

# SADASC'18 THE INTERNATIONAL CONFERENCE

## ON SMART APPLICATION & DATA ANALYSIS FOR SMART CITIES

27 - 28 feb  
**2018**

**Hotel Idou Anfa  
Casablanca  
MOROCCO**

### SESSIONS

- |   |   |   |   |
|---|---|---|---|
|  | Smart Cities  |  | IoT and Cloud Computing                   |
|  | IoT and Big Data  |  | Software Engineering                      |
|  | Communication and Network Protocols   |  | Machine Learning And Applications         |
|  | Intelligent and Industrial Systems, Robot Interaction, Control, Communication and Corporation |  | Lean and TPM in Manufacturing environment |
|  | Electrical and Electronic Systems   |  | Biotechnology                             |

VISIT US  
[WWW.SADASC.NET](http://WWW.SADASC.NET)



- 
- 17) Soukaina Merzouk, Sakina Elhadi, Abdessamad Cherkaoui, Abdelaziz Marzak and Nawal Sael. [Agile Software Development: Comparative study](#)
  - 18) Ihab Agha, Jaafar Gaber and Maxim Wack. [A Physiological Approach for Minimizing Dead Reckoning Velocity Readings Drifts.](#)
  - 19) Houda Zaim, Mohammed Ramdani and Adil Haddi. [A Model of E-Commerce Self-Assessment System Based on E-Customer Behavior.](#)
  - 20) Ismail El Moudden, Houda Jouhari, Mounir Ouzir. Souad ElBernoussi, [Learned Model For Human Activity Recognition Based On Dimensionality Reduction.](#)

**Session 2.2 (Communication and network protocols) (salle 2)**

- 21) Safa Saadaoui, Mohamed Tabaa, Fabrice Monteiro, Mouhamad Chehaitly, Abbas Dandache and Karim Alami. [Industrial WSN based on Discrete Wavelet Packet Transform for Smart Factory Wireless communications.](#)
- 22) Mohamed Amine Boukhal, Ismail Lagrat and Omar Elbannay. [Design and Implementation of multicore system for Wireless intelligent control.](#)
- 23) Sara Tamy, Nabila Rabbah, Mahmoud Almostafa Rabbah, Mounir Rifi and Hicham Belhadaoui. [Study of strategies for real-time supervision of industrial network security.](#)
- 24) Souad Ezzbady, Abdelwahad Namir and Sanaa El Filali. [Contribution, Modeling and Conception of a fraud detector to securing connections in a communications network.](#)
- 25) Rana Abdallah, Raed Kouta, Jaafar Gaber, Charles Sarraf and Maxime Wack. [Reliability of data transmission of UAVs.](#)

**session 3.1 (Machine learning & applications) (salle 1)**

- 26) Assia Mezhar, Amal El Mzabi and Mohammed Ramdani. [Towards a novel weakly supervised joint approach of Named Entity Recognition and Normalization for noisy text.](#)
- 27) Walid Cherif, Abdellah Madani and Mohamed Kissi. [A Novel Similarity-based Algorithm for supervised binary classification: Sandalwood odor application.](#)
- 28) Elmahdi Khoudry, Abdelaziz Belfqih, Jamal Boukherouaa, Faissal El Mariami, Abdelmajid Berdai and Mohamed Nouh Dazahra. [Empirical Mode Decomposition and Cascade Feed-Forward Artificial Neural Network based Intelligent Fault Classifier.](#)
- 29) Hicham Moutachaouik, Ismail El moudden. [Mining Prostate Cancer Behavior using Parsimonious Factors and Shrinkage Methods.](#)
- 30) Mohammed Lahraichi, Khalid Housni and Samir Mbarki. [Foreground Detection using Mean Shift and LBP.](#)
- 31) Said Broumi, Assia Bakali, Mohamed Talea, Florentin Smarandache and Kifayat Ullah. [Bipolar Neutrosophic Minimum Spanning Tree.](#)

**session 3.2 (Intelligent and Industrial Systems, Robot Interaction, Control, Communication and Cooperation) (salle 2)**

- 32) Rabbah Mahmoud Almostafa, Rabbah Nabil, Hicham Belhadaoui and Mounir Rifi. [Python In Real Time Application For Mobile Robot.](#)
- 33) Abderrahmane Jarrou, Dominique Sauter, Karim Alami, Brahim AbouaibChouri and Abdellah Ailane. [Model predictive control \(MPC\) for building optimal temperature control.](#)

# Bipolar Neutrosophic Minimum Spanning Tree

Said Broumi

Laboratory of Information Processing, Faculty of Science  
Ben M'Sik, University Hassan II, B.P 7955, Sidi Othman,  
Casablanca, Morocco  
broumisaid78@gmail.com

