

A method of obtaining large primes based on Carmichael numbers

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Abstract. Playing with Carmichael numbers, a set of numbers I've always been fond of (I've "discovered" Fermat's "Little" Theorem and the first few Carmichael numbers before I know they had already been discovered), I noticed that the formula $C + 81 \cdot 2^{(4 \cdot d)}$, where C is a Carmichael number and d one of its prime factors, gives often primes or products of very few primes. For instance, for $C = 1493812621027441$ are obtained in this manner three primes: 2918779690625137, 6729216728661136606577017055290271857 and 644530914387083488233375393598279808770191171433362641802841314053534708129737067311868017 (a 90-digit prime!), respectively for $d = 11$, $d = 29$ and $d = 73$.

Observation:

The formula $C + 81 \cdot 2^{(4 \cdot d)}$, where C is a Carmichael number and d one of its prime factors, gives often primes or products of very few primes.

The set of such Carmichael numbers:

(that generates primes through the formula mentioned)

- : $C = 1105 = 5 \cdot 13 \cdot 17$ generates for $d = 17$:
 - : 23906980319527578895441, prime;

 - : $C = 2465 = 5 \cdot 17 \cdot 29$ generates for $d = 17$:
 - : 23906980319527578896801, prime;

 - : $C = 6601 = 7 \cdot 23 \cdot 41$ generates for $d = 7$ and $d = 23$:
 - : 21743278537, prime;
 - : 401092572728463209067316255177, prime;

 - : $C = 101101 = 7 \cdot 11 \cdot 13 \cdot 101$ generates for $d = 7, 13$:
 - : 21743373037, prime;
 - : 364791569817111277, prime;

 - : $C = 188461 = 7 \cdot 13 \cdot 19 \cdot 109$ generates for $d = 7, 13, 19$:
 - : 21743460397, prime;
 - : 364791569817198637, prime;
 - : 6120186961799060197138477, prime;
- (...)

Four such 16-digit Carmichael numbers:

(that generates primes through the formula mentioned)

- : C1 = 1436697831295441 generates for d = 13, 31:
 - : 366228267648305617, prime;
 - : 17226794825372509712833335386821157865937, prime;
- : C2 = 1493812621027441 generates for d = 11, 29, 73:
 - : 2918779690625137, prime;
 - : 6729216728661136606577017055290271857, prime;
 - : 644530914387083488233375393598279808770191171433362641802841314053534708129737067311868017, prime;
- : C3 = 2842648863161185 generates for d = 13:
 - : 367634218680171361, prime;
- : C4 = 5778659093725441 generates for d = 7:
 - : 5778680836997377, prime.

Note: only checked for prime factors d lesser than or equal to 73.

Note: for all four Carmichael numbers above the formula $C + 81 \cdot 2^d$ also generates primes:

- : 1436871777470929 for [C, d] = [C1, 31];
- : 1493812621193329 for [C, d] = [C2, 11];
- : 2842692349705057 for [C, d] = [C3, 29];
- : 5778659136192769 for [C, d] = [C4, 19];
- : 5789791648956673 for [C, d] = [C4, 37].