

Violation of no-signaling constraint by local quantum measurement discrimination with numerous eight-qubit entangled states

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ABSTRACT

The discrimination of quantum measurements is an important subject of quantum information processes. In this paper we present a novel protocol for local quantum measurement discrimination (LQMD) with multi-qubit entanglement systems. It is shown that, for two spacelike separated parties, the local discrimination of two different kinds of measurement can be completed via numerous eight-qubit GHZ entangled states and selective projective measurements without help of classical information. This means that no-signaling constraint can be violated by the LQMD.

Keywords: No-signaling constraint, Local quantum measurement discrimination, Multi-qubit GHZ entangled states, Selective projective measurement

1. Introduction

Quantum entanglement is one of the striking features of quantum mechanics [1]. The nonlocal nature of entanglement is the essential resource for many quantum information tasks including teleportation [2] and superdense coding [3]. However, although entanglement appears to allow particles which are separated in space to influence one another instantaneously [4], it has been pointed that this cannot be used to signal without help of classical communication [5-8], *i. e.* the no-signaling constraint [9] holds that one cannot exploit quantum entanglement to transmit classical information across spacelike intervals.

On the other hand, it is well-known that measurement is a central tenet of quantum mechanics. The problem of discrimination between quantum measurements has been recently considered in quantum information tasks [10-13]. Ji *et al.* [10] have proposed simple schemes that can perfectly identify projective measurement apparatuses secretly chosen from a finite set. Entanglement is used in this schemes both to make possible the perfect identification and to improve the efficiency significantly. Fiurasek and Micuda [11] have studied optimal discrimination between two projective quantum measurements on a single qubit. Ziman *et al.* [12] have investigated the unambiguous comparison of unknown quantum measurements represented by nondegenerate sharp positive operator valued measures (POVM). One can notice that, in above works [10-13] of discriminating quantum measurement, employing classical communication is necessary.

For two spacelike separated parties, existing researches [5-9] have pointed that since no-signaling constraint, the local discrimination of quantum operations cannot be completed. In the last decade, the correctness of no-signaling constraint has been frequently discussed and proved (*e. g.* [14-19]). It is easy found that, however, in these discussions and demonstrations, only a single two- or multi-particle entangled state has been employed. By a careful analysis, it may be found that, if multiple multi-qubit entangled states and a kind of special measurement (called selective projective measurement) are employed, the local discrimination of quantum measurements can be realized without assistance of classical communication. In this work, we first present a protocol for local quantum measurement discrimination (LQMD) via selective projective measurement with numerous eight-qubit GHZ states. It is shown that, in this protocol, if both two observers (Alice and Bob) agreed in advance that one of them (*e.g.* Alice) should measure her qubits before an appointed time (it is equivalent that, after her measurement, Alice only announced publicly that she had completed the measurement, and did not declare the result of her measurement), the local discrimination of two different kinds of measurement can be realized by using a series of single-qubit correlative measuring basis without help of classical communication. This means that the LQMD protocol may be not restricted by the no-signaling.

2. Local discrimination of quantum measurements with a single entangled state

To present our protocol more clearly, let us first review existing scheme of LQMD (*e. g.* [19]). Assume that Alice and Bob share bipartite quantum system described by a known state ρ . They can make local measurements, with elements

$$\sum_i A_i^\dagger A_i = I \quad , \quad \sum_j B_j^\dagger B_j = I \quad (1)$$

on the subsystems A and B respectively, where A_i and B_j are the “detector operators”

associated to the elements of a POVM for the observation of results μ_A by Alice and ν_B by Bob. If

Bob is not informed that Alice got outcome μ_A , the mean value that he gets any observable ν_B is

$$\begin{aligned} \langle \nu_B \rangle &= tr_{AB} \left\{ \sum_i A_i \rho A_i^\dagger \nu_B \right\} = tr_A \left\{ \sum_i A_i^\dagger A_i tr_B \left\{ \rho \nu_B \right\} \right\} \\ &= tr_B \left\{ tr_A \left\{ \rho \right\} \nu_B \right\} . \end{aligned} \quad (2)$$

Since the result of Eq. (2) does not depend on Alice’s operators, Bob cannot decide what measurements Alice did without her help. As described above, it is clearly shown that the LQMD with a single entangled state must obey the no-signaling constraint.

