

# **Bounds upon Graviton mass, and making use of the difference between Graviton propagation speed and HFGW transit speed to observe post Newtonian corrections to Gravitational potential fields.**

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The author presents a post Newtonian approximation based upon an earlier argument / paper by Clifford Will as to Yukawa revisions of gravitational potentials in part initiated by gravitons with explicit mass dependence in their Compton wave length. Prior work with Clifford Will's idea was stymied by the application to binary stars and other such astro-physical objects with non useful frequencies topping off as up to 100 Hertz, thereby rendering Yukawa modifications of Gravity due to gravitons effectively an experimental curiosity which was not testable with any known physics equipment.

Key words: Graviton mass, Yukawa potential, Post Newtonian Approximation

## 1. Introduction

Post Newtonian approximations to General relativity have given physicists a view as to how and why inflationary dynamics can be measured via deviation from simple gravitational potentials. One of the simplest deviations from the Newtonian inverse power law gravitational potential being a Yukawa potential modification of gravitational potentials. So happens that the mass of a graviton would factor directly into the Yukawa exponential term modification of gravity. This present paper tries to indicate how a smart experimentalist could use a suitably configured gravitational wave detector as a way to obtain more realistic upper bounds as to the mass of a graviton and to use it as a template to investigate modifications of gravity along the lines of a Yukawa potential modification as given by Clifford Will.

Secondly, this paper will address an issue of great import to the development of experimental gravity. Namely, if an upper mass to the graviton mass is identified, can an accelerator physicist use the theoretical construction Eric Davis raised in his book in the section “producing Gravitons via Quantization of the coupled Maxwell- Einstein fields” as to how an experimental bound to the graviton mass as considered in this document can aid in refinement of graviton Synchrotron radiation . A brief review of Chen and Chen and Nobles application of the Gersenshetein effect will be made as to potentially improve their statistical estimates as to the range of graviton production.

## 2. Giving an upper bound to the mass of a graviton.

The easiest way to ascertain the mass of a graviton is to investigate if or not there is a slight difference in the speed of graviton ‘particle’ propagation and of HFGW in transit from a ‘source’ to the detector. Visser’s (1998) mass of a graviton paper presents a theory which passes the equivalence test, but which has problem with depending upon a non-dynamical background metric. I.e. gravitons are assumed by both him, and also Clifford Will’s write up of experimental G.R. to have mass

This document accepts that there is a small graviton mass, which the author has estimated to be on the order of  $10^{-60}$  kilograms. Small enough so the following approximation is valid. Here,  $v_g$  is the speed of graviton ‘propagation’,  $\lambda_g$  is the Compton wavelength of a graviton with  $\lambda_g = h/m_g c$ , and  $f \approx 10^{10}$  Hertz in line with L. Grischuck’s treatment of relic HFGW’s . In addition, the high value of relic HFGW’s leads to naturally fulfilling  $hf \gg m_g c^2$  so that

$$v_g/c \approx 1 - \frac{1}{2} \cdot (c/\lambda_g \cdot f)^2 \quad (1)$$

But equation (1) above is an approximation of a much more general result which may be rendered as

$$(v_g/c)^2 \equiv 1 - (m_g c^2/E)^2 \quad (2)$$

The terms  $m_g$  and E refers to the graviton rest mass and energy, respectively. Now physics researchers can ascertain what E is, with experimental data from a gravitational wave detector, and then the next question needs to be addressed, namely if D is the distance between a detector, and the source of a HFGW/ Graviton emitter source

$$1 - v_g/c = 5 \times 10^{-17} \cdot \left[ \frac{200Mpc}{D} \right] \cdot \left( \frac{\Delta t}{1sec} \right) \quad (3)$$

The above formula depends upon,  $\Delta t = \Delta t_a - (1+Z) \cdot \Delta t_e$  with where  $\Delta t_a$  and  $\Delta t_e$  are the differences in arrival time and emission time of the two signals ( HFGW and Graviton propagation ), respectively, and Z is the redshift of the source. Z is meant to be the red shift.

Specifically, the situation for HFGW is that for early universe conditions, that  $Z \geq 1100$ , in fact for very early universe conditions in the first few milliseconds after the big bang, that  $Z \sim 10^{25}$ . An enormous number.

