

## ON THE PARTICULAR DISTRIBUTION OF PRIME NUMBERS

On the particular distribution of prime numbers is a case to be treated in several parts. In the first place, I will treat the prime identity  $\Delta$ , which is the method that allows one to discern with certainty prime numbers  $\gamma$ , of strong non-prime numbers  $\omega$ , and non-prime numbers  $\mu$ , amongst the series of natural wholes  $A$ , as in :

$$\omega, \mu, \Upsilon \subset A$$

The prime identity  $\Delta$ , indicates the characteristics of prime numbers  $\gamma$ , of strong non-prime numbers  $\omega$ , and non-prime numbers  $\mu$ , in the following way :

- 1) A prime number  $\gamma$ , is a number which is divisible only by 1 and by itself  $Z$ , so that :  
 $\Upsilon=Z$
- 2) A strong non-prime number  $\omega$ , is a even multiple  $\beta$ , so that :  $\omega = \beta$
- 3) A no-prime number  $\mu$ , is an odd multiple  $\xi$ .

The second step consists of analysing the natural wholes  $A$ , to have a standard idea of prime numbers  $\Upsilon$ , and their distribution.

All numbers  $N$  containing any even unit  $\Phi$ , no matter its size  $I$  will always be an even number  $\Pi$ , as well as all numbers  $N$ , containing any odd unit  $M$ , whatever its size  $I$ , will always be an odd number  $\pi$ , because of the fact that the unit  $\eta$  contributes to determining the even nature  $\Phi'$ , or the odd nature  $M'$  of a number  $N$ , so that :  $N \subset \Phi = n \wedge N \subset M = \pi$ .

The unit  $\eta$ , being a finite size serving as a base to measure other sizes  $I$  of same sort  $\Gamma$ . One can then spread all  $n$  numbers greater than 10, having as their unit  $\eta$  one of the following numbers : 0,2,4,6, or 8, as strong non-prime numbers  $\omega$ , and all numbers greater than 10 having for their unit  $\eta$  one of the following numbers : 1,3,7 or 9 will be either non-prime numbers  $\mu$  or prime numbers  $\Upsilon$ . Because prime numbers  $\Upsilon$  obey a precise rule of distribution which I am going to demonstrate.

First of all I begin by defining a test which will allow to know if a number  $N'$  superior to 1 is prime or not, it is the identification test of prime numbers that take place in two stades :

- the first stade consist in dividing a number  $N'$  by 3 and by 7, if the number  $N'$  is divisible by 3, by 7 or by the two numerals, it is not prime, otherwise at this stade of the test it's possibly chances for numbers  $N'$  to be prime.
- the second stade consist in confirming or invalidating the number the number  $N'$  is prime or not, for that I need to define explicitly the characteristics of numbers  $N'$ .

[ Definitions of numbers  $N'$  ] in accordance with convention, only the numbers  $N'$  could to be submitted to the identification test of prime numbers. There are two types of numbers  $N'$  (these are numbers  $N'$ , unequal to 10, they are all odd numbers  $\pi$  which are not multiple of 2, and the numbers  $N'$  superior to 10, they are odd numbers  $\pi$  except multiples of 5). (we'll consider that the identification test of prime numbers "guarantee" that numbers  $N'$  3 and 7 are prime).

3 and 7 moreover being the smallest common dividers (SCS) of non-prime numbers  $\mu$ , (indeed, the non-prime numbers  $\mu$ , are odd multiples  $M^i$ , in that sense they are divisible). They does't always allow to "find" all non-prime numbers  $\mu$ , (some numbers, are not divisible by 3 or 7, they are pseudo-prime numbers  $\gamma'$  - see the first stade of the identification test of prime numbers.)

The consequence, rules determining the identification test of prime numbers, just as the definition of numbers  $N'$ , is that all strong non-prime numbers  $\omega$  and all the multiples of 5 not being able to be prime number  $\gamma$  on no account, they are useless because they cannot be submitted to identification test of prime numbers

Because among others :

$$\omega = \alpha^p \times b^p \vee \alpha^p \times b^i$$

and :

$$M_5 = \alpha^p \times 5 \vee b^i \times 5$$

(or  $\alpha^p$ , is an even number superior or equal to 2,  $b^p$  an other some even number superior or equal to 2,  $b^i$  an ODD number superior or equal to 3,  $M_5$ , a multiple of 5).

In this same way :

$$\left\{ \begin{array}{l} P_3/3=F_1 \\ P_9/3=F_3 \\ P_1/3=F_7 \\ P_7/3=F_9 \end{array} \right. \quad \text{knowing that :} \quad \left\{ \begin{array}{l} P_3 > F_1 \\ P_9 > F_3 \\ P_1 < F_7 \\ P_7 > F_9 \end{array} \right. \quad \begin{array}{l} \text{(where 3 and 7} \\ \text{are SCD)*} \\ \\ \text{(note that 3} \\ \text{and 7 are also} \\ \text{prime dividers)} \end{array}$$

Or :

$$\left\{ \begin{array}{l} P_7/7=F_1 \\ P_1/7=F_3 \\ P_9/7=F_7 \\ P_3/7=F_9 \end{array} \right. \quad \text{knowing what :} \quad \left\{ \begin{array}{l} P_7 > F_1 \\ P_1 > F_3 \\ P_9 > F_7 \\ P_3 > F_9 \end{array} \right.$$

But also :

$$\left\{ \begin{array}{l} 3 \times F_1=P_3 \\ 3 \times F_3=P_9 \\ 3 \times F_7=P_1 \\ 3 \times F_9=P_7 \end{array} \right. \quad \text{or :} \quad \left\{ \begin{array}{l} 7 \times F_1=P_7 \\ 7 \times F_3=P_1 \\ 7 \times F_9=P_3 \\ 7 \times F_7=P_9 \end{array} \right. \quad \begin{array}{l} \text{(where 3 and 7} \\ \text{are SCM)**} \end{array}$$

(Among the common dividers at two or several non-prime numbers  $\omega$ , there are two among all which smaller than all the others, they are the smallest common dividers (SCS)\*

(Among the common odd multipliers at two or several non-prime numbers  $\omega$ , there are two which among all are smallest than all the others, they are smallest common multipliers (SCM)\*\*

(The smallest common multipliers (SCM) non-prime numbers  $\omega$ , can allow to find new non-prime numbers  $\omega$ )

(Either  $F_1$ , is a number superior to 10 having like unit numeral 1, or  $F_3$  is a number superior to 10 having like unit numeral 3, or  $F_7$  is a number to 10 having like unit numeral 7, or  $F_9$  is a number superior to 10 having like unit numeral 9,  $P_1$  is a product having numeral 1 like unit,  $P_3$  is a product having numeral 3 like unit,  $P_7$  is a product having numeral 7 like unit,  $P_9$  is a product having numeral 9 like unit)

- To know if a number  $N'$ , having get the 1<sup>st</sup> stade of the identification test of prime numbers is prime or not require use of the “magical key” which I call like this because it is at the root of the opening of a way between on the one hand a prime numbers  $\gamma$  “landscape” appearing so as uncertain, and on the other hand a another “landscape” where it seems that a concealed order is ruling as for their distribution among the natural wholes A.

