} + \frac{kG\bar{Q}^2}{\bar{r}^2 c^4}\right) d\bar{t}^2 + \frac{d\bar{r}^2}{1 - \frac{2G\bar{M}}{\bar{r}c^2} + \frac{kG\bar{Q}^2}{\bar{r}^2 c^4}} + \bar{r}^2 d\bar{\theta}^2 + \bar{r}^2 \sin^2 \bar{\theta} d\bar{\phi}^2 \\
&= \bar{g}_{\mu\nu} d\bar{x}^\mu d\bar{x}^\nu
\end{aligned}$$

$$\sqrt{K}t = \bar{t}, \sqrt{K}r = \bar{r}, \theta = \bar{\theta}, \phi = \bar{\phi}, \sqrt{KM} = \bar{M}, KQ^2 = \bar{Q}^2 \quad (28)$$

Kerr-Newman solution is

$$\begin{aligned} ds^2 &= g_{\mu\nu} dx^\mu dx^\nu \\ &= -c^2 \left(1 - \frac{2c^2 GMr - kGQ^2}{c^4 \Sigma}\right) dt^2 + 2(2c^2 MGr - kGQ^2) \frac{a \sin^2 \theta}{c^4 \Sigma} c dt d\phi \\ &\quad - \frac{c^4 \Sigma}{r^2 - c^2 2GMr + a^2 + kGQ^2} dr^2 - \Sigma d\theta^2 \\ &\quad - \sin^2 \theta [r^2 + a^2 + (2c^2 MGr - kGQ^2) \frac{a^2 \sin^2 \theta}{c^4 \Sigma}] d\phi^2 \\ \Sigma &= r^2 + a^2 \cos^2 \theta \end{aligned} \quad (29)$$

The other representation of Kerr-Newman solution is

$$\begin{aligned} ds'^2 &= f_{\mu\nu} dx^\mu dx^\nu = K g_{\mu\nu} dx^\mu dx^\nu = K \cdot ds^2 \\ &= -Kc^2 \left(1 - \frac{2c^2 GMr - kGQ^2}{c^4 \Sigma}\right) dt^2 + 2K(2c^2 MGr - kGQ^2) \frac{a \sin^2 \theta}{c^4 \Sigma} c dt d\phi \\ &\quad - \frac{K\Sigma c^4}{r^2 - 2c^2 GMr + a^2 + kGQ^2} dr^2 - K\Sigma d\theta^2 \\ &\quad - K \sin^2 \theta [r^2 + a^2 + (2c^2 MGr - kGQ^2) \frac{a^2 \sin^2 \theta}{c^4 \Sigma}] d\phi^2 \\ &= -c^2 \left(1 - \frac{2c^2 G\sqrt{KM}\sqrt{Kr} - kGKQ^2}{K\Sigma c^4}\right) d\bar{t}^2 + 2(2c^2 \sqrt{KM}G\sqrt{Kr} - kGKQ^2) \frac{\sqrt{K}a \sin^2 \theta}{K\Sigma c^4} c d\sqrt{K}t d\bar{\phi} \\ &\quad - \frac{K\Sigma c^4}{Kr^2 - 2c^2 G\sqrt{KM}\sqrt{Kr} + Ka^2 + kGKQ^2} d(\sqrt{Kr})^2 - K\Sigma d\bar{\theta}^2 \\ &\quad - \sin^2 \theta [Kr^2 + Ka^2 + (2c^2 G\sqrt{KM}\sqrt{Kr} - kGKQ^2) \frac{Ka^2 \sin^2 \theta}{K\Sigma c^4}] d\bar{\phi}^2 \\ &= -c^2 \left(1 - \frac{2c^2 G\bar{M}\bar{r} - kG\bar{Q}^2}{\bar{\Sigma} c^4}\right) d\bar{t}^2 + 2(2c^2 \bar{M}G\bar{r} - kG\bar{Q}^2) \frac{\bar{a} \sin^2 \bar{\theta}}{\bar{\Sigma} c^4} c d\bar{t} d\bar{\phi} \\ &\quad - \frac{\bar{\Sigma} c^4}{\bar{r}^2 - 2c^2 G\bar{M}\bar{r} + \bar{a}^2 + kG\bar{Q}^2} d\bar{r}^2 - \bar{\Sigma} d\bar{\theta}^2 \\ &\quad - \sin^2 \bar{\theta} [\bar{r}^2 + \bar{a}^2 + (2c^2 G\bar{M}\bar{r} - kG\bar{Q}^2) \frac{\bar{a}^2 \sin^2 \bar{\theta}}{c^4 \bar{\Sigma}}] d\bar{\phi}^2 \\ &= \bar{g}_{\mu\nu} d\bar{x}^\mu d\bar{x}^\nu \end{aligned}$$

