

**Two Measured Fermion Masses
Determine All Fermion Masses and Charges
(revised , simplified & updated)**

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Yes, I will show, herein, that all the fermion masses may be determined from merely two well chosen constants, and all the fermion charges thereafter.

My book, "Reality is a Mathematical Model" (reference [1]), lays out the foundations of the algebraic construction of the vector-geometry of space-time and how the smooth functions represent the fundamental objects therein.

From there, my book, "A Mathematical Preon Foundation for the Standard Model" (reference [2]), gives an introductory look at how fundamental object mass originates from charge; an architecture of these fundamental objects; and the interactions of these fundamental objects.

Here, the picture of the mass of the fundamental objects is extended.

the field equations of the electromagnetic-nuclear field, which can be expressed in the form:

$$\begin{aligned} \overset{m}{\nabla}_3 \times \mathbf{E} + D_0 \mathbf{B} &= \mathbf{0} & \text{and} & & \overset{m}{\nabla}_3 \cdot \mathbf{B} &= \mathbf{0} \\ \overset{m}{\nabla}_{3\uparrow} \times \mathbf{B} - D_0 \mathbf{E} &= \mathbf{J}_3 & \text{and} & & \overset{m}{\nabla}_{3\uparrow} \cdot \mathbf{E} &= \rho \equiv J^0 ; \end{aligned}$$

$$\text{where: } \overset{m}{\nabla}_3 \equiv \mathbf{w}^{4:1} D_1 + \mathbf{w}^{4:2} D_2 + \mathbf{w}^{4:3} D_3$$

$$\overset{m}{\nabla}_{3\uparrow} \equiv \mathbf{w}^{4:1} D_1^\uparrow + \mathbf{w}^{4:2} D_2^\uparrow + \mathbf{w}^{4:3} D_3^\uparrow$$

$$D_i^+ \equiv (\partial_i + m_i) \quad , \quad D_i^- \equiv (\partial_i - m_i)$$

$$D_i \equiv \begin{pmatrix} D_i^+ & 0 \\ 0 & D_i^- \end{pmatrix} \quad , \quad D_i^\uparrow \equiv \begin{pmatrix} D_i^- & 0 \\ 0 & D_i^+ \end{pmatrix}$$

$$\mathbf{E} = \mathbf{w}^{4:1} (-D_0^\uparrow f^1 - D_1 f^0) + \mathbf{w}^{4:2} (-D_0^\uparrow f^2 - D_2 f^0) + \mathbf{w}^{4:3} (-D_0^\uparrow f^3 - D_3 f^0)$$

$$\mathbf{B} = \mathbf{w}^{4:1} (D_2 f^3 - D_3 f^2) + \mathbf{w}^{4:2} (-D_1 f^3 + D_3 f^1) + \mathbf{w}^{4:3} (D_1 f^2 - D_2 f^1)$$

$$f^i \equiv \begin{pmatrix} f_+^i \\ f_-^i \end{pmatrix}$$

that is, the mass-generalized Maxwell's or Maxwell-Cassano equations, are a representation of the equations also obtained from the Helmholtzian matrix product form noted at the beginning of my video, [3]:

Now, from [2], the fermion architecture is as follows:

$e^- = e(1) = \overline{(E^1, E^2, E^3)}_1$	$\mu^- = e(2) = \overline{(E^1, E^2, E^3)}_2$	$\tau^- = e(3) = \overline{(E^1, E^2, E^3)}_3$
$\nu_e = \nu(1) = (B^1, B^2, B^3)_1$	$\nu_\mu = \nu(2) = (B^1, B^2, B^3)_2$	$\nu_\tau = \nu(3) = (B^1, B^2, B^3)_3$
$u_R = u_1(1) = (B^1, E^2, E^3)_1$	$c_R = u_1(2) = (B^1, E^2, E^3)_2$	$t_R = u_1(3) = (B^1, E^2, E^3)_3$
$u_G = u_2(1) = (E^1, B^2, E^3)_1$	$c_G = u_2(2) = (E^1, B^2, E^3)_2$	$t_G = u_2(3) = (E^1, B^2, E^3)_3$
$u_B = u_3(1) = (E^1, E^2, B^3)_1$	$c_B = u_3(2) = (E^1, E^2, B^3)_2$	$t_B = u_3(3) = (E^1, E^2, B^3)_3$
$d_R = d_1(1) = \overline{(E^1, B^2, B^3)}_1$	$s_R = d_1(2) = \overline{(E^1, B^2, B^3)}_2$	$b_R = d_1(3) = \overline{(E^1, B^2, B^3)}_3$
$d_G = d_2(1) = \overline{(B^1, E^2, B^3)}_1$	$s_G = d_2(2) = \overline{(B^1, E^2, B^3)}_2$	$b_G = d_2(3) = \overline{(B^1, E^2, B^3)}_3$
$d_B = d_3(1) = \overline{(B^1, B^2, E^3)}_1$	$s_B = d_3(2) = \overline{(B^1, B^2, E^3)}_2$	$b_B = d_3(3) = \overline{(B^1, B^2, E^3)}_3$

