## **A Generalized Similarity Measure** ISSN 1751-3030

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# **Technical Note**

# **Abstract**

In this research Technical Note the author has presented a novel method of finding a Generalized Similarity Measure between two Vectors or Matrices or Higher Dimensional Data of different sizes.

## **Theory**

Considering two different vectors of different sizes namely

 $A_{1xm}$  and  $B_{1xn}$  , we first find the Proximity Matrix between elements of the given vectors wherein the Proximity Matrix is given by

$$
P_A = \begin{bmatrix} d(1,1) & d(1,2) & d(1,3) & \dots & d(1,(m-1)) & d(1,m) \\ d(2,1) & d(2,2) & d(2,3) & \dots & d(2,(m-1)) & d(2,m) \\ d(3,1) & d(3,2) & d(3,3) & \dots & d(3,(m-1)) & d(3,m) \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ d((m-1),1) & d((m-1),2) & d((m-1),3) & \dots & d((m-1),(m-1)) & d((m-1),m) \\ d(m,1) & d(m,2) & d(m,3) & \dots & d(m,(m-1)) & d(m,m) \end{bmatrix}
$$

and

$$
P_B = \begin{bmatrix} d(1,1) & d(1,2) & d(1,3) & \dots & d(1,(n-1)) & d(1,n) \\ d(2,1) & d(2,2) & d(2,3) & \dots & d(2,(n-1)) & d(2,n) \\ d(3,1) & d(3,2) & d(3,3) & \dots & d(3,(n-1)) & d(3,n) \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ d((n-1),1) & d((n-1),2) & d((n-1),3) & \dots & d((n-1),(n-1)) & d((n-1),n) \\ d(n,1) & d(n,2) & d(n,3) & \dots & d(n,(n-1)) & d(n,n) \end{bmatrix}
$$

d indicates the distance measured in some metric (default = Eucleadean)

We then find the Norm Of  $P_A$  as  $\|P_A \cdot P_A\|$ . For the Euclidean case, it is given by  $P_{A} \cdot P_{A}$  =  $\sum_{i=1}^{m} \sum_{j=1}^{m} P(i, j) \cdot P(i, j)$ *j i*  $A \cap A \parallel \neg \sum_{i=1}^{\infty} \sum_{i=1}^{\infty} A \cdot (i, j) \cap A \cdot (i, j)$  $\Vert P_A \Vert = \sum_{i=1} \sum_{i=1} P(i, j).$ . Also,  $m < n$ . Similarly, we compute the Norm of  $P_B$  as  $\|P_B \cdot P_B\|$ 

. For the Euclidean case, it is given by  $||P_B \cdot P_B|| = \sum_{i=1}^{n} \sum_{j=1}^{n} P(i, j) \cdot P(i, j)$ *j n i*  $B \cap B \parallel \quad \sum_{i=1}^{\infty} \sum_{i=1}^{n} (x_i, y_i) \in (0, 1)$  $\Vert P_B \Vert = \sum_{i=1} \sum_{i=1} P(i, j).$ .

We then find the ratio *A A B B P P*  $P_{\cdot} \cdot P$  $k_1 = \frac{\mathbf{p} - \mathbf{b}}{\mathbf{p}}$  $\mathbf{I} = \frac{\left\| \mathbf{I}_B \cdot \mathbf{I}_B \right\|}{\left\| \mathbf{I}_B - \mathbf{I}_B \right\|}$ 

Actually, we can note that there are only  $N_B = \frac{N}{2}$  $N_B = \frac{n^2 - n}{2}$  number of possibly distinct values of Proximity Matrix elements in  $P_B$  and similarly, there are only  $N_A = \frac{m}{2}$  $N_A = \frac{m^2 - m}{2}$  number of possibly distinct values of Proximity Matrix elements in  $P_{\scriptscriptstyle A}$ .

Similarly, we find some more ratio's  $k_{N_n-1} = \frac{f_{(N_B-1)}(P_B)}{f_{(N_B-1)}}$  $\dot{P}_{(N_B-1)}(P_{_A})$  $N_p-1$ )  $\leftarrow$  *B*  $N_B-1$   $f(N_B-1)(P)$  $f(x) = \frac{f_{(N_B-1)}(P)}{P}$ *B*  $f_{N_p-1}$  $I_{-1} = \frac{J(N_B-1)(I_B)}{I(R_B)}$  where  $f_{(N_B-1)}(P_B)$  is some Scalar Function \_ of the Matrix  $P_B$  . And so is  $f_{(N_B-1)}(P_A)$ . Note that  $f_{(N_B-1)}$  is the same in  $f_{(N_B-1)}(P_B)$  and  $f_{(N_B-1)}(P_A)$ . We now consider a fictitious Vector  $A_{B_{1x\mu}}$ , i.e., Vector A in the basis of Vector B, colloquially speaking. Let this be  $A_{B_{1,m}} = \begin{bmatrix} c_1 & c_2 & c_3 & \dots & c_{n-1} & c_n \end{bmatrix}$ . Now, for this, vector, we find the Proximity Matrix  $P_{A_{B_{1,m}}}$  and now assert that  $k_{N_B-1} = \frac{f_{(N_B-1)}(P_B)}{f_A}$  $\sum_{(N_B-1)}^{N_B-1} (A_{B_{1xn}})$  $\int_{(N_B-1)}^{B^{-1}} (A_B - A)$  $N_B$ -1)  $\left\{$  *B*  $N_B$ <sup>-1</sup>  $f_{(N_B-1)}(A)$  $f_{(N_{n-1})}(P)$ *k*  $-1)$   $(4 - B_1)$ 1 1 - $I_{-1} = \frac{J(N_B-1)(I_B)}{I_{-1}}$ . This gives us  $N_B$  number of equations from which we can solve for elements of  $A_{B_{1:n}}$ . Now, we can find distance between  $A_{B_{1:n}}$ and  $B_{1xn}$  and can also consequently find the Similarity co-efficient between them. We can also, repeat this procedure using the normalized values of the vectors  $A_{1xm}^+$  and  $B_{1xn}^+$  . In the same fashion as detailed above, we can repeat this procedure for Matrices or Higher Dimensional Data of differing sizes.

#### **References**

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[http://www.vixra.org/author/ramesh\\_chandra\\_bagadi](http://www.vixra.org/author/ramesh_chandra_bagadi)