

ON IONIZATION POTENTIALS of ATOMS And IONS

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Abstract

In the article the ionization potentials of atoms are considered, the similar electronic structure of ions with identical number of electrons is shown and the formulas of calculation of potentials of ionization of any multicharge ions are given.

In the tables of experimental values of potentials of ionization a lot of information on a constitution of atoms is enciphered, but, while, this information will not be utilized rather effectively because of absence of constitutive ideas. Knowledge, which one we have obtained from the previous chapters could clear up this problem (qualitatively, these tables are already clear and in them there is no "by abnormal" numerals), but the business strongly is complicated by that the binding energy of a given electron with a nucleus includes not only electrostatic interaction, but also interaction of a given electron with all other electrons and simultaneously effective magnetic interaction. Besides at removal of an electron there is a reorganization of all electronic structure of atom. At the same structure of electrons, with increase of nuclear charge the eccentricity of orbits of electrons, as we have found out on an example of helium, drops at first sharply, then slowly. It gives in strengthening connection of an electron with a nucleus at the expense more near-circular orbits on the one hand, and to abatement of this connection at the expense of the greater interaction with other electrons, on the other hand. We have an analytical expression only for one of three simultaneously of varying parameters - binding energy of a given electron with a nucleus, which one of the theory of hydrogen-like atoms can be noted so:

$$Z = \sqrt{\frac{E_Z}{E_H}} \quad (1),$$

where: E_Z - potential of ionization of a hydrogen-like atom with nuclear charge Z , and E_H - potential of an atomic ionization of hydrogen. Apparently, that here we have that case, when without good mathematical idea to decide a problem about potentials of ionization of atoms it is impossible. And the idea is encompass following (by the way, it has blanket character and can be utilized for a wide range of similar problems). Let's enter into the formula (1) concepts of an effective charge:

$$Z_{eff} = AZ \quad (2),$$

where A reflects combined effect of interaction of electrons among themselves and magnetic interaction. Let's substitute (2) in (1) and is conversed to a view:

$$\sqrt{E_{Mn}} = AZ \sqrt{E_{M1}} \quad (3),$$

where: E_{Mn} - n -th potential of ionization M - similar of atom, E_{M1} - first potential of ionization of M -similar atom, Z - charge of an ion, which one will be formed at removal of a given electron, A - parameter depending on a constitution of electronic shells of M -similar atom.

The formula (3) will be valid, at $A = \text{const}$, only at $Z \rightarrow \infty$, since the shape of orbits of electrons depends from Z , especially at small Z . More often in the tables give experimental values of the first ten potentials of ionization and even it completely insufficiently to compute a precise parameter value A in the formula (3). To decide this problem, we shall describe experimental values of potentials of ionization M -similar of atoms by any empirical expression, but with indispensable by a requirement, that it at $Z \rightarrow \infty$ gave the formula (3). Then it is not required to know a major series of potentials of ionization and parameter A it is possible to compute with any precision for anyone M -similar of atom.

For example, for the first three periods of the table of the Mendeleev I tender following semiempirical dependence (deduction it is not given, since does not introduce interest, parameter B in this dependence no object):

$$\sqrt{E_{Mn}} = \sqrt{E_{M1}} \left\{ 1 + (Z-1) \left[A + \frac{B}{\sqrt{Z}} \left(1 + \frac{1}{\sqrt{Z}} \right) \right] \right\} \quad (4).$$

The expression (4) at $Z \rightarrow \infty$ gives (3), that is an indispensable requirement.

For boron-like of atoms (as an example), in (4): $A=0.63406$, $B=0.06633$. The matching of experimental values of ionization energy with calculation on (4) is given in table 1.

Table 1.

Boron-like atom	C ⁺¹	N ⁺²	O ⁺³	F ⁺⁴	Ne ⁺⁵
Z	2	3	4	5	6
E exp. (eV)	24.376	47.426	77.39	114.21	157.9
E on (57), eV	24.376	47.350	77.25	114.06	157.8
Boron-like atom	Na ⁺⁶	Mg ⁺⁷	Al ⁺⁸	Si ⁺⁹	
Z	7	8	9	10	
E exp. (eV)	208.44	256.84	330.1	401.3	
E on (57), eV	208.37	256.83	330.1	401.3	

As the error does not exceed 0.2 %, we shall consider expression (4) satisfactory for practical use.

