

## Fermat's theorem. Proof by 2 operations

The essence of the contradiction. The hypothetical Fermat's equality is contradictory between the second digits of the factors of the number  $A$ .

All calculations are done with numbers in base  $n$ , a prime number greater than 2.

The notations that are used in the proofs:

$A', A''$  – the first, the second digit from the end of the number  $A$ ;

$A_2$  is the two-digit ending of the number  $A$  (i.e.  $A_2 = A \bmod n^2$ );

Consider the Fermat's equality in the base case (its properties 2°-3° are proved here: <http://vixra.org/abs/1707.0410>) for co-primes positive  $A, B, C$ ;  $A' \neq 0$ , prime  $n$ ,  $n > 2$ :

1°)  $A^n = C^n - B^n = (C-B)P$ , where (as is known)

2°)  $A' \neq 0$ ,  $C-B = a^n$ ,  $P = p^n$ ,  $A = ap$ ,  $p' = 1$ ,  $a' \neq 0$ ,  $a^{n'} = a'$ ,  $a'^{n-1} = 1$  (Fermat's small theorem);

3°)  $(A+B-C)_2 = 0$ , from here

3a°)  $(ap)_2 = a^n_2$  and therefore

3b°)  $p_2 = a^{n-1}_2$ .

4°) If  $p'' = 0$ , then we multiply term by term equality 1° by such  $g^m$ , that  $p'' \neq 0$ .

Properties 2°-3° are preserved, and we leave the notation of the numbers as before.

And now **the proof itself FLT.**

We represent the endings  $a_2$  and  $p_2$  in the form:

$a_2 = (xn + a^m)_2$  and  $p_2 = p''n + 1$ , where  $x$  and  $y$  are digits.

First we substitute these values of the endings in the left-hand side of the equality 3a°:

5°)  $[(xn + a^m)(p''n + 1)]_2 = a^n_2$ , from here

5a°)  $(a^m p''n + xn)_2 = 0$ , or (see 2°)  $a' p'' + x = 0 \pmod{n}$ .

Now, we substitute the value of  $a_2$  in the right-hand side of the equality 3b°:

6°)  $(xn + a^m)^{n-1}_2 = [(n-1)xn a'^{n-2} + 1]_2 = (-nxa'^{n-2} + 1)_2 = (-nxa'^{n-1}/a' + 1)_2$ . From 3b° we have:

6a°)  $-xa'^{n-1}/a'+p''=0 \pmod n$ , or  $-xa'^{n-1}+a'p''=0 \pmod n$ , or  $-x+a'p''=0 \pmod n$ ,

It follows from 5a° and 6a° that  $x=y=0$ , which contradicts to 2° and 4°. From this contradiction follows the truth of the FLT.

(Mezos, France. 4 September 2017)