If the fermion masses may be described by the mass-generalized Maxwell's equations, then denote them as follows:

$m(3,1) = m_e : e^- = e(1)$	$m(3,2) = m_\mu : \mu^- = e(2)$	$m(3,3) = m_\tau : \tau^- = e(3)$
$m(0,1) = m_{\nu_e} : \nu_e = \nu(1)$	$m(0,2) = m_{\nu_\mu} : \nu_\mu = \nu(2)$	$m(0,3) = m_{\nu_\tau} : \nu_\tau = \nu(3)$
$m(2,1) = m_u : u_X = u_X(1)$	$m(2,2) = m_c : c_X = u_X(2)$	$m(2,3) = m_t : t_X = u_X(3)$
$m(1,1) = m_d : d_X = d_X(1)$	$m(1,2) = m_s : s_X = d_X(2)$	$m(1,3) = m_b : b_X = d_X(3)$

Where for an object's mass: $m(h, i)$:

h indicates the number of E^l 's In the object's S_R architecture.

i indicates the generation of the object's S_R architecture.

After much analysis, the following relationships arise.

Define:

$$w(h) \equiv (h^2 + 1)^{h \cdot T_0} \left(T_0(h) + \delta_{-1}^{(-1)^h} \right)$$

$$v(h, i) \equiv \frac{1}{h^2 i^{i+1} + (-1)^h h i + 2i - 1}$$

$$f(h) \equiv w(h) \left[\left(1 - \delta_h^{T_0(h)} \right) (T_0(h+1))^{2h} + (h!)^{h-1} \left(\sqrt{2^{h-1}} \right)^h \right]$$

$$g(h, i) \equiv [w(3-h)]^{T_0(i)} \left[(v(h, i))^{T_0(h)T_0(i-1)} \left(\left[2h + (-1)^h 2^{\frac{1}{2}} [1+(-1)^h] \right] k \right)^{i-1} \right]^{(i-1)T_0(h)}$$

$$T_0(j) = \frac{1}{2} [j - 1 + \delta_{(-1)^j}^1]$$

$$(h, i \in \mathbb{N} ; 0 \leq h \leq 3, 1 \leq i \leq 3)$$

From which the masses may be written:

$$\frac{m(h, 1)}{m \left(\left[h + \delta_{-1}^{(-1)T_0(h+1)} \right] \delta_{-1}^{(-1)T_0(h+1)}, 1 \right)} = f(h)$$

$$\frac{m(h, i)}{m \left(h + (-1)^{h+1} \delta_{-1}^{(-1)T_0(h+1)} (1 - \delta_1^i), 1 \right)} = g(h, i)$$

which may be written out explicitly as:

$\frac{m(0,1)}{m(0,1)} = f(0)$	$\frac{m(0,i)}{m(0,1)} = g(0,i)$
$\frac{m(1,1)}{m(2,1)} = f(1)$	$\frac{m(1,i)}{m(2,1)} = g(1,i) , (i \neq 1)$
$\frac{m(2,1)}{m(3,1)} = f(2)$	$\frac{m(2,i)}{m(1,1)} = g(2,i) , (i \neq 1)$
$\frac{m(3,1)}{m(0,1)} = f(3)$	$\frac{m(3,i)}{m(3,1)} = g(3,i)$

or:

$m(0,1) = m(0,1)f(0)$	$m(0,i) = m(0,1)g(0,i)$
$m(1,1) = m(2,1)f(1)$	$m(1,i) = m(2,1)g(1,i) , (i \neq 1)$
$m(2,1) = m(3,1)f(2)$	$m(2,i) = m(1,1)g(2,i) , (i \neq 1)$
$m(3,1) = m(0,1)f(3)$	$m(3,i) = m(3,1)g(3,i)$

So, the $f(h)$ are: :

$$\begin{aligned} f(0) &\equiv (0^2 + 1)^{0 \cdot T_0 \binom{T_0(0) + \delta_{-1}^{(-1)^0}}{}} \left[(1 - \delta_0^{T_0(0)}) (T_0(0+1))^{2 \cdot 0} + (0!)^{0-1} (\sqrt{2^{0-1}})^0 \right] \\ &= 1^0 \left[0 [T_0(1)]^0 + (1)^{-1} (\sqrt{2^{-1}})^0 \right] = 1 \left[0 \cdot 0^0 + (1)^{-1} (\sqrt{2^{-1}})^0 \right] \\ &= 1 \left[0 + 1 \left(\sqrt{\frac{1}{2}} \right)^0 \right] = 1 [0 + 1] = 1 \end{aligned}$$

$$\begin{aligned} f(1) &= (1^2 + 1)^{1 \cdot T_0 \binom{T_0(1) + \delta_{-1}^{(-1)^1}}{}} \left[(1 - \delta_1^{T_0(1)}) (T_0(1+1))^{2 \cdot 1} + (1!)^{1-1} (\sqrt{2^{1-1}})^1 \right] \\ &= 2^0 \left[1 \cdot [T_0(2)]^2 + (1)^0 (\sqrt{2^0})^1 \right] = 1 \left[[1]^2 + (1)^0 (\sqrt{2^2})^0 \right] \\ &= 1 [1 + 1(2)^0] = 1 [1 + 1] = 2 \end{aligned}$$

$$\begin{aligned} f(2) &= (2^2 + 1)^{2 \cdot T_0 \binom{T_0(2) + \delta_{-1}^{(-1)^2}}{}} \left[(1 - \delta_1^{T_0(1)}) (T_0(2+1))^{2 \cdot 2} + (2!)^{2-1} (\sqrt{2^{2-1}})^2 \right] \\ &= 2^0 \left[1 \cdot [T_0(3)]^4 + (2)^1 (\sqrt{2^1})^2 \right] = 1 \left[[1]^4 + (2)^1 (\sqrt{2^1})^2 \right] \\ &= 1 [1 + 2(2)^1] = 1 [1 + 4] = 5 \end{aligned}$$

$$\begin{aligned} f(3) &= (3^2 + 1)^{3 \cdot T_0 \binom{T_0(3) + \delta_{-1}^{(-1)^3}}{}} \left[(T_0(3+1))^{2 \cdot 3} + (3!)^{3-1} (\sqrt{2^{3-1}})^3 \right] \\ &= 10^3 \left[[T_0(4)]^6 + (6)^2 (\sqrt{2^2})^3 \right] = 1000 \left[[2]^6 + (6)^2 (\sqrt{2^2})^3 \right] \\ &= 1000 [64 + 36(2)^3] = 1000 [64 + 288] = 352000 \end{aligned}$$

Continuing, the following table may be built:

$f(0) = 1$	$m_{\nu_e} = m(0, 1) = m(0, 1)f(0) = m(0, 1)$
$f(1) = 2$	$m_d = m(1, 1) = m(2, 1)f(1) = 2m(2, 1)$
$f(2) = 5$	$m_u = m(2, 1) = m(3, 1)f(2) = 5m(3, 1)$
$f(3) = 352000$	$m_e = m(3, 1) = m(0, 1)f(3) = 352000m(0, 1)$

$$\text{Note: } w(h) = \begin{cases} 1 & , h = 0, 1, 2 \\ 1000 & , h = 3 \end{cases}$$

$$[w(3-h)]^{T_0(i)} = \begin{cases} 1 & , h \neq 0 \\ 1 & , h = 0, i = 1 \\ 1000 & , h = 0, i = 2, 3 \end{cases}$$

The fermion measured to the greatest accuracy is the electron. So, instead of assigning a mass to the electron neutrino, the mass of the electron will be taken as the basis, and the mass of the electron neutrino determined from that and the above equation.

