# ARTICLE 11 LAN PLAINS FOR TETE-VIC EQUATION **Javier Silvestre** [www.eeatom.blogspot.com](http://www.eeatom.blogspot.com/)

# **ABSTRACT**

This is 11th article of 24 dedicated to atomic model based on Victoria equation (Articles index is at end). Torrebotana Central Energetic Line  $(E_J)$  [1] supplies energetic values for electron excited states very close to reference [2]. Excited states are grouped into curves that are destiny function, and consequently orbital quantum number plays major role, and attraction towards Torrebotana Central Energetic Line is greater when orbital quantum number increases ( $s < p < d$ ) [1]. LAN factor is included in Tete-Vic Equation to give circulation to different routes divided by destination reason. Analogy is as follows: 1s Original electronic system (1s OES) creates main ideal line (Torrebotana Central Energetic Line) considering Born electronic system (BES) and simultaneously draws Serelles Secondary Lines in which energy of excited states runs according to destiny (within destiny has special importance orbital quantum number as indicated before, as well as J or Term).

LAN plain is jump to Serelles Secondary Line with jumps in which LAN is practically constant throughout Serelles Secondary Line since LAN has small variation with energy.  $1s^22s$  as non-excited or initial state and  $1s^2ns$  as excited or final state are selected to show such LAN behaviour.

# **KEYWORDS**

Tete-Vic equation. Torrebotana Central Line, Serelles Secondary Line, LAN plain, Relation of Riquelme de Gozy,  $z_{CT}$  (Zon Equation).

### **INTRODUCTION**

Torrebotana Central Line created from 1s Original electronic system (1s OES) based on Born electronic system (BES) is charge-energy ideal line in n function. Jump for various atoms from  $1s<sup>2</sup>$  and  $2s$  to different excited state (lower and upper levels with electronic configuration, Term and J defined) are studied by way of example. Excited states are found near Torrebotana Central Line and, depending on destiny (Term and J), excited states are located inside curves without discontinuities that tend to Torrebotana Central Line and are still more attracted when n and l grows. [1] Abbreviations Table is at end article.

These curves, where excited states are located according to their defined jump, are called Serelles Secondary Line. Defined jump is lower and upper levels with electronic configuration, Term and J defined. Serelles Secondary Line includes LAN factor.

P45 Excited state charge  $(z_{CT})$  [1] in Torrebotana Central Line is ideal charge to which excited state are attracted to greater or lesser extent depending on destiny quantum numbers and is given by "Zon Equation"(1):

$$
(1)z_{\rm ct}=\frac{z_{\rm s}^2}{n^2z_{\rm o}}
$$

- z<sup>s</sup> Start charge according to P46
- z<sub>o</sub> 1s Origin charge according to P46
- n Principal quantum number of excited state

#### **P48 LAN factor for Serelles Secondary Line.**

Serelles Secondary Line is defined by LAN inclusion. (1) is transformed into (2) by LAN inclusion where  $z_{SS}$  (Serelles secondary charge) is excited state charge in Serelles Secondary Line.

$$
(2)z_{ss} = \frac{z_s^2}{\left(n - LAN\right)^2 z_o}
$$

Therefore, jump energy  $(E_J)$  predicted by Tete-Vic Equation [1] is modified by including  $z_{SS}$  instead of  $z_{CT}$ . This fact makes  $E_J$  and  $E_d$  which refer to Torrebotana Central Line, becomes  $E_{JS}$  and  $E_{dS}$  where S is Serelles. Serelles Secondary Line with  $z_{SS}$ incorporation is given by (3):

$$
(3)E_{\text{JS}} = E_{\text{dS}} - I E = \frac{z_s^2 E_o}{z_o^2 (n - LAN)^2} - I E
$$

LAN expression (4) and (5) can be obtained from (2) or (3) respectively:

$$
(4) - LAN = \left(\frac{z_s^2}{z_{ss}z_o}\right)^{1/2} - n
$$

$$
(5) - LAN = \left(\frac{z^2 E_o}{z_o^2 E_{\text{ds}}}\right) - n = \left(\frac{z^2 E_o}{z_o^2 (E_{\text{ds}} + IE)}\right) - n
$$