Assia Bakali

Ecole Royale Navale, Boulevard Sour Jdid, B.P 16303  
Casablanca, Morocco.  
assiabakali@yahoo.fr

Mohamed Talea

Laboratory of Information Processing, Faculty of Science  
Ben M'Sik, University Hassan II, B.P 7955, Sidi Othman,  
Casablanca, Morocco  
taleamohamed@yahoo.fr

Florentin Smarandache

Department of Mathematics, University of New Mexico,  
705 Gurley Avenue, Gallup, NM 87301, USA  
fsmarandache@gmail.com; smarand@unm.edu

Kifayat Ullah

Department of Mathematics and Statistics, International Islamic University, Islamabad.  
kifayat.phdma72@iiu.edu.pk

**Abstract**— The aim of this article is to introduce a matrix algorithm for finding minimum spanning tree (MST) in the environment of undirected bipolar neutrosophic connected graphs (UBNCG). Some weights are assigned to each edge in the form of bipolar neutrosophic number (BNN). The new algorithm is described by a flow chart and a numerical example by considering some hypothetical graph. By a comparison, the advantage of proposed matrix algorithm over some existing algorithms are also discussed.

**Keywords**—Neutrosophic sets, bipolar neutrosophic sets, spanning tree problem, score function.

## I. INTRODUCTION

The concept of neutrosophic set (NS) in 1998 was proposed by Smarandache [1], from the philosophical point of view, to represent uncertain, imprecise, incomplete, inconsistent, and indeterminate information that are exist in the real world. The concept of the classic set, fuzzy set and intuitionistic fuzzy set (IFS) is generalized by the concept of neutrosophic set. Within the real standard or non-standard unit interval  $]^{-}0, 1^{+}[$ , the neutrosophic sets are categorized into three membership functions called truth-membership function ( $t$ ), an indeterminate-membership function ( $i$ ) and a false-membership function ( $f$ ). For the first, Smarandache [1] introduced the single valued neutrosophic set (SVNS) to apply in science and engineering applications. Later on, some properties related to single valued neutrosophic sets was studied by Wang et al.[2]. For dealing with real, scientific, and engineering applications, the neutrosophic set model is an important tool because it can handle not only incomplete information but also the inconsistent information and indeterminate information. One may refer to regarding the basic theory of NS, SVNS and their extensions with applications in several fields. Many researches making particularizations on the T, I, F components

which leads to define particular case of neutrosophic sets such as simplified neutrosophic sets [20], interval valued neutrosophic sets [22], bipolar neutrosophic sets [23], trapezoidal neutrosophic set [24], rough neutrosophic set [25] and so on. As a special case of NSs, Ye[24] introduced the concept of single-valued trapezoidal neutrosophic set. In addition, a new ranking method to define the concept of cut sets for SVTNNs were proposed by Deli and Subas [26]. The authors applied it for solving MCDM problem. Mumtaz et al.[28] defined the concept of bipolar neutrosophic soft sets and applied it to decision making problem.

Prim and Kruskal algorithm are the common algorithms for searching the minimum spanning tree including in classical graph theory. A new theory is developed and called single valued neutrosophic graph theory (SVNGT) by applying the concept of single valued neutrosophic sets on graph theory. The concept of SVNGT and their extensions finds its applications in diverse fields [6-19]. To search the minimum spanning tree in neutrosophic environment recently few researchers have used neutrosophic methods. Ye [4] developped a method to find minimum spanning tree of a graph where nodes (samples) are represented in the form of SVNS and distance between two nodes which represents the dissimilarity between the corresponding samples has been derived. To cluster the data represented by double-valued neutrosophic information, Kandasamy [3] proposed a double-valued Neutrosophic Minimum Spanning Tree (DVN-MST) clustering algorithm. A solution approach of the optimum spanning tree problems considering the inconsistency, incompleteness and indeterminacy of the information, which was proposed by Mandal and Basu [5]. The authors consider a network problem with multiple criteria, which are represented by weight of each edge in neutrosophic set. The approach proposed by the authors is based on similarity measure. In another paper, Mullai [20] discussed the MST problem on a graph in which a bipolar

neutrosophic number is associated to each edge as its edge length, and illustrated it by a numerical example.

The main objective of this paper is to present a neutrosophic version of Kruskal algorithm for searching the cost minimum spanning tree of an undirected graph in which a bipolar neutrosophic number is associated to each edge as its edge length.

The rest of the paper is organized as follows. The concepts of neutrosophic sets, single valued neutrosophic sets, bipolar neutrosophic sets and the score function of bipolar neutrosophic number are briefly presented in section 2. A novel approach for finding the minimum spanning tree of neutrosophic undirected graph is proposed in section 3. A numerical example is presented to illustrate the proposed method in Section 4. A comparative study with existing methods is proposed in section 5, Finally, the main conclusion is presented in section 6.

