# The Recursive Future And Past Equation Based On The Ananda-Damayanthi Normalized Similarity Measure Considered To Exhaustion ISSN 1751-3030

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# Abstract

In this research investigation, the author has presented a Recursive Past Equation and a Recursive Future Equation based on the Ananda-Damayanthi Normalized Similarity Measure considered to Exhaustion [1].

### **The Recursive Future Equation**

Given a Time Series 
$$Y = \{y_1, y_2, y_3, ..., y_{n-1}, y_n\}$$

we can find  $y_{n+1}$  using the following Recursive Future Equation

$$y_{n+1} = \underset{p \to \infty}{\textit{Limit}} \frac{\left\{ \sum_{k=1}^{n} y_k \left\{ \left\{ \frac{S_k}{L_k} \right\} + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\} + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\} + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\} + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\} \right\} \right\}}{\sqrt{\sum_{k=1}^{n} \left\{ \left\{ \frac{S_k}{L_k} \right\}^2 + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\}^2 + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\}^2 + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\}^2 + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\}^2 \right\}}}$$

where

$$\begin{split} S_{k} &= Smaller \ of \ \left(y_{n+1}, y_{k}\right) \text{ and } L_{k} = Larg \ er \ of \ \left(y_{n+1}, y_{k}\right) \\ S_{k+1} &= Smaller \ of \ \left(\left(L_{k} - S_{k}\right), y_{k}\right) \text{ and } L_{k+1} = Larg \ er \ of \ \left(\left(L_{k} - S_{k}\right), y_{k}\right) \\ S_{k+2} &= Smaller \ of \ \left(\left(L_{k+1} - S_{k+1}\right), y_{k}\right) \text{ and } L_{k+2} = Larg \ er \ of \ \left(\left(L_{k+1} - S_{k+1}\right), y_{k}\right) \\ S_{k+p-1} &= Smaller \ of \ \left(\left(L_{k+p-2} - S_{k+p-2}\right), y_{k}\right) \text{ and } L_{k+p-1} = Larg \ er \ of \ \left(\left(L_{k+p-2} - S_{k+p-2}\right), y_{k}\right) \\ S_{k+p} &= Smaller \ of \ \left(\left(L_{k+p-1} - S_{k+p-1}\right), y_{k}\right) \text{ and } L_{k+p} = Larg \ er \ of \ \left(\left(L_{k+p-1} - S_{k+p-1}\right), y_{k}\right) \\ \text{where } p \text{ is a Number which makes the aforementioned Difference Residual } \left(L_{k+p-1} - S_{k+p-1}\right) \text{ tend to Zero.} \end{split}$$

# From the above Recursive Equation, we can solve for $y_{n+1}$ . **Proof:**

We consider  $y_1$  and find the Ananda-Damayanthi Similarity [1] between  $y_1$  and  $y_{n+1}$  which turns out to be  $\left\{\frac{S_1}{L_1}\right\}$ . We now consider the lack of similarity part, i.e.,  $(L_1 - S_1)$  and again find the Similarity between  $y_1$ 

and  $(L_1 - S_1)$  which turns out to be  $\left\{\frac{S_{1+1}}{L_{1+1}}\right\} = \left\{\frac{S_2}{L_2}\right\}$ . And similarly, we find  $\left\{\frac{S_{1+2}}{L_{1+2}}\right\} = \left\{\frac{S_3}{L_3}\right\}$ ,  $\left\{\frac{S_{1+3}}{L_{1+3}}\right\} = \left\{\frac{S_4}{L_4}\right\}$ , ...,  $\left\{\frac{S_{1+p-1}}{L_{1+p-1}}\right\} = \left\{\frac{S_p}{L_p}\right\}$ ,  $\left\{\frac{S_{1+p}}{L_{1+p}}\right\}$ . We now add them all. Similarly, we consider  $y_2$ ,