EJS calculation has not been defined and jump reference value [2] is going to be employed instead. As E<sub>JS</sub> is not yet known, E<sub>dS</sub> and z<sub>SS</sub> are not either. Suffix R, indicating Reference use  $[2]$ , is inserted in LAN and  $E_d$  to be differentiated. Energy needed to reach excited states with reference energy is abbreviated as  $E_k$  (indicated in [1]) and is applied as  $E_{JS}$  (6):

$$
(6) - LAN \approx -LAN_R = \left(\frac{{z_s}^2 E_o}{{z_o}^2 E_{aR}}\right)^{1/2} - n = \left(\frac{{z_s}^2 E_o}{{z_o}^2 (E_K + IE)}\right)^{1/2} - n
$$

(6) can be simplified in (7):

$$
(7) \text{ - LAN} \approx -LAN_{\text{R}} = \frac{(-E_{\text{o}})^{1/2} z_{\text{s}}}{(-E_{\text{dR}})^{1/2} z_{\text{o}}} - n
$$

## **LAN behaviour with Energy**

1s<sup>2</sup> Be is selected as example and values applicable in (6) or (7) are included in **Table 1**.



Excited energy or destiny energy is varied from 0.01 IE to IE with 0.01 IE increments for n=[2,7] in **Figure 1**:

a) Curves cut at E<sup>d</sup> value provided by Torrebotana Central Line when LAN=0.

b) Curves are shifted downward by n increments. Same fact is observed in **Figure 2** where X axis changes from  $E_d$  to  $E_J$ .

c) If LAN of Serelles Secondary Line is the same for all n,  $E_d$  and  $E_J$  curves approach or move away as LAN increases or decreases respectively.





**Table 2** is centred in Be electron jump from  $1s^2$  to 1sns (both with Term  ${}^1S$ ; J=0) and remembers  $E_k$  and  $E_j$  [1] together with the  $E_{JS}$  resulting calculations with fixed LAN=0.05 Lanitos for all n. Lanito is LAN unit. Difference between  $E_J$  and  $E_k$  is difference between Torrebotana Central Line and reference data [2] and is studied for this Be jump in [1]. Actual change (and its corresponding Relative Change) are low but existents and decrease when n and l quantum numbers increase [1]. These low

differentials are especially reduced when E<sub>JS</sub> with LAN=0.05 is applied. For example and when n=2, Actual Change is ≈1.629 eV for E<sub>J</sub>-E<sub>k</sub> and drops sharply to only ≈0.039 for  $E_{\text{JS}}$  LAN -  $E_k$ . Actual change drops are also produced in following n as represented in **Figure 3**.



### **P49 LAN plain: Jump in Serelles Secondary Line**

Electron jumps to excited states in which, being all constant except n, fulfil that LAN  $\approx$ constant with linear tendency that is jump energy function. 2s jump is taken to exemplify P49. Minimum energy state  $(IE)$  and final states with  $E_k$  (jump reference value  $[2]$ ) are in **Table 3** and **Table 4**. Charge ( $z_{CT}$ ) and Energy ( $E_J$ ) are contained for Torrebotana Central Line in Table 4. Serelles Secondary Lines indicated in Table 3 have  $E_k$  (jump reference value [2]) as Es, Ep, Ed and Ef according excited state or destiny state is ns, np, nd or nf respectively. Actual Change (8) is represented in **Figure 4**. E<sup>k</sup> (Jump reference energy) [2], as in [1] examples, are even more attracted to Torrebotana Central Line when n and l increase.