3. Two different kinds of quantum projective measurement

Suppose that an eight-qubit GHZ state is shared by Alice and Bob,

$$|\Phi\rangle = \frac{1}{\sqrt{2}} \left(|00000000\rangle + |11111111\rangle \right)_{A_1 A_2 A_3 A_4 A_5 A_6 A_7 B} , \quad (3)$$

where qubits A_1, A_2, \dots, A_7 are in the possession of Alice and B belongs to Bob. Assume that Alice and Bob agreed in advance that Alice should measure her qubits before an appointed time. Now, let Alice make two different kinds of measurement on the state $|\Phi\rangle$. In the first kind of measurement, Alice makes common projective measurements (CPMs) on her qubits $A_1, A_2, \dots,$ and A_7 under the measurement basis $\{|+\rangle, |-\rangle\}$, where $|+\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$, $|-\rangle = \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle)$, successively.

One can see that, after measurements of Alice, 128 possible final collapsed states of the qubit B will always be $\frac{1}{8\sqrt{2}}|+\rangle_B$ or $\frac{1}{8\sqrt{2}}|-\rangle_B$. Now we turn to the second kind of measurement. To realize

the LQMD, Alice will utilize a novel kind of projective measurements, which we refer to as selective projective measurements (SPMs), with a series of single-qubit correlative measuring basis, on her qubits. Firstly, Alice measures the qubit A_1 in the state $|\Phi\rangle$ under the basis $\{|\nu\rangle, |\nu^\perp\rangle\}$, where $|\nu\rangle = x|0\rangle + y|1\rangle$, $|\nu^\perp\rangle = y|0\rangle - x|1\rangle$, x and y are real, $x^2 + y^2 = 1$, and let $x = \sqrt{6}/3$, $y = \sqrt{3}/3$. If measurement outcome of Alice is $|\nu\rangle_{A_1}$, the state of qubits A_2, A_3, \dots, A_7 and B will evolve as

$$|\phi_1\rangle = \frac{1}{\sqrt{2}}(x|0000000\rangle + y|1111111\rangle)_{A_2 A_3 A_4 A_5 A_6 A_7 B}, \quad (4)$$

she can in turn measure the qubits A_2, A_3, \dots, A_7 under the basis $\{|+\rangle, |-\rangle\}$. After that, the qubit

B will always be in the state $\frac{1}{8}|\mu^+\rangle_B$ or $\frac{1}{8}|\mu^-\rangle_B$, here $|\mu^+\rangle = \frac{1}{\sqrt{2}}(x|0\rangle + y|1\rangle)$

and $|\mu^-\rangle = \frac{1}{\sqrt{2}}(x|0\rangle - y|1\rangle)$. If measurement result of Alice is $|\nu^\perp\rangle_{A_1}$, the qubits $A_2, A_3, \dots,$

A_6 and B will be in the state of

$$|\phi_1'\rangle = \frac{1}{\sqrt{2}}(y|0000000\rangle - x|1111111\rangle)_{A_2 A_3 A_4 A_5 A_6 A_7 B}. \quad (5)$$

Then Alice measures the qubit A_2 under the measurement basis $\{|\lambda_1\rangle, |\lambda_1^\perp\rangle\}$, which is given by

$$|\lambda_1\rangle = \frac{1}{F_2} \left(\frac{x}{y}|0\rangle + \frac{y}{x}|1\rangle \right), \quad |\lambda_1^\perp\rangle = \frac{1}{F_2} \left(\frac{y}{x}|0\rangle - \frac{x}{y}|1\rangle \right), \quad (6)$$

where $F_2 = \left[(x/y)^2 + (y/x)^2 \right]^{1/2}$. Corresponding to Alice's measurement outcome $|\lambda_1\rangle_{A_2}$ or $|\lambda_1^\perp\rangle_{A_2}$, the state of qubits A_3, \dots, A_7 and B will evolve as $|\phi_2\rangle$ or $|\phi_2'\rangle$, which can be expressed as

$$\begin{aligned} |\phi_2\rangle &= \frac{1}{\sqrt{2}F_2} (x|000000\rangle - y|111111\rangle)_{A_3A_4A_5A_6A_7B}, \\ |\phi_2'\rangle &= \frac{1}{\sqrt{2}F_2} \left(\frac{y^2}{x}|000000\rangle + \frac{x^2}{y}|111111\rangle \right)_{A_3A_4A_5A_6A_7B}. \end{aligned} \quad (7)$$

