

## **Four conjectures on the numbers obtained concatenating to the right a prime with the digit 9**

**Abstract.** In this paper I state the following four conjectures: (I) There exist an infinity of primes  $p$  which, concatenated to the right with the digit 9, form also prime numbers; (II) There exist an infinity of primes obtained concatenating the reversal of  $p$  as is defined in Conjecture I to the right with the digit 9; (III) There exist an infinity of semiprimes obtained concatenating primes to the right with the digit 9, semiprimes  $m \cdot n$  having the property that  $n - m + 1$  is prime; (IV) There exist an infinity of semiprimes obtained concatenating the reversal of  $p$  as is defined in Conjecture I to the right with the digit 9, semiprimes  $m \cdot n$  having the property that  $n - m + 1$  is prime.

### **Conjecture I:**

There exist an infinity of primes  $p$  which, concatenated to the right with the digit 9, form also prime numbers  $q$ .

The sequence of primes  $q$ :

: 59, 79, 139, 179, 199, 239, 379, 419, 439, 479, 599,  
619, 719, 739, 839, 1019, 1039, 1279, 1319, 1399,  
1499, 1579, 1979, 1999, 2239, 2339, 2399, 2579,  
2699, 2719, 2819, 2939, 3079, 3119, 3319, 3499,  
3539, 3739, 4019, 4099, 4219 (...)

### **Conjecture II:**

There exist an infinity of primes  $r$  obtained concatenating the reversal of  $p$  as is defined in Conjecture I to the right with the digit 9.

The sequence of primes  $q$ :

: 719, 919, 739, 149, 349, 179, 379, 389, 1019, 3019,  
7219, 1319, 9319, 9419, 7919, 3229, 3329, 7529,  
9629, 3929, 7039, 9439, 3539, 3739, 1049, 9049, 1249  
(...)

### **Conjecture III:**

There exist an infinity of semiprimes obtained concatenating primes to the right with the digit 9, semiprimes  $m \cdot n$  having the property that  $n - m + 1$  is prime.

The sequence of semiprimes  $m*n$ :

: 119 (=  $7*17$  and  $17 - 7 + 1 = 11$ , prime), 299 (=  $13*23$  and  $23 - 13 + 1 = 11$ , prime), 319 (=  $11*29$  and  $29 - 11 + 1 = 19$ , prime), 799 (=  $17*47$  and  $47 - 17 + 1 = 31$ , prime), 899 (=  $29*31$  and  $31 - 29 + 1 = 3$ , prime), 979 (=  $11*89$  and  $89 - 11 + 1 = 79$ , prime), 1079 (=  $13*83$  and  $83 - 13 + 1 = 73$ , prime), 1099 (=  $7*157$  and  $157 - 7 + 1 = 151$ , prime), 1379 (=  $7*197$  and  $197 - 7 + 1 = 191$ , prime), 1639 (=  $11*149$  and  $149 - 11 + 1 = 139$ , prime), 1739 (=  $37*47$  and  $47 - 37 + 1 = 11$ , prime), 1799 (=  $7*257$  and  $257 - 7 + 1 = 251$ , prime), 1919 (=  $19*101$  and  $101 - 19 + 1 = 83$ , prime), 1939 (=  $7*277$  and  $277 - 7 + 1 = 271$ , prime), 2119 (=  $13*163$  and  $163 - 13 + 1 = 151$ , prime), 2279 (=  $43*53$  and  $53 - 43 + 1 = 11$ , prime), 2419 (=  $41*59$  and  $59 - 41 + 1 = 19$ , prime), 2839 (=  $17*167$  and  $167 - 17 + 1 = 151$ , prime), 3139 (=  $43*73$  and  $73 - 43 + 1 = 31$ , prime), 3379 (=  $31*109$  and  $109 - 31 + 1 = 79$ , prime), 3599 (=  $59*61$  and  $61 - 59 + 1 = 3$ , prime), 3679 (=  $13*283$  and  $283 - 13 + 1 = 271$ , prime), 3799 (=  $29*131$  and  $131 - 29 + 1 = 103$ , prime), 3979 (=  $23*173$  and  $173 - 23 + 1 = 151$ , prime)...

#### **Conjecture IV:**

There exist an infinity of semiprimes  $m*n$  obtained concatenating the reversal of  $p$  as is defined in Conjecture I to the right with the digit 9, semiprimes having the property that  $n - m + 1$  is prime.

The sequence of semiprimes  $m*n$ :

: 319 (=  $11*29$  and  $29 - 11 + 1 = 19$ , prime), 329 (=  $7*47$  and  $47 - 7 + 1 = 41$ , prime), 749 (=  $7*107$  and  $107 - 7 + 1 = 101$ , prime), 959 (=  $7*137$  and  $137 - 7 + 1 = 131$ , prime), 7519 (=  $73*103$  and  $103 - 73 + 1 = 31$ , prime), 1829 (=  $31*59$  and  $59 - 31 + 1 = 29$ , prime)...