<b>Tabla 3</b> – Final or destiny states selected for jumps from 2s								
Final state	$1s^2$ ns	$1s^2np$	1s <sup>2</sup> nd	$1s^2$ nf				
Term	$\frac{1}{2}$	$2p^{\circ}$ 3/2	$^{2}D$ 5/2	$2F^{\circ}$ 7/2				

(8) Actual Change =  $AC = \Delta = E_J - E_k$ 





LAN<sub>R</sub> (7) can be calculated with Table 4 and these  $LAN_R$  are compiled in **Table 5** and represented in **Figure 5**. LAN<sub>R</sub> plains can be checked both in Table 5 and in Figure 5. Value marked with (\*) is not really jump because is precisely electronic configuration of lowest energy and, consequently, minimum energy state or initial state. LAN at initial state is developed in following point: P50.





 $E_k$  changes with increments of 0.5% for 1s<sup>2</sup>4s and 1s<sup>2</sup>6s and 0.1% for 1s<sup>2</sup>8s are done to visualize variation in LAN<sub>R</sub>. For example,  $E_k$  (1s<sup>2</sup>4s) passes from 4,340942 to 4,362646 as result to change to be 1,005  $E_k$ . In **Table 6** and **Figure 6**, high LAN<sub>R</sub> variations are observed even though percentage increases in  $E_k$  are low and  $LAN_R$  plain is broken by discontinuities. LAN<sub>R</sub> with E<sub>k</sub> modification is represented by  $\text{LAN}_{\text{R,M}}$ . Relative Change in percentage for  $\text{LAN}_R$  is given in (9) but the most direct information column is the last

one where %RC(LAN<sub>R</sub>) is referenced to %RC(E<sub>k</sub>) because E<sub>k</sub> variation for 1s<sup>2</sup>8s is lower. For case of 1s<sup>2</sup>8s, %RC(LAN<sub>R</sub>) is  $\approx$ 211 times higher than %RC(E<sub>k</sub>). Conclusion is than  $LAN_R$  has great sensitivity to  $E_k$  variation.



$$
(9)\% RC(LAN_{R}) = \frac{(LAN_{R,M} - LAN_{R})}{/LAN_{R}/} * 100
$$



Higher sensibility when n is higher (Table 6 and Figure 6) is clearly influenced because LAN<sub>R</sub> calculation is performed with  $E_{dR}$  and not with  $E_k$  (6) or (7). n increase implications are:

$$
\uparrow n \to \uparrow E_k \to \downarrow/E_{dR}/\to \uparrow/\% RC(LAN_R)/
$$

Some disparity or distance from LAN plain ideality can occur especially when n increases due to data with less accuracy (or even with similar deviation) and / or effects not yet developed and that are increased, as just observed, because of this higher sensitivity when n increases.

#### **P50 Initial LAN value in jump from ns to ns.**

Initial LAN value in ns to ns jump is corresponding to initial state and is not first jump. Consequently, initial  $LAN_R$  value is result of applying IE [3] instead  $E_{dR}$  [2]. First value calculated in this way is found in Table 6 marked with (\*) and is not really jump as indicated above. ns to ns jump is OES from OES jump and has this special behaviour. Initial LAN value in jump from ns to ns is called: LAN(P50) and (7) is transformed into (10):

$$
(10)\text{-} LAN(P50)=-LAN_\text{ns} \rightarrow \text{ns}=\frac{(-E_\text{o})^{1/2}z_\text{s}}{(-IE)^{1/2}z_\text{o}}-\text{n}_\text{initial}
$$

Therefore, LAN and associated "distance" or deviation with respect to Torrebotana Central Line can be easily know for ns to ns jump with only IE [3] and without experiencing any jump [2] because LAN value has plain ideal behaviour, that is to say LAN has little variation with n, and LAN(P50) can be used as first estimate for jumps from ns to ns. (This approach is treated more closely at later article as "Xorrador Approximation").

2s Li example initiated within P49 is continued with Relation of Riquelme de Gozy once P50 has been included.

### **Relation of Riquelme de Gozy**

Relation of Riquelme de Gozy is linear tendency LAN vs electron energy or jump energy. P50 LAN plain: Jump in Serelles Secondary Line is introduced with: "Electron jumps to excited states in which, being all constant except n, fulfil that LAN  $\approx$  constant with linear tendency that is jump energy function". This linear tendency can be expressed with absolute value of destiny energy or excited electron energy ( $/E<sub>d</sub>$  or  $/E<sub>dR</sub>$ ) if is obtained with reference data).