The first question which needs to be asked is, if or not the Visser non-dynamical background metric correct, for early universe conditions so as to avoid the problem of the limit of small graviton mass does not coincide with pure GR, and the predicted perihelion advance, for example, violates experiment . A way forward would be to configure data sets so in the case of early universe conditions that one is examining appropriate  $Z \gg 1100$  but with extremely small  $\Delta t_e$  times, which would reflect upon generation of HFGW before the electro weak transition, and after the INITIAL onset of inflation.

I.e. a Gravitational wave detector system should be employed as to pin point experimental conditions so to high accuracy , the following is an adequate presentation of the difference in times,  $\Delta t$  . I.e.

$$\Delta t = \Delta t_a - (1+Z) \cdot \Delta t_e \rightarrow \Delta t_a - \varepsilon^+ \approx \Delta t_a \quad (4)$$

The closer the emission times for production of the HFGW and Gravitons are to the time of the initial nucleation of vacuum energy of the big bang, the closer we can be to experimentally using equation (4) above as to give experimental criteria for stating to very high accuracy the following.

$$1 - v_g/c \cong 5 \times 10^{-17} \cdot \left[ \frac{200Mpc}{D} \right] \cdot \left( \frac{\Delta t_a}{1sec} \right) \quad (5)$$

More exactly this will lead to the following relationship which will be used to ascertain a value for the mass of a graviton. By necessity, this will push the speed of graviton propagation very close to the speed of light. In this, we are assuming an enormous value for D

$$v_g/c \cong 1 - 5 \times 10^{-17} \cdot \left[ \frac{200Mpc}{D} \right] \cdot \left( \frac{\Delta t_a}{1sec} \right) \quad (6)$$

This equation (6) relationship should be placed into  $\lambda_g = h/m_g c$ , with a way to relate this above value of  $(v_g/c)^2 \cong 1 - (m_g c^2/E)^2$ , with an estimated value of E as an average value from field theory calculations, as well as to make the following argument rigorous, namely

$$\left[ 1 - 5 \times 10^{-17} \cdot \frac{200Mpc}{D} \cdot \frac{\Delta t_a}{1sec} \right]^2 \cong 1 - \left( \frac{m_g c^2}{E} \right)^2 \quad (7)$$

A suitable numerical treatment of this above equation, with data sets could lead to a range of bounds for  $m_g$ , as a refinement of the result given by Clifford Will for graviton Compton wavelength bounded behavior for a lower bound to the graviton mass, assuming that  $h$  is the Planck's constant.

$$\begin{aligned} \lambda_g &\cong \frac{h}{m_g c} > 3 \times 10^{12} km \cdot \left( \frac{D}{200Mpc} \cdot \frac{100Hz}{f} \right)^{1/2} \cdot \left( \frac{1}{f \Delta t_a} \right)^{1/2} \\ &\cong 3 \times 10^{12} km \cdot \left( \frac{D}{200Mpc} \cdot \frac{100Hz}{f} \right)^{1/2} \cdot \left( \frac{1}{f \Delta t_a} \right)^{1/2} \end{aligned} \quad (8)$$

The above equation (8) gives an upper bound to the mass  $m_g$  as given by

$$m_g < \left( \frac{c}{h} \right) / 3 \times 10^{12} km \cdot \left( \frac{D}{200Mpc} \cdot \frac{100Hz}{f} \right)^{1/2} \cdot \left( \frac{1}{f \cdot \Delta t_a} \right)^{1/2} \quad (9)$$

Needless to say that an estimation of the bound for the graviton mass  $m_g$ , and the resulting Compton wavelength  $\lambda_g$  would be important to get values of the following formula, namely

$$V(r)_{gravity} \cong \frac{MG}{r} \exp(r/\lambda_g) \quad (10)$$

Clifford Will gave for values of frequency  $f \cong 100$  Hertz enormous values for the Compton wave length, i.e. values like  $\lambda_g > 6 \times 10^{19} km$ . Such enormous values for the Compton wave length make experimental tests of equation (10) practically infeasible. Values of  $\lambda_g \approx 10^{-5}$  centimeters or less for very high HFGW data makes investigation of equation (10) above far more tractable.