And, so, assigning:

$$\begin{aligned} m(3, 1) &= m_e = .510998928 \text{MeV}/c^2 \\ \Rightarrow m(3, 1) &= m\left(\left[0 + \delta_{-1}^{(-1)T_0(0+1)}\right] \delta_{-1}^{(-1)T_0(0+1)}, 1\right) \cdot 352000 \\ &= m\left(\delta_{-1}^{(-1)T_0(1)} \cdot \delta_{-1}^{(-1)T_0(1)}, 1\right) \cdot 352000 \\ &= m\left(\delta_{-1}^{(-1)0} \cdot \delta_{-1}^{(-1)0}, 1\right) \left[[2]^6 + (6)^2 (\sqrt{2^2})^3 \right] \cdot 352000 \\ &= m(\delta_{-1}^1 \cdot \delta_{-1}^1, 1) \cdot 352000 = m(0 \cdot 0, 1) \cdot 352000 = m(0, 1) \cdot 352000 \\ \Rightarrow m_{\nu_e} &= m(0, 1) = \frac{m(3, 1)}{352000} = \frac{.510998928}{352000} = .0000014517015 \text{MeV}/c^2 = m_{\nu_e} \end{aligned}$$

And, so, following the chain:

$$\begin{aligned} m_u &= m(2, 1) = m(3, 1)f(2) = 5m(3, 1) = 2.55499464 \\ m_d &= m(1, 1) = m(2, 1)f(1) = 2m(2, 1) = 5.10998928 \end{aligned}$$

Continuing, the first generation fermion masses may be calculated into the following table.

$m_e = m(3, 1) \approx .510998928 \text{MeV}/c^2$
$m_{\nu_e} = m(0, 1) \approx .0000014517015 \text{MeV}/c^2$
$m_u = m(2, 1) \approx 2.55499464 \text{MeV}/c^2$
$m_d = m(1, 1) \approx 5.10998928 \text{MeV}/c^2$

The $g(h, i)$ simplify to:

$$g(h, 1) = [w(3 - 1)]^{T_0(1)} \left[(v(h, 1))^{T_0(h)T_0(1-1)} \left([2h + (-1)^h 2^{\frac{1}{2}[1+(-1)^h]}] k \right)^{1-1} \right]^{(1-1)T_0(h)}$$

$$= 1$$

and:

$$g(h, 2) = [w(3 - h)]^{T_0(2)} \left[(v(h, 2))^{T_0(h)T_0(2-1)} \left([2h + (-1)^h 2^{\frac{1}{2}[1+(-1)^h]}] k \right)^{2-1} \right]^{(2-1)T_0(h)}$$

$$= [w(3 - h)] \left[(v(h, 2))^0 \left([2h + (-1)^h 2^{\frac{1}{2}[1+(-1)^h]}] k \right)^1 \right]^1$$

$$= [w(3 - h)] \left([2h + (-1)^h 2^{\frac{1}{2}[1+(-1)^h]}] k \right)$$

and:

$$g(h, 3) = [w(3 - h)]^{T_0(3)} \left[\left(\frac{1}{h^2 3^{3+1} + (-1)^h 3h + 2 \cdot 3 - 1} \right)^{T_0(h)T_0(3)} \left([2h + (-1)^h 2^{\frac{1}{2}[1+(-1)^h]}] k \right)^2 \right]^{2T_0(h)}$$

$$= [w(3 - h)] \left[\left(\frac{1}{81h^2 + (-1)^h 3h + 5} \right)^{T_0(h)} \left([2h + (-1)^h 2^{\frac{1}{2}[1+(-1)^h]}] k \right)^2 \right]^{2T_0(h)}$$

Yielding:

$$m(h, 1) = m(h, 1)$$

$$\frac{m(h, 2)}{m\left(h + (-1)^{h+1} \delta_{-1}^{(-1)T_0(h+1)}, 1\right)} = g(h, 2)$$

$$\frac{m(h, 3)}{m\left(h + (-1)^{h+1} \delta_{-1}^{(-1)T_0(h+1)}, 1\right)} = g(h, 3)$$

which may be written out explicitly as:

$m(0, 1) = m(0, 1)$	$\frac{m(0, 2)}{m(0, 1)} = g(0, 2)$	$\frac{m(0, 3)}{m(0, 1)} = g(0, 3)$
$m(1, 1) = m(1, 1)$	$\frac{m(1, 2)}{m(2, 1)} = g(1, 2)$	$\frac{m(1, 3)}{m(2, 1)} = g(1, 3)$
$m(2, 1) = m(2, 1)$	$\frac{m(2, 2)}{m(1, 1)} = g(2, 2)$	$\frac{m(2, 3)}{m(1, 1)} = g(2, 3)$
$m(3, 1) = m(3, 1)$	$\frac{m(3, 2)}{m(3, 1)} = g(3, 2)$	$\frac{m(3, 3)}{m(3, 1)} = g(3, 3)$

Since the first column is a set of identities ($g(h, 1) = 1$), the case: $i = 1$ may be ignored.

The $g(h, i)$ may be calculated into the following table ($g(h, 1) = 1$).

$g(0,2) = [w(3-0)] \left(\left[2 \cdot 0 + (-1)^0 2^{\frac{1}{2}[1+(-1)^0]} \right] k \right) = 1000([0+2^1]k) = 1000 \cdot (2k)$
$g(1,2) = [w(3-1)] \left(\left[2 \cdot 1 + (-1)^1 2^{\frac{1}{2}[1+(-1)^1]} \right] k \right) = 1([2-2^0]k) = 1 \cdot (k)$
$g(2,2) = [w(3-2)] \left(\left[2 \cdot 2 + (-1)^2 2^{\frac{1}{2}[1+(-1)^2]} \right] k \right) = 1([4+2^1]k) = 1 \cdot (6k)$
$g(3,2) = [w(3-3)] \left(\left[2 \cdot 3 + (-1)^3 2^{\frac{1}{2}[1+(-1)^3]} \right] k \right) = 1([6-2^0]k) = 1 \cdot (5k)$
$g(0,3) = [w(3-0)] \left[\left(\frac{1}{81 \cdot 0^2 + (-1)^0 3 \cdot 0 + 5} \right)^{T_0(0)} \left(\left[2 \cdot 0 + (-1)^0 2^{\frac{1}{2}[1+(-1)^0]} \right] k \right)^2 \right]^{2^{T_0(0)}}$
$= 1000 \cdot \left[\left(\frac{1}{5} \right)^0 ([0+2^1]k)^2 \right]^{2^0} = 1000 \cdot [(0+2^1]k)^2 = 1000 \cdot (2k)^2$
$g(1,3) = [w(3-1)] \left[\left(\frac{1}{81 \cdot 1^2 + (-1)^1 3 \cdot 1 + 5} \right)^{T_0(1)} \left(\left[2 \cdot 1 + (-1)^1 2^{\frac{1}{2}[1+(-1)^1]} \right] k \right)^2 \right]^{2^{T_0(1)}}$
$= 1 \cdot \left[\left(\frac{1}{81-3+5} \right)^0 ([2-2^0]k)^2 \right]^{2^0} = 1([2-2^0]k)^2 = 1 \cdot (k)^2$
$g(2,3) = [w(3-2)] \left[\left(\frac{1}{81 \cdot 2^2 + (-1)^2 3 \cdot 2 + 5} \right)^{T_0(2)} \left(\left[2 \cdot 2 + (-1)^2 2^{\frac{1}{2}[1+(-1)^2]} \right] k \right)^2 \right]^{2^{T_0(2)}}$
$= 1 \cdot \left[\left(\frac{1}{81 \cdot 4 + 6 + 5} \right)^1 ([4+2^1]k)^2 \right]^{2^1} = 1 \cdot \left[\left(\frac{1}{335} \right) (6k)^2 \right]^2$
$g(3,3) = [w(3-h)] \left[\left(\frac{1}{81 \cdot 3^2 + (-1)^3 3 \cdot 3 + 5} \right)^{T_0(3)} \left(\left[2 \cdot 3 + (-1)^3 2^{\frac{1}{2}[1+(-1)^3]} \right] k \right)^2 \right]^{2^{T_0(3)}}$
$= 1 \cdot \left[\left(\frac{1}{81 \cdot 9 - 9 + 5} \right)^1 ([6-2^0]k)^2 \right]^{2^1} = 1 \cdot \left[\left(\frac{1}{725} \right) (5k)^2 \right]^2$

From these tables the constant k may be determined, as well as a host of relationships between the fermion masses.

