# The Planckian Hierarchal Schematic

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#### Abstract

The construction of the Planckian hierarchal schematic, comprised of four very well-known Planck constants, i.e., h, h, lp and tp. The reintroduction of a forgotten constant,  $\frac{1}{2}h$ . The postulation of a new Planck constant - the Planck circumference, symbol O, where the Planck length is its diameter. The natural outcome of  $\pi$  as the ratio of the Planck length and Planck circumference. Also, the initialization of the ratio of  $\frac{1}{2}h$  and the Planck circumference, O, with a value of 1.038499006, referred to, as the ratio of attribute. The crux of this paper is to show that the dimensionless ratios of the Planckian schematic (i.e., 2, 1.038499006,  $\pi$  and c) can be utilized to enumerate the Planck momentum, Planck mass and the Planck energy constants.

Standard model (incomplete) Planckian hierarchal schematic:

(five well-known Planck constants in an hierarchal configuration)

 $\begin{array}{c} ({\sf Planck\ constant}) & 6.626068909\ x10^{-34} & h \\ ({\sf reduced\ Planck\ constant}) & 1.054571620\ x10^{-34} & h & 2\pi \\ ({\sf half\ reduced\ Planck\ constant}) & 5.272858101\ x10^{-35} & (\frac{1/2}{2}h) & 2 \\ \end{array}$   $\begin{array}{c} ({\sf Planck\ length}) & 1.616181480\ x10^{-35} & lp & \\ ({\sf Planck\ time}) & 5.391001132\ x10^{-44} & tp & c \end{array}$ 

Proposed (complete) Planckian hierarchal schematic, with the postulated Planck circumference constant, symbol P, and two respective ratios:  $\pi$  & 1.038499006.

(Planck constant)  $6.626068909 \times 10^{-34}$  h (reduced Planck constant)  $1.054571620 \times 10^{-34}$  h  $2\pi$ (half reduced Planck constant)  $5.272858101 \times 10^{-35}$  ( $\frac{1}{2}$ h) 2 (Planck circumference\*)  $5.077383865 \times 10^{-35}$  (Planck length)  $1.616181480 \times 10^{-35}$  lp  $\pi$ (Planck time)  $5.391001132 \times 10^{-44}$  tp c **Half of the reduced Planck constant**, ( $\frac{1}{2}\hbar$ ) "The forgotten constant", During the quantum revolution, Neils Bohr proposed that the reduced Planck constant, symbol  $\hbar = h/2\pi$ , was the smallest attribute of a particle, .i.e., the quantization of its orbital angular momentum. Then, in 1925, physicists Sam Goudsmit and George Uhlenbech discovered that the electron also possessed spin angular momentum with a magnitude of half of the reduced Planck constant, symbol ( $\frac{1}{2}\hbar$ ). This gave Dirac the fourth quantum number to codify his equation. [4] Though, the importance of spin cannot be over-stated; It will be demonstrated that half of the reduced Planck constant ( $\frac{1}{2}\hbar$ ), is a crucial player (above and beyond its definition of spin) in the scheme of fundamental physics. It will be shown to have a prominent role in the hierarchical evolution of the constants. The National Institute of Standards and Technology (NIST) does not list half of the reduced Planck constant ( $\frac{1}{2}\hbar$ ).[1]

 $\pi$ , In the thirty-five hundred years since its discovery, physicists have been unable to give  $\pi$  a definable function within the context of fundamental equations, albeit ubiquitous. The Planckian schematic shows the first  $\pi$  as a ratio in the hierarchal schematic.

### First pi equation:

$$\pi = \frac{\mathscr{P}}{lp}$$

# **Ratio of attribute**

(half of the reduced Planck constant,  $\frac{1}{2}\hbar$  divided by the Planck circumference, D)

$$\frac{(\frac{1}{2})\hbar}{\mathscr{D}} = 1.038499006$$

# Enumerated constants, via ratios of the Planckian hierarchal schematic:

Planck momentum  
MOp = 
$$2\left[\frac{(\frac{1}{2})\hbar}{\varnothing}\right]\pi$$
 = 6.52508

**Planck mass** 

mp = 
$$\frac{2\left[\frac{(\frac{1}{2})\hbar}{\mathcal{D}}\right]\pi}{c}$$
 = 2.176532972 x10<sup>-8</sup> kg

(The speed of light, c, value: 299792458, utilized as a dimensionless constant)

Note: within the 2010 (NIST) CODATA value: 2.17651(13) x10<sup>-8</sup> kg

The NIST lists the Planck mass equation (standard model) as:  $mp = (\hbar c/G)^{\frac{1}{2}}$  [1]

**Planck energy** 

Ep = 
$$2\left[\frac{(\frac{1}{2})\hbar}{\mathcal{P}}\right]\pi c$$
 = 1.9561 x10<sup>9</sup>

half of reduced Planck constant

$$(\frac{1}{2})\hbar = \mathcal{P}\left[\frac{(\frac{1}{2})\hbar}{\mathcal{P}}\right] = 5.272858101 \text{ x}10^{-35}$$

## Reduced Planck constant (h-bar)

$$\hbar = 2 \mathcal{P}\left[\frac{(\frac{1}{2})\hbar}{\mathcal{P}}\right] = 1.054571619 \text{ x}10^{-34}$$

### **Planck Constant**

h = 
$$4\pi \mathscr{P}\left[\frac{(\frac{1}{2})\hbar}{\mathscr{P}}\right]$$
 = 6.626068909 x10<sup>-34</sup>

### **Planck Temperature**

Tp = 
$$2\left[\frac{(\frac{1}{2})\hbar}{\mathcal{D}}\right]\pi c$$
 = 1.41684693 x10<sup>32</sup>

where: k = 1.38065048 x10<sup>-23</sup> (Boltzmann constant)

#### Conclusion

The enumeration of the Planck – momentum, mass and energy, solely by the dimensionless constants of the Planckian hierarchal schematic: 2, 1.038499006,  $\pi$  and 299792458. (something that has never been done before)

#### References

- [1]. NIST, Fundamental Physical Constants (2006 / 2010 / 2014)
- [2]. Quantum Dance, Princeton.edu, Feb. 18, 2009
- [3]. Kenneth W. Ford, The Quantum World, Harvard University Press, USA (2004)
- [4] John D. Barrow, The Constants, Pantheon Books, USA (2002)