The parameter values A for elements of the first three periods are given in table 2.

Table 2.

Element	H	He	Li	Be	B
A	1.00000	0.74271	0.78910	0.60122	0.63406
Element	C	N	O	F	Ne
A	0.54574	0.48029	0.49382	0.43789	0.39704
Element	Na	Mg	Al	Si	P
A	0.54411	0.45078	0.50804	0.44081	0.39181
Element	S	Cl	Ar		
A	0.39043	0.35119	0.31984		

For all remaining elements the expression (4) does not allow any more enough precisely to compute parameter A because completely of other constitution of shells (see tab. 15.1 [1]) and other empirical expression is required, which one us now to interest will not be, as the principle is clear.

Because of that parameter A is liberated from influence of interaction of an electron with a nucleus and its value does not depend on a constitution M -similar of atom (including from reorganization of electronic structure at removal of a given electron), apparently, that the electrons forms the same shell of atom and which are taking place from its nucleus on same distance should have and identical ionization energy E_0 :

$$\Delta E_{M1} = \frac{E_0}{A^2} \quad (5).$$

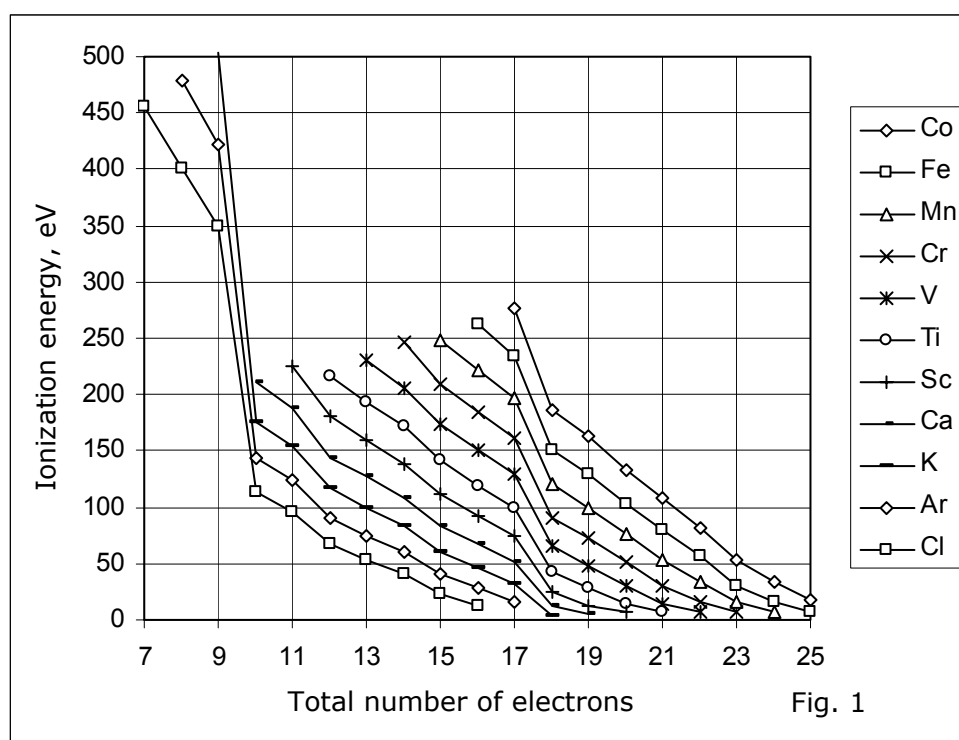
It is clearly, that in the first short period $E_0=13.595$ eV, i.e. is peer to ionization energy of atom of hydrogen. Really, for helium: $E_0 = E_{He1} \cdot A^2 = 24.58 \cdot 0.74271^2 = 13.559$ eV, therefore value $24.58 - 13.559 = 11.021$ eV is stipulated, in basic, magnetic interaction of two electrons in atom of helium (if not to take into consideration gravidynamic interaction). For elements of the second period $E_0=3.3535$ eV, and third period $E_0=1.5771$ eV. Substituting these values in (16.5), we shall discover the first potentials of ionization of these elements; they are shown in table 3.