### FORMULA OF THE “MAGICAL KEY”

$\alpha$ ) It is important to find the two multiplicative operations  $O_1$  and  $O_3$  wich by their respective products  $P$  must have the most weak gap possible with the number  $N'$  having passed the first stade that is to say those being in front of and following e possible third multiplicative operation  $O_2$ , whose product  $P$  is supposed to be the number  $N'$  having passed the first stade of the identification test of prime numbers, it can exist only if the number  $N'$  in question is a non-prime numbers  $\omega$ , otherwise there can only be two multiplicative operations  $O_1$  and  $O_3$ , this imply that the number  $N'$  having passed the first stade of the identification test of prime numbers, is really prime number  $\Upsilon$ .

- Equations bell, I make explicit the required conditions to know if number  $N'$  having passed the first stade of the identification test of prime numbers is prime or not.

Case where the number  $N'$  having passed the first stade of the identification test of prime numbers is a non-prime number  $\omega$ .

Then :

$$\left\{ \begin{array}{l} O_1 \Rightarrow M_A \times M_1 = P_1 \\ O_2 \Rightarrow M_A \times M_2 = P_2 \\ O_3 \Rightarrow M_A \times M_2 = P_3 \end{array} \right. \quad (\text{let's note that for multiplicative})$$

operations  $O_1$ ,  $O_2$  and  $O_3$ ,  $M_A$  is identical.

As :

$$\left\{ \begin{array}{l} M_1 < M_2 < M_3 \\ P_1 < P_2 < P_3 \\ P_1 \wedge P_3 = N_p \\ P_2 = \omega \\ \Delta \propto M_A \end{array} \right.$$

In the case where the number  $N'$  having passed the first stade of the identification test of prime numbers, is a prime number  $\Upsilon$ .

Then :

$$\left\{ \begin{array}{l} O_1 \Rightarrow M_A \times M_1 = P_1 \\ O_3 \Rightarrow M_A \times M_3 = P_3 \end{array} \right.$$

(Let's note that for multiplicative  
O<sub>1</sub> and O<sub>3</sub>, M<sub>A</sub> is identical)

As :

$$\left\{ \begin{array}{l} M_1 < M_3 \\ P_1 < P_3 \\ P_1 \wedge P_3 = N_P \\ \Delta \propto M_A \end{array} \right.$$

:

$$\left\{ \begin{array}{l} N' \Leftrightarrow Y \\ P_1 < Y \\ O_3 > Y \end{array} \right.$$

:

$$\Lambda \left\{ \begin{array}{l} Y - P_1 = 1 \\ P_3 - Y = 1 \end{array} \right.$$

(Either O<sub>1</sub>, first multiplicative operation, or O<sub>2</sub> second multiplicative operation, or O<sub>3</sub> third multiplicative operation, or M<sub>A</sub> multiplicande, or M<sub>1</sub> first multiplier, or M<sub>2</sub> second multiplier, or M<sub>3</sub> third multiplier, or P<sub>1</sub> first product, or P<sub>2</sub> second product, or P<sub>3</sub> third product, or  $\Delta$  gap between products of multiplicative operation, or  $\Lambda$  gap between the number N' which passed the first stade of the identification test of prime numbers and the products)

For better understand this work, I will add the following sieves :

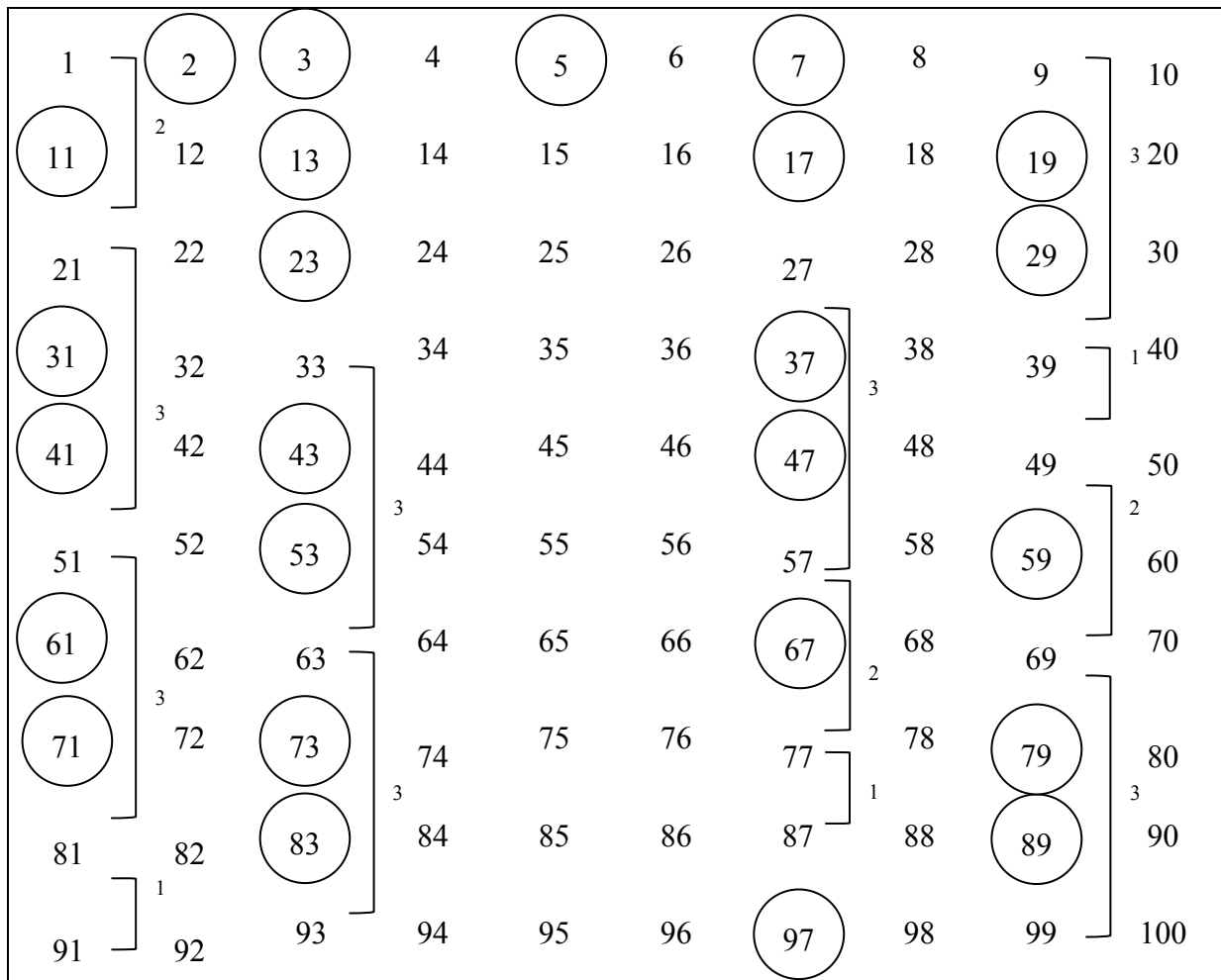
- 1) from 1 to 100
- 2) from 100 to 200
- 3) form 200 to 300
- 4) form 300 to 400
- 5) from 400 to 500

