

The Recursive Future And Past Equation Based On The Ananda-Damayanthi Normalized Similarity Measure Considered To Exhaustion

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Abstract

In this research investigation, the author has presented a Recursive Past Equation and a Recursive Future Equation based on the Ananda-Damayanthi Normalized Similarity Measure considered to Exhaustion [1].

The Recursive Future Equation

Given a Time Series $Y = \{y_1, y_2, y_3, \dots, y_{n-1}, y_n\}$

we can find y_{n+1} using the following Recursive Future Equation

$$y_{n+1} = \lim_{p \rightarrow \infty} \frac{\left\{ \sum_{k=1}^n y_k \left\{ \left\{ \frac{S_k}{L_k} \right\} + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\} + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\} + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\} + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\} \right\} \right\}}{\sqrt{\sum_{k=1}^n \left\{ \left\{ \frac{S_k}{L_k} \right\}^2 + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\}^2 + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\}^2 + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\}^2 + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\}^2 \right\}}}$$

where

$S_k = \text{Smaller of } (y_{n+1}, y_k) \text{ and } L_k = \text{Larger of } (y_{n+1}, y_k)$

$S_{k+1} = \text{Smaller of } ((L_k - S_k), y_k) \text{ and } L_{k+1} = \text{Larger of } ((L_k - S_k), y_k)$

$S_{k+2} = \text{Smaller of } ((L_{k+1} - S_{k+1}), y_k) \text{ and } L_{k+2} = \text{Larger of } ((L_{k+1} - S_{k+1}), y_k)$

$S_{k+p-1} = \text{Smaller of } ((L_{k+p-2} - S_{k+p-2}), y_k) \text{ and } L_{k+p-1} = \text{Larger of } ((L_{k+p-2} - S_{k+p-2}), y_k)$

$S_{k+p} = \text{Smaller of } ((L_{k+p-1} - S_{k+p-1}), y_k) \text{ and } L_{k+p} = \text{Larger of } ((L_{k+p-1} - S_{k+p-1}), y_k)$

From the above Recursive Equation, we can solve for y_{n+1} .

Proof:

We consider y_1 and find the Ananda-Damayanthi Similarity [1] between y_1 and y_{n+1} which turns out to be $\left\{ \frac{S_1}{L_1} \right\}$. We now consider the lack

of similarity part, i.e., $(L_1 - S_1)$ and again find the Similarity between y_1 and $(L_1 - S_1)$ which turns out to be $\left\{ \frac{S_{1+1}}{L_{1+1}} \right\} = \left\{ \frac{S_2}{L_2} \right\}$. And similarly,

we find $\left\{ \frac{S_{1+2}}{L_{1+2}} \right\} = \left\{ \frac{S_3}{L_3} \right\}$, $\left\{ \frac{S_{1+3}}{L_{1+3}} \right\} = \left\{ \frac{S_4}{L_4} \right\}$, $\left\{ \frac{S_{1+p-1}}{L_{1+p-1}} \right\} = \left\{ \frac{S_p}{L_p} \right\}$, $\left\{ \frac{S_{1+p}}{L_{1+p}} \right\}$. We now add them all. Similarly, we consider y_2, y_3, \dots ,

upto y_{n-1} and y_n and compute such aforementioned quantities and add them all. We now Normalize, i.e., divide each of this value by the

quantity $\sqrt{\sum_{k=1}^n \left\{ \left\{ \frac{S_k}{L_k} \right\}^2 + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\}^2 + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\}^2 + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\}^2 + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\}^2 \right\}}$. We equate this value to y_{n+1} as the RHS is the Total

Normalized Similarity contribution from each element of the Time Series Set with respect to y_{n+1} .

The Recursive Past Equation

Given a Time Series $Y = \{y_1, y_2, y_3, \dots, y_{n-1}, y_n\}$

we can find y_0 using the following Recursive Past Equation

$$y_n = \lim_{p \rightarrow \infty} \frac{\left\{ \sum_{k=0}^{n-1} y_k \left\{ \left\{ \frac{S_k}{L_k} \right\} + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\} + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\} + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\} + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\} \right\} \right\}}{\sqrt{\sum_{k=0}^{n-1} \left\{ \left\{ \frac{S_k}{L_k} \right\}^2 + \left\{ \frac{S_{k+1}}{L_{k+1}} \right\}^2 + \left\{ \frac{S_{k+2}}{L_{k+2}} \right\}^2 + \dots + \left\{ \frac{S_{k+p-1}}{L_{k+p-1}} \right\}^2 + \left\{ \frac{S_{k+p}}{L_{k+p}} \right\}^2 \right\}}}$$

where

$S_k = \text{Smaller of } (y_n, y_k) \text{ and } L_k = \text{Larger of } (y_n, y_k)$

$S_{k+1} = \text{Smaller of } ((L_k - S_k), y_k) \text{ and } L_{k+1} = \text{Larger of } ((L_k - S_k), y_k)$

$S_{k+2} = \text{Smaller of } ((L_{k+1} - S_{k+1}), y_k) \text{ and } L_{k+2} = \text{Larger of } ((L_{k+1} - S_{k+1}), y_k)$

$S_{k+p-1} = \text{Smaller of } ((L_{k+p-2} - S_{k+p-2}), y_k) \text{ and } L_{k+p-1} = \text{Larger of } ((L_{k+p-2} - S_{k+p-2}), y_k)$

$S_{k+p} = \text{Smaller of } ((L_{k+p-1} - S_{k+p-1}), y_k) \text{ and } L_{k+p} = \text{Larger of } ((L_{k+p-1} - S_{k+p-1}), y_k)$

From the above Recursive Equation, we can solve for y_0 .

References

1. Bagadi, R. (2016). Proof Of As To Why The Euclidean Inner Product Is A Good Measure Of Similarity Of Two Vectors. *PHILICA.COM* Article number 626. See the Addendum as well.
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3. <http://philica.com/advancedsearch.php?author=12897>