Table 3.

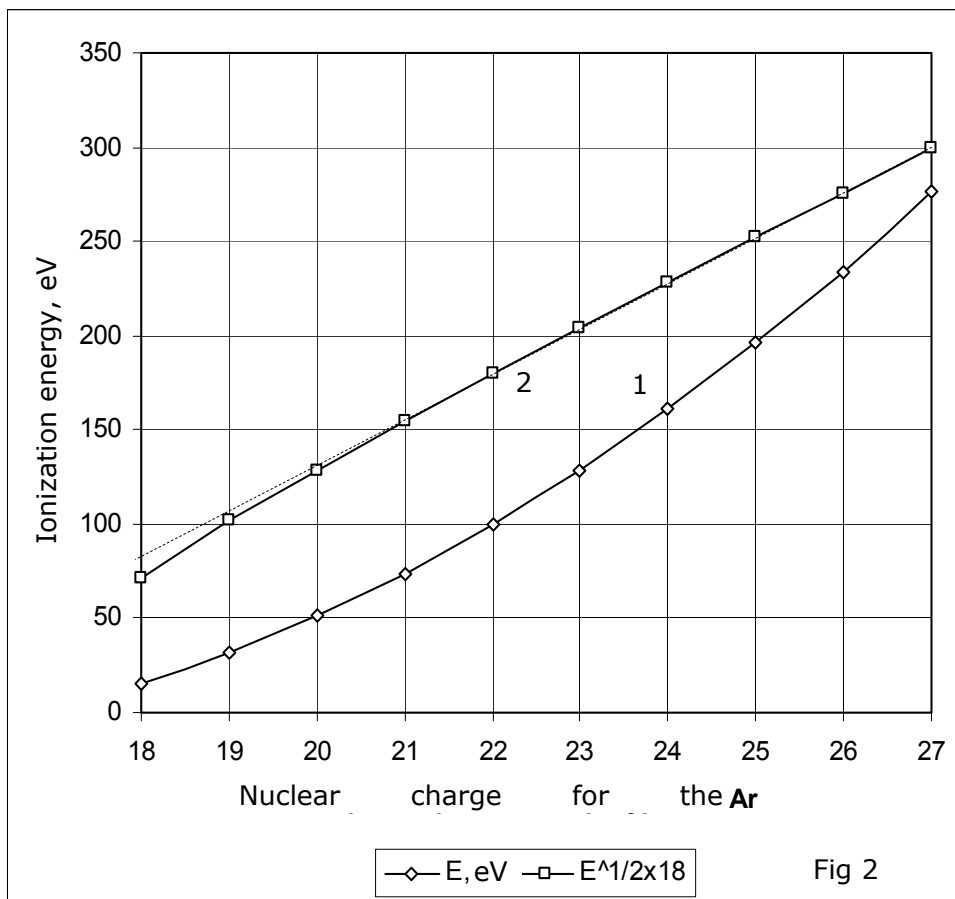
Element	Li	Be	B	C	N
E exp. (eV)	5.39	9.32	8.296	11.264	14.54
E on (16.5), (eV)	5.39	9.28	8.341	11.259	14.54
Element	O	F	Ne	Na	Mg
E exp. (eV)	13.614	17.418	21.559	5.138	7.644
E on (16.5), (eV)	13.752	17.493	21.273	5.327	7.761
Element	Al	Si	P	S	Cl
E exp. (eV)	5.984	8.149	10.55	10.357	13.01
E on (16.5), (eV)	6.110	8.116	10.27	10.346	12.79
Element	Ar				
E exp. (eV)	15.755				
E on (16.5), (eV)	15.416				

Structural parameter A completely correlates with that electronic constitution of atoms, which one we have established earlier. As well as it was necessary to expect, the constitution of atom completely determines energy of connections of electrons in its composition. Shell arrangement of electrons around of a nucleus was confirmed. Is shown the essential influence of magnetic interaction to electron-binding energy with atom (in which one is included and gravidynamic interaction, but it in this case is insignificant). The experimental potentials of ionization completely correspond to a constitution of atoms enunciated in this book.

