

**Conjecture on the period of the rational number  $P/d + d/P$  where  $P$  is a 2-Poulet number and  $d$  its least prime factor**

**Abstract.** In this paper I state the following conjecture: let  $P$  be a 2-Poulet number,  $d$  its least prime factor and  $q$  the other one; then the length of the period of the rational number  $P/d + d/P$  is equal to  $(q - 1)/n$ , where  $n$  positive integer.

**Conjecture:**

Let  $P$  be a 2-Poulet number,  $d$  its least prime factor and  $q$  the other one; then the length of the period of the rational number  $P/d + d/P$  is equal to  $(q - 1)/n$ , where  $n$  positive integer.

**Note:**

The sequence of 2-Poulet numbers: 341, 1387, 2047, 2701, 3277, 4033, 4369, 4681, 5461, 7957, 8321, 10261, 13747, 14491, 15709, 18721, 19951, 23377, 31417, 31609, 31621, 35333, 42799, 49141, 49981, 60701, 60787, 65077, 65281, 80581, 83333, 85489, 88357, 90751, 104653, 123251, 129889, 130561 (...). See the sequence A214305 that I submitted on OEIS.

**Verifying the conjecture:**

(true for the first  $n$  2-Poulet numbers)

- : for  $P = 341 = 11 \cdot 31$ , the period of  $P/d + d/P$  is equal to 322580645161290, which has the length  $15 = (31 - 1)/2$ ;
- : for  $P = 1387 = 19 \cdot 73$ , the period of  $P/d + d/P$  is equal to 13698630, which has the length  $8 = (73 - 1)/9$ ;
- : for  $P = 2047 = 23 \cdot 89$ , the period of  $P/d + d/P$  has the length  $44 = (89 - 1)/2$ ;
- : for  $P = 2701 = 37 \cdot 73$ , the period of  $P/d + d/P$  has the length  $8 = (73 - 1)/9$ ;
- : for  $P = 3277 = 29 \cdot 113$ , the period of  $P/d + d/P$  has the length  $112 = 113 - 1$ ;
- : for  $P = 4033 = 37 \cdot 109$ , the period of  $P/d + d/P$  has the length  $108 = 109 - 1$ ;
- : for  $P = 4369 = 17 \cdot 257$ , the period of  $P/d + d/P$  has the length  $256 = 257 - 1$ ;
- : for  $P = 4681 = 31 \cdot 151$ , the period of  $P/d + d/P$  has the length  $75 = (151 - 1)/2$ ;
- : for  $P = 5461 = 43 \cdot 127$ , the period of  $P/d + d/P$  has the length  $42 = 43 - 1$ ;

: for  $P = 7957 = 73 \cdot 109$ , the period of  $P/d + d/P$  has the  
length  $108 = 109 - 1$ ;  
: for  $P = 8321 = 53 \cdot 157$ , the period of  $P/d + d/P$  has the  
length  $78 = (157 - 1)/2$ ;  
: for  $P = 10261 = 31 \cdot 331$ , the period of  $P/d + d/P$  has the  
length  $110 = (331 - 1)/3$ ;  
: for  $P = 13747 = 59 \cdot 233$ , the period of  $P/d + d/P$  has the  
length  $232 = 233 - 1$ ;  
: for  $P = 14491 = 43 \cdot 337$ , the period of  $P/d + d/P$  has the  
length  $336 = 337 - 1$ ;  
: for  $P = 15709 = 23 \cdot 683$ , the period of  $P/d + d/P$  has the  
length  $341 = (683 - 1)/2$ ;  
: for  $P = 18721 = 97 \cdot 193$ , the period of  $P/d + d/P$  has the  
length  $192 = 193 - 1$ ;  
: for  $P = 19951 = 71 \cdot 281$ , the period of  $P/d + d/P$  has the  
length  $28 = (281 - 1)/10$ ;  
: for  $P = 23377 = 97 \cdot 241$ , the period of  $P/d + d/P$  has the  
length  $30 = (241 - 1)/8$ ;  
: for  $P = 31417 = 89 \cdot 353$ , the period of  $P/d + d/P$  has the  
length  $32 = (353 - 1)/11$ ;  
: for  $P = 31609 = 73 \cdot 433$ , the period of  $P/d + d/P$  has the  
length  $432 = 433 - 1$ ;  
: for  $P = 31621 = 103 \cdot 307$ , the period of  $P/d + d/P$  has the  
length  $153 = (307 - 1)/2$ ;  
: for  $P = 35333 = 89 \cdot 397$ , the period of  $P/d + d/P$  has the  
length  $99 = (397 - 1)/4$ ;  
: for  $P = 42799 = 127 \cdot 337$ , the period of  $P/d + d/P$  has the  
length  $336 = 337 - 1$ ;  
: for  $P = 49141 = 157 \cdot 313$ , the period of  $P/d + d/P$  has the  
length  $312 = 313 - 1$ ;  
: for  $P = 49981 = 151 \cdot 331$ , the period of  $P/d + d/P$  has the  
length  $110 = (331 - 1)/3$ ;  
: for  $P = 60701 = 101 \cdot 601$ , the period of  $P/d + d/P$  has the  
length  $300 = (601 - 1)/2$ ;  
: for  $P = 60787 = 89 \cdot 683$ , the period of  $P/d + d/P$  has the  
length  $341 = (683 - 1)/2$ ;  
: for  $P = 65077 = 59 \cdot 1103$ , the period of  $P/d + d/P$  has the  
length  $1102 = 1103 - 1$ ;  
: for  $P = 65281 = 97 \cdot 673$ , the period of  $P/d + d/P$  has the  
length  $224 = (673 - 1)/3$ ;  
: for  $P = 80581 = 61 \cdot 1321$ , the period of  $P/d + d/P$  has the  
length  $55 = (1321 - 1)/24$ ;  
: for  $P = 83333 = 167 \cdot 499$ , the period of  $P/d + d/P$  has the  
length  $498 = 499 - 1$ ;  
: for  $P = 85489 = 53 \cdot 1613$ , the period of  $P/d + d/P$  has the  
length  $403 = (1613 - 1)/4$ ;  
: for  $P = 88357 = 149 \cdot 593$ , the period of  $P/d + d/P$  has the  
length  $592 = 593 - 1$ ;  
: for  $P = 90751 = 151 \cdot 601$ , the period of  $P/d + d/P$  has the  
length  $300 = (601 - 1)/2$ .