As described above, we can easily find that the goal of the SPMs is as much as possible to make the qubit B collapsed into the state $\frac{1}{R}|\mu^+\rangle$ or $\frac{1}{R}|\mu^-\rangle$ after all, where R is a constant or a coefficient related to x and y . To present the SPMs more clearly, by mentioned above, we can generalize the general approach of the SPMs as follows:

If the state of qubits $A_{n+1}, A_{n+2}, \dots, A_m$ and B becomes

$$|\phi_n'\rangle = \frac{1}{\sqrt{2}T_n} \left(\frac{y^{p_n}}{x^{p_n-1}}|00\dots 00\rangle + \frac{x^{p_n}}{y^{p_n-1}}|11\dots 11\rangle \right)_{A_{n+1}A_{n+2}\dots A_m B}, \quad (8)$$

where $n=1, 2, \dots, m$, $T_n = F_1 F_2 \dots F_n$, $p_n = 2^{n-1}$, $F_n = \left[(x/y)^{p_n} + (y/x)^{p_n} \right]^{1/2}$, and let

$F_1 = 1$, Alice should make a new single-qubit projective measurement on the qubit A_{n+1} under the basis $\{|\lambda_n\rangle, |\lambda_n^\perp\rangle\}$, which can be expressed as

$$\begin{aligned} |\lambda_n\rangle &= \frac{1}{F_{n+1}} \left[\left(\frac{x}{y} \right)^{p_n} |0\rangle + \left(\frac{y}{x} \right)^{p_n} |1\rangle \right], \\ |\lambda_n^\perp\rangle &= \frac{1}{F_{n+1}} \left[\left(\frac{y}{x} \right)^{p_n} |0\rangle - \left(\frac{x}{y} \right)^{p_n} |1\rangle \right]. \end{aligned} \quad (9)$$

If the measurement outcome of Alice is $|\lambda_n\rangle$, the state of qubits $A_{n+2}, A_{n+3}, \dots, A_m$ and B will evolve as $|\phi_{n+1}\rangle$, which may be expressed as

$$|\phi_{n+1}\rangle = \frac{1}{\sqrt{2}T_{n+1}} (x|00\dots 00\rangle + y|11\dots 11\rangle)_{A_{n+2}A_{n+3}\dots A_m B}, \quad (10)$$

she can in turn measure the qubits $A_{n+2}, A_{n+3}, \dots, A_m$ under the measurement basis $\{|+\rangle, |-\rangle\}$,

the state of qubit B will evolve as $\frac{1}{2^d T_{n+1}} |\mu^+\rangle$ or $\frac{1}{2^d T_{n+1}} |\mu^-\rangle$, here $d = (m - n - 1) / 2$. If

measurement result of Alice is $|\lambda_n^\pm\rangle$, the state of qubits $A_{n+2}, A_{n+3}, \dots, A_m$ and B will become

$$|\phi_{n+1}'\rangle = \frac{1}{\sqrt{2} T_{n+1}} \left(\frac{y^{p_{n+1}}}{x^{p_{n+1}-1}} |00 \dots 00\rangle - \frac{x^{p_{n+1}}}{y^{p_{n+1}-1}} |11 \dots 11\rangle \right)_{A_{n+2} A_{n+3} \dots A_m B}, \quad (11)$$

she should repeat above similar approach, until the outcome of measurement $|\lambda_{m-1}\rangle_{A_m}$ or $|\lambda_{m-1}^\pm\rangle_{A_m}$

under the basis $\{|\lambda_{m-1}\rangle, |\lambda_{m-1}^\pm\rangle\}$ has been obtained, and the state of qubit B becomes $\frac{1}{T_m} |\mu^+\rangle_B$

or $\frac{1}{\sqrt{2} T_m} \left(\frac{y^{p_m}}{x^{p_m-1}} |0\rangle - \frac{x^{p_m}}{y^{p_m-1}} |1\rangle \right)_B$ after all.