 $y_{3}, \dots, \text{ upto } y_{n-1} \text{ and } y_{n} \text{ and compute such aforementioned quantities and add them all. We now Normalize,}$ i.e., divide each of this value by the quantity  $\sqrt{\sum_{k=1}^{n} \left\{ \left\{ \frac{S_{k}}{L_{k}} \right\}^{2} + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\}^{2} + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\}^{2} + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\}^{2} + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\}^{2} \right\}}. \text{ We equate this value to } y_{n+1}$ 

as the RHS is the Total Normalized Similarity contribution from each element of the Time Series Set  $Y = \{y_1, y_2, y_3, \dots, y_{n-1}, y_n\}$  with respect to  $y_{n+1}$ .

# **General Form**

We can note that the above equation  

$$y_{n+1} = \underset{p \to \infty}{Limit} \frac{\left\{\sum_{k=1}^{n} y_{k} \left\{\left\{\frac{S_{k}}{L_{k}}\right\} + \left\{\frac{S_{k+1}}{L_{k+1}}\right\} + \left\{\frac{S_{k+2}}{L_{k+2}}\right\} + \dots + \left\{\frac{S_{k+p-1}}{L_{k+p-1}}\right\} + \left\{\frac{S_{k+p}}{L_{k+p}}\right\}\right\}\right\}}{\sqrt{\sum_{k=1}^{n} \left\{\left\{\frac{S_{k}}{L_{k}}\right\}^{2} + \left\{\frac{S_{k+1}}{L_{k+1}}\right\}^{2} + \left\{\frac{S_{k+2}}{L_{k+2}}\right\}^{2} + \dots + \left\{\frac{S_{k+p-1}}{L_{k+p-1}}\right\}^{2} + \left\{\frac{S_{k+p}}{L_{k+p}}\right\}^{2}\right\}}}$$

is in general of the form

$$y_{n+1} = \underset{p \to \infty}{Limit} \frac{\left\{a_1 y_{n+1} + \frac{a_2}{y_{n+1}}\right\}}{\sqrt{\left\{\left(a_3 y_{n+1}\right)^2 + \left(\frac{a_4}{y_{n+1}}\right)^2\right\}}}$$

where,  $a_1^{}, a_2^{}, a_3^{}$  and  $a_4^{}$  are some positive integers.

We can further write the above equation as

$$(y_{n+1})^2 \left\{ (a_3 y_{n+1})^2 + \left(\frac{a_4}{y_{n+1}}\right)^2 \right\} = \left\{ a_1 y_{n+1} + \frac{a_2}{y_{n+1}} \right\}^2$$

$$(a_3)^2 (y_{n+1})^6 - (a_1)^2 (y_{n+1})^4 + \{(a_4)^2 - (2a_1a_2)\} (y_{n+1})^2 - (a_2)^2 = 0$$
 Equation A

#### **Defining Error**

We define Error in the following fashion:

For the Recursive Future Equation:

#### Method 1

Given a Time Series  $Y = \{y_1, y_2, y_3, \dots, y_{n-1}, y_n\}$  we consider only  $Y = \{y_1, y_2, y_3, \dots, y_{n-1}\}$  and use the aforementioned Recursive Future Equation to find the  $n^{th}$  term. Say this is  ${}^p y_n$  where the p stands for the 'predicted' or 'forecasted' value. Then, the Error is defined by

$$\varepsilon_F = \left(\frac{y_n - y_n}{y_n}\right)$$

### Method 2

Given a Time Series  $Y = \{y_1, y_2, y_3, \dots, y_{n-1}, y_n\}$  we consider it and use the aforementioned Recursive Future Equation to find the  $(n+1)^{th}$  term. Say this is  ${}^p y_{n+1}$  where the p stands for the 'predicted' or 'forecasted' value. We now consider the Time Series Set  $Y = \{y_2, y_3, \dots, y_{n-1}, y_n, y_{n+1}\}$  and use the aforementioned Recursive Past Equation to generate the term previous to  $y_2$ , i.e.,  ${}^p y_1$ . Then, the Error is defined by