The upper generation fermion masses thus, fill out the following table.

(It is rather remarkable how simple the relationships are.)

$\frac{m(0,2)}{m(0,1)} = 1000 \cdot (2k)$	$\frac{m(0,3)}{m(0,1)} = 1000 \cdot (2k)^2$
$\frac{m(1,2)}{m(2,1)} = 1 \cdot (k)$	$\frac{m(1,3)}{m(2,1)} = 1 \cdot (k)^2$
$\frac{m(2,2)}{m(1,1)} = 1 \cdot (6k)$	$\frac{m(2,3)}{m(1,1)} = 1 \cdot \left[\left(\frac{1}{335} \right) (6k)^2 \right]^2$
$\frac{m(3,2)}{m(3,1)} = 1 \cdot (5k)$	$\frac{m(3,3)}{m(3,1)} = 1 \cdot \left[\left(\frac{1}{725} \right) (5k)^2 \right]^2$

From which follow:

$$k = \frac{1}{2} \left(\frac{1}{1000} \left[\frac{m(0,2)}{m(0,1)} \right] \right) = \frac{m(1,2)}{m(2,1)} = \frac{1}{6} \left[\frac{m(2,2)}{m(1,1)} \right] = \frac{1}{5} \left[\frac{m(3,2)}{m(3,1)} \right]$$

$$= \frac{1}{2} \sqrt{\frac{1}{1000} \left[\frac{m(0,3)}{m(0,1)} \right]} = \sqrt{\frac{m(1,3)}{m(2,1)}} = \frac{1}{6} \sqrt{335 \left[\frac{m(2,3)}{m(1,1)} \right]} = \frac{1}{5} \sqrt{725 \left[\frac{m(3,3)}{m(3,1)} \right]}$$

Now, the muon mass is well measured, which is why k was determined in terms of the muon mass.

(The table above shows that it could have been determined in terms of any other non-first generation mass - though to less accuracy.)

Assigning:

$$m(3,2) = m_\mu = 105.6583668 \text{ MeV}/c^2$$

and using the already above assigned value:

$$m(3,1) = m_e = .510998928 \text{ MeV}/c^2$$

$$\Rightarrow k = \frac{1}{5} \left[\frac{m(3,2)}{m(3,1)} \right] = \frac{1}{5} \left[\frac{m_\mu}{m_e} \right] = \frac{1}{5} \left[\frac{105.6583668}{.510998928} \right]$$

$$= 41.35365497$$

All the above mass ratio relationships may be verified using this value.

Computed mass values:

$$\frac{m(1,2)}{m(2,1)} = 1 \cdot (k)$$

$$\Rightarrow m_s = m(1,2) = m(2,1)k = 105.6583668$$

$$\frac{m(2,2)}{m(1,1)} = 1 \cdot (6k)$$

$$\Rightarrow m_c = m(2,2) = 6m(1,1)k = 1267.9004016$$

$$\frac{m(3,2)}{m(3,1)} = 1 \cdot (5k)$$

$$\Rightarrow m_\mu = m(3,2) = 5m(3,1)k = 105.6583668$$

$$\frac{m(0,2)}{m(0,1)} = 1000 \cdot (2k)$$

$$\Rightarrow m_{\nu_{\mu e}} = m(0,2) = 2000m(0,1)k = 0.12006632591$$

$$\frac{m(1,3)}{m(2,1)} = 1 \cdot (k)^2$$

$$\Rightarrow m_b = m(1,3) = m(2,1)k^2 = 4369.359646$$

$$\frac{m(2,3)}{m(1,1)} = 1 \cdot \left[\left(\frac{1}{335} \right) (6k)^2 \right]^2$$

$$\Rightarrow m_t = m(2,3) = \left[\left(\frac{1}{335} \right) (6k)^2 \right]^2 m(1,1) = 172580.2034$$

$$\frac{m(3,3)}{m(3,1)} = 1 \cdot \left[\left(\frac{1}{725} \right) (5k)^2 \right]^2$$

$$\Rightarrow m_\tau = m(3,3) = \left[\left(\frac{1}{725} \right) (5k)^2 \right]^2 m(3,1) = 1776.967943$$

$$\frac{m(0,3)}{m(0,1)} = 1000 \cdot (2k)^2$$

$$\Rightarrow m_{\nu_\tau} = m(0,3) = 4000m(0,1)k^2 = 9.930362831$$

And all the fermion masses may be tabulated as follows.
(in Mev/c^2)

