

# The analysis of the $\beta$ -decay that occurs in the nucleus

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## ABSTRACT

In the special relativity theory and the quantum mechanics, if the  $\beta$ -decay that occurs in the nucleus is analyzed by the Yukawa's pion theory, a virtual electron and a virtual anti-neutrino move in the velocity  $u_0$  in neutrons during the uncertainty time. If the nucleus give the enough energy  $E$  a neutron, the virtual electron, the virtual anti-neutrino and a neutron do the free electron, the free anti-neutrino of the velocity  $c - \Delta v$  and the proton. And a virtual positive electron and a virtual neutrino move in the velocity  $u_0$  in protons during the uncertainty time. If the nucleus give the enough energy  $E$  a proton, the virtual positive electron, the virtual neutrino and a proton do the free positive electron, the free neutrino of the velocity  $c - \Delta v$  and a neutron.

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## I. Introduction

The article treats that the  $\beta$ -decay is analyzed by the Yukawa's pion theory.

The Yukawa's pion theory treats the uncertainty principle. If the virtual pion moves in nucleons, you can say that a proton is equal to a neutron in the nucleus.

$$\Delta E \cdot \Delta t \geq \hbar \quad (1)$$

$$\Delta t \sim \frac{v}{c} \sim \frac{r}{c}, \quad \Delta E \sim m_\pi c^2$$

$$\Delta E \cdot \Delta t \sim \hbar$$

$$(m_\pi c^2) \left( \frac{r}{c} \right) \sim \hbar \quad (2)$$

Therefore,

$$m_\pi \sim \frac{\hbar}{rc} = \frac{1.05 \times 10^{-34} J \cdot s}{(1.7 \times 10^{-15} m)(3 \times 10^8 m/s)} \sim 2.1 \times 10^{-28} kg \quad (3)$$

If use the Yukawa's pion theory, understand the strong force.

In this time,  $r = 1.7 \times 10^{-15} m = 1.7 fm$  is the distant that the strong force work.

$$1 fm = 10^{-15} m$$

In this time, if give the energy  $E = m_\pi c^2$  a nucleon, to do the law of an energy conservation in the nucleus, the virtual pion does a free pion.

## II. Additional chapter-I

If the  $\beta$ -decay that occurs in the nucleus is analyzed by the Yukawa's pion theory, the virtual electron and the virtual anti-neutrino move in the velocity  $u_0$  in neutrons during the uncertainty time. And the virtual positive electron and the virtual neutrino move in the velocity  $u_0$  in protons during the uncertainty time.

The virtual electron and the virtual anti-neutrino move in the velocity  $u_0$  in neutrons during the uncertainty time. Because, the nucleons' a spin and a magnetic moment is conserved by that the virtual electron and the virtual anti-neutrino move in the same velocity  $u_0$  in nucleons.

$$\Delta E \cdot \Delta t \sim \hbar \quad (4),$$

$$\Delta E_e \cdot \Delta t_e + \Delta E_{\bar{\nu}} \cdot \Delta t_{\bar{\nu}} \sim 2\hbar$$

$$\Delta t_e = \Delta t_{\bar{\nu}} \sim \frac{r}{u_0}$$

$$\Delta E_e \sim m_e c^2, \Delta E_{\bar{\nu}} \sim m_{\bar{\nu}} c^2 \quad (5)$$

$$(m_e c^2) \frac{r}{u_0} + (m_{\bar{\nu}} c^2) \frac{r}{u_0} = \{(m_e c^2) + (m_{\bar{\nu}} c^2)\} \frac{r}{u_0} \sim 2\hbar \quad (6)$$

if  $m_e c^2 / u_0 \gg m_{\bar{\nu}} c^2 / u_0$ ,

$$r \sim \frac{2\hbar}{(m_e c^2)/u_0 + (m_{\bar{\nu}} c^2)/u_0} \sim \frac{2\hbar}{(m_e c^2)/u_0} = \frac{2\hbar u_0}{m_e c^2} \sim R_0 = 1.2 \times 10^{-15} m$$

$$\frac{2\hbar}{m_e c} = \frac{2 \times (1.05 \times 10^{-34} J \cdot s)}{(9.1 \times 10^{-31} kg) \times (3 \times 10^8 m/s)} = 7.7 \times 10^{-13} m = 770 fm$$

$$R_0 \sim 1.2 \times 10^{-15} m = 1.2 fm, R_0 \text{ is a nucleon's radius}$$

Therefore,

$$\frac{u_0}{c} = \frac{1.2 \times 10^{-15} m}{7.7 \times 10^{-13} m} = 1.56 \times 10^{-3}, u_0 \sim c \times 1.56 \times 10^{-3} \quad (7)$$