**Table 7** collects  $/E_{dR}/LM(P50)$  and  $LAN_R$  for jumps up to 8s.  $LAN_R$  decreases smoothly with some slight divergence for higher n.





First three points pairs of Table 7 (/Ed<sub>R</sub>/ and LAN(P50) or LAN<sub>R</sub> for  $n=[2,4]$ ) have been taken in **Figure 7**. Lineal trend has optimal adjustment with  $R^2=1,000000$  and has low slope  $0.002272$  Lanitos/eV = 2,2 mLanitos/eV. Therefore, P49 LAN plain: Jump in Serelles Secondary Line is fulfilled with energy function linear tendency and LAN plain with low slope  $\rightarrow$  LAN  $\approx$  constant. Linear equation general expression of Riquelme de Gozy is given in (11) and for Li 2s to  $1s<sup>2</sup>2s$  (Term= $<sup>2</sup>S$  J=1/2) in (12). Serelles Secondary</sup> Line is ideal when has optimum linear adjustment as in this case.



 $(11)$ LAN<sub>R</sub> = a + b/E<sub>dR</sub>/

 $(12)$ LAN<sub>R</sub> = 0,399192732 + 0,002272163/E<sub>dR</sub>/ R<sup>2</sup> = 1,000000

 $/Ed_R/$  has been used to obtain (12) and  $E_{dR1}$  is ideal destiny energy obtained by extrapolation from reference energy equation (12).

#### **Riquelme de Gozy extrapolation to rest of excited states**

First step for Riquelme de Gozy extrapolation to rest of excited states and achieving ideal Serelles Secondary Line is to shorten (7) considering (13). K<sub>LAN</sub> is constant made up of three known constants: -E<sup>o</sup> (1s Ionization Energy), z<sup>s</sup> (Start or initial charge) and  $z<sub>o</sub>$  (1s Origin charge) [1]. Three constants are in Table 4 for Lithium example.

$$
(13)K_{\rm LAN} = \frac{(-E_{\rm o})^{1/2}z_{\rm s}}{z_{\rm o}}
$$

On the other hand and also in (7), principal quantum number n and destiny energy, that is estimated from ideal behaviour, are not constant. This ideal destiny energy is called  $E_{dI}$  where Ideal is marked with suffix I. Finally,  $E_{dI}$  is compared with  $E_{dR}$  (Reference destiny Energy) [2].

(14) is obtained by equating (11) and (7) with  $K_{LAN}$  (13). In addition,  $E_{dI}$  is already included with absolute value. Equalization allows to pass from two unknowns  $(LAN<sub>I</sub>)$ and  $E_{dI}$ ) to a single one ( $E_{dI}$ ). LAN<sub>I</sub> and  $E_{dI}$  have suffix I although in both cases is "Ideal" behaviour from reference data that are extrapolated.  $E_{dR}$  (ideal  $E_{dR}$  for n obtained from extrapolation of initials E<sub>dR</sub> satisfying Relation of Riquelme de Gozy) is obtained, although  $E_{dI}$  is used in formulas development, because Relation of Riquelme de Gozy has actually been achieved by using references values (IE and  $E_{dR}$ )

$$
(14)a + b/E_{\rm dl} / = \frac{-K_{\rm LAN}}{(E_{\rm dl})^{1/2}} + n
$$

n is taken to equation left and whole equation is squared to remove  $E_{dI}$  square root (15):

$$
(15)a^{2} + b^{2}/E_{di}/^{2} + n^{2} + 2ab/E_{di}/-2an - 2bn/E_{di}/ = \frac{(-K_{LAN})^{2}}{E_{di}/}
$$

 $(15)$  is equalized to zero and terms are rearranged based on  $E<sub>dl</sub>$  exponent. Result is third degree equation (16) where there are terms with  $E_{dI}$  raised to 3, 2, 1 and 0.

$$
(16)b^{2}/E_{dI}/^{3} + 2b(a-n)/E_{dI}/^{2} + (a^{2}+n^{2}-2an)/E_{dI}/-K_{LAN}^{2} = 0
$$