$$\varepsilon_F = \left(\frac{y_1 - {}^p y_1}{y_1}\right)$$

Therefore, simple Error can be given by

$$\varepsilon_{F} = (y_{1} - {}^{p}y_{1}) = \begin{cases} y_{1} - Desired \ Root \ Of \begin{cases} (c_{3})^{2}(y_{n+1})^{6} - (c_{1})^{2}(y_{n+1})^{4} + \\ (c_{4})^{2} - (2c_{1}c_{2})(y_{n+1})^{2} - (c_{2})^{2} = 0 \end{cases} \end{cases} \text{ where the}$$

$$Equation (c_{3})^{2}(y_{n+1})^{6} - (c_{1})^{2}(y_{n+1})^{4} + (c_{4})^{2} - (2c_{1}c_{2})(y_{n+1})^{2} - (b_{2})^{2} = 0 \text{ is analogously developed}$$

as equation B using the Time Series Set  $Y = \{y_2, y_3, \dots, y_{n-1}, y_n, y_{n+1}\}$  to find  $y_1$ , where where,  $c_1, c_2$ 

,  $\mathcal{C}_3$  and  $\mathcal{C}_4$  are some positive integers.

# The Functional Form Equation For Making Future Forecast

We consider the equation shown below

$$\varepsilon_{F} = (y_{1} - {}^{p}y_{1}) = \left\{ y_{1} - Desired \text{ Root } Of \left\{ (c_{3})^{2} (y_{n+1})^{6} - (c_{1})^{2} (y_{n+1})^{4} + \left\{ (c_{4})^{2} - (2c_{1}c_{2}) \right\} (y_{n+1})^{2} - (c_{2})^{2} = 0 \right\} \right\}$$

and minimize the Error w.r.t  $y_{n+1}$ , i.e.,

$$\frac{d\varepsilon_F}{dy_{n+1}} = 0 \quad \text{with } \frac{d^2 \varepsilon_F}{dy_{n+1}^2} > 0 \text{ at the value of } y_{n+1} \Big|_{\varepsilon_F \text{ min}} \quad \text{where is } \varepsilon_F \text{ minimum. The Equation at which this}$$

error is Minimum i.e.,  $\frac{d\varepsilon_F}{dy_{n+1}} = 0 \Big|_{\varepsilon_F Min}$  can be used to re-calculate the  $a_1, a_2, a_3$  and  $a_4$  and say these are

 $a_{1new}, a_{2new}, a_{3new}$  and  $a_{4new}$ , The Functional Form Equation For Making Future Forecast becomes

$$(a_{3new})^2 (y_{n+1})^6 - (a_{1new})^2 (y_{n+1})^4 + \{(a_{4new})^2 - (2a_{1new}a_{2new})\} (y_{n+1})^2 - (a_{2new})^2 = 0$$

### **The Recursive Past Equation**

Given a Time Series 
$$Y = \{y_1, y_2, y_3, ..., y_{n-1}, y_n\}$$

we can find  $y_0$  using the following Recursive Past Equation

$$y_{n} = \underset{p \to \infty}{\textit{Limit}} \frac{\left\{ \sum_{k=0}^{n-1} y_{k} \left\{ \left\{ \frac{S_{k}}{L_{k}} \right\} + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\} + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\} + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\} + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\} \right\} \right\}}{\sqrt{\sum_{k=0}^{n-1} \left\{ \left\{ \frac{S_{k}}{L_{k}} \right\}^{2} + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\}^{2} + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\}^{2} + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\}^{2} + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\}^{2} \right\}}}$$

where

$$S_{k} = Smaller of (y_{n}, y_{k}) \text{ and } L_{k} = Larger of (y_{n}, y_{k})$$
  

$$S_{k+1} = Smaller of ((L_{k} - S_{k}), y_{k}) \text{ and } L_{k+1} = Larger of ((L_{k} - S_{k}), y_{k})$$