The real event occurs about the uncertainty principle.

$$\Delta p \cdot \Delta d \geq \hbar \quad (8)$$

But, the event that the virtual electron and the virtual anti-neutrino move in the velocity  $u_0$  isn't a real event.

$$\Delta p_e = m_e u_0, \Delta p_{\bar{\nu}} = m_{\bar{\nu}} u_0, \Delta d_e = \Delta d_{\bar{\nu}} = \Delta d = r \sim \frac{2\hbar u_0}{m_e c^2}$$

$$\Delta p_e \cdot \Delta d_e + \Delta p_{\bar{\nu}} \cdot \Delta d_{\bar{\nu}} = (m_e + m_{\bar{\nu}}) u_0 \cdot \frac{2\hbar u_0}{m_e c^2}, \Delta p_{\bar{\nu}} = m_{\bar{\nu}} u_0 \sim 0$$

$$= m_e u_0 \cdot \frac{2\hbar u_0}{m_e c^2} = 2\hbar \frac{u_0^2}{c^2} < 2\hbar \quad (9)$$

In this time, if the nucleus give the energy  $E = (m_e + m_{\bar{\nu}}) c^2 + \frac{1}{2} (m_e + m_{\bar{\nu}}) u_0^2 \approx m_e c^2$  a neutron,

to do the law of an energy conservation in the nucleus, the virtual electron, the virtual anti-neutrino and a neutron do the free electron, the free anti-neutrino of the velocity  $c - \Delta v$  and the proton and therefore the  $\beta$ -decay that occurs in the nucleus is

$$n \rightarrow p + e^- + \bar{\nu} \quad (10)$$

$$KE = \gamma_e m_e c^2 - m_e c^2 + \gamma_{\bar{\nu}} m_{\bar{\nu}} c^2, m_{\bar{\nu}} c^2 \sim 0, \gamma_e = 1/\sqrt{1 - V_e^2/c^2} \quad (11)$$

The virtual positive electron and the virtual neutrino move in the velocity  $u_0$  in the protons during the uncertainty time. Because, the nucleons' a spin and a magnetic moment is conserved by that the virtual positive electron and the virtual neutrino move in the same velocity  $u_0$  in nucleons.

Instead Eq(6),if use the virtual positive electron and the virtual neutrino

$$\Delta E \cdot \Delta t \sim \hbar$$

$$\Delta E_{e^+} \cdot \Delta t_{e^+} + \Delta E_{\nu} \cdot \Delta t_{\nu} \sim 2\hbar$$

$$\Delta t_{e^+} = \Delta t_\nu \sim \frac{r}{u_0}$$

$$\Delta E_{e^+} \sim m_{e^+}c^2, \Delta E_\nu \sim m_\nu c^2$$

$$(m_{e^+}c^2) \frac{r}{u_0} + (m_\nu c^2) \frac{r}{u_0} = \{(m_{e^+}c^2) + (m_\nu c^2)\} \frac{r}{u_0} \sim 2\hbar \quad (12)$$

if  $m_{e^+}c^2/u_0 \gg m_\nu c^2/u_0$ ,

$$r \sim \frac{2\hbar}{(m_{e^+}c^2)/u_0 + (m_\nu c^2)/u_0} \sim \frac{2\hbar}{(m_{e^+}c^2)/u_0} = \frac{2\hbar u_0}{m_{e^+}c^2} \sim R_0 = 1.2 \times 10^{-15} m$$

$$\frac{2\hbar}{m_{e^+}c} = \frac{2 \times (1.05 \times 10^{-34} J \cdot s)}{(9.1 \times 10^{-31} kg) \times (3 \times 10^8 m/s)} = 7.7 \times 10^{-13} m = 770 fm$$

$$R_0 \sim 1.2 \times 10^{-15} m = 1.2 fm, R_0 \text{ is a nucleon's radius}$$

Therefore,

$$\frac{u_0}{c} = \frac{1.2 \times 10^{-15} m}{7.7 \times 10^{-13} m} = 1.56 \times 10^{-3}, u_0 \sim c \times 1.56 \times 10^{-3} \quad (13)$$