## II. Preliminaries

Some of the important background knowledge for the materials that are presented in this paper is presented in this section. These results can be found in [1, 2, 23].

**Definition 2.1** [1] Let  $\xi$  be a universal set. The neutrosophic set A on the universal set  $\xi$  categorized into three membership functions called the true  $T_A(x)$ , indeterminate  $I_A(x)$  and false  $F_A(x)$  contained in real standard or non-standard subset of  $]0, 1+[$  respectively.

$$-0 \leq \sup T_A(x) + \sup I_A(x) + \sup F_A(x) \leq 3 \quad (1)$$

**Definition 2.2** [2] Let  $\xi$  be a universal set. The single valued neutrosophic sets (SVNs) A on the universal  $\xi$  is denoted as following

$$A = \{< x: T_A(x), I_A(x), F_A(x) > | x \in \xi\} \quad (2)$$

The functions  $T_A(x) \in [0, 1]$ ,  $I_A(x) \in [0, 1]$  and  $F_A(x) \in [0, 1]$  are named degree of true, indeterminate and false membership of x in A, satisfy the following condition:

$$0 \leq T_A(x) + I_A(x) + F_A(x) \leq 3 \quad (3)$$

**Definition 2.3** [23]. A bipolar neutrosophic set A in  $\xi$  is defined as an object of the form

$A = \{<x, T^p(x), I^p(x), F^p(x), T^n(x), I^n(x), F^n(x)> | x \in X\}$ , where  $T^p, I^p, F^p: \xi \rightarrow [1, 0]$  and  $T^n, I^n, F^n: \xi \rightarrow [-1, 0]$ . The positive membership degree  $T^p(x)$ ,  $I^p(x)$ ,  $F^p(x)$  denotes the true membership, indeterminate membership and false membership of an element  $x \in \xi$  corresponding to a bipolar neutrosophic set A and the negative membership degree  $T^n(x)$ ,  $I^n(x)$ ,  $F^n(x)$  denotes the true membership, indeterminate membership and false membership of an element  $x \in \xi$  to some implicit counter-property corresponding to a bipolar neutrosophic set A.

To compare two Bipolar neutrosophic numbers (abbr.BNNs), Deli et al.[23] introduced the concept of score function and in case where the score value of two BNNs are same, they can be distinguished by using accuracy function and certainty function as follow

**Definition 2.4**[23]. Let  $\tilde{A} = < T^p, I^p, F^p, T^n, I^n, F^n >$  be a bipolar neutrosophic number, then, the score function  $s(\tilde{A})$ , accuracy function  $a(\tilde{A})$  and certainty function  $c(\tilde{A})$  of a BNN are defined as follows:

$$(i) \quad s(\tilde{A}) = \left( \frac{1}{6} \right) \times \left[ T^p + 1 - I^p + 1 - F^p + 1 + T^n - I^n - F^n \right] \quad (4)$$

$$(ii) \quad a(\tilde{A}) = T^p - F^p + T^n - F^n \quad (5)$$

$$(iii) \quad c(\tilde{A}) = T^p - F^n \quad (6)$$

For any two BNNs  $\tilde{A}_1$  and  $\tilde{A}_2$ :

- i. If  $s(\tilde{A}_1) > s(\tilde{A}_2)$ , then  $\tilde{A}_1$  is greater than  $\tilde{A}_2$ , that is,  $\tilde{A}_1$  is superior to  $\tilde{A}_2$ , denoted by  $\tilde{A}_1 > \tilde{A}_2$
- ii. If  $s(\tilde{A}_1) = s(\tilde{A}_2)$  and  $a(\tilde{A}_1) > a(\tilde{A}_2)$ , then  $\tilde{A}_1$  is greater than  $\tilde{A}_2$ , that is,  $\tilde{A}_1$  is superior to  $\tilde{A}_2$ , denoted by  $\tilde{A}_1 > \tilde{A}_2$
- iii. If  $s(\tilde{A}_1) = s(\tilde{A}_2)$ ,  $a(\tilde{A}_1) = a(\tilde{A}_2)$ , and  $c(\tilde{A}_1) > c(\tilde{A}_2)$  then  $\tilde{A}_1$  is greater than  $\tilde{A}_2$ , that is,  $\tilde{A}_1$  is superior to  $\tilde{A}_2$ , denoted by  $\tilde{A}_1 > \tilde{A}_2$
- iv. If  $s(\tilde{A}_1) = s(\tilde{A}_2)$ ,  $a(\tilde{A}_1) = a(\tilde{A}_2)$ , and  $c(\tilde{A}_1) = c(\tilde{A}_2)$  then  $\tilde{A}_1$  is equal to  $\tilde{A}_2$ , that is,  $\tilde{A}_1$  is indifferent to  $\tilde{A}_2$ , denoted by  $\tilde{A}_1 = \tilde{A}_2$

