

On the sum of three consecutive values of the MC function

Abstract. In a previous paper I defined the $MC(x)$ function in the following way: Let $MC(x)$ be the function defined on the set of odd positive integers with values in the set of primes such that: $MC(x) = 1$ for $x = 1$; $MC(x) = x$, for x prime; for x composite, $MC(x)$ has the value of the prime which results from the following iterative operation: let $x = p(1)*p(2)*...*p(n)$, where $p(1),..., p(n)$ are its prime factors; let $y = p(1) + p(2) +...+ p(n) - (n - 1)$; if y is a prime, then $MC(x) = y$; if not, then $y = q(1)*q(2)*...*q(m)$, where $q(1),..., q(m)$ are its prime factors; let $z = q(1) + q(2) +...+ q(m) - (m - 1)$; if z is a prime, then $MC(x) = z$; if not, it is iterated the operation until a prime is obtained and this is the value of $MC(x)$. In this paper I present a property of this function.

The sequence of the first 100 values of $MC(x)$, for $1 \leq x \leq 199$:

1, 3, 5, 7, 5, 11, 13, 7, 17, 19, 5, 23, 5, 7, 29, 31, 13, 11, 37, 7, 41, 43, 5, 47, 13, 19, 53, 7, 5, 59, 61, 11, 17, 67, 5, 71, 73, 11, 17, 79, 5, 83, 5, 31, 89, 19, 13, 23, 97, 7, 101, 103, 13, 107, 109, 7, 113, 7, 7, 23, 5, 43, 13, 127, 5, 131, 5, 11, 137, 139, 13, 23, 13, 7, 149, 151, 5, 11, 157, 7, 29, 163, 17, 167, 5, 23, 173, 7, 61, 179, 181, 11, 41, 7, 13, 191, 193, 19, 197, 199.

As I mentioned in abstract, in my previous paper “An interesting property of the primes congruent to 1 mod 45 and an idea for a function” I defined the MC function, without having already found applications for it in diophantine analysis but sensing that for sure such applications do exist.

Calculating the value of MC function for several sets of relatively large, consecutive, odd numbers, I found out that the value of MC function is obtained in fewer steps (in other words, a prime is obtained easier through the iterative operation that defines the function) for the numbers which are equal to the sum of the values of MC function for three consecutive numbers (odd, of course, the function is defined only on odd numbers). To exemplify, $MC(x)$, where $x = MC(193) + MC(195) + MC(197)$ is found immediately (in one step), because $MC(x) = x = 409$, a prime number. In other words, $MC(MC(n) + MC(n + 1) + MC(n + 2))$ appear to be obtained easier than the average $MC(m)$, where m are the numbers comparable as length (number of digits) to $MC(n) + MC(n + 1) + MC(n + 2)$.

Examples:

Let's consider the consecutive odd numbers 181811, 181813, 181815, 181817, 181819 with the following corresponding values for MC: 23, 181813, 11, 1721, 7.

Let's calculate $MC(23 + 181813 + 11) = MC(181847)$

: $181847 = 43*4229$;

: $43 + 4229 - 1 = 4271$, prime, so is the value of $MC(x)$, obtained in two steps.

Let's calculate $MC(181813 + 11 + 1721) = MC(183545)$

: $183545 = 5*36709$;

: $5 + 36709 - 1 = 36713$, prime, so is the value of $MC(x)$, obtained in two steps.

Let's calculate $MC(11 + 1721 + 7) = MC(1739)$

: $1739 = 37*47$;

: $37 + 47 - 1 = 83$, prime, so is the value of $MC(x)$, obtained in two steps.

Let's consider the consecutive odd numbers 982451651, 982451653, 982451655, 982451657, 982451657 with the following corresponding values for MC: 59, 982451653, 14251, 7873, 787.

Let's calculate $MC(59 + 982451653 + 14251) = MC(982465963)$
: 982465963 is prime, so is the value of $MC(x)$, obtained in one step.

Let's calculate $MC(982451653 + 14251 + 7873) = MC(982473777)$
: $982473777 = 3*3*109163753$;
: $3 + 3 + 109163753 - 2 = 109163757 = 3*1223*29753$;
: $3 + 1223 + 29753 - 2 = 30977$, prime, so is the value of $MC(x)$, obtained in three steps.

Let's calculate $MC(14251 + 7873 + 787) = MC(22911)$
: $22911 = 3*7*1091$;
: $3 + 7 + 1091 - 2 = 1099 = 7*157$;
: $7 + 157 - 1 = 163$, prime, so is the value of $MC(x)$, obtained in three steps.