$$\bar{\Sigma} = K\Sigma = Kr^2 + Ka^2 \cos^2 \theta = \bar{r}^2 + \bar{a}^2 \cos^2 \bar{\theta}$$

$$\sqrt{K}t = \bar{t}, \quad \sqrt{K}r = \bar{r}, \quad \theta = \bar{\theta}, \quad \phi = \bar{\phi}, \quad \sqrt{KM} = \bar{M}, \quad KQ^2 = \bar{Q}^2, \quad \sqrt{K}a = \bar{a},$$

$$\bar{J} = c\bar{M}\bar{a} = KcMa = KJ \quad (30)$$

In this time, we obtain the data of the time  $t$ , the distance  $r$ , the mass  $M$ , the charge  $Q$  and the angular momentum  $J$ .

Robertson-Walker solution is

$$\begin{aligned} ds^2 &= g_{\mu\nu} dx^\mu dx^\nu \\ &= -c^2 dt^2 + \Omega^2(t) \left[ \frac{dr^2}{1-kr^2} + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2 \right] \\ k &= (-1, 0, 1) \end{aligned} \quad (31)$$

The other representation of Robertson-Walker solution is by Eq(1-i)

$$\begin{aligned} ds^2 &= f_{\mu\nu} dx^\mu dx^\nu = g_{\mu\nu} dx^\mu dx^\nu \\ &= -c^2 d\bar{t}^2 + \bar{\Omega}^2(\bar{t}) \left[ \frac{d\bar{r}^2}{1-k\bar{r}^2} + \bar{r}^2 d\bar{\theta}^2 + \bar{r}^2 \sin^2 \bar{\theta} d\bar{\phi}^2 \right] \\ &= \bar{g}_{\mu\nu} d\bar{x}^\mu d\bar{x}^\nu \\ k &= (-1, 0, 1), \quad t = \bar{t}, \quad \Omega(t) = \bar{\Omega}(\bar{t}), \quad r = \bar{r}, \quad \theta = \bar{\theta}, \quad \phi = \bar{\phi} \end{aligned} \quad (32)$$

#### 4. Obtaining process information of Hawking radiation

Stephen Hawking found black -hole's thermodynamics. By Hawking Radiation, we obtain the new data from formulas of black-hole's thermodynamics. We start the obtaining process informations of Hawking Radiation. In Wikipedia (Hawking Radiation), we know formulas of Hawking Radiation.

The radiation temperature  $T$  of Schwarzschild black hole (In this theory, PMBH)

$$T = \frac{\hbar c^3}{8\pi GMk_B} \quad (33)$$

The radiation temperature  $\bar{T}$  is in Data General Relativity theory.

$$\bar{T} = \frac{\hbar c^3}{8\pi GMk_B} = \frac{\hbar c^3}{8\pi G\sqrt{KM}k_B} = \frac{T}{\sqrt{K}} \quad (34)$$