## III. MINIMUM SPANNING TREE ALGORITHM OF BN- UNDIRECTED GRAPH

In this section, a neutrosophic version of Kruskal algorithm is proposed to handle minimum spanning tree in a bipolar neutrosophic environment. In the following, we propose a bipolar neutrosophic minimum spanning tree algorithm, whose steps are defined below:

### Algorithm:

**Input:** The weight matrix  $M = [W_{ij}]_{n \times n}$  for the undirected weighted neutrosophic graph  $G$ .

**Output:** Minimum cost Spanning tree  $T$  of  $G$ .

**Step 1:** Input neutrosophic adjacency matrix  $A$ .

**Step 2:** Translate the BN-matrix into score matrix  $[S_{ij}]_{n \times n}$  by using score of bipolar neutrosophic number.

**Step 3:** Iterate step 4 and step 5 until all  $(n - 1)$  entries matrix of  $S$  are either marked or set to zero or other words all the nonzero elements are marked.

**Step 4:** Find the score matrix  $S$  either columns-wise or row-wise to find the unmarked minimum entries  $S_{ij}$ , which is the weight of the corresponding edge  $e_{ij}$  in  $S$ .

**Step 5:** If the corresponding edge  $e_{ij}$  of selected  $S_{ij}$  produce a cycle with the previous marked entries of the score matrix  $S$  then set  $S_{ij} = 0$  else mark  $S_{ij}$ .

**Step 6:** Building the graph  $T$  including only the marked entries from the score matrix  $S$  which shall be desired minimum cost spanning tree of  $G$ .

**Step 7:** Stop.

An illustrative flow chart of the given algorithm is presented in fig. 3.

#### IV. NUMERICAL EXAMPLE

In this section, a numerical example is explained based on the above algorithm. Consider a hypothetical graph with edge values are given in the table below.

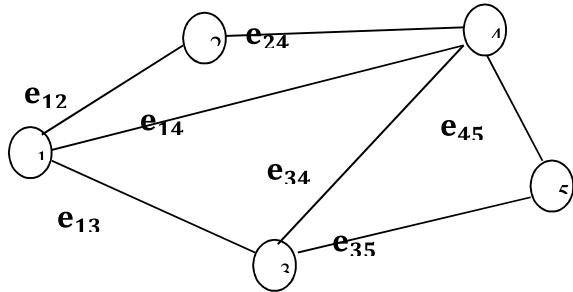


Fig 2. Undirected bipolar neutrosophic- graphs

E	Edge length
$e_{12}$	$< 0.3, 0.1, 0.2, -0.8, -0.5, -0.1 >$
$e_{13}$	$< 0.4, 0.5, 0.4, -0.2, -0.4, -0.5 >$
$e_{14}$	$< 0.6, 0.7, 0.8, -0.6, -0.4, -0.4 >$
$e_{24}$	$< 0.4, 0.8, 0.3, -0.2, -0.5, -0.7 >$
$e_{34}$	$< 0.2, 0.3, 0.7, -0.2, -0.4, -0.4 >$
$e_{35}$	$< 0.4, 0.6, 0.5, -0.4, -0.4, -0.3 >$
$e_{45}$	$< 0.5, 0.4, 0.3, -0.4, -0.5, -0.8 >$

