

Prime density formula

1. Introduction

$$i^2 = -1$$

$$i^{2^n} = 1 \quad n \in \mathbb{N}^*$$

this paper "1" is Prime density

So Design function as

$$\frac{1 - i^{2^{|n-a|+1}}}{2} \quad a \in \mathbb{C} \quad " | \quad | " \text{ Absolute value}$$

Or

$$\frac{1 - (-1)^{2^{|n-a|}}}{2}$$

$$p(n) = n \left(1 - \frac{1 - i^{2^{|\prod_{k=1}^n (\prod_{m=1}^n (n - (k+1)(m+1)))|+1}}}{2} \right)$$

$$s(n) = \frac{\sum_1^n \left(1 - \frac{1-i^2 \left| \prod_{k=1}^n \left(\prod_{m=1}^n (n-(k+1)(m+1)) \right) \right| + 1}{2} \right)}{n}$$

Prime density formula s(n)

$$t(n) = \frac{1-i^2 \left| (n-a_1) \right| + 1}{2}$$

$$\frac{1-i^2 \left| (n-a_1) \right| + 1}{2} + \frac{1-i^2 \left| (n-a_2) \right| + 1}{2} = \frac{1-i^2 \left| (n-a_1)(n-a_2) \right| + 1}{2}$$

$a_1 \neq a_2$

$$\frac{1-i^2 \left| (n-a_1) \right| + 1}{2} = \frac{1 - \sin \left(\frac{\pi i^2 \left| (n-a_1) \right| + 1}{2} \right)}{2}$$

2. Derivation process

Set a function as follows

$$t(n) = \frac{1 - i^{2|n-a|+1}}{2} \quad 1.1$$

$a \in \mathbb{N}^*$ $n \in \mathbb{N}^*$ i is Imaginary unit

when $n=a$ $t(a)=1$

when $n \neq a$ $t(n)=0$

Use this property Set a function as follows

$$t(n) = \frac{1 - i^{2|(n-a_1)(n-a_2)(n-a_3)(n-a_4)\dots(n-a_m)|+1}}{2} \quad 1.2$$

$a_m = km$ $k, m \in \mathbb{N}^*$

When $n \in a_m$ $t(a_m)=1$

When $n \neq a_m$ $t(n)=0$

As follows

$a_m = 2m$

$$t(n) = \frac{1 - i^{2(|\prod_{m=1}^n (n - a_m)|) + 1}}{2}$$

$$\begin{aligned} \prod_{m=1}^n (n - a_m) &= (n - a_1)(n - a_2)(n - a_3) \dots (n - a_n) \\ &= (n - 2)(n - 4)(n - 6)(n - 8) \dots (n - a_n) \\ &= \prod_{m=1}^n (n - 2m) \end{aligned}$$

when $n \in 2m$ $t(n) = 1$

when $n \notin 2m$ $t(n) = 0$

$m, n \in \mathbb{N}^*$

$t(1) = 0$ $t(2) = 1$ $t(3) = 0$ $t(4) = 1$

$t(2n) = 1$ $t(2n - 1) = 0$

so

$$1 - t(n) = \frac{1 - i^{2(|\prod_{m=1}^n (n - (2m - 1))|) + 1}}{2}$$

$2 * 2$	$2 * 3$	$2 * 4$	$2 * 5$	$2(m + 1)$
$3 * 2$	$3 * 3$	$3 * 4$	$3 * 5$	$3(m + 1)$
$4 * 2$	$4 * 3$	$4 * 4$	$4 * 5$	$4(m + 1)$
$5 * 2$	$5 * 3$	$5 * 4$	$5 * 5$	$5(m + 1)$
$6 * 2$	$6 * 3$	$6 * 4$	$6 * 5$	$6(m + 1)$

$$\begin{array}{cccccc}
 \cdot & & \cdot & & \cdot & & \cdot & & \cdot & \dots & & \cdot \\
 \cdot & & \cdot & & \cdot & & \cdot & & \cdot & \dots & & \cdot \\
 \cdot & & \cdot & & \cdot & & \cdot & & \cdot & \dots & & \cdot \\
 \cdot & & \cdot & & \cdot & & \cdot & & \cdot & \dots & & \cdot \\
 \cdot & & \cdot & & \cdot & & \cdot & & \cdot & \dots & & \cdot \\
 (k+1)*2 & & (k+1)*3 & & & & & & & & & (k+1)(m+1)
 \end{array}$$

$K, m \in \mathbb{N}^*$

$H(n) =$

$$\begin{aligned}
 & \left(\prod_{m=1}^n (n - 2(m + 1)) \right) \left(\prod_{m=1}^n (n - 3(m + 1)) \right) \dots \\
 & = \left(\prod_{k=1}^n \left(\prod_{m=1}^n (n - (k + 1)(m + 1)) \right) \right) \quad 1.3
 \end{aligned}$$

When $n \in$ Composite number

$$H((k+1)(m+1)) = 0$$

When $n \notin$ Composite number

$$|H(n)| \in \mathbb{N}^*$$

So this formula

$$h(n) = \frac{1 - i^{2^{|H(n)|+1}}}{2}$$

When $n \in$ Composite number

$$h(n) = 1$$

When $n \notin$ Composite number

$$h(n) = 0$$

so

when $n \in$ prime number or 1

$$h(n) = \frac{1 - i^{2^{|H(n)|+1}}}{2} = 0$$

and so

$$1 - \frac{1 - i^{2^{|H(n)|+1}}}{2} = 1$$

So The Number of primes for 1 to n as follows

$$n, k, m \in \mathbb{N}^*$$

$P(n)=$

$$1 - \frac{1 - i^{2^{|H(n)|+1}}}{2} = 1 - \frac{1 - i^{2^{|\prod_{k=1}^n (\prod_{m=1}^n (n - (k+1)(m+1)))|+1}}}{2}$$

Number of primes =

$$\sum_1^n P(n)$$

=

$$\sum_1^n \left(1 - \frac{1 - i^{2^{|H(n)|+1}}}{2} \right)$$

=

$$\sum_1^n \left(1 - \frac{1 - i^{2^{|\prod_{k=1}^n (\prod_{m=1}^n (n - (k+1)(m+1)))|+1}}}{2} \right)$$

So the Prime density formula $s(n)$

$$= \frac{\sum_1^n \left(1 - \frac{1-i^2}{2} \left| \prod_{k=1}^n \left(\prod_{m=1}^n (n - (k+1)(m+1)) \right) \right| + 1 \right)}{n}$$