Ion structure



On a figure 1 the relation of an ionization energy of ions of different elements to total of electrons, inhering to an ion is shown. At 10 electrons the electronic configuration of ions corresponds to a neon, and at 18 electrons - argon. Therefore at the subsequent ionization of such ions the sharp increase of an ionization energy is watched, since it is necessary to shatter filled electronic shell of inert gases. The similarity of curves of a fig. 1 demonstrates a similarity of electronic structure of the applicable ions. Here only it is necessary to add, that though the electronic structures of ions with the same total number of electrons are similar, but electrons are arranged much closer to a nucleus for multicharge ions, that is quite natural.



In a fig. 2 for the electronic configuration of ions applicable to argon, the ionization energies E are adduced depending on nuclear charge of an ion (curve 1) and same values which have been counted up on the formula $18\sqrt{E}$ (curve 2). In matching from a dashed straight line it is visible, that with increase of nuclear charge at the same configuration of electrons the ionization energy is proportional to a square of nuclear charge. The more charge of an ion, the more precisely is executed quadratic relation, i.e. the interplay of electrons among themselves in this case can be fling aside.

To receive a spectral line in optical range, the loss of exuberant energy of an electron, order 5-10 eV is necessary. At the same time, the electron-binding energy in an ion Fe^{+13} beaming a green line «coronium» in a spectrum of the Sun makes approximately 450 eV. This ion has 13 electrons and their configuration is look-alike to the electronic configuration of aluminum. The eccentricity of orbit of an exited electron is peer to ratio of exuberant energy to bond energy. This eccentricity is approximately peer a considered case 0.015. Orbits with such small eccentricity are near to a ground state (circular orbit) therefore metastable - electrons the much greater time for transition in a ground state is necessary. In similar cases we can watch «forbidden» (in the terms of official physics) spectral lines, if the ion is in very rarefied environment and can not lose exuberant energy at impacts with other particles.

Calculation of ionization potentials

Who though once saw spectra of composite atoms, that can sympathize to the astronomers, which one are compelled to be disassembled in thousand spectral lines not only given element, but also in their mixture with other elements, as it is substantially watched in space objects. In outcome before eyes of the explorer there is such bar code in which one practically it is impossible to be disassembled. Let's presume, that we have a set of spectra of all suspected elements existing on investigated object. Then the modern computer equipment can section a spectrum of a complex mixture into spectra of separate elements. But here there is one more severe difficulty: we do not know spectra of multicharge ions. For example, in a corona of the Sun the bright green line of ions Fe^{+13} (it

is watched assigned to a new element «coronium»). And what all spectrum of this ion and similar to it? It cannot be played back in laboratory conditions, and to make idealized calculation, it is necessary, at least to know potentials of ionization of transition $Fe^{+12} \rightarrow Fe^{+13} \rightarrow Fe^{+14}$, which one also cannot be defined experimentally. The given chapter will help to leave from this desperate situation and to calculate potentials of ionization of any multicharge ions with a high accuracy.

New physics introduces formation of atomic spectra thus. All electrons of atom are in a ground state and nothing beam. For each electron this condition is strict individually. If atom properly to jolt, the obtained energy is reallocated between all electrons and they will take everyone the personal exited state. At returning in a ground state each electron will beam some serials of spectral lines, number of lines in each serial, basically, is indefinite. Only limit of each serial indicates, that the electron again has taken a ground state. At increase of nuclear charge density of power condition near to a ground state is augmented, therefore spacing interval between spectral lines changes. But as though electron-binding energy with a nucleus was not great, near to a ground state it will beam photons optical and infra-red diapason. On the basis of the set up mechanism of formation of atomic spectra there is a understandable occurrence of spectra, inclusive many thousand of lines.