By above general approach, after Alice's measurements, 128 possible final collapsed states of the qubit B can be obtained. The relation of the results of Alice's measurement and the possible final collapsed states of the qubit B can be expressed as follows:

$$|\nu\rangle_{A_1} \rightarrow |\psi_1^\pm\rangle_B = \frac{1}{8} |\mu^\pm\rangle_B \quad (64 \text{ terms})$$

$$|\lambda_1\rangle_{A_2} \rightarrow |\psi_2^\pm\rangle_B = \frac{1}{4\sqrt{2} T_2} |\mu^\pm\rangle_B \quad (32 \text{ terms})$$

$$|\lambda_2\rangle_{A_3} \rightarrow |\psi_3^\pm\rangle_B = \frac{1}{4 T_3} |\mu^\pm\rangle_B \quad (16 \text{ terms})$$

$$|\lambda_3\rangle_{A_4} \rightarrow |\psi_4^\pm\rangle_B = \frac{1}{2\sqrt{2} T_4} |\mu^\pm\rangle_B \quad (8 \text{ terms})$$

$$|\lambda_4\rangle_{A_5} \rightarrow |\psi_5^\pm\rangle_B = \frac{1}{2 T_5} |\mu^\pm\rangle_B \quad (4 \text{ terms})$$

$$|\lambda_5\rangle_{A_6} \rightarrow |\psi_6^\pm\rangle_B = \frac{1}{\sqrt{2} T_6} |\mu^\pm\rangle_B \quad (2 \text{ terms})$$

$$|\lambda_6\rangle_{A_7} \rightarrow |\psi_7^+\rangle_B = \frac{1}{T_7} |\mu^+\rangle_B \quad (1 \text{ term})$$

$$|\lambda_6^\pm\rangle_{A_7} \rightarrow |\psi_7^-\rangle_B = P |\eta\rangle_B, \quad (1 \text{ term}) \quad (12)$$

where $P = \frac{\sqrt{x^{254} + y^{254}}}{\sqrt{2} T_7 x^{63} y^{63}}$, $|\eta\rangle_B$ is a normalized state, which is given by

$$|\eta\rangle_B = \frac{1}{\sqrt{x^{254} + y^{254}}} (y^{127}|0\rangle - x^{127}|1\rangle)_B. \quad (13)$$

Thus much Alice's selective measurements have been completed. From Eqs. (12) and (13), it is easy

noted that, after Alice performing the SPMs on her all qubits, the states $\frac{1}{g_n T_n} |\mu^\pm\rangle_B$

($g_n = 2^{(7-n)/2}$, $n=1, 2, \dots, 7$) in all 128 collapsed states of the qubit B accounted for 127, and the

state $|\psi_7^-\rangle_B$ for 1. On the other hand, by simple calculation, one can find that, after Alice's

measurements the probability of the qubit B being in the state $\frac{1}{g_n T_n} |\mu^\pm\rangle_B$

($g_n = 2^{(7-n)/2}$, $n=1, 2, \dots, 7$) is 0.75, and in the state $|\eta\rangle_B$ is 0.25. It must be pointed out that it is

just these measured results of the SPM that led to the realization of the LQMD.

Clearly, after Alice performing the CPMs or SPMs on her qubits respectively, the final collapsed states of the qubit B are obvious different. As mentioned above, if Alice makes the CPMs on her qubits, after her measurements, 128 possible final collapsed states of the qubit B will always be

$\frac{1}{8\sqrt{2}} |+\rangle_B$ or $\frac{1}{8\sqrt{2}} |-\rangle_B$. If Alice employs the SPMs on her qubits, after her measurements, 128

possible final collapsed states of the qubit B can be given by Eq. (12). It must be emphasized that, whether Alice's measurements are the CPMs or SPMs, since Alice and Bob agreed in advance that Alice should measure her qubits before an appointed time, Bob can always know that the qubit B must be collapsed into the state corresponded to one of Alice's 128 results of measurement after Alice's measurements.

