

# Conjectured Compositeness Tests for Specific Classes of $b^n - b + 1$ and $b^n + b - 1$

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**Abstract:** Compositeness criteria for specific classes of numbers of the form  $b^n - b + 1$  and  $b^n + b - 1$  are introduced .

**Keywords:** Compositeness test , Polynomial time , Prime numbers .

**AMS Classification:** 11A51 .

## 1 Introduction

In 2008 Ray Melham provided unconditional , probabilistic , lucasian type primality test for generalized Mersenne numbers [1] . In this note I present polynomial time compositeness tests for specific classes of numbers of the form  $b^n - b + 1$  and  $b^n + b - 1$  .

## 2 The Main Result

**Definition 2.1.** Let  $P_m(x) = 2^{-m} \cdot \left( (x - \sqrt{x^2 - 4})^m + (x + \sqrt{x^2 - 4})^m \right)$  , where  $m$  and  $x$  are nonnegative integers .

**Conjecture 2.1.** Let  $N = b^n - b + 1$  such that  $n > 3$  ,  $b \equiv 0, 2 \pmod{8}$  .

*Let  $S_i = P_b(S_{i-1})$  with  $S_0 = P_{b/2}(6)$  , thus  
If  $N$  is prime then  $S_{n-1} \equiv P_{b/2}(6) \pmod{N}$*

**Conjecture 2.2.** Let  $N = b^n - b + 1$  such that  $n > 3$  ,  $b \equiv 4, 6 \pmod{8}$  .

*Let  $S_i = P_b(S_{i-1})$  with  $S_0 = P_{b/2}(6)$  , thus  
If  $N$  is prime then  $S_{n-1} \equiv -P_{(b-2)/2}(6) \pmod{N}$*

**Conjecture 2.3.** Let  $N = b^n + b - 1$  such that  $n > 3$  ,  $b \equiv 0, 2 \pmod{8}$  .

*Let  $S_i = P_b(S_{i-1})$  with  $S_0 = P_{b/2}(6)$  , thus  
If  $N$  is prime then  $S_{n-1} \equiv P_{(b-2)/2}(6) \pmod{N}$*

**Conjecture 2.4.** *Let  $N = b^n + b - 1$  such that  $n > 3$ ,  $b \equiv 4, 6 \pmod{8}$ .*

*Let  $S_i = P_b(S_{i-1})$  with  $S_0 = P_{b/2}(6)$ , thus  
If  $N$  is prime then  $S_{n-1} \equiv -P_{b/2}(6) \pmod{N}$*

## References

- [1] R. S. Melham , "Probable prime tests for generalized Mersenne numbers," , *Bol. Soc. Mat. Mexicana* , 14 (2008) , 7-14 .