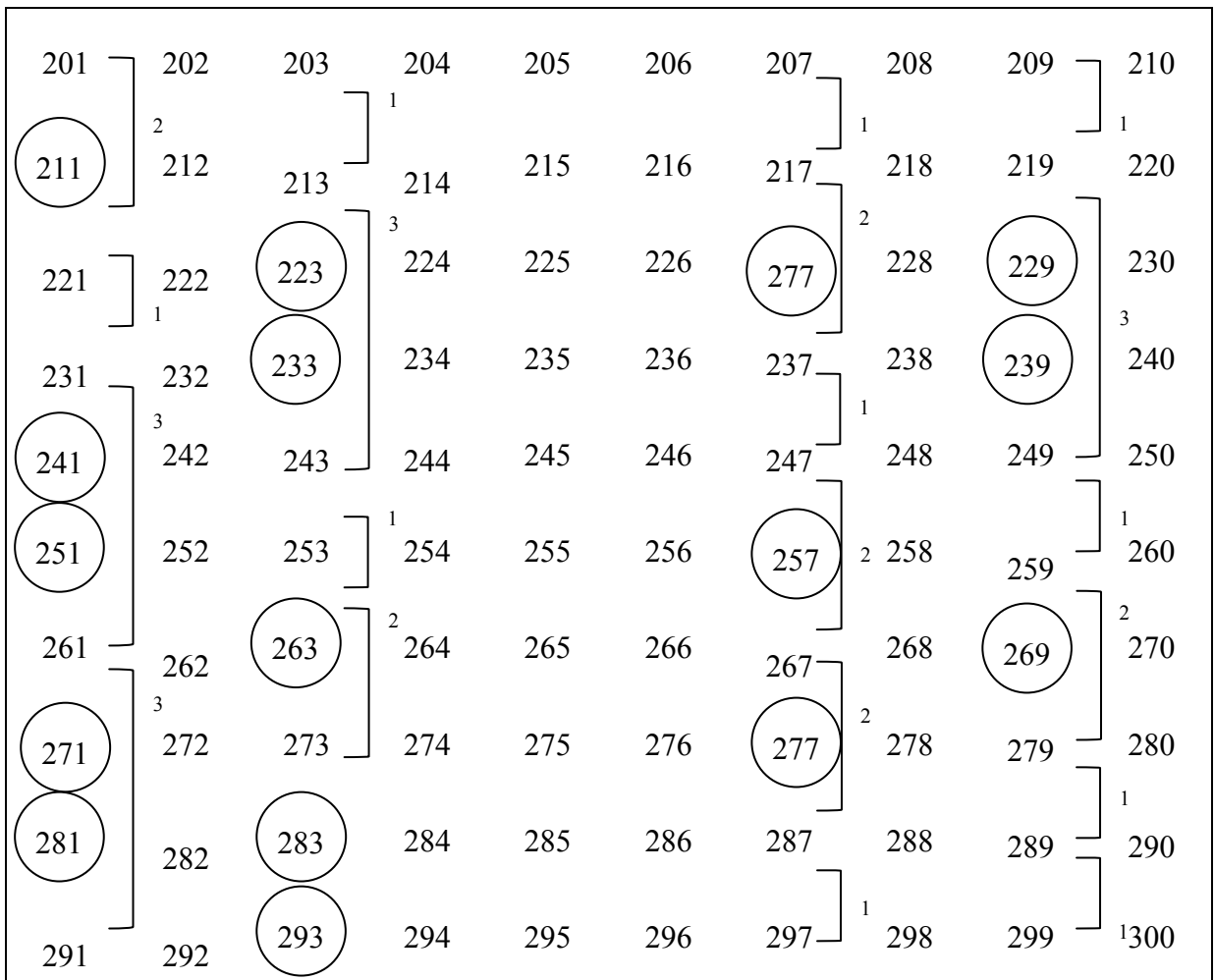
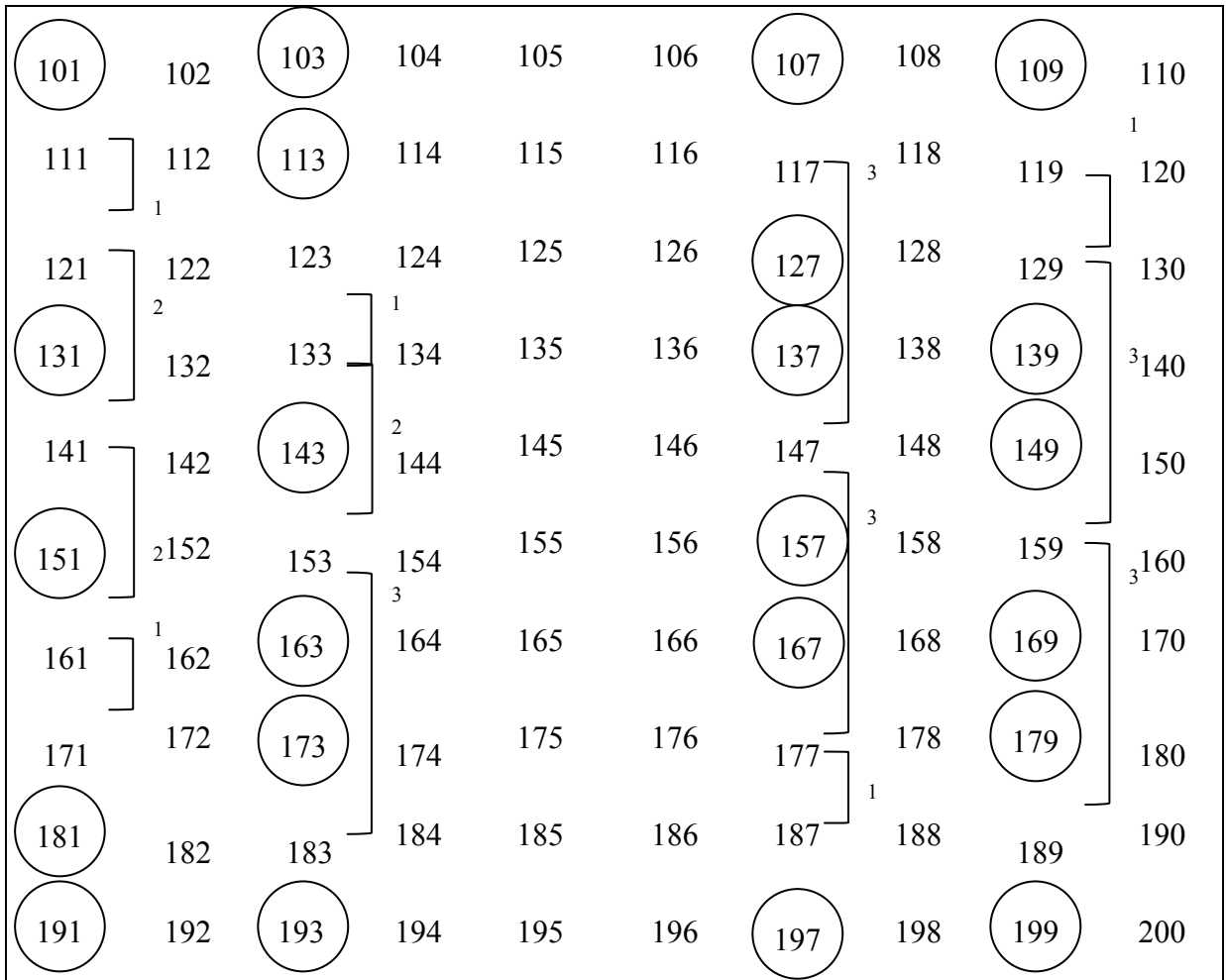
- 6) from 500 to 600
- 7) from 600 to 700
- 8) from 700 to 800
- 9) from 800 to 900
- 10) from 900 to 1000