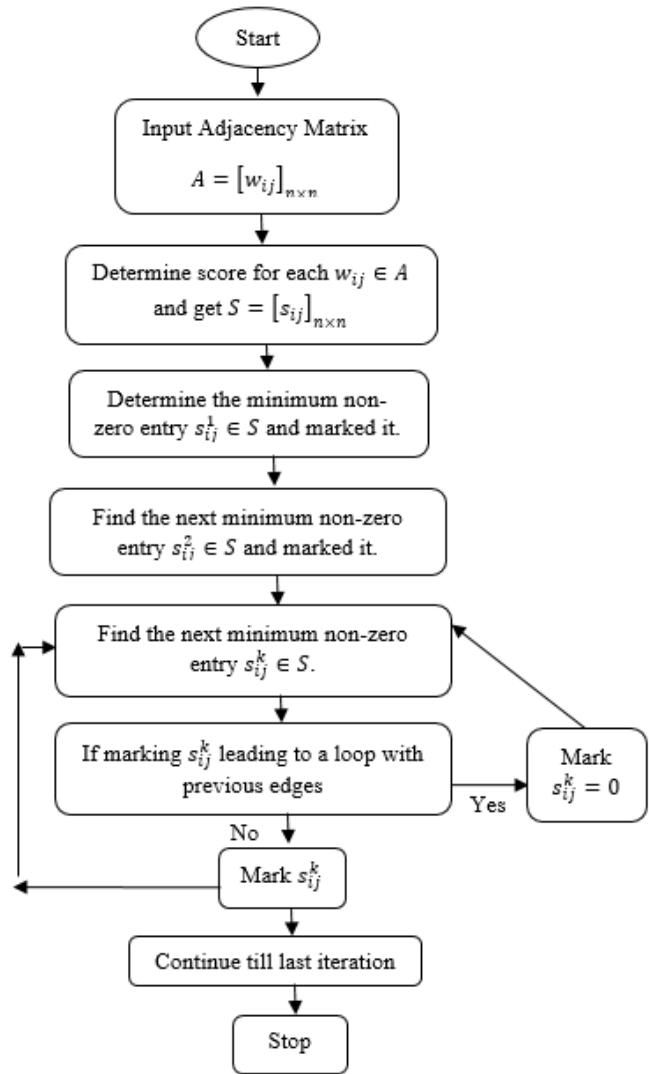


Fig. 3 (Flow chart describing proposed algorithm)

The BN- adjacency matrix  $A$  is given below:

$$\begin{aligned}
 &= \\
 &\begin{bmatrix}
 0 & < 0.3, 0.1, 0.2, -0.8, -0.5, -0.1 > \\
 < 0.3, 0.1, 0.2, -0.8, -0.5, -0.1 > & 0 \\
 < 0.4, 0.5, 0.4, -0.2, -0.4, -0.5 > & 0 \\
 < 0.6, 0.7, 0.8, -0.6, -0.4, -0.4 > & < 0.4, 0.8, 0.3, -0.2, -0.5, -0.7 > \\
 0 & 0 \\
 < 0.4, 0.5, 0.4, -0.2, -0.4, -0.5 > & < 0.6, 0.7, 0.8, -0.6, -0.4, -0.4 > \\
 0 & < 0.4, 0.8, 0.3, -0.2, -0.5, -0.7 > \\
 0 & < 0.2, 0.3, 0.7, -0.2, -0.4, -0.4 > \\
 < 0.2, 0.3, 0.7, -0.2, -0.4, -0.4 > & 0 \\
 < 0.4, 0.6, 0.5, -0.4, -0.4, -0.3 > & < 0.5, 0.4, 0.3, -0.4, -0.5, -0.8 > \\
 0 & \\
 < 0.4, 0.6, 0.5, -0.4, -0.4, -0.3 > & \\
 < 0.5, 0.4, 0.3, -0.4, -0.5, -0.8 > & \\
 0 &
 \end{bmatrix}$$

Hence, using the score function introduced in definition 2.1, we get the score matrix

$$S = \begin{bmatrix} 0 & 0.47 & 0.53 & \textcolor{red}{0.38} & 0 \\ 0.47 & 0 & 0 & 0.55 & 0 \\ 0.53 & 0 & 0 & 0.52 & 0.43 \\ 0.38 & 0.55 & 0.52 & 0 & 0.62 \\ 0 & 0 & 0.43 & 0.62 & 0 \end{bmatrix}$$

Fig. 4. Score matrix

Clearly from figure 4, it is observed that 0.38 is the least value so edge (1, 4) is marked as red as shown in figure 5. This process shall be continued until last iteration.

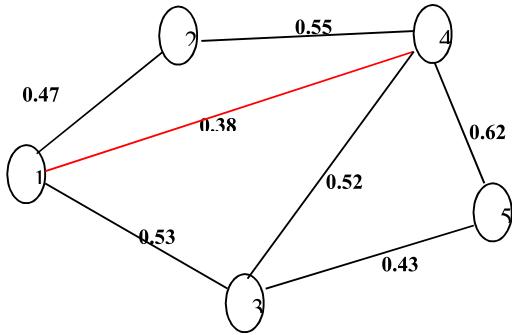


Fig. 5

Clearly from the figure 6, the next non zero minimum entries 0.43 is marked and colored corresponding edge (3, 5) is given in figure 7.

$$S = \begin{bmatrix} 0 & 0.47 & 0.53 & \textcolor{red}{0.38} & 0 \\ 0.47 & 0 & 0 & 0.55 & 0 \\ 0.53 & 0 & 0 & 0.52 & 0.43 \\ 0.38 & 0.55 & 0.52 & 0 & 0.62 \\ 0 & 0 & \textcolor{red}{0.43} & 0.62 & 0 \end{bmatrix}$$