4. Local discrimination of two different kinds of measurement with numerous eight-qubit GHZ states

The detailed procedure of our LQMD protocol can be described as follows. Suppose that two spacelike separated observers, Alice and Bob, share N eight-qubit GHZ states. To ensure the following analysis becomes exact, here we take $N = 30$ [20]. Thus, the 30 eight-qubit GHZ states can be given by

$$|\Phi^{(k)}\rangle = \frac{1}{\sqrt{2}} (|00000000\rangle + |11111111\rangle)_{A_1^{(k)} A_2^{(k)} A_3^{(k)} A_4^{(k)} A_5^{(k)} A_6^{(k)} A_7^{(k)} B^{(k)}}, \quad (14)$$

where $k = 1, 2, \dots, 30$, and the qubits $A_1^{(k)}$, $A_2^{(k)}$, ..., $A_7^{(k)}$ are in the possession of Alice and

$B^{(k)}$ belong to Bob. Different from previous quantum operation discrimination schemes, we assume that there is no classical channel between Alice and Bob. In this case, before the agreed time t , Alice should randomly make two different kinds of measurements, CPMs or SPMs, on her qubits in the

state $|\Phi^{(k)}\rangle$ ($k=1,2,\dots,30$) respectively. Now we will consider the local discrimination of two different measurements.

(s1) If Alice performs the CPMs on her qubits, after Alice's measurements, all qubits $B^{(k)}$ will be in the states $\frac{1}{8\sqrt{2}}|+\rangle_{B^{(k)}}$ or $\frac{1}{8\sqrt{2}}|-\rangle_{B^{(k)}}$. At the appointed time t , Bob measures his qubits

$B^{(k)}$ all in the basis $\{|0\rangle, |1\rangle\}$. After Bob's measurements, by statistics theory, the probability of all qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to one.

(s2) If Alice's measurements are the SPMs, by mentioned above, after Alice's selective measurements, the probability of all qubits $B^{(k)}$ in the states $\frac{1}{g_n T_n}|\mu^+\rangle_B$ or $\frac{1}{g_n T_n}|\mu^-\rangle_B$

($g_n = 2^{(7-n)/2}$, $n=1,2,\dots,7$) is $(0.75)^{30} \approx 0.00018$, *i.e.*, the probability of at least one qubit

$B^{(k')}$ in the state $|\psi_7^-\rangle_B$ is $1 - (0.75)^{30} \approx 0.99982$. This means that, after Alice's SPMs, at least

one qubit $B^{(k')}$ will be collapsed into the state $|\psi_7^-\rangle_B$. Then, at the appointed time t , Bob measures

the qubits $B^{(k)}$ all in the basis $\{|0\rangle, |1\rangle\}$. One can find that, after Bob's measurements, the

probability of the qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be different from the case Alice employed the CPMs. To illustrate this clearly, without loss of generality, we first discuss the situation in

which only one qubit $B^{(k')}$ in the state $|\psi_7^-\rangle_B$ after Alice's measurements. From the state $|\psi_7^-\rangle_B$

in Eq. (12), it is easily found that, after measurements of Bob, the probability of the qubit $B^{(k')}$ in the

state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to u ($u = (\alpha^{127}/\beta^{127})^2 \approx 1.7 \times 10^{38}$), that is, the

qubit $B^{(k')}$ will be always collapsed into the state $|1\rangle$. As a special case, we also assume that all the

other 29 qubits $B^{(k)}$ are in the states $|\psi_1^\pm\rangle_B$ after Alice's measurements and then all the 29 qubits

are in the state $|0\rangle$ after Bob's measurements. In this case, one can easily find that the probability of

the 30 qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of 1 to 1.655 after Bob's

measurements. For general cases in which only one qubit $B^{(k')}$ in the state $|\psi_7^-\rangle_B$ and other 29

qubits $B^{(k)}$ collapsed randomly into the states $\frac{1}{g_n T_n} |\mu^\pm\rangle_B$ ($g_n = 2^{(7-n)/2}$, $n = 1, 2, \dots, 7$) after

Alice's measurements, it is easily found that the probability of the 30 qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to $w_{(1)}$ ($w_{(1)} > 1.655$) after Bob's measurements.

(s3) Now let us discuss the situation in which there are two qubits $B^{(k')}$ and $B^{(k'')}$ in the state $|\psi_7^-\rangle$ after Alice's measurements. Similar to the above mentioned, one can see that the probability of the 30 qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to $w_{(2)}$ ($w_{(2)} \geq 3.43$) after Bob's measurements.