### 3. Application to Gravitational Synchrotron radiation, in accelerator physics

Eric Davis, quoting Pisen Chen's article written in 1994 estimates that a typical storage ring for an accelerator will be able to give approximately  $10^{-6} - 10^3$  gravitons per second. Quoting Pisen Chen's 1994 article, the following for graviton emission values for a circular accelerator system, with  $m$  the mass of a graviton, and  $M_p$  being Planck mass.  $N$  as mentioned below is the number of 'particles' in a ring for an accelerator system, and  $n_b$  is an accelerator physics parameter for bunches of particles which for the LHC is set by Pisen Chen as of the value 2800, and  $N$  for the LHC is about  $10^{11}$ . And, for the LHC Pisen Chen sets  $\gamma$  as  $.88 \times 10^2$ , with  $\rho[m] \approx 4300$ . Here,  $m \sim m_{graviton}$  acts as a mass charge.

$$N_{GSR} \sim 5.6 \cdot n_b^2 \cdot N^2 \cdot \frac{m^2}{M_p^2} \cdot \frac{c \cdot \gamma^4}{\rho} \quad (11)$$

The immediate consequence of the prior discussion would be to obtain a more realistic set of bounds for the graviton mass, which could considerably refine the estimate of  $10^{11}$  gravitons produced per year at the LHC, with realistically  $365 \times 86400 \text{ seconds} = 31536000 \text{ seconds}$  in a year, leading to  $3.171 \times 10^3$  gravitons produced per second. Refining an actual permitted value of bounds for the accepted graviton mass,  $m$ , as given above, while keeping  $M_p \sim 1.2209 \times 10^{19} \text{ GeV}/c^2$  would allow for a more precise set of gravitons per second which would significantly enhance the chance of actual detection, since right now for the LHC there is too much general uncertainty as to the likelihood of where to place a detector for actually capturing / detecting a graviton.

### 4. Conclusion, falsifiable tests for the Graviton are closer than the physics community thinks

The physics community now has an opportunity to experimentally infer the existence of gravitons as a knowable and verifiable experimental datum with the onset of the LHC as an operating system. Even if the LHC is not used, Pisen Chens parameterization of inputs from his table right after his equation (8) as inputs into equation (11) above will permit the physics community to make progress as to detection of Gravitons for , say the Brookhaven laboratory site circular ring accelerator system. Tony Rothman's predictions as to needing a detector the size of Jupiter to obtain a single experimentally falsifiable set of procedures is defensible only if the wave- particle duality induces so much uncertainty as to the mass of the purported graviton, that worst case model building and extraordinarily robust parameters for a Rothman style graviton detector have to be put in place.

A suitably configured detector can help with bracketing a range of masses for the graviton, as a physical entity subject to measurements. Such an effort requires obtaining rigorous verification of the approximation used to the effect that  $\Delta t = \Delta t_a - (1 + Z) \cdot \Delta t_e \rightarrow \Delta t_a - \varepsilon^+ \approx \Delta t_a$  is a defensible approximation. Furthermore, obtaining realistic inputs for distance  $D$  for inputs into equation (9) above is essential

The expected pay offs of making such an investment would be to determine the range of validity of equation (10) , i.e. to what degree is gravitation as a force amendable to post Newtonian approximations.

The author asserts that equation (10) can only be realistically be tested and vetted for sub atomic systems, and that with the massive Compton wavelength specified by Clifford Will cannot be done with low frequency gravitational waves.

Furthermore, a realistic bounding of the graviton mass would permit a far more precise calibration of equation (11) as given by Pisen Chen in his 1994 article.

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## **Bibliography**

Pisen Chen, “Resonant Photon-Graviton Conversion in E M fields: From Earth to Heaven”, SLAC Pub 6666, September (1994)

Eric Davis, “Producing Gravitons via Quantization of the Coupled Maxwell Fields,” in *Frontiers of Propulsion Science, Progress in Astronautics and Aeronautics Series*, Vol. 227, eds. M. G. Millis and E. W. Davis, AIAA Press, Reston, VA, (2009)

Matt Visser,” Mass of the Graviton “, arXiv ,gr-qc/ 9705051 v 2 Feb 26, 1998

Clifford Will, “Bounding the Mass of the Graviton using Gravitational-Wave observations of inspiralling compact Binaries”, arXiv gr-qc/ 9709011 v1 Sept 4, 1997

Clifford Will, “The confrontation between General Relativity and Experiment”, *Living Rev. of Relativity*,9, (2006),3, <http://www.livingreviews.org/lrr-2006-3>