$$\begin{split} S_{k+2} &= Smaller \ of \ \left( \left( L_{k+1} - S_{k+1} \right), y_k \right) \ \text{and} \ L_{k+2} = Larg \ er \ of \ \left( \left( L_{k+1} - S_{k+1} \right), y_k \right) \\ S_{k+p-1} &= Smaller \ of \ \left( \left( L_{k+p-2} - S_{k+p-2} \right), y_k \right) \ \text{and} \ L_{k+p-1} = Larg \ er \ of \ \left( \left( L_{k+p-2} - S_{k+p-2} \right), y_k \right) \\ S_{k+p} &= Smaller \ of \ \left( \left( L_{k+p-1} - S_{k+p-1} \right), y_k \right) \ \text{and} \ L_{k+p} = Larg \ er \ of \ \left( \left( L_{k+p-1} - S_{k+p-1} \right), y_k \right) \\ \text{where} \ p \ \text{is a Number which makes the aforementioned Difference Residual} \ \left( L_{k+p-1} - S_{k+p-1} \right) \ \text{tend to Zero.} \\ \text{From the above Recursive Equation, we can solve for } Y_0. \end{split}$$

# \_\_\_\_

We consider  $y_0$  and slate the Ananda-Damayanthi Similarity [1] between  $y_0$  and  $y_n$  which turns out to be  $\left\{\frac{S_0}{L_0}\right\}$ . We now consider the lack of similarity part, i.e.,  $(L_0 - S_0)$  and again find the Similarity between  $y_0$ 

and 
$$(L_0 - S_0)$$
 which turns out to be  $\left\{\frac{S_{0+1}}{L_{0+1}}\right\} = \left\{\frac{S_1}{L_1}\right\}$ . And similarly, we find  $\left\{\frac{S_{0+2}}{L_{0+2}}\right\} = \left\{\frac{S_2}{L_2}\right\}$ ,  $\left\{\frac{S_{0+3}}{L_{0+3}}\right\} = \left\{\frac{S_3}{L_3}\right\}$ , ...,  $\left\{\frac{S_{0+p-1}}{L_{0+p-1}}\right\} = \left\{\frac{S_{p-1}}{L_{p-1}}\right\}$ ,  $\left\{\frac{S_{0+p}}{L_{0+p}}\right\} = \left\{\frac{S_p}{L_p}\right\}$ . We now add them all. Similarly, we

consider  $y_2$ ,  $y_3$ ,...., upto  $y_{n-1}$  and compute such aforementioned quantities and add them all. We now Normalize, i.e., divide each of this value by the quantity  $\sqrt{\sum_{k=0}^{n-1} \left\{ \left\{ \frac{S_k}{L_k} \right\}^2 + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\}^2 + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\}^2 + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\}^2 + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\}^2 \right\}}$ . We equate this value to  $y_n$ 

as the RHS is the Total Normalized Similarity contribution from each element of the Time Series Set  $Y = \{y_0, y_1, y_2, y_3, \dots, y_{n-1}\}$  with respect to  $y_n$ .

# **General Form**

We can note that the above equation  

$$y_{n} = \underset{p \to \infty}{Limit} \frac{\left\{\sum_{k=0}^{n-1} y_{k} \left\{\left\{\frac{S_{k}}{L_{k}}\right\} + \left\{\frac{S_{k+1}}{L_{k+1}}\right\} + \left\{\frac{S_{k+2}}{L_{k+2}}\right\} + \dots + \left\{\frac{S_{k+p-1}}{L_{k+p-1}}\right\} + \left\{\frac{S_{k+p}}{L_{k+p}}\right\}\right\}\right\}}{\sqrt{\sum_{k=0}^{n-1} \left\{\left\{\frac{S_{k}}{L_{k}}\right\}^{2} + \left\{\frac{S_{k+1}}{L_{k+1}}\right\}^{2} + \left\{\frac{S_{k+2}}{L_{k+2}}\right\}^{2} + \dots + \left\{\frac{S_{k+p-1}}{L_{k+p-1}}\right\}^{2} + \left\{\frac{S_{k+p}}{L_{k+p}}\right\}^{2}\right\}}$$

is in general of the form

$$y_{n} = \frac{\left\{b_{1}y_{n} + \frac{b_{2}}{y_{n}}\right\}}{\sqrt{\left\{\left(b_{3}y_{n}\right)^{2} + \left(\frac{b_{4}}{y_{n}}\right)^{2}\right\}}}$$

where,  $b_1$ ,  $b_2$ ,  $b_3$  and  $b_4$  are some positive integers.