Fig. 6

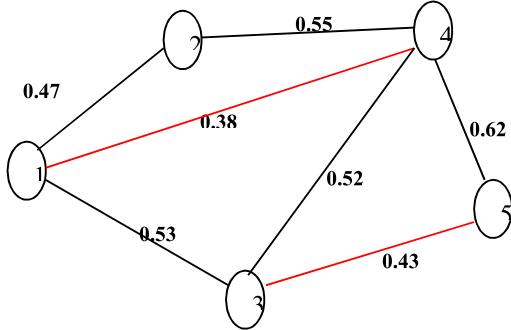


Fig 7

$$S = \begin{bmatrix} 0 & \textcolor{red}{0.47} & 0.53 & \textcolor{red}{0.38} & 0 \\ 0.47 & 0 & 0 & 0.55 & 0 \\ 0.53 & 0 & 0 & 0.52 & 0.43 \\ 0.38 & 0.55 & 0.52 & 0 & 0.62 \\ 0 & 0 & \textcolor{red}{0.43} & 0.62 & 0 \end{bmatrix}$$

Fig.8

Clearly from the figure 8, the next minimum non-zero element 0.47 is marked and the colored corresponding edge is given in figure 9.

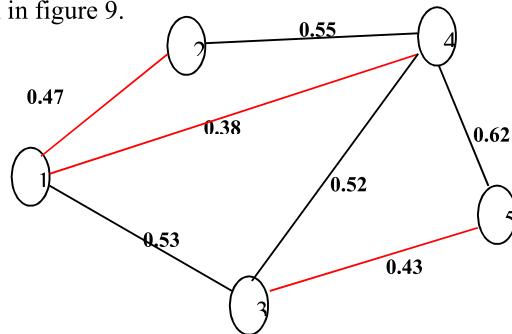


Fig 9

Clearly from the figure 10. The next minimum non-zero element 0.52 is marked, and colored corresponding edge (3, 4) is given in figure 11.

$$S = \begin{bmatrix} 0 & \textcolor{red}{0.47} & 0.53 & \textcolor{red}{0.38} & 0 \\ 0.47 & 0 & 0 & 0.55 & 0 \\ 0.53 & 0 & 0 & \textcolor{red}{0.52} & 0.43 \\ 0.38 & 0.55 & 0.52 & 0 & 0.62 \\ 0 & 0 & \textcolor{red}{0.43} & 0.62 & 0 \end{bmatrix}$$

Fig.10

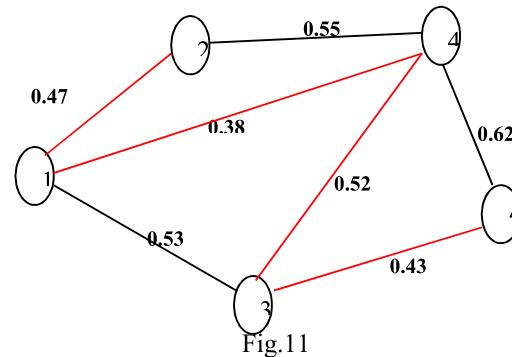


Fig.11

Clearly from the figure 12. The next minimum non-zero element 0.53 is marked. But while drawing the edges it produces the cycle. So we reject and mark it as 0 instead of 0.53

$$S = \begin{bmatrix} 0 & \textcolor{red}{0.47} & 0.53 & \textcolor{red}{0.38} & 0 \\ 0.47 & 0 & 0 & 0.55 & 0 \\ \textcolor{red}{0.53} & 0 & 0 & \textcolor{red}{0.52} & 0.43 \\ 0.38 & 0.55 & 0.52 & 0 & 0.62 \\ 0 & 0 & \textcolor{red}{0.43} & 0.62 & 0 \end{bmatrix}$$

Fig.12

The next least value is 0.55 but including this edge results in the formation of a cycle. So this value is marked as zero as shown in the figure 13.

$$S = \begin{bmatrix} 0 & 0.47 & 0.53 & 0.38 & 0 \\ 0.47 & 0 & 0 & 0.55 & 0 \\ 0.53 & 0 & 0 & 0.52 & 0.43 \\ 0.38 & 0.55 & 0.52 & 0 & 0.62 \\ 0 & 0 & 0.43 & 0.62 & 0 \end{bmatrix}$$

Fig .13

Clearly from the figure 14. The next minimum non-zero element 0.62 is marked. But while drawing the edges it produces the cycle. So we reject and mark it as 0 instead of 0.62.

$$S = \begin{bmatrix} 0 & 0.47 & 0.53 & 0.38 & 0 \\ 0.47 & 0 & 0 & 0.55 & 0 \\ 0.53 & 0 & 0 & 0.52 & 0.43 \\ 0.38 & 0.55 & 0.52 & 0 & 0.62 \\ 0 & 0 & 0.43 & 0.62 & 0 \end{bmatrix}$$

Fig .14

After the above steps, the final path of minimum cost of spanning tree of  $G$  is given in figure 15.