(s4) For the cases in which more qubits $B^{(1)}, B^{(2)}, \dots, B^{(l)}$ ($l = 3, 4, \dots, 30$) collapsed into the state $|\psi_7^-\rangle_B$ after Alice's measurements, the probability of the 30 qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to $w_{(l)}$ ($w_{(l)} > w_{(2)}$, $l = 3, 4, \dots, 30$) after Bob's measurements.

As described above, after measurements of Alice, the probability of the 30 qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to W ($W \geq 1.655$) (we call W the discriminated parameter) after Bob's measurements, where $W \in \{w_{(j)} : j = 1, 2, \dots, 30\}$.

(s5) To ensure the outcome of Bob's measurements more reliable, it can be further supposed that Alice and Bob share 20 entangled states groups (ESGs), each consisting of 30 eight-qubit GHZ states $|\Phi^{(k)}\rangle$ (see Eq. (14)). If Alice's measurements are the CPMs, it is easy found that, after Alice's and Bob's measurements, the probability of all qubits $B^{(k)}$ of each ESG in the state $|0\rangle$ or $|1\rangle$ will be still in the ratio of one to one. If Alice's measurements are the SPMs, by statistics theory, after Alice's and Bob's measurements, in all ESGs the probability of the qubits $B^{(k)}$ of each ESG in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to W ($W \geq 1.655$).

As mentioned above, one can see that, in this protocol, at the appointed time t , Bob should measure his qubits $B^{(k)}$ all in the basis $\{|0\rangle, |1\rangle\}$. If Alice performs the CPMs on her qubits, after Bob's measurements, the probability of all qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to one. If Alice's measurements are the SPMs, after Bob's measurements, the probability of the qubits $B^{(k)}$ of each ESG in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to W ($W \geq 1.655$).

According to these results, Bob can distinguish that the measurements used by Alice are CPMs or SPMs. Thus, the LQMD is realized successfully without help of classical information. This means that our LQMD protocol may be not restricted by the no-signaling constraint.

5. Discussion and conclusion

Before conclusion, we make some discussion. (i) It should be noted that, in the present LQMD protocol, Bob did not obtain Alice's quantum information, *i.e.*, if Alice's measurements are SPMs, Bob couldn't have learned the coefficients x and y in the measuring basis performed by Alice since he is not informed that Alice got result of measurement. In fact, Bob doesn't need to know Alice's quantum information (*e.g.* the coefficients x and y). As mentioned above, after his measurements, Bob can determine that the measurements performed by Alice are CPMs or SPMs only according to the probability of his qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$. That is to say, in our LQMD protocol, the entanglement can be used for transmission of information (*e.g.* the classical messages 0 and 1 can be represented by CPMs and SPMs respectively) without assistance of classical communication. (ii) It must be pointed that, in our protocol, it is essential that eight-particle GHZ states are applied. It is easy found that if l -particle GHZ states ($l < 8$) are employed, the LQMD will not be completed. For example, if 30 seven- or six-particle GHZ states are used, from (s2) in section 4 one can see that, the discriminated parameter W will be 0.83 or 0.41. In this case, the CPMs and SPMs cannot be distinguished. On the other hand, to ensure the discriminated parameter $W \geq 1.655$, one can only use 15 seven-particle or 7 (7.5) six-particle GHZ states. However, in these cases, the exact of measurement results will not be guaranteed. (iii) If only a single eight-qubit GHZ state was employed in our protocol, the LQMD cannot be realized, as described in Sec. 2. It is just because of that numerous eight-qubit GHZ states and the SPMs have been used, our LQMD protocol can be completed successfully. (iv) We should emphasize that our work has been completed in the framework of standard quantum mechanics.

In conclusion, we have proposed a theoretical protocol for local discrimination of two different kinds of measurement by using selective measurement and numerous eight-qubit GHZ states. To realize the protocol, a series of single-qubit correlative measuring basis has been employed. It is shown that, in this protocol, if both two observers agreed in advance that one of them (*e.g.* Alice) should measure her qubits before an appointed time, LQMD can be realized successfully without assistance of classical information. This means that the no-signaling constraint can be violated by the LQMD. Compared with previous LQMD scheme [19], the advantage of the present LQMD protocol is that it does not restricted by the no-signaling. So far there has been experiment implementing the eight-qubit GHZ state [21], hence, we hope our work can be experimentally realized in the near future and stimulate further research on quantum communication and quantum information processing.

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