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\_imitations of I-Diversity

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# Data Anonymization Techniques

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The Summer School in Software Engineering and Verification (SSSEV 2011)

2011-07-26

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## 2 Limitations of I-Diversity

- Skewness Attack
- Similarity Attack

- The t-closeness Privacy Measure
- The t-closeness Principle
- Computing D[P, Q]

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# 1 Introduction

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- Organizations typically need to publish microdata e.g., census data or election data
- Data publishing gives useful information to researchers and analyzers
- At the same time, it extends a privacy risk to individuals whose data is being published
- We need strong privacy notions that enable us to confine the disclosure risk while simultaneously maximize the benefits

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| Skewness Attack |                            |             |         |

#### Skewness Attack

- When the overall distribution is skewed, satisfying l-diversity does not prevent attribute disclosure
- Original data → one sensitive attribute → test result for a virus (positive or negative)
- Population of 10 000 records  $\rightsquigarrow$  99% negative, 1% positive
- In one EC  $\rightsquigarrow$  positive records = negative records  $\rightsquigarrow$  2-diversity
- Privacy risk → anyone in this EC has 50% possibility of being positive

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| Similarity Attack |                            |                      |         |

### Similarity Attack

• When the sensitive attribute values in an EC are distinct but semantically similar, an adversary can learn important information

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| Circulture Arrest |                            |             |         |

|   | ZIP Code | Age | Salary | Disease        |
|---|----------|-----|--------|----------------|
| 1 | 47677    | 29  | 3K     | gastric ulcer  |
| 2 | 47602    | 22  | 4K     | gastritis      |
| 3 | 47678    | 27  | 5K     | stomach cancer |
| 4 | 47905    | 43  | 6K     | gastritis      |
| 5 | 47909    | 52  | 11K    | flu            |
| 6 | 47906    | 47  | 8K     | bronchitis     |
| 7 | 47605    | 30  | 7K     | bronchitis     |
| 8 | 47673    | 36  | 9K     | pneumonia      |
| 9 | 47607    | 32  | 10K    | stomach cancer |

# Table 3. Original Salary/Disease Table

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|   | ZIP Code | Age       | Salary | Disease        |
|---|----------|-----------|--------|----------------|
| 1 | 476**    | 2*        | 3K     | gastric ulcer  |
| 2 | 476**    | 2*        | 4K     | gastritis      |
| 3 | 476**    | 2*        | 5K     | stomach cancer |
| 4 | 4790*    | $\geq 40$ | 6K     | gastritis      |
| 5 | 4790*    | $\geq 40$ | 11K    | flu            |
| 6 | 4790*    | $\geq 40$ | 8K     | bronchitis     |
| 7 | 476**    | 3*        | 7K     | bronchitis     |
| 8 | 476**    | 3*        | 9K     | pneumonia      |
| 9 | 476**    | 3*        | 10K    | stomach cancer |

## Table 4. A 3-diverse version of Table 3

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| The t-closeness Privacy Measure |                            |                      |         |

#### The t-closeness Privacy Measure

- Privacy is measured by the information gain of an observer
- Before seeing the released table, the observer has a prior belief about the sensitive attribute value
- After seeing the released table, the observer has a posterior belief about the sensitive attribute value
- Information gain = posterior belief prior belief
- Prior belief is influenced by Q = the distribution of the sensitive attribute value in the whole table
- Posterior belief is influenced by *P* = the distribution of the sensitive attribute value in the EC
- Information gain = D[P, Q]

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| The t-closeness Principle |                                    |                      |         |

#### The t-closeness Principle

- An EC has t-closeness if  $D[P, Q] \leq t$
- A table has t-closeness if all ECs have t-closeness
- ↓ D[P, Q] ~→ ↓ the information gained by the observer ~→ ↓ privacy risk
- ↑ D[P, Q] ~→ ↑ the information gained by the observer ~→ ↑ benefit of published data

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| Computing $D[P, Q]$ |                            |                      |         |

#### The Earth Mover Distance (EMD)

• The minimal amount of work needed to transform one distribution to another by moving the distribution mass

• 
$$D[P, Q] = WORK(P, Q, F) = \sum_{i=1}^{m} \sum_{j=1}^{m} d_{ij}f_{ij}$$

• 
$$P = (p_1, p_2, ..., p_m), Q = (q_1, q_2, ..., q_m)$$

- *d<sub>ij</sub>* the ground distance between element *i* of *P* and element *j* of *Q*
- $F = [f_{ij}]$  is the flow of mass from element *i* of *P* to element *j* of *Q* that minimizes the overall work

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| Computing $D[P, Q]$ |                            |                      |         |

|   | ZIP Code | Age       | Salary | Disease        |
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| 1 | 476**    | 2*        | 3K     | gastric ulcer  |
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## Table 4. A 3-diverse version of Table 3

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| Computing $D[P, Q]$ |                            |                      |         |

# $D[P_1, Q]$

- $Q = \{3k, 4k, 5k, 6k, 7k, 8k, 9k, 10k, 11k\}$
- $P_1 = \{3k, 4k, 5k\}$
- If we have an ordered list  $\{v_1, v_2 ... v_m\}$  then the ground distance is  $\frac{|i-j|}{m-1} = \frac{|i-j|}{8}$

• If we flow 
$$\frac{1}{9}$$
 mass from  $P_1$  to  $Q$  as follow  
 $(5k \rightarrow 11k), (5k \rightarrow 10k), (5k \rightarrow 9k), (4k \rightarrow 8k), (4k \rightarrow 7k), (4k \rightarrow 6k), (3k \rightarrow 5k), (3k \rightarrow 4k)$  then  
 $EMD = 1/9 \times (6+5+4+4+3+2+2+1)/8 = 0.375$ 

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- A number of privacy notions for protecting data publishing have been proposed
- Nevertheless, data anonymization is still an active research direction
- The trade-off between utility and privacy should be taken into account
- The search is ongoing for measures that scale and maintain probabilistic nature

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# Thank you!