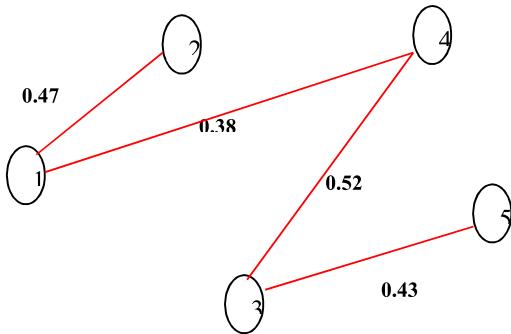


Fig .15. Final path of minimum cost of spanning tree of  $G$  .

Following the steps of proposed algorithm presented in section 3. Therefore the crisp minimum cost spanning tree is 1,8 and the final path of minimum cost of spanning tree is {2,1},{1,4},{4,3},{3,5}.

## V. COMPARATIVE STUDY

In this section, the same process is carried out by the algorithm of Mullai et al [20]. The results obtained in different iterations by this existing algorithm are illustrated below.

Let  $C_1 = \{1\}$  and  $\overline{C}_1 = \{2, 3, 4, 5\}$

Iteration 2:

Let  $C_2 = \{1, 4\}$  and  $\overline{C}_2 = \{2, 3, 5\}$

Iteration 3:

Let  $C_3 = \{1, 4, 3\}$  and  $\overline{C}_3 = \{2, 5\}$

Iteration 4:

Let  $C_4 = \{1, 4, 5, 3\}$  and  $\overline{C}_4 = \{2\}$

Based on these iterations of Mullai's algorithm, we have the following MST.

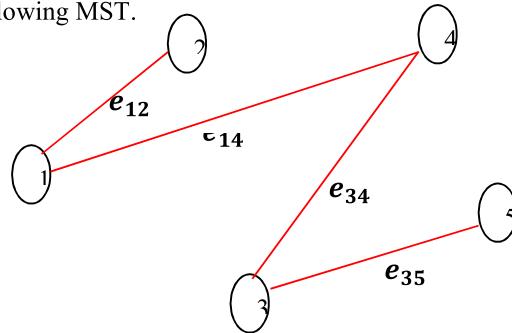


Fig .16.MST obtained by Mullai's Algorithm

This comparison makes the point that that both the existing and new algorithm leads to the same results.

The advantage of new algorithm over existing algorithm is that the new algorithm is matrix based and can be easily performed in MATLAB while Mullai's algorithm is based on edge comparison and is difficult to be performed.

## VI. CONCLUSION

This paper considers a minimum spanning tree problem under the situation where the weights of edges are represented by BNNs. It is discussed how proposed algorithm is better in formulation and implementation. This work can be extended to the case of directed neutrosophic graphs and other types of neutrosophic graphs such as interval valued bipolar neutrosophic graphs

## ACKNOWLEDGMENT

The authors are very grateful to the chief editor and reviewers for their comments and suggestions, which is helpful in improving the paper.

## REFERENCES

- [1] F. Smarandache, Neutrosophy. Neutrosophic Probability, Set, and Logic, ProQuest Information & Learning, Ann Arbor, Michigan, USA, 1998, 105 pages.
- [2] H. Wang, F.Smarandache, Y. Zhang and R. Sunderraman, Single valued Neutrosophic Sets. Multispace and Multistructure 4,2010,pp. 410-413.
- [3] I. Kandasamy, Double-Valued Neutrosophic Sets, their Minimum Spanning Trees, and Clustering Algorithm, Journal of Intelligent system 2016, pp.1-17.
- [4] J. Ye, single valued neutrosophic minimum spanning tree and its clustering method, Journal of Intelligent system 23, 2014, pp.311-324
- [5] K. Mandal and K. Basu, Improved similarity measure in neutrosophic environment and its application in finding minimum spanning tree, Journal of Intelligent & Fuzzy System 31, 2016, pp. 1721-1730.
- [6] S. Broumi, A. Bakali, M. Talea, F. Smarandache, and L. Vladareanu, Computation of Shortest Path Problem in a Network with SV-Trapezoidal Neutrosophic Numbers. Proceedings of the 2016 International Conference on Advanced Mechatronic Systems, Melbourne, Australia, 2016, pp. 417-422.
- [7] S. Broumi, A. Bakali, T. Mohamed, F. Smarandache and L. Vladareanu, Shortest Path Problem Under Triangular Fuzzy Neutrosophic Information, 10th International Conference on Software, Knowledge,