The black hole (PMBH)'s entropy

$$\begin{aligned} dS &= 8\pi Gk_B M dM / \hbar c = \frac{8\pi GMk_B}{\hbar c^3} c^2 dM = \frac{dQ}{T}, \\ dQ &= c^2 dM \end{aligned} \quad (35)$$

The black-hole (PMBH)'s entropy  $\bar{S}$  is in Data General Relativity theory.

$$\begin{aligned}
d\bar{S} &= 8\pi\bar{M}d\bar{M}Gk_B / \hbar c = \frac{8\pi Gk_B\bar{M}}{\hbar c^3} c^2 d\bar{M} = \frac{d\bar{Q}}{\bar{T}} \\
&= \frac{8\pi Gk_B\sqrt{KM}}{\hbar c^3} c^2 d(\sqrt{KM}) \\
&= K \frac{8\pi Gk_B M}{\hbar c^3} c^2 dM \\
&= K \frac{dQ}{T} = K dS, dQ = c^2 dM \\
d\bar{Q} &= c^2 d\bar{M} = \sqrt{K} c^2 dM = \sqrt{K} dQ \\
\bar{S} &= KS, \quad \bar{Q} = \sqrt{K} Q
\end{aligned} \tag{36}$$

Black-hole (PMBH) radiation's power  $P_{ev}$  is

$$P_{ev} = A_s \varepsilon \sigma T^4, \quad A_s = 4\pi r_s^2, \quad r_s = \frac{2GM}{c^2}, \quad \varepsilon, \sigma \text{ is constant} \tag{37}$$

Black-hole (PMBH) radiation's power  $\bar{P}_{ev}$  is in Data General Relativity theory.

$$\begin{aligned}
\bar{A}_s &= 4\pi\bar{r}_s^2 = K4\pi r_s^2 = KA_s, \quad \bar{r}_s = \frac{2G\bar{M}}{c^2} = \frac{2G\sqrt{KM}}{c^2} = \sqrt{K} r_s \\
\bar{P}_{ev} &= \bar{A}_s \varepsilon \sigma \bar{T}^4 = KA_s \varepsilon \sigma \frac{T^4}{K^2} = \frac{P_{ev}}{K}
\end{aligned}$$

$$\text{Stefan-Boltzmann constant } \sigma = \frac{\pi^2 k_B^4}{60 \hbar^3 c^2},$$

Black-hole (PMBH) is a perfect black body ( $\varepsilon = 1$ )

(38)

The evaporation time  $t_{ev}$  of a black hole (PMBH) is

$$t_{ev} = \frac{5120 \pi G^2 M^3}{\hbar c^4} \tag{39}$$

The evaporation time  $\bar{t}_{ev}$  of a black hole (PMBH) is in Data General Relativity theory.

$$\bar{t}_{ev} = \frac{5120 \pi G^2 \bar{M}^3}{\hbar c^4} = \frac{5120 \pi G^2 K \sqrt{KM}^3}{\hbar c^4} = K \sqrt{K} t_{ev} \tag{40}$$

The power of evaporation energy of the black-hole (PMBH) is

$$P_{ev} = -\frac{dE_{ev}}{dt_{ev}} \quad (41)$$

The power of evaporation energy of the black-hole (PMBH) is in Data General Relativity theory.

$$\bar{P}_{ev} = -\frac{d\bar{E}_{ev}}{d\bar{t}_{ev}} = -\frac{d(E_{ev}\sqrt{K})}{K\sqrt{K}dt_{ev}} = \frac{P_{ev}}{K},$$

$$\bar{M}_{ev}c^2 = \bar{E}_{ev} = \sqrt{K}E_{ev} = \sqrt{K}M_{ev}c^2 \quad (42)$$

## 5. PMBH Data and DGRT Data

In DGRT, we have to apply only black-holes (PMBHs).

According to [27]Paul H. Frampton, Physical Letter B(2017), if the mass of sun is  $M_{\odot}$ , data is

Table 1.

