

Conjecture on the consecutive concatenation of the numbers $nk+1$ where k multiple of 3

Abstract. In this paper I make the following conjecture: for any k multiple of 3, the sequence obtained by the consecutive concatenation of the numbers $n*k + 1$, where n positive integer, has an infinity of prime terms. Examples: for $k = 3$, the sequence 1, 14, 147, 14710 (...) has the prime terms 14710131619, 14710131619222528313437 (...); for $k = 6$, the sequence 1, 7, 13, 19 (...) has the prime terms 17, 17131925313743495561 (...).

Conjecture:

For any k multiple of 3, the sequence obtained by the consecutive concatenation of the numbers $n*k + 1$, where n positive integer, has an infinity of prime terms. Examples: for $k = 3$, the sequence 1, 14, 147, 14710 (...) has the prime terms 14710131619, 14710131619222528313437 (...); for $k = 6$, the sequence 1, 7, 13, 19 (...) has the prime terms 17, 17131925313743495561 (...).

The sequence of primes for $k = 3$:

: 14710131619, 14710131619222528313437 (...)

The sequence of primes for $k = 6$:

: 17, 17131925313743495561, 171319253137434955616773 (...)

The sequence of primes for $k = 12$:

: 11325374961738597109121133145157169181193205217,
1132537496173859710912113314515716918119320521722924
1253 (...)

The sequence of primes for $k = 24$:

: 125497397, 125497397121145169 (...)

The sequence of primes for $k = 30$:

: 131 (...)

The sequence of primes for $k = 33$:

: 13467100133 (...)

The sequence of primes for $k = 36$:

: 13773109145181217253289325361397433469505541577613649
(...)

The sequence of primes for $k = 60$:

: 161121181241301361,
1611211812413013614214815416016617217818419019611021
10811141 (...)

The sequence of primes for $k = 90$:

: 191, 191181271, 191181271361,
1911812713614515416317218119019911081 (...)

The sequence of primes for $k = 120$:

: 1121241361841 (...)

The sequence of primes for $k = 150$:

: 1151, 1151301451 (...)

The sequence of primes for $k = 180$:

: 1181361541721901108112611441162118011981216123412521
2701 (...)

The sequence of primes for $k = 300$:

: 1301, 1301601901120115011801 (...)

The sequence of primes for $k = 900$:

: 1901, 190118012701360145015401 (...)