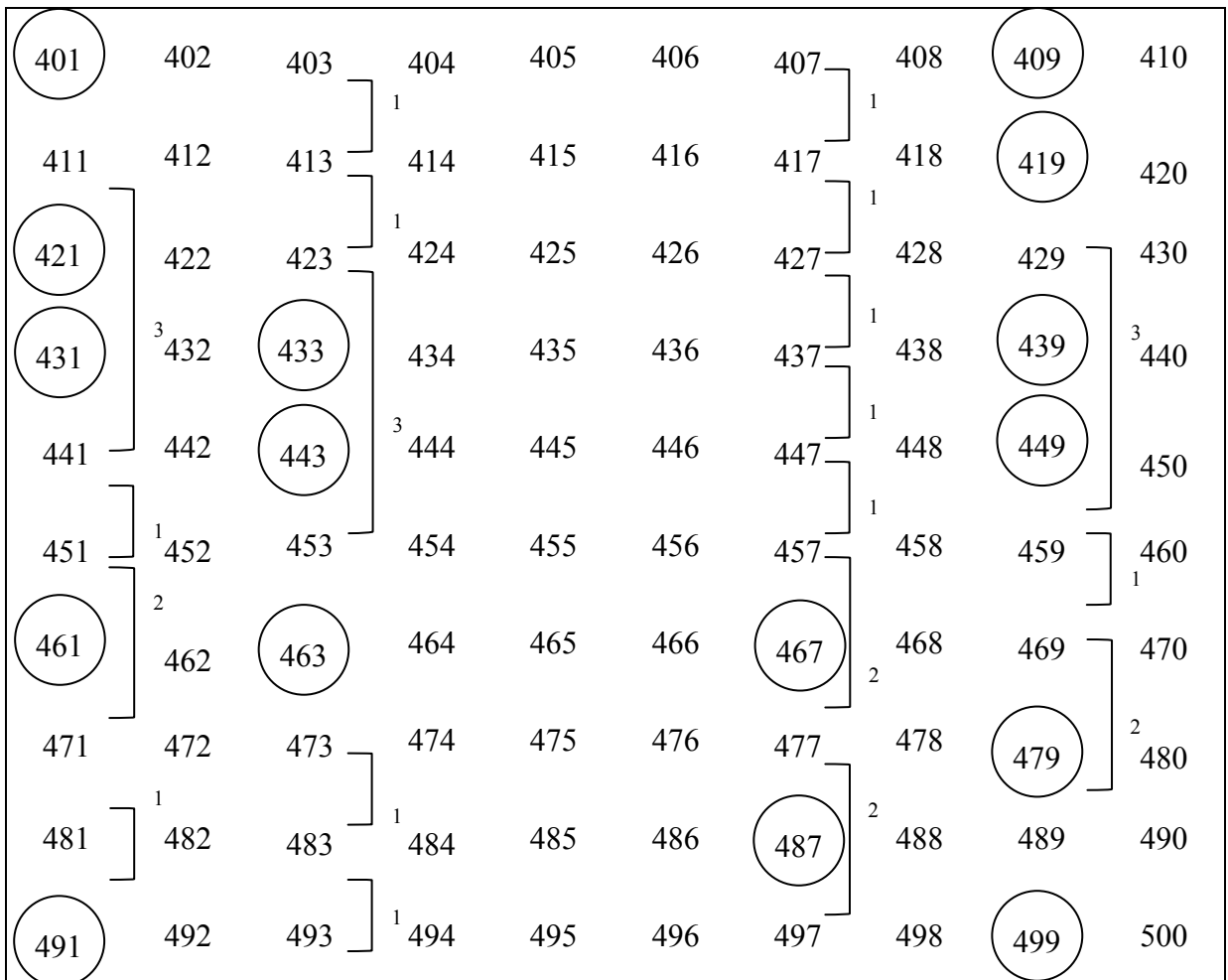
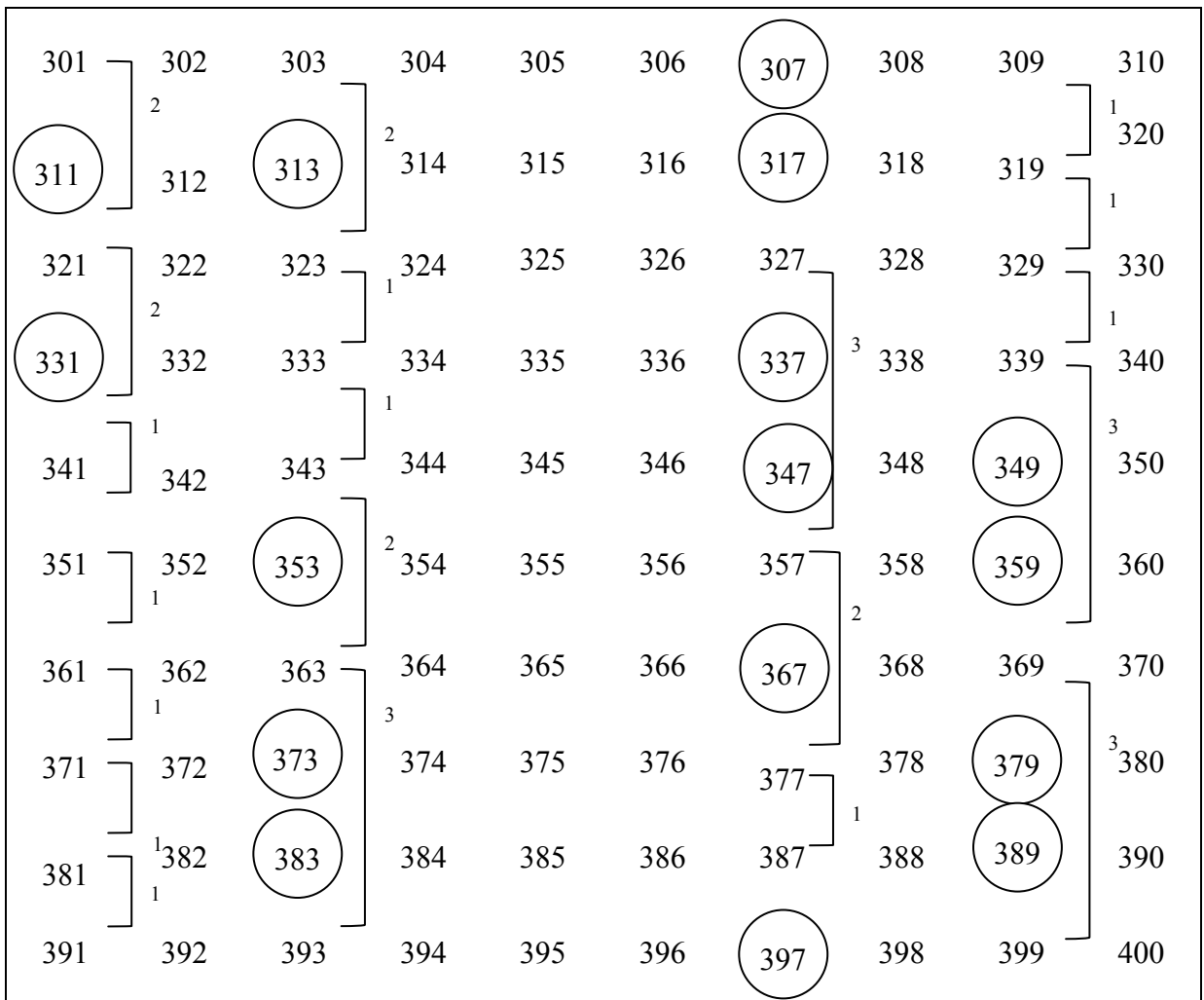
(By convention so sieve will start with its original number)