$m_d = m(1,1) \approx 5.10998928$	$m_s = m(1,2) = 105.6583668$	$m_b = m(1,3) = 4369.359646$
$m_u = m(2,1) \approx 2.55499464$	$m_c = m(2,2) = 1267.9004016$	$m_t = m(2,3) = 172580.2034$
$m_e = m(3,1) \approx 0.510998928$	$m_\mu = m(3,2) = 105.6583668$	$m_\tau = m(3,3) = 1776.967943$
$m_{\nu_e} = m(0,1) \approx 0.0000014517015$	$m_{\nu_\mu} = m(0,2) = 0.12006632591$	$m_{\nu_\tau} = m(0,3) = 9.930362831$

For comparison, as of this publication the reported mass values:

$m_d = m(1,1) \approx 4.9(0.8)$	$m_s = m(1,2) = 105(25)$	$m_b = m(1,3) = 4190(40)$
$m_u = m(2,1) \approx 2.4(0.7)$	$m_c = m(2,2) = 1260(80)$	$m_t = m(2,3) = 172750(750)$
$m_e = m(3,1) \approx 0.510998910(13)$	$m_\mu = m(3,2) = 105.6583668(38)$	$m_\tau = m(3,3) = 1,776.84(17)$
$m_{\nu_e} = m(0,1) < 0.0000022[35]$	$m_{\nu_\mu} = m(0,2) < 0.17[35]$	$m_{\nu_\tau} = m(0,3) < 15.5[35]$

<https://en.wikipedia.org/wiki/Lepton#Mass>

<https://en.wikipedia.org/wiki/Electron>

<https://en.wikipedia.org/wiki/Muon>

<https://en.wikipedia.org/wiki/Tauon>

<https://en.wikipedia.org/wiki/Quark>

https://en.wikipedia.org/wiki/Down_quark

https://en.wikipedia.org/wiki/Up_quark

https://en.wikipedia.org/wiki/Charm_quark

https://en.wikipedia.org/wiki/Strange_quark

https://en.wikipedia.org/wiki/Bottom_quark

https://en.wikipedia.org/wiki/Top_quark

https://en.wikipedia.org/wiki/Current_quark_mass
<http://pdg.lbl.gov/2012/tables/rpp2012-sum-leptons.pdf>
<http://pdg.lbl.gov/2012/tables/rpp2012-sum-quarks.pdf>

There are variations between the references on some of the masses.

All the calculated masses above are accurate within their margin of error for all the references, except for the Strange & Bottom Quarks which are in range for one and slightly out of range for another.

Now, any two dimensional transformation may be used to transform the arbitrarily chosen two masses to determine the rest. If some transformation exists such that from two constants from a list of fundamental constants, such as: $1, \pi, e$; then all the fermion masses would be fixed by those fundamental constants alone - not even a single arbitrary constant to fix them all.

Is it just a coincidence that all the fermion masses may be calculated from merely two well chosen constants, indexed via the two field strength fundamentals founded by the constructed doublet- \mathbb{R} -algebra?

Even if so, how does the Higgs mechanism explain the above mass ratio relationships?

Does SUSY predict this relationship? How about S&M Theory?

Now, that it has just been shown that all the fermion masses may be determined by two well chosen constants via the mass-generalized Maxwell's equations field strengths \mathbf{E} & \mathbf{B} ; the issue of the relationship of charge to the mass-generalized Maxwell's equations field strengths and possibly to mass may be re-examined in this new context from another direction.

