

Two conjectures about the pairs of primes separated by a certain distance

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Abstract. In this paper I make two conjectures about the pairs of primes $[p_1, q_1]$, where the difference between p_1 and q_1 is a certain even number d . I state that any such pair has at least one other corresponding, in a specified manner, pair of primes $[p_2, q_2]$, such that the difference between p_2 and q_2 is also equal to d .

Conjecture 1:

For any pair of primes, greater than 3, $[p_1, q_1]$, where $q_1 - p_1 = d$, there exist at least a pair of positive integers $[m, n]$, where $n - m = d$, such that the numbers $p_2 = p_1 * q_1 - n + 1$ and $q_2 = p_1 * q_1 - m + 1$ are both primes.

Examples:

- : For $[p_1, q_1] = [5, 7]$ there exist the pair $[m, n] = [5, 7]$ such that $p_2 = 5*7 - 7 + 1 = 29$ and $q_2 = 5*7 - 5 + 1 = 31$ are both primes;
- : For $[p_1, q_1] = [5, 11]$ there exist the pair $[m, n] = [3, 9]$ such that $p_2 = 5*11 - 9 + 1 = 47$ and $q_2 = 5*11 - 3 + 1 = 53$ are both primes;
- : For $[p_1, q_1] = [5, 13]$ there exist the pair $[m, n] = [5, 13]$ such that $p_2 = 5*13 - 13 + 1 = 53$ and $q_2 = 5*13 - 5 + 1 = 61$ are both primes;
- : For $[p_1, q_1] = [7, 11]$ there exist the pair $[m, n] = [7, 11]$ such that $p_2 = 7*11 - 11 + 1 = 67$ and $q_2 = 7*11 - 7 + 1 = 71$ are both primes;
- : For $[p_1, q_1] = [7, 13]$ there exist the pair $[m, n] = [7, 11]$ such that $p_2 = 7*11 - 11 + 1 = 67$ and $q_2 = 7*11 - 7 + 1 = 71$ are both primes;
- : For $[p_1, q_1] = [11, 13]$ there exist the pair $[m, n] = [5, 7]$ such that $p_2 = 11*13 - 5 + 1 = 137$ and $q_2 = 11*13 - 7 + 1 = 139$ are both primes.

Conjecture 2:

For any even number d there exist an infinity of pairs of primes $[p_1, q_1]$, where $q_1 - p_1 = d$, such that the numbers $p_2 = p_1 * q_1 - p_1 + 1$ and $q_2 = p_1 * q_1 - q_1 + 1$ are both primes.

Note: See, for instance, from the examples to the Conjecture 1 from above, the pair $[5, 7]$ for $d = 2$, the pair $[7, 11]$ for $d = 4$, the pair $[5, 13]$ for $d = 8$.