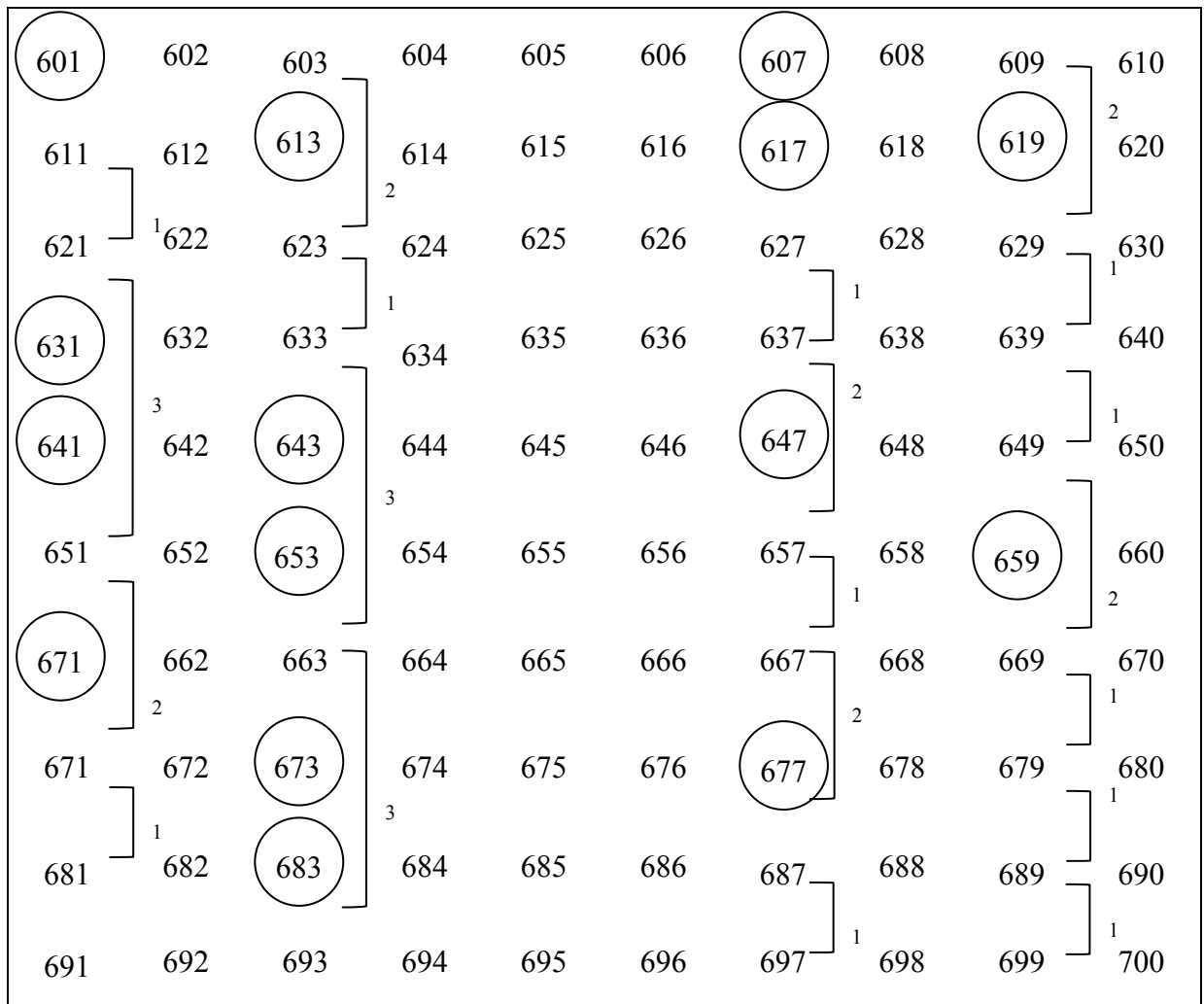
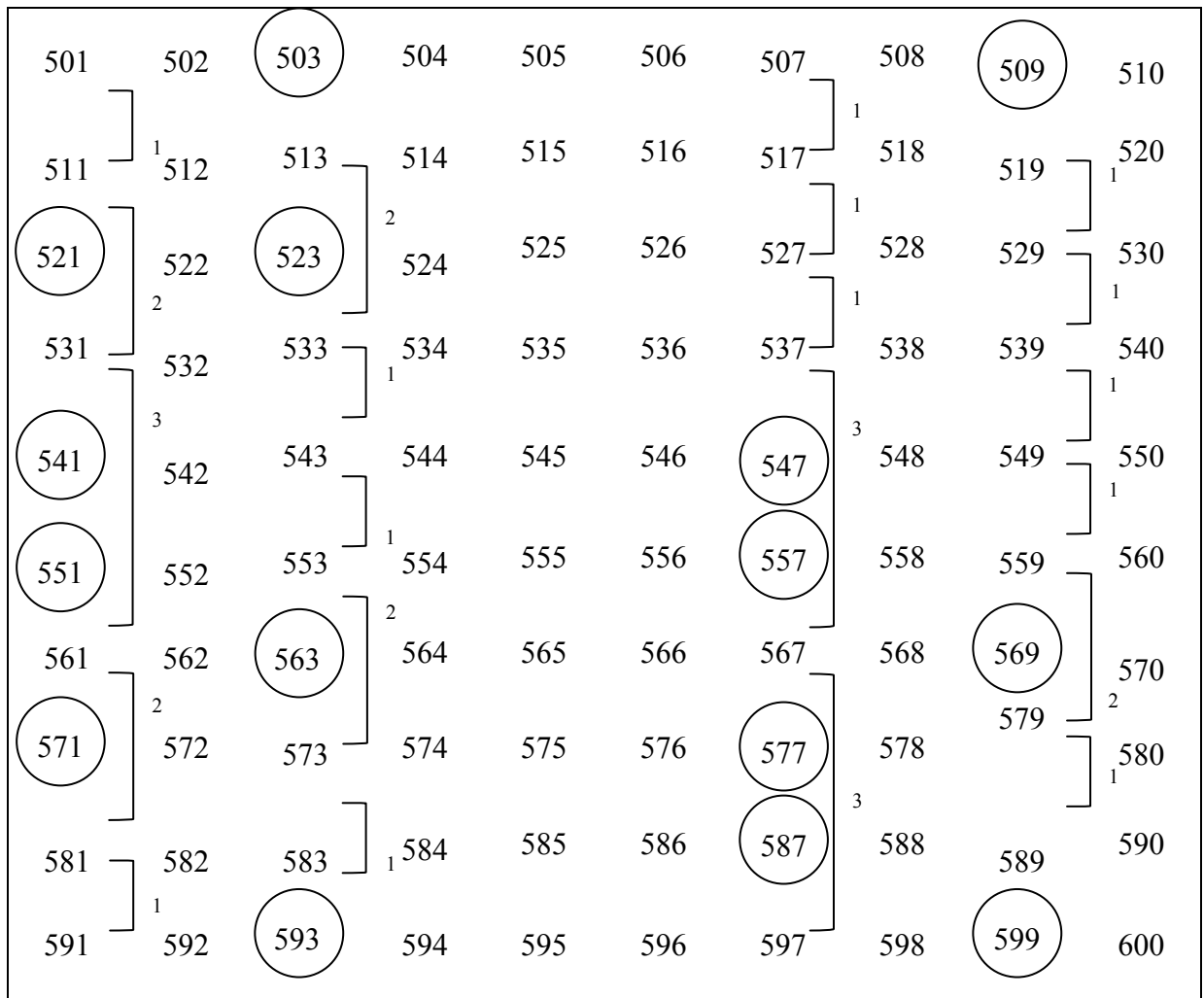
(In general, all sieves contain 100 numbers N arranged according to the natural wholes)