Astrophysical oboect	Mass solar masses	Period $\tau$ seconds	Angular momentum $\text{kgkm}^2/\text{s}$
PIMBH1	$20M_{\odot}$	0.013s	$3.0 \times 10^{37}$
PIMBH2	$100M_{\odot}$	0.063s	$7.2 \times 10^{38}$
PIMBH3	$1000M_{\odot}$	0.63s	$7.2 \times 10^{40}$
PIMBH4	$10^4 M_{\odot}$	6.3s	$7.2 \times 10^{42}$
PIMBH5	$10^5 M_{\odot}$	63s	$7.2 \times 10^{44}$
PSMBH6(M87)	$6 \times 10^9 M_{\odot}$	$3.8 \times 10^6 \text{s}$	$2.6 \times 10^{54}$

According to DGRT, BH (PMBH)'s mass  $M$  is to be  $\sqrt{K}M$ , time  $\tau$  is to be  $\tau\sqrt{K}$ , Angular momentum  $J$  is to be  $KJ$ . Hence, PIMBH2's (from PIMBH1)  $\sqrt{K}$  is 5, PIMBH3's (from PIMBH 2)  $\sqrt{K}$  is 10, PIMBH4's (from PIMBH3)  $\sqrt{K}$  is 10, PIMBH5's (from PIMBH4)  $\sqrt{K}$  is 10, PSMBH6's (from PIMBH5)  $\sqrt{K}$  is  $6 \times 10^4$ .

In this time, PIMBH is Primordial Intermediate Massive Black hole, PSMBH is Primordial Super Massive Black Hole. According to [27]"Angular momentum of dark matter black holes",

$$20M_{\odot} \leq M_{PIMBH} \leq 100,000M_{\odot}$$

$$10^5M_{\odot} \leq M_{PSMBH} \leq 10^{17}M_{\odot}$$

Therefore, calculated data is in DGRT,

Table 2.

Astrophysical oboect	Mass solar	Period $\tau$ seconds	Angular momentum $\text{kgkm}^2/\text{s}$
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	masses		
PIMBH1	20M <sub>⊙</sub>	0.013s	3.0 × 10 <sup>37</sup>
PIMBH2	100M <sub>⊙</sub>	0.065s	7.5 × 10 <sup>38</sup>
PIMBH3	1000M <sub>⊙</sub>	0.65s	7.5 × 10 <sup>40</sup>
PIMBH4	10 <sup>4</sup> M <sub>⊙</sub>	6.5s	7.5 × 10 <sup>42</sup>
PIMBH5	10 <sup>5</sup> M <sub>⊙</sub>	65s	7.5 × 10 <sup>44</sup>
PSMBH6(M87)	6 × 10 <sup>9</sup> M <sub>⊙</sub>	3.9 × 10 <sup>6</sup> s	2.7 × 10 <sup>54</sup>

If we compare Table 1. and Table 2., we know DGRT has to apply PMBHs.

## 6. Conclusion

We find the other representation of solutions in the General relativity theory. We more obtain the information of black-hole thermodynamics in Data General Relativity theory.

If we use variable  $\bar{A}$  instead of  $A$ , Data General Relativity theory is reduced to normal general relativity theory. This theory's remarkable thing is if  $\sqrt{K} = 2$  and black hole (PMBH)'s mass  $M$  is  $M\sqrt{K} = 2M$ , black hole (PMBH)'s distant of gravitation  $r$  is  $r\sqrt{K} = 2r$ , black hole (PMBH)'s proper time  $\tau$  is  $\tau\sqrt{K} = 2\tau$ . If rotating black hole (PMBH)'s mass  $M$  is to be  $M\sqrt{K} = 2M$ , we predict the angular momentum  $J$  of the black-hole (PMBH) is to be  $KJ = 4J$ .

In this time, we have to apply only black-holes (PMBHs) because black hole (PMBH) is an idealistic structure. BH is Black hole.

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