Cubic equation is solved by Cardano method, although first is verified if is possible to erase term with  $E<sub>dl</sub>$  raised to 3 and transform it into a second-degree equation. For this, general equation coefficients (16) are inserted in **Table 8** for Li example.  $E_{dR}$  is employed because E<sub>dI</sub> is unknown although, considering  $R^2=1.000000$  (12) obtained with  $E_{dR}$ ,  $E_{dR} \approx E_{dI}$ 





$$
(17)Ax3 + Bx2 + Cx + D = 0 \t(x = / Edl or / EdRI/)
$$

Although  $E_{dR}$  has been used, not  $E_{dI}$ , not even  $E_{dRI}$  (ideal  $E_{dR}$  for high n obtained from extrapolation of others  $E_{dR}$  satisfying Relation of Riquelme de Gozy), Table 8 serves to verify several facts:

a) C and D coefficients are similar for every n. This fact is consequence of Y-intercept being much superior to slope. (14) can be approximated to (19) when (18) is satisfied:

$$
(18) a \gg b
$$

$$
(19)a \approx \frac{-K_{\text{LAN}}}{\sqrt{E_{\text{dl}}/^{1/2}}} + n \left( E_{\text{dR} \text{ used in Table 8}} \right)
$$

(19) development leads to (20) that, considering (16) and (17), are same coefficients C and  $D$  (21). In addition, as n increases and therefore  $E<sub>dl</sub>$  decreases, C coefficient continues to override A and B coefficients because C has  $n^2$  and E<sub>dI</sub>, B has n and E<sub>dI</sub><sup>2</sup> and A has  $E_{dI}^3$  and not n term.

$$
(20)(a^2 + n^2 - 2an)/E_{dI} + K_{LAN}^2 \approx 0
$$
 (E<sub>dR</sub> used in Table 8)

(21)  $C/E_{dI}$  + D  $\approx$  0 If (18) and better when n $\uparrow$  (E<sub>dR</sub> used in Table 8)

This approach is equivalent to the one indicated as "Xorrador Approximation" in previous paragraph to this point and, as is commented there, is expended in following article.

b) A and B coefficients make up other balance of terms and compensate for difference between C and D. B and A are divided in the last column on the right in Table 8: cubic term is more negligible and error when approaching square relation is smaller when quotient increases. For same reason discussed in previous point, i.e. different exponents of n and EdI in coefficients, B preponderance over A grows as n increases.

c) Summation of four coefficients is made in column titled "Sum". "Sum" dos not give exactly 0 because destiny energy used is  $E_{dR}$  and is not  $E_{dI}$ . Even not giving 0, can be highlighted:

c.1) n=[2,4]. Summation is practically 0 for first three values (Sum $\approx$ 10<sup>-5</sup> eV). This result is predictable since first three values make up (12) and have exceptionally good linear tendency with  $R^2=1,000000$ .

c.2) n>4. Following points that can be created from this straight line of Riquelme de Gozy created with  $E_{dR}$  are  $E_{dR}$ , and based on low summation values, should not be far from  $E_{dR}$  applied in Table 8. Cardano method is applied to know  $E_{dRI}$  and compare with  $E_{dR}$ .

#### **Cardano method application to know EdRI and compare with EdR.**

Comments made on Cardano method application:

a) Riquelme de Gozy equation is obtained with only two points (22): initial state and first excited state. Figure 7 and (12) employ three states (initial state and first two excited states) to demonstrate optimum linearity between them. Consequently, (22) is very similar to (12).