- Information Management & Applications (SKIMA),2016,pp.169-174.
- [8] S. Broumi, A. Bakali, M. Talea, F. Smarandache, and L. Vladareanu, Applying Dijkstra Algorithm for Solving Neutrosophic Shortest Path Problem. Proceedings of the 2016 International Conference on Advanced Mechatronic Systems, Melbourne, Australia, November 30 - December 3, (2016) 412-416.
- [9] S. Broumi, F. Smarandache, M. Talea and A. Bakali, Operations on Interval Valued Neutrosophic Graphs, chapter in book- New Trends in Neutrosophic Theory and Applications- Florentin Smarandache and Surpatri Pramanik (Editors), 2016, pp. 231-254. ISBN 978-1-59973-498-9
- [10] S. Broumi, A. Bakali, M. Talea, F. Smarandache and M. Ali, Shortest Path Problem under Bipolar Neutrosophic Setting, Applied Mechanics and Materials, Vol. 859, 2016, pp 59-66.
- [11] S. Broumi, A. Bakali, M. Talea and F. Smarandache and P.K, Kishore Kumar, Shortest Path Problem on Single Valued Neutrosophic Graphs, 2017 International Symposium on Networks, Computers and Communications (ISNCC) , 2017( in press)
- [12] S. Broumi, A. Bakali, M. Talea, F. Smarandache, and L. Vladareanu, Applying Dijkstra Algorithm for Solving Neutrosophic Shortest Path Problem. Proceedings of the 2016 International Conference on Advanced Mechatronic Systems, Melbourne, Australia, November 30 - December 3, (2016) 412-416.
- [13] S. Broumi, M. Talea, A. Bakali, F. Smarandache, On Bipolar Single Valued Neutrosophic Graphs, *Journal of New Theory*, N11, 2016, pp.84-102.
- [14] S. Broumi, M. Talea, A. Bakali, F. Smarandache, Interval Valued Neutrosophic Graphs, Critical Review, XII, 2016. pp. 5-33.
- [15] S. Broumi, F. Smarandache, M. Talea and A. Bakali, An Introduction to Bipolar Single Valued Neutrosophic Graph Theory. Applied Mechanics and Materials, vol.841, 2016, 184-191.
- [16] S. Broumi, M. Talea, A. Bakali, F. Smarandache, Single Valued Neutrosophic Graphs, *Journal of New Theory*, N 10, 2016, pp. 86-101.
- [17] S. Broumi, F. Smarandache, M. Talea and A. Bakali, Decision-Making Method Based On the Interval Valued Neutrosophic Graph, Future Technologie, 2016, IEEE, pp. 44-50.
- [18] S. Broumi, M. Talea, F. Smarandache and A. Bakali, Single Valued Neutrosophic Graphs: Degree, Order and Size. IEEE International Conference on Fuzzy Systems (FUZZ), 2016, pp. 2444-2451.
- [19] S. Broumi, A. Bakali, M. Talea, and F. Smarandache, Isolated Single Valued Neutrosophic Graphs. *Neutrosophic Sets and Systems*, Vol. 11, 2016, pp.74-78.
- [20] M. Mullai, S. Broumi , A. Stephen, Shortest path problem by minimal spanning tree algorithm using bipolar neutrosophic numbers, *International Journal of Mathematic Trends and Technology*, Vol 46, N2, 2017, pp.80-87.
- [21] J. J. Peng, J. Q. Wang, J. Wang, H. Y. Zwang, X. H. Chen, Simplified neutrosophic sets and their applications in multi-criteria group decision-making problems, *International journal of Systems science*, Vol. 47, 2015, pp. 2342-2358.
- [22] J. Ye, Similarity measures between interval neutrosophic sets and their applications in multicriteria decision-making, *Journal of Intelligent and Fuzzy Systems*, 26, 2014, pp. 165 172.
- [23] I. Deli, M. Ali, F. Smarandache, Bipolar Neutrosophic Sets And Their Application Based On Multi-Criteria Decision Making Problems, Proceedings of the 2015 International Conference on Advanced Mechatronic Systems, 2015, pp. 249-254.
- [24] J. Ye, Trapezoidal neutrosophic set and its application to multiple attribute decision-making, *Neural Computing and Applications*, July 2015, Volume 26,Issue 5, 2015, pp. 1157–1166.
- [25] S. Broumi, F. Smarandache, M. Dhar, Rough Neutrosophic sets, *Neutrosophic Sets and Systems*, Vol. 3, 2014.
- [26] I. Deli, Y. Subas, A ranking method of single valued neutrosophic numbers and its applications to multi-attribute decision making problems, *Int. J. Mach. Learn. and Cyber* 2016.
- [27] <http://fs.gallup.unm.edu/NSS>
- [28] A.Mumtaz, S. Le Hoang, I. Deli and T. Nguyen Dang, Bipolar neutrosophic soft sets and applications in decision making, *Journal* of Intelligent & Fuzzy Systems, vol. 33, no. 6, 2017, pp. 4077-4087.