In this article the empirical-formula dependences for calculation of potentials of ionization are adduced, but they cannot be recognized satisfactory. In the figure 1 is shown, that of ions structure with identical number of electrons is look-alike, and on a figure 2 is shown, what the ionization energy in a degree 1/2 begin with $Z+5$ and is higher practically linearly depends on nuclear charge (at the same number of electrons). At a charge $< Z+5$ interplays of electrons among themselves (magnetic and electrostatic) are reduces a potential of ionization, as far as the potential of ionization in each particular case decreases it is impossible to count up, as it is impossible to decide a many-body problem. At rather large nuclear charge the interplay of electrons among themselves practically does not influence interplay with a nucleus, therefore function $E_{ion}^{(1/2)} \sim Z$ becomes linear.

The author, using the data «the reference Book of the chemist», т.1, 1963, page 325-327 was not too lazy to compound computational equations for all of elements, the data on an ionization energy (eV) which one are accessible. The outcomes are shown in table 4. In the first column - character of an element, in the second column - nuclear charge of this element, in the third column - formula for calculation of an ionization energy of any ions, which one contain quantity of electrons, equal number of the formula (and only this quantity!), in the subsequent columns matching experimental value of an ionization energy of ions with calculation under the indicated formula is resulted. For example, we shall count up an ionization energy of an ion Fe^{+12} . The nuclear charge iron 26, in the indicated ion is contained $26-12=14$ electrons. Therefore this ion attributes to Si-similar atoms (by analogy with hydrogen-like atoms inclusive one electron). Therefore calculated formula will be N_{14} : $E_{14}=(1.302Z-14.783)^2$. We in this formula should substitute $Z=26$. In outcome we shall receive a required potential of ionization 363.63 eV. For an ion Fe^{+14} the similar calculations under the formula 12 will give 460.92 eV.

Table 4.

Symbol of element	Nuclear charge Z	Calculated formula	Nuclear charge	Z+4	Z+5	Z+6	Z+7	Z+8	Z+9
H	1	$E_1=(3.688Z)^2$	E(exp)	340.03	489.65	666.47	870.49	1101.71	1360.13
			E(calc)	340.03	489.65	666.47	870.49	1101.71	1360.13
He	2	$E_2=(3.701Z-2.441)^2$	E(exp)	391.99	551.93	739.11	953.8	1195.4	1464.7
			E(calc)	390.65	550.65	738.05	952.83	1195	1454.5
Li	3	$E_3=(1.852Z-3.062)^2$	E(exp)	97.86	138.08	185.14	239.1	299.7	367.2
			E(calc)	98.05	138.16	185.12	238.95	299.64	367.18
Be	4	$E_4=(1.857Z-4.182)^2$	E(exp)	113.87	157.12	207.2	264.2	328	398.6
			E(calc)	113.93	157.03	207.01	263.9	327.68	398.36
B	5	$E_5=(1.869Z-6.134)^2$	E(exp)	114.21	157.9	208.44	265.84	330.1	401.3
			E(calc)	114.21	157.65	208.08	265.49	329.89	401.28
C	6	$E_6=(1.881Z-7.59)^2$	E(exp)	126.4	172.4	225.3	285.13	351.8	425.4