 $(22)$ LAN = 0,399186272 + 0,002273521/EdR/

b) Cubic equation (16) and square equation obtained by discarding cubic term are solved to n=[4,8], obtaining  $E_{dRI}$ , which is compared with  $E_{dR}$  and also for n>8 to see how evolves.

c) Cardano method has discriminant which, depending on its sign, equation has different solutions. In this case, discriminant is negative and real solution with physical sense has 90 degrees and  $cos(90)=0$ . Other solutions provide  $/E_{dRI}/E/IE/$  and therefore are meaningless.

d) **Table 9** has  $E_{dR}$  and  $E_{dRI}$  with Cubic equation ( $E_{dRI}$  (3)) and square equation ( $E_{dRI}$ (2)) and their respective LAN:

d.1) Differences between  $E_{dRI}$  and  $E_{dR}$  are minima: ( $\approx 10^{-5}$ ).

d.2) Differences between  $E_{dRI}(2)$  and  $E_{dRI}(3)$  in n=2 and n=3 are approximation consequence that has greater weight when n is low and destiny energy is greater (Cubic term= $Ax^3 = b^2E_{dRI}^3$  (17)).

d.3)  $E_{dRI}(2) \approx E_{dRI}(3)$  when n>4 which is from where is interesting to see approximation effect.

d.4)  $E_{dRI}(2)$  and  $E_{dRI}(3)$  are expressed with same significant digits as  $E_{dR}$  for better comparison.

e) Destiny energy vs. LAN is in **Figure 8**. In a first impression, LAN<sup>R</sup> is well located in linearity of Relation of Riquelme de Gozy. **Figure 9** is Figure 8 enlargement and is centred on 1s<sup>2</sup>ns with n=[4,8], that is to say in extrapolated  $E_{dRI}$  and  $LAN_{RI}$ . LAN<sub>R</sub> in 4s, 5s and 7s is very close to linearity of Relation of Riquelme de Gozy, slightly deviated for 6s and something more for 8s. Poor energetic deviation of 0,0003 eV  $($ /Ed<sub>R</sub>/(1s<sup>2</sup>8s)=0,23557 vs. /Ed<sub>RI</sub>/ (2) (1s<sup>2</sup>8s) = /Ed<sub>RI</sub>/ (3) (1s<sup>2</sup>8s)= 0,23554) provides visible effect on LAN.

f) Linearity of Relation of Riquelme de Gozy and its sensitivity to small energetic deviations are interesting support to bifurcated Torrebotana Central Line in Serelles Secondary Lines.

g) Relation of Riquelme de Gozy fulfilment including non-excited ns state in ns to ns jump (LANP50) adds more strength to its origin character.



$m \sim 100$ at $\sim 100$ and $\sim 100$									
$\mathbf n$	$/Ed_R/$	$/Ed_{RI}/(2)$	$/Ed_{RI}/(3)$	$\text{LAN}_{\text{R}}$ ns	$LAN_{RI}(2)$	$LAN_{RI}(3)$			
$\overline{2}$	5,39171476	5,3920409	5,39171476	0,411444	0,411492	0,411444			
3	2,018586	2,018592	2,018586	0,403776	0,403780	0,403776			
$\overline{4}$	1,050773	1,050769	1,050768	0,401584	0,401576	0,401575			
5	0,643182	0,643189	0,643189	0,400624	0,400649	0,400649			
6	0,433880	0,433893	0,433893	0,400090	0,400173	0,400173			
7	0,31234	0,31234	0,31234	0,399877	0,399896	0,399896			
8	0,23557	0,23554	0,23554	0,400135	0,399722	0,399722			
9		0,18395	0,18395		0,399604	0,399604			
12		0,10110	0,10110		0,399416	0,399416			
16		0,05590	0,05590		0,399313	0,399313			
20		0,03541	0,03541		0,399267	0,399267			
30		0,01553	0,01553		0,399222	0,399222			
40		0,00868	0,00868		0,399206	0,399206			
50		0,00553	0,00553		0,399199	0,399199			
75		0,00244	0,00244		0,399192	0,399192			
100		0,00137	0,00137		0,399189	0,399189			
200		0,00034	0,00034		0,399187	0,399187			

**Table 9** - Li 2s - Energía de destino de referencia e ideal por ecuación cúbica (3) o aproximación cuadrada (2). Valores de LAN complementarios a dichas Energías. Línea Secundaria Serelles de configuración  $1s<sup>2</sup>ns$  (Term=  $2S y J=1/2$ )

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