

# Affirmative resolve of Legendre's conjecture if Riemann Hypothesis is true.

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## Abstract

Near  $m$ , the distance of primes is lower order than  $\log m$ . This is the key to solve the Legendre's conjecture.

## 1

**Theorem 1.1.** *Legendre's conjecture*  
*There is at least 1 prime  $n^2$  and  $(n + 1)^2$*

**Definition 1.1.**

$$Li(x) := \int_2^{\infty} \frac{1}{\log x} dx$$

**Theorem 1.2.** *The prime number less than  $m$  is*

$$\pi(m) = Li(m) + O(\sqrt{m} \log m)$$

We think constant  $K$ , for enough large  $m$ , "distance of primes"  $\ll K\sqrt{m} \log m$ .  $K$  is not depend on  $m$ . Remark  $K$  is taken less than 1. So, Legendre's conjecture is true for  $m$ .