			E(calc)	125.89	171.64	224.46	284.36	351.34	425.39
N	7	$E_7=(1.881Z-8.918)^2$	E(exp)	138.6	186.8	241.8	304	372.8	448.5
			E(calc)	138.6	186.43	241.34	303.32	372.37	448.51
O	8	$E_8=(1.891Z-10.806)^2$	E(exp)	141.23	190.42	246.41	309.3	378.9	455.3
			E(calc)	141.28	189.8	245.49	308.32	378.3	455.44
F	9	$E_9=(1.905Z-12.404)^2$	E(exp)	153.8	205.1	263.3	328.4	400.3	479
			E(calc)	152.79	203.52	261.5	326.74	399.24	479
Ne	10	$E_{10}=(1.915Z-13.94)^2$	E(exp)	166.73	220.41	280.99	348.5	422.6	503.8
			E(calc)	165.64	218.6	278.89	346.52	421.48	503.78
Na	11	$E_{11}=(1.303Z-11.524)^2$	E(exp)	65.01	88	114.2	143.4	176	211.3
			E(calc)	64.34	86.94	112.93	142.32	175.11	211.29
Mg	12	$E_{12}=(1.296Z-12.227)^2$	E(exp)	72.5	96.6	123.9	154.3	187.9	224.9
			E(calc)	72.4	96.14	123.23	153.69	187.5	224.67
Al	13	$E_{13}=(1.293Z-13.719)^2$	E(exp)	67.8	91.3	117.9	143.3	180.2	216.9
			E(calc)	68.26	91.3	117.68	147.4	180.47	216.88
Si	14	$E_{14}=(1.302Z-14.783)^2$	E(exp)	75	99.4	127.9	159.2	193.1	230.2
			E(calc)	74.87	99.1	126.72	157.73	192.13	229.92
P	15	$E_{15}=(1.319Z-15.977)^2$	E(exp)	82.6	109	139	172	206	246
			E(calc)	82.52	108.22	137.4	170.07	206.21	245.83
S	16	$E_{16}=(1.311Z-16.995)^2$	E(exp)	84	111	141	174	209	249
			E(calc)	85.1	111	140.35	173.13	209.35	249
Cl	17	$E_{17}=(1.321Z-18.16)^2$	E(exp)	91.8	119	151	185	221	262
			E(calc)	91.8	118.85	149.4	183.44	220.97	261.99
Ar	18	$E_{18}=(1.33Z-19.27)^2$	E(exp)	99.8	128.9	161.1	196.4	234.4	276.9
			E(calc)	99.8	128.14	160.02	195.44	234.4	276.89
K	19	$E_{19}=(1.362Z-23.176)^2$	E(exp)	65.2	90.6	120	151	185.9	224
			E(calc)	66.42	90.48	118.24	149.72	184.91	223.8
Ca	20	$E_{20}=(1.381Z-24.525)^2$	E(exp)	73	100	130	163	200	241
			E(calc)	74.29	100	129.53	162.87	200.02	240.99
Sc	21	$E_{21}=(1.4Z-26.272)^2$	E(exp)	76	103	133	168	206	247
			E(cal)	76.18	102.58	132.89	167.13	205.29	247.37
Ti	22	$E_{22}=(1.515Z-30.497)^2$	E(exp)	79	109	143	182	224	271
			E(calc)	79.08	108.33	142.16	180.58	223.59	271.19
V	23	$E_{23}=(1.542Z-32.601)^2$	E(exp)	82	113	148	188	231	280
			E(calc)	81.59	111.83	146.82	186.57	231.07	280.33
Cr	24	$E_{24}=(1.528Z-33.879)^2$	E(exp)	79	109	144	183	226	274
			E(calc)	79.3	108.85	143.06	181.95	225.51	273.74
Mn	25	$E_{25}=(1.529Z-35.193)^2$	E(exp)	83	114	149	189	234	282
			E(calc)	83.69	114	148.99	188.65	232.99	282
Fe	26	$E_{26}=(1.549Z-37.156)^2$	E(exp)	86	118	155	196	241	291
			E(calc)	86.75	118	154.06	194.91	240.56	291
Co	27	$E_{27}=(1.557Z-38.75)^2$	E(exp)	90	123	160	202	248	300
			E(calc)	90.57	122.63	159.54	201.3	247.9	299.36
Ni	28	$E_{28}=(1.338Z-32.854)^2$	E(exp)	93.4	127.5	155	193	234	277
			E(calc)	99.24	127.69	159.72	195.33	234.52	277.29
Cu	29	$E_{29}=(1.061Z-27)^2$	E(exp)	62.9	82.1	103	126	150	177
			E(calc)	64.21	82.34	102.72	125.35	150.23	177.37
Zn	30	$E_{30}=(1.102Z-29.148)^2$	E(exp)	68.3	88.6	111	136	162	191
			E(calc)	69.22	88.77	110.75	135.16	162	191.27
Ga	31	$E_{31}=(1.073Z-29.767)^2$	E(exp)	59.7	78.5	99.2	122.3	146.2	173