The relationship between the mass-generalized Maxwell's equations field strengths and the fermion charges may be established by constructing a function $c()$ is defined simply by:

$$c((R^1, R^2, R^3)_h) = c(R_h^1) + c(R_h^2) + c(R_h^3),$$

$$c(\overline{R}_h^i) = -c(R_h^i),$$

$$c(E_h^i) = x,$$

$$c(B_h^i) = y, .$$

then the objects are:

$$c(e(i)) = -3x, c(v(i)) = 3y, c(u_j(i)) = 2x + y, c(d_j(i)) = -(x + 2y).$$

From here, two different calibrations are consistent with current empirical evidence. Each has its advantages.

Calibrating this with: $-1 = c(e(1)) = -3x, 0 = c(v(1)) = 3y \Rightarrow x = \frac{1}{3}, y = 0$

Operating this linear function on the objects, yields:

$$c(e(i)) = -1, c(v(i)) = 0$$

$$c(u_j(i)) = \frac{2}{3}, c(d_j(i)) = -\frac{1}{3}$$

These correspond to the charge characteristics of all the fermions.

If, on the other hand, the calibration is as follows:

$$\text{Let: } x = \lambda m_{e((h))}^2, \quad y = \lambda m_{v((h))}^2$$

$$\text{Calibrating this with: } -1 = c(e(1)) = -3x = -3\lambda m_{e((h))}^2 \Rightarrow x = \frac{1}{3}$$

$$\text{and: } \lambda = \frac{1}{3} m_{e((h))}^{-2}$$

$$\Rightarrow c(v(h)) = 3y = 3\lambda m_{v((h))}^2 = \left(\frac{m_{v((h))}}{m_{e((h))}} \right)^2 \Rightarrow y = \frac{1}{3} \left(\frac{m_{v((h))}}{m_{e((h))}} \right)^2$$

Operating this linear function on the objects, yields:

$$c(e(h)) = -1, c(v(h)) = \left(\frac{m_{v((h))}}{m_{e((h))}} \right)^2$$

$$c(u_j(h)) = \frac{2}{3} + \frac{1}{3} \left(\frac{m_{v((h))}}{m_{e((h))}} \right)^2, c(d_j(i)) = -\frac{1}{3} - \frac{2}{3} \left(\frac{m_{v((h))}}{m_{e((h))}} \right)^2$$

From the above discussion:

$$\left(\frac{m_{v((1))}}{m_{e((1))}} \right)^2 = \left(\frac{m(0,1)}{m(3,1)} \right)^2 = \left(\frac{.0000014517015}{.510998928} \right)^2 \approx 8.07 \times 10^{-12}$$

This neutrino mass estimate is near the high end possibility, but this charge function is still within measurement error range.

The advantage of this calibration is that because Noether's Theorem applied to the charge density (see [1]) insists the above charge function is a global invariant, so is mass/energy. Noether's Theorem doesn't have to be asserted twice, but Hamilton's principle (for charge density) is a consequence of the \mathbb{R} -algebra and Noether's Theorem applied to that, with the above insight, establishes conservation of charge and mass/energy, as a single consequence.

And, this illustrates that charge, being a measure of first order object (lepton) masses, only exists where a fermion rest mass exists. That is, charges do not exist in isolation - in a vacuum - but only where \mathbf{S}_R field strength component matrix entries exist. The generalized electric field strength \mathbf{S}_R matrix entries are basically directly proportional to the charge, and also where the preponderance of the mass of second order objects (quarks) rests.

Nowhere here was there found in this discussion Hilbert space, annihilation operators, spontaneous symmetry breaking, path integrals, Feynman diagrams, or

any other inveigles or obfuscations.

The coincidences mount.

The space-time we recognize is described by the constructive \mathbb{R} -doublet-algebra

The vector dot and cross products we all learned in high school are natural products in the constructed \mathbb{R} -doublet-algebra.

The mass-generalized Maxwell's equations are satisfied for all smooth functions in the constructed \mathbb{R} -doublet-algebra which satisfy the four-vector-doublet Klein-Gordon equation, yet reduce to Maxwell's equations for zero mass (something the Dirac equation does not do).

The fermions and photons are natural fundamental constructions from the field strengths of the mass-generalized Maxwell's equations. (and the hadrons are natural constructions therein, as well).

The charges of the fermions are a natural function of the field strengths of the mass-generalized Maxwell's equations.

The masses of the fermions may be calculated from merely two constants indexed via the field strengths of the mass-generalized Maxwell's equations.

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