

A NEW PERSPECTIVE OF THE TWIN PRIME CONJECTURE

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*“Innovation is not the product of logical thought, even
though the final product is tied to a logical structure.”*

----- Albert Einstein

The *twin prime conjecture* [1] is a beautiful open problem in *Number Theory* about primes, a pair of primes are called *twin primes* such as $\{11,13\}$, $\{29,31\}$ or $\{101,103\}$ of the form $\{p, p+2\}$, and the *twin prime conjecture states* that there exist infinitely many primes p such that $p+2$ is also prime [1].

Since p and $p+2$ all is odd primes in every pair of *twin primes* of the form $\{p, p+2\}$, thus, there must be $2|p+1$ and $p+1 \geq 4$, assume $p+1=2n$, $n \in \mathbb{N}$; then there be $2n \geq 4$, $n \geq 2$, $p=2n-1$, $p+2=2n+1$, and $(2n+1)=(2n-1)+2$, therefore, a pair of *twin primes* of the form $\{p, p+2\}$ is also a pair of primes of the form $\{2n-1, 2n+1\}$. At the same time, the *twin prime conjecture states* is equivalently converted to that there exist infinitely many evens $2n$ such that $2n \pm 1$ all be odd primes.

Essentially, either way of expression, both are expressing the same proposition that *there are infinitely many twin primes*.

References

- [1] M. B. Nathanson, *Elementary Methods in Number Theory*, Beijing, Springer-Verlag, 2003.
Section II, Divisors and Primes in Multiplicative Number Theory, 8--Prime Numbers, 8.4,
notes.3, 287