			E(calc)	60.65	78.52	98.68	121.15	145.93	173
Ge	32	$E_{32}=(1.119Z-32.233)^2$	E(exp)	64.7	84.4	106	129	154	186
			E(calc)	64.82	84.09	105.86	130.14	156.93	186.21
As	33	$E_{33}=(1.053Z-30.298)^2$	E(exp)	71	90.8	116	139	165	194
			E(calc)	75.05	94.4	115.97	139.76	165.77	193.99
Se	34	$E_{34}=(1.08Z-32.476)^2$	E(exp)	71.6	93	116	141	167	195
			E(calc)	73.34	93.01	115	139.33	166	195
Br	35	$E_{35}=(1.19Z-37.663)$	E(exp)	77	99.4	124	153	183	216
			E(calc)	76.51	98.74	123.81	151.71	182.44	216
Kr	36	$E_{36}=(1.123Z-35.535)^2$	E(exp)	82.3	110.4	131	161	192	225
			E(calc)	88.08	110.42	135.28	162.66	192.57	225
Rb	37	$E_{37}=(1.252Z-44.25)^2$	E(exp)	50	67	94	119	147	178
			E(calc)	50.15	69.45	91.89	117.46	146.17	178
Sr	38	$E_{38}=(1.239Z-44.558)^2$	E(exp)	61.2	76	100	126	155	187
			E(calc)	55.95	76.02	99.16	125.37	154.65	187.01
Y	39	$E_{39}=(1.238Z-45.46)^2$	E(exp)	59	81	105	132	162	195
			E(calc)	60.43	81.22	105.06	131.97	161.95	194.99
Zr	40	$E_{40}=(1.263Z-47.604)^2$	E(exp)	63	85	111	139	170	204
			E(calc)	63.49	85.21	110.12	138.23	169.52	204
Nb	41	$E_{41}=(1.277Z-49.256)^2$	E(exp)	67	90	116	146	178	213
			E(calc)	67.39	89.98	115.84	144.96	177.34	212.98
Mo	42	$E_{42}=(1.28Z-50.754)^2$	E(exp)	66	89	115	144	176	211
			E(calc)	66.03	88.47	114.19	143.18	175.46	211
Tc	43	$E_{43}=(1.293Z-52.404)^2$	E(exp)	70	94	121	151	184	220
			E(calc)	70	93.32	119.97	149.96	183.3	219.99
Ru	44	$E_{44}=(1.308Z-54.191)^2$	E(exp)	73	98	126	157	192	229
			E(calc)	73.84	98.03	125.64	156.67	191.13	229.01
Rh	45	$E_{45}=(1.335Z-56.663)^2$	E(exp)	77	103	132	164	200	238
			E(calc)	76.6	101.75	130.46	162.74	198.58	237.99
Pd	46	$E_{46}=(1.273Z-54.015)^2$	E(exp)	91	119	149	182	218	256
			E(calc)	92.83	116.98	148.38	181.01	216.88	256
Ag	47	$E_{47}=(1.065Z-46.328)^2$	E(exp)	63.8	83	104	126	150	158
			E(calc)	63.79	81.94	102.35	125.04	150	177.21
Cd	48	$E_{48}=(0.944Z-40.963)^2$	E(exp)	66	83	102	122	144	165
			E(calc)	66.02	82.25	100.26	120.06	141.63	164.99
In	49	$E_{49}=(0.938Z-41.289)^2$	E(exp)	71	89	108	127	151	172
			E(calc)	70.98	87.67	106.11	126.31	148.28	172
Sn	50	$E_{50}=(1.023Z-47.629)^2$	E(exp)	57	74	93	114	137	162
			E(calc)	57.96	74.58	93.3	114.1	137.01	162
Sb	51	$E_{51}=(1.041Z-49.383)^2$	E(exp)	62	80	100	122	146	171
			E(calc)	61.97	79.44	99.08	120.89	144.86	171.01
Te	52	$E_{52}=(1.056Z-51.263)^2$	E(exp)	62	80	100	122	147	173
			E(calc)	61.98	79.73	99.7	121.9	146.34	173
J	53	$E_{53}=(1.066Z-52.638)^2$	E(exp)	66	85	106	129	154	181
			E(calc)	66	84.46	105.18	128.19	153.46	181.01
Xe	54	$E_{54}=(1.06Z-53.105)^2$	E(exp)	70	89	111	135	161	187
			E(calc)	70.14	89.02	110.14	133.52	159.14	187.01
NO DATA			E(exp)						
			E(calc)						
Tu	69	$E_{69}=(1.075Z-71.767)^2$	E(exp)	45	61	79	99	121	146
			E(calc)	45	60.57	78.46	98.66	121.18	146
Yb	70	$E_{70}=(1.088Z-73.583)^2$	E(exp)	48	65	89	104	127	153

