Observations on Poulet numbers having only odd digits based on their reversals

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Abstract. The set of Poulet numbers having only odd digits is: 1333333, 1993537, 3911197, 5351537, 5977153, 7759937, 11777599...(22 from the first 7196 Poulet numbers belong to this set). Question: is this sequence infinite? Observations: the numbers n*P + R(P) – n respectively P + n*R(P) - n, where R(P) is the reversal of P and n positive integer, are often primes. Examples: for P = 1333333, the number 1333333 + 3333331 – 1 = 4666663, prime; also 3*1333333 + 3333331 – 3 = 7333327, prime; also 5*1333333 + 3333331 – 5 = 9999991, prime. For the same P, the number 1333333 + 2*3333331 - 2 = 7999993, prime; also the number 1333333 + 4*3333331 - 4 = 14666653, prime.

The first twenty-two Poulet numbers having only odd digits (complete set up to the 7196-th Poulet number):

1333333, 1993537, 3911197, 5351537, 5977153, 7759937, 11777599, 15139199, 17777191, 33193117, 53711113, 59913157, 59955331, 79539197, 79739713, 151533377, 177951973, 191191933, 971515777, 977755351, 1191153937, 1791157537.

Question: is this sequence infinite?

Observation:

The numbers n*P + R(P) – n, where R (P) is the reversal of P, P is Poulet number having only odd digits and n positive integer, are often primes.

Primes for n smaller than or equal to 5 are obtained for 7 from the first 22 such numbers P:

: 1*1333333 + 3333331 – 1 = 4666663, prime, also
: 3*1333333 + 3333331 – 3 = 7333327, prime, also
: 5*1333333 + 3333331 – 5 = 9999991, prime;

: 2*5351537 + 7351535 – 2 = 18054607, prime;

: 3*5977153 + 3517795 – 3 = 21449251, prime, also
: 4*5977153 + 3517795 – 4 = 27426403, prime;

: 5*11777599 + 99577711 – 5 = 158465701, prime;

:   4*17777191 + 19177771 – 4 = 158465701, prime, also
:   5*17777191 + 19177771 – 5 = 108063721, prime;

:   5*191191933 + 339191191 – 5 = 1295150851, prime;

:   1*977755351 + 153557779 – 1 = 1131313129, prime.

Observation:

The numbers P + n*R(P) - n, where R (P) is the reversal of P, P is Poulet number having only odd digits and n positive integer, are often primes.

Primes for n smaller than or equal to 5 are obtained for 11 from the first 22 such numbers P:

:   1333333 + 1*3333331 – 1 = 4666663, prime,
:   1333333 + 2*3333331 - 2 = 7999993, prime, also
:   1333333 + 4*3333331 - 4 = 14666653, prime;

:   3911197 + 5*7911193 - 5 = 43467157, prime;

:   11777599 + 5*99577711 – 5 = 509666149, prime;

:   17777191 + 5*19177771 – 5 = 113666041, prime;

:   53711113 + 5*31111735 – 5 = 209269783, prime;

:   79739713 + 3*31793797 – 3 = 175121101, prime, also
:   79739713 + 5*31793797 – 5 = 238708693, prime;

:   151533377 + 5*773335151 – 5 = 4018209127, prime;

:   177951973 + 2*379159771 – 2 = 936271513, prime, also
:   177951973 + 5*379159771 – 5 = 2073750823, prime;

:   191191933 + 2*339191191 – 2 = 869574313, prime;

:   971515777 + 3*777515179 – 3 = 3304061311, prime, also
:   971515777 + 4*777515179 – 4 = 4081576489, prime;

:   977755351 + 1*153557779 – 1 = 1131313129, prime.