(The circled numbers are prime )



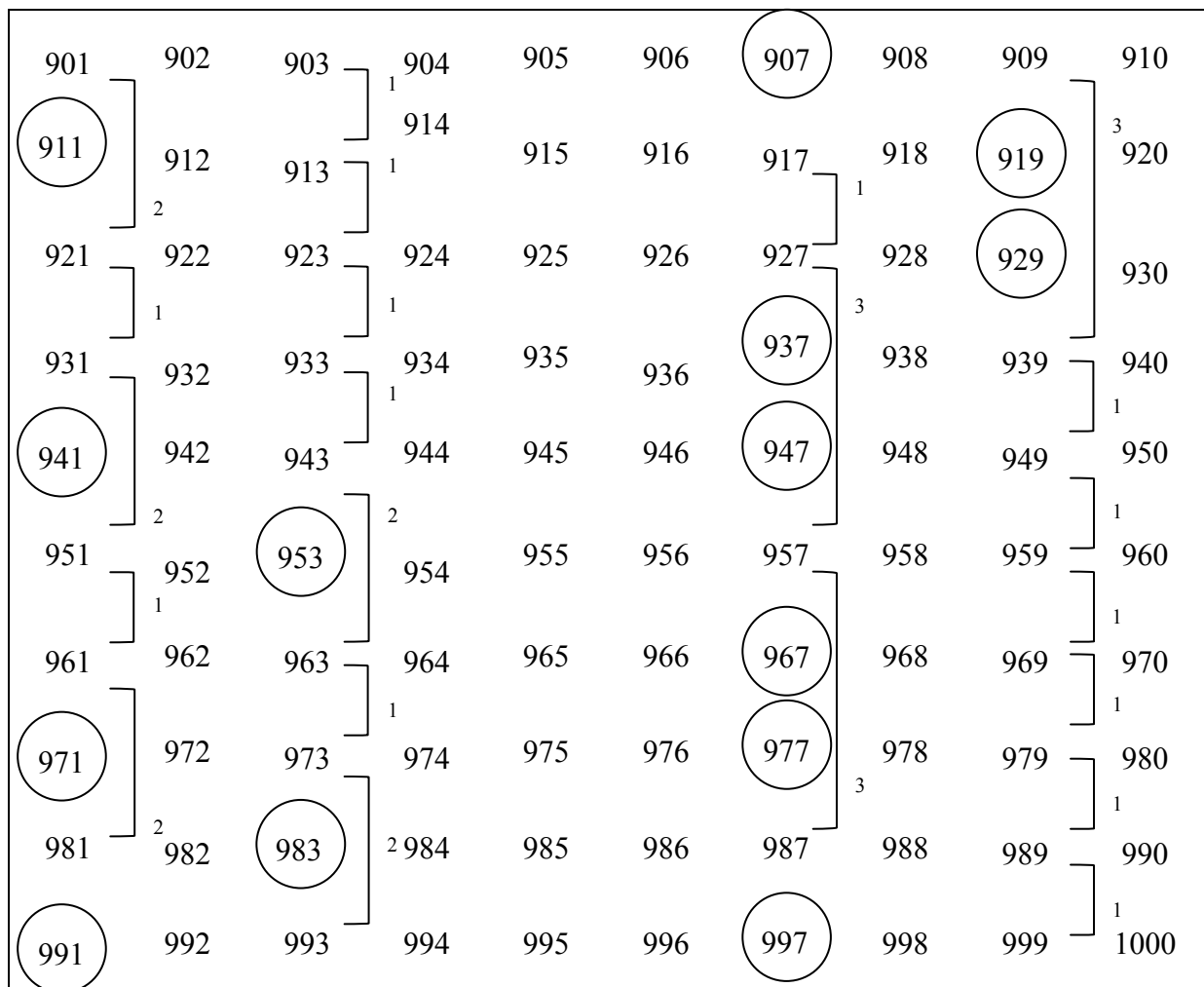












To be able to study and analyse a sieve, we will class its numbers  $N$  (knowing it contains 100) in ten decimal series  $\varepsilon$ , arranged in ten columns  $F^x$  and ten series of  $n$  natural wholes  $A$ , arranged in ten lines  $F^y$ .

A decimal series  $\varepsilon$ , is a group  $E$ , composed of  $n$  numbers (where  $n$  numbers-where  $n = 10$ -each being greater than 10, having the same common unit  $\chi$  (in exception with decimal series  $\varepsilon$  from 1 to 10 of sieve from 1 to 100).

And all being lined up in order from least to greatest, as in :

$$\varepsilon = (\alpha_x, b_x, c_x, \dots, n_x)$$

(where  $\alpha, b, c, \dots, n$ , are the numbers in the decimal series  $\chi$ ,  $X$ , the common unit of the numbers in the decimal serie).

A series of  $n$  natural wholes  $W$ , is a group  $E$ , composed of  $n$  numbers (where  $n = 10$ ), which contain the same number  $N$  of even numbers  $\pi$  and the same numbers  $N$  of odd numbers  $\pi$ , such that :  $W = n \Leftrightarrow \pi$ . As well, the  $n$  number of a series of  $n$  natural wholes  $W$ , are arranged in increasing order.

One can notice that the presence of prime numbers  $Y$ , is greater than in decimal series  $\varepsilon$  in relation to series of  $n$  natural wholes  $W$ , so that :  $Y \subset \varepsilon > Y \subset W$   
(see the sieves)

$$\left\{ \begin{array}{l} \pi_1 \subset Y_1 \\ (\pi \times 10) \\ \\ T = \frac{N_1}{\sqrt{N_2}} \end{array} \right. \quad \text{in relation to} \quad \left\{ \begin{array}{l} \pi_2 \subset Y_2 \\ (\pi \times 5) \\ T' = \frac{N_1}{\sqrt{N_2}} \end{array} \right.$$

note that  $N_1 \Leftrightarrow Y$

(Where  $\pi_1$ , some ODD numbers of a decimal serie,  $Y_1$  some numbers of a decimal series  $\pi_2$ , some ODD numbers of a series of  $n$  natural wholes,  $N_1$  are non-multiple odd numbers,  $N_2$  are ODD multiples,  $T$  the number of prime numbers contained in a decimal series,  $T'$  the number of prime numbers contained in a series of  $n$  natural wholes.

It is in this way, possible, by the sieves method and by identification test of prime numbers to know the distribution of prime numbers no matter what their size.

On can then from a number  $N$ , establish a sieve if the sieve contains only one hundred numbers  $N$ , composed in ten decimal series  $\varepsilon$  and in ten  $n$  natural wholes series  $W$ .

To understand the distribution of prime numbers  $Y$ , it is necessary to analyse a decimal series  $\varepsilon$ , grasp the place prime numbers  $Y$  occupy in this series, thanks to the introduction of a new concept which is the decimal difference  $B$ , this only reveals non-prime numbers  $\mu$  of a decimal series  $\varepsilon$ , obtained thanks to the identification test of prime numbers which allows the evaluation of prime numbers  $Y$  (number and distribution in a decimal series  $\varepsilon$ ) respecting the decimal difference  $B$  between each non-prime numbers  $\mu$  of a decimal series  $\varepsilon$ , (that is to say, calculating the number of numbers  $N$  separating non-prime numbers  $\mu$  from one another, as in :  $\mu - \mu \Rightarrow \mu \neq \mu$

(Were  $\mu$  is a non-prime number,  $\mu'$  a another non-prime number,  $D$  the difference)

In other words, the  $n$  numbers which separate a non-prime number  $\mu$  from another gives a difference  $D$  and are counted in a decimal form  $L$  (where  $L=10$ ), which permits the attribution for each difference  $D$  A  $n$  number of decimal  $L$  equal to A  $n$  number  $R$ , so that :  $L \Leftrightarrow R$   
(see the sieves).