			E(calc)	48.01	64.27	82.9	103.9	127.26	152.99
Lu	71	$E_{71}=(1.091Z-74.671)^2$	E(exp)	51	68	88	109	133	159
			E(calc)	51.18	67.98	87.16	108.72	132.66	158.99
Hf	72	$E_{72}=(1.1Z-76.216)^2$	E(exp)	54	72	92	114	139	166
			E(calc)	54.52	71.98	91.85	114.15	138.86	166
Ta	73	$E_{73}=(1.123Z-78.933)^2$	E(exp)	57	75	96	120	145	173
			E(calc)	56.82	75.01	95.73	118.96	144.72	173
W	74	$E_{74}=(1.126Z-80.458)^2$	E(exp)	55	73	94	117	142	169
			E(calc)	54.32	72.18	92.58	115.52	140.99	169
Re	75	$E_{75}=(1.123Z-81.066)^2$	E(exp)	58	77	98	112?	148	176
			E(calc)	58.54	76.98	97.95	121.44	147.45	175.99
Os	76	$E_{76}=(1.144Z-83.712)^2$	E(exp)	61	81	103	127	154	183
			E(calc)	60.96	80.14	101.93	126.34	153.36	183.01
Ir	77	$E_{77}=(1.157Z-85.718)^2$	E(exp)	64	84	107	132	160	190
			E(calc)	63.98	83.83	106.36	131.56	159.44	190
Pt	78	$E_{78}=(1.137Z-84.883)^2$	E(exp)	69.7	94.4	112	138	166	197
			E(calc)	69.74	90.02	112.89	138.34	166.38	197.01
Au	79	$E_{79}=(Z-75.51)^2$	E(exp)	56	73	91	111	133	156
			E(calc)	56.1	72.08	90.06	110.04	132.02	156
Hg	80	$E_{80}=(0.999Z-76.105)^2$	E(exp)	61	78	97	117	140	164
			E(calc)	61.01	77.62	96.22	116.81	139.4	163.99
Tl	81	$E_{81}=(0.98Z-76.158)^2$	E(exp)	51	67	84	103	123	145
			E(calc)	51.01	65.97	82.85	101.65	122.37	145.01
Pb	82	$E_{82}=(0.996Z-78.226)^2$	E(exp)	55	71	89	109	130	154
			E(calc)	55.2	71	88.77	108.53	130.28	154.01
Bi	83	$E_{83}=(1.01Z-80.192)^2$	E(exp)	59	76	95	115	138	162
			E(calc)	58.95	75.48	94.05	114.66	137.31	162
Po	84	$E_{84}=(1.01Z-81.215)^2$	E(exp)	59	76	94	115	137	?
			E(calc)	58.75	75.26	93.8	114.38	137.01	?

References:

1 <http://www.new-physics.narod.ru>