We can further write the above equation as

$$(y_n)^2 \left\{ (b_3 y_n)^2 + \left(\frac{b_4}{y_n}\right)^2 \right\} = \left\{ b_1 y_n + \frac{b_2}{y_n} \right\}^2$$

$$(b_3)^2 (y_n)^6 - (b_1)^2 (y_n)^4 + \left\{ (b_4)^2 - (2b_1b_2) \right\} (y_n)^2 - (b_2)^2 = 0$$
Equation B
where,  $b_1, b_2, b_3$  and  $b_4$  are some positive integers.

**Defining Error** 

We define Error in the following fashion:

For the Recursive Past Equation:

#### Method 1

Given a Time Series  $Y = \{y_1, y_2, y_3, \dots, y_{n-1}, y_n\}$  we consider only  $Y = \{y_2, y_3, \dots, y_{n-1}, y_n\}$  and use the aforementioned Recursive Future Past to find the 1<sup>st</sup> term. Say this is  ${}^{p} Y_1$  where the p stands for the 'predicted' or 'forecasted' value. Then, the Error is defined by

$$\varepsilon_P = \left(\frac{y_1 - {}^p y_1}{y_1}\right)$$

Method 2

Given a Time Series  $Y = \{y_1, y_2, y_3, \dots, y_{n-1}, y_n\}$  we consider it and use the aforementioned Recursive Future Equation to find the term previous to  $y_1$ . Say this is  ${}^p y_0$  where the p stands for the 'predicted' or 'forecasted' value. We now consider the Time Series Set  $Y = \{y_0, y_1, y_2, y_3, \dots, y_{n-1}\}$  and use the aforementioned Recursive Future Equation to generate the term next to  $y_{n-1}$ , i.e.,  ${}^p y_n$ . Then, the Error is defined by

$$\varepsilon_F = \left(\frac{y_n - y_n}{y_n}\right)$$

### **Functional Form Equation For Making Past Forecast**

A Seasoned reader of author Literature, especially the section on '*Functional Form Equation For Making Future Forecast*' can infer the procedure for the Past Forecast which is very much similar to the Future Forecast.

#### **Computation Complexity**

For the World's fastest Chineese Super-Computer which can compute 33,870 Trillion Computations per second we can use the equation

 $2^{n} + m(2^{n}) = 33870 \times 10^{9}$  to calculate the Maximum Number of Terms of the Time Series n for which we wish to predict the  $(n+1)^{th}$  term and m is the Number Of Difference Residual Terms we wish to consider for each term, to find the n for a given m so that the  $(n+1)^{th}$  term is computed in one second.

Furthermore, if we take m = 3 and for different amounts of times we can spare for getting the computed answer, the Number of Terms of the Time Series n that we can consider is given below:

Serial Number	Duration Of Computation	Number of Terms To Consider
1	1 Second	43.36011
2	1 Hour	55.17389
3	1 Day	59.75885
4	1 Week	62.56621
5	1 Month (31 Days)	64.71305
6	1 Year	68.27061

## References

1.Bagadi, R. (2016). Proof Of As To Why The Euclidean Inner Product Is A Good Measure Of Similarity Of Two Vectors. *PHILICA.COM Article number 626*. See the Addendum as well.

http://philica.com/display\_article.php?article\_id=626

 $2.http://www.vixra.org/author/ramesh\_chandra\_bagadi$ 

3.http://philica.com/advancedsearch.php?author=12897