The decimal differences  $B$  are represented by the traces (of the braces) represented in each sieve. They permit one two distinguish the non-prime numbers  $\mu$  from prime numbers  $Y$  from a decimal series  $\varepsilon$ , recognising them and indicating their position.

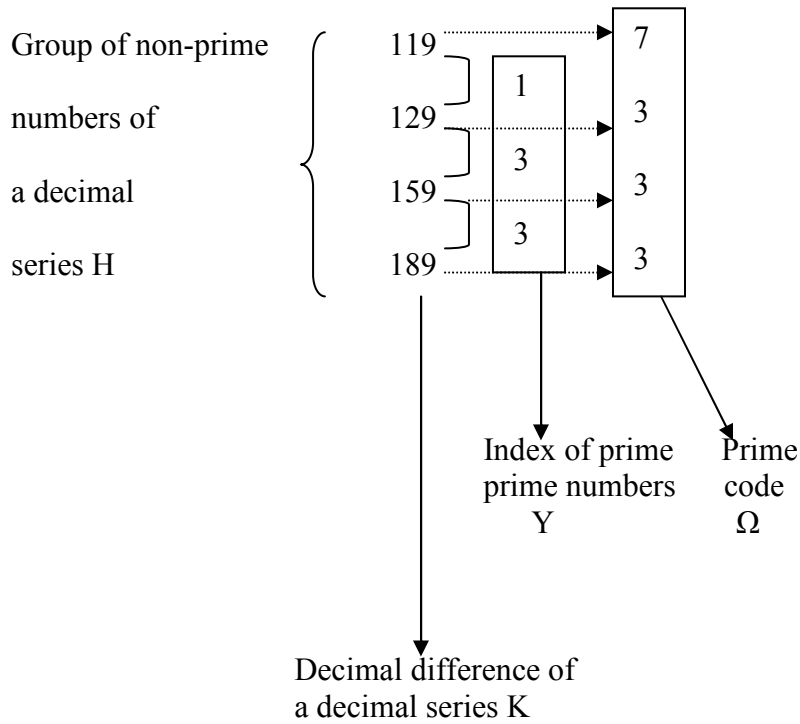
An index of prime numbers  $\Upsilon$ , is a group  $E$  composed of  $n$  numbers  $R$  corresponding to  $n$  decimal differences  $B$  of a decimal series  $\varepsilon$ , in other words, an index of prime numbers  $\Upsilon$  and the decimal differences of a decimal series  $K$  are of the same sort of order, such that :

$$f(\Upsilon) \leq f(K)$$

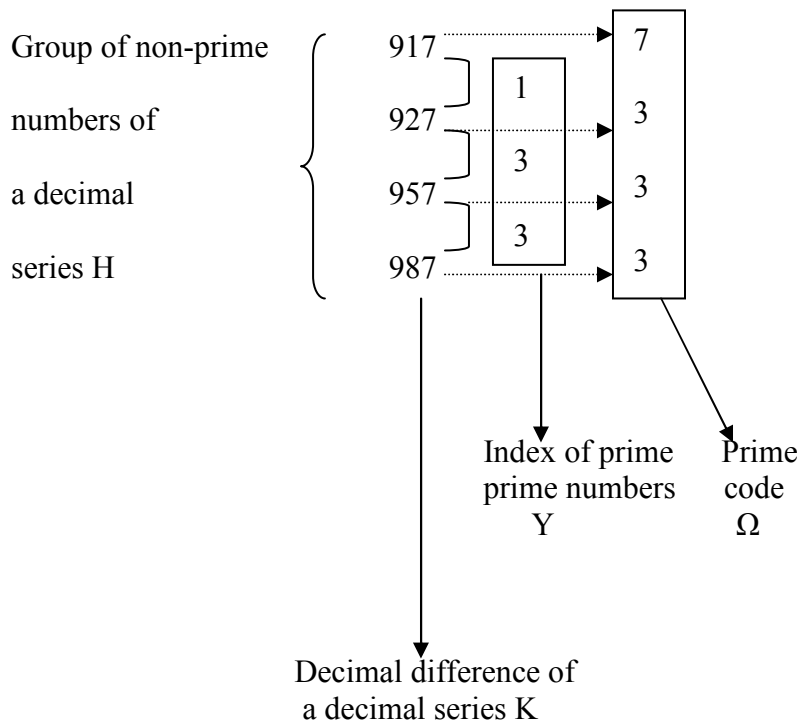
We also note the existence of prime codes  $\Omega$ , a prime code  $\Omega$ , is a group  $E$  composed of  $n$  prime dividers  $\Xi$  (in this case 3 and 7) corresponding to  $n$  non-prime numbers  $\mu$  of a decimal series  $\varepsilon^*$  is equotent to the prime code  $\Omega$  which corresponds.

\* (a group of non-prime numbers of a decimal series  $H$ , is an under-group  $S^E$ , composed of non-prime numbers  $\mu$  of a decimal series  $\varepsilon$ , such that :  $H \subseteq \varepsilon$ ).

### EXAMPLE OF CONFIGURATIONS F SIEVE 100 TO 200



### SIEVE 900 TO 1000



When two or more decimal series  $\varepsilon$  have the same index of prime numbers  $Y$  (there fore the same prime codes  $\Omega$ ) it is said they have the same configuration  $F$ . One may notice that there exists several types of index of prime numbers  $Y$ , (see the sieve) because the diversity of index of prime numbers , depend on the distribution of prime numbers  $Y$  and non-prime numbers  $\mu$  in each decimal series  $\varepsilon$ .

One can then says that :  $\Sigma = 0$

(where  $\Sigma$ , is the diversity of index of prime numbers of a sieve, 0 the diversity of distribution of prime numbers and non-prime numbers in each decimal series of the same sieve).

Each time that we will have recourse to second stade of the identification test of prime numbers, and only when we will find non-prime numbers  $\mu$  which are not divisible by 3 or by 7, we will note by the greek letter in the prime code  $\Omega$ , for symbolizing this action (instead of numerals).

**THE LAW ON THE INVARIABILITY OF THE RULES USED TO RECOGNIZE A  
PRIME NUMBER OF WHATEVER SIZE.**

A prime number, on any  $n$  size always obey the same rule to satisfy identification test of prime numbers wheter it is  $n$  times smaller or  $n$  times larger than another know prime number.