A Generalized Similarity Measure ISSN 1751-3030

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Technical Note

Abstract

In this research Technical Note the author has presented a novel method of finding a Generalized Similarity Measure between two Vectors or Matrices or Higher Dimensional Data of different sizes.

Theory

Considering two different vectors of different sizes namely

 A_{1xn} and B_{1xn} , we first find the Proximity Matrix between elements of the given vectors wherein the Proximity Matrix is given by

$$P_{A} = \begin{bmatrix} d(1,1) & d(1,2) & d(1,3) & \dots & d(1,(m-1)) & d(1,m) \\ d(2,1) & d(2,2) & d(2,3) & \dots & d(2,(m-1)) & d(2,m) \\ d(3,1) & d(3,2) & d(3,3) & \dots & d(3,(m-1)) & d(3,m) \\ \vdots & \vdots & \ddots & \vdots & \vdots & \vdots \\ d((m-1),1) & d((m-1),2) & d((m-1),3) & \dots & d((m-1),(m-1)) & d((m-1),m) \\ d(m,1) & d(m,2) & d(m,3) & \dots & d(m,(m-1)) & d(m,m) \end{bmatrix}$$

and

$$P_{B} = \begin{bmatrix} d(1,1) & d(1,2) & d(1,3) & \dots & d(1,(n-1)) & d(1,n) \\ d(2,1) & d(2,2) & d(2,3) & \dots & d(2,(n-1)) & d(2,n) \\ d(3,1) & d(3,2) & d(3,3) & \dots & d(3,(n-1)) & d(3,n) \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ d((n-1),1) & d((n-1),2) & d((n-1),3) & \dots & d((n-1),(n-1)) & d((n-1),n) \\ d(n,1) & d(n,2) & d(n,3) & \dots & d(n,(n-1)) & d(n,n) \end{bmatrix}$$

d indicates the distance measured in some metric (default = Eucleadean)

We then find the Norm Of P_A as $\|P_A \cdot P_A\|$. For the Euclidean case, it is given by $\|P_A \cdot P_A\| = \sum_{j=1}^m \sum_{i=1}^m P(i,j) \cdot P(i,j)$. Also, m < n. Similarly, we compute the Norm of P_B as $\|P_B \cdot P_B\|$

. For the Euclidean case, it is given by $\|P_B \cdot P_B\| = \sum_{j=1}^n \sum_{i=1}^n P(i,j) \cdot P(i,j)$.

We then find the ratio $k_1 = \frac{\left\|P_B \cdot P_B\right\|}{\left\|P_A \cdot P_A\right\|}$.

Actually, we can note that there are only $N_B=\frac{n^2-n}{2}$ number of possibly distinct values of Proximity Matrix elements in P_B and similarly, there are only $N_A=\frac{m^2-m}{2}$ number of possibly distinct values of Proximity Matrix elements in P_A .

References

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