The real event occurs about the uncertainty principle.

$$\Delta p \cdot \Delta d \geq \hbar \quad (14)$$

But, the event that the virtual positive electron and the virtual neutrino move in the velocity  $u_0$  isn't a real event.

$$\Delta p_{e^+} = m_{e^+}u_0, \Delta p_\nu = m_\nu u_0, \Delta d_{e^+} = \Delta d_\nu = \Delta d = r \sim \frac{2\hbar u_0}{m_{e^+}c^2}$$

$$\Delta p_{e^+} \cdot \Delta d_{e^+} + \Delta p_\nu \cdot \Delta d_\nu = (m_{e^+} + m_\nu)u_0 \cdot \frac{2\hbar u_0}{m_{e^+}c^2}, \Delta p_\nu = m_\nu u_0 \sim 0$$

$$= m_{e^+}u_0 \cdot \frac{2\hbar u_0}{m_{e^+}c^2} = 2\hbar \frac{u_0^2}{c^2} < 2\hbar \quad (15)$$

In this time, if the nucleus give the energy  $E = (m_{e^+} + m_\nu)c^2 + \frac{1}{2}(m_{e^+} + m_\nu)u_0^2 \approx m_{e^+}c^2$  a proton, to do the law of an energy conservation in the nucleus, the virtual positive electron, the virtual

neutrino and a proton do the free positive electron, the free neutrino of the velocity  $c - \Delta v$  and a neutron and therefore the  $\beta$ -decay that occur in the nucleus is

$$p \rightarrow n + e^+ + \nu \quad (16),$$

$$KE = \gamma_{e^+} m_{e^+} c^2 - m_{e^+} c^2 + \gamma_{\nu} m_{\nu} c^2, m_{\nu} c^2 \sim 0, \gamma_{e^+} = 1/\sqrt{1 - V_{e^+}^2/c^2} \quad (17)$$

### III. Conclusion

Therefore, the  $\beta$ -decay that occurs in the nucleus is concerned about the uncertainty principle. In specially, the  $\beta$ -decay of a nucleon (ex, a proton, a neutron) out of the nucleus doesn't understand by this theory and the  $\beta$ -decay understands by this theory only in the nucleus.

$$p + e^- \rightarrow n + \nu \quad (18)$$

In the time that Eq(18)'s phenomenon occur, if Eq(16)'s phenomenon occur

$$p + e^- \rightarrow n + e^- + e^+ + \nu \rightarrow n + \nu + \gamma \quad (19)$$

Therefore, Eq(18)'s phenomenon is understood by this theory.

The inverse  $\beta$ -decay,

$$p + \bar{\nu} \rightarrow n + e^+ \quad (20)$$

$$n + \nu \rightarrow p + e^- \quad (21)$$

In the time that Eq(20)'s and Eq(21)'s phenomenon occur, if Eq(16)'s and Eq(10)'s phenomenon occur,

$$p + \bar{\nu} \rightarrow n + e^+ + \nu + \bar{\nu} \rightarrow n + e^+ + \gamma \quad (22)$$

$$n + \nu \rightarrow p + e^- + \bar{\nu} + \nu \rightarrow p + e^- + \gamma \quad (23)$$

Therefore, Eq(20)'s and Eq(21)'s phenomenon, the inverse  $\beta$ -decay is understood by this theory.

Hence, the  $\beta$ -decay that occurs in the nucleus is understood by this theory.

Finally, the Yukawa's pion theory expands to be the Gell-Mann theory, this theory expands to be the Weinberg –Salam theory.

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